STAT 652: Predicting Flight Delays Project

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1 Introduction

The goal of this project is to predict the response variable, departure delays for a particular flight given the explanatory variables.

2 Data

The dataset consists of information about all the flights leaving from New York City in 2013. The dataset contains 43 variables in total. The dataset is an amalgamation of several datasets including datasets containing information on weather, the airports, the flights, and the models of airplanes. The training dataset provided to us contains 200,000 observations. Please see table 1 for what the data looks like.

3 Methods:

We will now outline the various methods used to clean and perform prediction on the data. We will discuss our techniques for data preprocessing, and cross validation, and the different models that we tried.

3.1 Data Preprocessing

I performed data preprocessing on the nycflights 13 dataset. My data preprocessing steps include the following:

- loading the data from a csv
- setting the random seed for reproducibility of results
- casting all the columns with the character data type into the factor data type
- converting the shed_arr_time and sched_dep_time columns into the POSIX time format so that I can accurately take the difference of them.
- Dropping columns that contain data from after the planes' departure which may leak information about the response variable dep_delay. We drop columns "dep_time", "arr_time", "air_time", and "arr_delay".
- We drop column "year.x" because all the values are 2013
- We also drop tailnum because it produces too many dummy variable columns for one hot encoding.
- Dropping columns which consists of over 50% NAs which include the speed column. However, it should
 be noted that a rule of thumb suggested by Professor McNeney is to drop any columns with over 5%
 NAs. We use a different threshold for dropping columns leading to us keeping columns such as model
 instead of dropping it.
- Afterwards, I impute the missing values. However, there are limitations to this approach of imputing the missing values. It is possible, that the missingness of the plane model variable is related to dep_delay. In this scenario, we may be creating an inferior feature set by keeping the variable 'model' and imputing it. For example, say a highly unreliable plane model that frequently causes long delays has a high probability of being labeled as NA and represents the majority of NAs in the dataset. We would not be able to capture the relationship between this plane model and dep_delay if we imputed the model with the mode. To counteract this affect, we imputed NAs for the remaining columns using the imputeMissings library, adding a Boolean flag which indicates 1 if the associated value was 1 and 0 otherwise. For example, the "model_flag" for a given row is 1 if the "model" value was NA for that given row. Hence, no information is lost from our imputation.
- Normalizing the data to work well with methods like lasso regression.
- Only kept data which had a departure delay of less than 30 minutes late, which reduced the dataset from 200,000 rows to approximately 170,000. This is because we consider extreme delays of of over 30 minutes late to be freak accidents which cannot be accurately predicted by the available explanatory variables.

3.2 Exploratory Analysis

3.2.1 Correlations

First, we created a correlation plot for the numeric variables to see if there any correlations between the variables.

We see that there is very little correlation between the response variable dep_delay and any of the other variables. Some of the strongest correlations include the correlation between distance and longitude and time zone and a smaller correlation between distance and latitude. This makes sense as most of the planes are inter US flights from west to east or vice versa, there is not as much distance flown in the north south direction. Please see Figure 1 for the correlation plot (Click on the number after Figure to jump to plot).

3.3 Principal Component Analysis (PCA)

Next we performed PCA on only the numeric variables as techniques to perform PCA on mixed datasets (numerical and categorical) was not covered in class. When looking at the contribution of each variable to the first principal component, we notice that the variables lon, distance, tz, seats, alt, sched_air_time have the greatest absolute coefficients for the first principal component. The fact that the aforementioned variables have large coefficients in the first principal component suggests that they are highly correlated with each other. The fact that dep_delay has a small coefficient in the first principal component suggests that dep_delay is not highly correlated with any of the above variables.

As expected, it turns out that variables like lon, distance and tz are not important for predicting dep_delay according to the gbm model. This maybe be because although variables like lon, distance and tz help explain most of the variance in the dataset, they have a weak relationship with dep_delay.

Please see table 2 for the proportion of variance explained by each principal component. Please see table 3 for the coefficient of each variable for each principal component ordered by magnitude of coefficient.

3.4 Cross Validation

Initially, I used the most basic cross validation technique where I have a training dataset and a cross validation dataset. I split the original data into a ratio of 2/3 train and 1/3 of the data for cross validation. There is a additional data which would be provided by the professor at a later date which we will use as the holdout test set. I believe that 2/3 of the data gives enough data for the models to train on while 1/3 is enough data for us to get an accurate assessment of the error. k-folds cross validation was not initially used in order to save on compute time as we were initially only exploring the models. k-folds cross validation would increase training time for the models by a factor of k. However, k-folds cross validation would lead to a more stable estimate of holdout test set error.

3.5 Models

We first explored some basic models to establish a baseline performance and compared it to our most sophisticated model, the Generalized Boosted Regression Model (GBM).

3.5.1 Basic Models

dep_delay is the number of minutes that the plane either departs early or late. Negative numbers are for early departures and positive numbers are for the number of minutes the plane is late. First, I used a basic model of simply predicting the dep_delay to always be 0. This was done to establish baseline performance.

This model had an root mean squared error (RMSE) of 8.30571. TODO The model in which I predicted the mean for all the predictions had an RMSE of TODO.

3.5.2 Linear Regression

A linear regression model assumes a linear relationship between the explanatory variables and the response variable. The model minimizes the squared loss function. This minimization process generates coefficients which are used for a linear combination of the explanatory variables. The linear combination is the prediction. Then I tried linear regression with dep_delay as the response variables and all the other remaining variables as the explanatory variables. This model was better than predicting the mean with an RMSE of TODO. This suggests that there is some relationship between the dep_delay and the explanatory variables.

3.5.3 Generalized Boosted Regression Model (GBM)

How boosted regression models work is we first start off with a baseline prediction. For example, we can use the mean as our baseline prediction. Then we use a base classifier to iteratively predict on the residuals multiplied by the shrinkage hyperparameter. Then this base classifier is added to the enssemble of base classifiers trained so far. A lower shrinkage effectively means a lower learning rate and therefore you need more iterations to reduce the train set residuals by the same amount. The benefit of a smaller shrinkage (with sufficient trees) is that you end up with a larger ensemble of trees that can reach a lower cross validation loss. This iterative prediction process is called boosting. In our case, our base classifiers are regressor trees. Each tree decides on its splitting criterion greedily by picking the split which results in the lowest mean squared error or some other splitting heuristic. We continue for n number of trees where n is specified by the user. Each iteration produces one tree, so the number of iterations is equal to the number of trees. Afterwards, we tried a Generalized Boosted Regression Model (GBM). This model had the lowest RMSE of 7.94458 on the cross validation set after it was tuned to have a shrinkage of 0.01 and around 16,000 trees. Shrinkage is proportional to the learning rate. 16,000 trees is the number of trees used in the model. Each iteration uses 1 tree, so 16,000 trees also refers to the number of iterations. According to the vignette, the RMSE can always be improved by decreasing shrinkage, but this provides diminishing returns. A good strategy would be to pick a small shrinkage that balances performance and compute time. Then with this fixed shrinkage value, increase the number of trees until you get diminishing returns. We decided to follow the aforementioned strategy. Please see table @4 for a table of the relative influence of each explanatory variable. Here, you can see the relative influence for each variable for gbm.

For a gbm, the improvement in the splitting criterion (which is mean squared error for regression) for a given variable is calculated at each step. The relative influence for a given variable is the average of these improvements over all the trees where the aforementioned variable is used.

4 Results

In regression and gbm, I found different features to be important.

Please see table @5 for all the models and their root mean squared error (RMSE) on the cross validation set.

4.1 GBM

For the best gbm model, dest which refers to which airport a given plane was flying to was the most important feature. However, the one hot encoding versions of carrier were the most important features for regression. Based on the relative influence scores provided by the gbm, some of the most important feature variables include dest, model, and sched_dep_time_num_minute.mThe dest column contains the airport code for where a given flight is flying to. Based on my run of gbm with a shrinkage of 0.01 and 16834 trees, dest

was the most important feature with 49.56 relative influence. ("Gradient Boosting Machines · UC Business Analytics R Programming Guide" 2019).

4.2 Linear Regression

On the other hand, dest does appear as an important feature in linear regression as well but it is not the most important feature. I surmise that if we can somehow sum up all the contributions from each of the one-hot-encoded variables derived from dest then, it might appear as the most important feature for linear regression as well. We can try using ANOVA in order to measure the statistical significance of dest. Performing ANOVA on comparing linear regression model with and without dest, it was determined that due to the low p-value of 0.0001863 associated with having dest that keeping at least one of the one hot categorical variables derived from dest is beneficial for the linear regression model.

4.3 Comparison

Dest was most important feature in gbm. It is possible that dest is important in combination with other variables which is something that the linear model without interaction terms cannot capture the relationship of whereas gbm can discover these non linear relationships.

TODO: try interaction terms , try anova.

5 Conclusion and Discussion

5.1 Discussion

We considered removing outliers in terms of 'dep_delay' in train but not in test, then use k-folds cross validation on test to determine how many outliers we should remove to boost performance on the cross-validation set. We considered removing highly influential points in order to train a better model. In this case, we consider highly influential points to be points with high cook's distances. However, this was infeasible as we did not have enough computational resources available and it took too long.

5.2 Conclusion

None of the models that we tried performed particularly well. We surmise that this may be due to the explanatory variables having a weak relationship with the 'dep_delay' variable. There is a lack of information about a particular flight before it reaches NYC. Instead, we get information about where the flight is going next which through commons sense, would reveal less information about the current condition of the plane and what kind of maintenance it would need and therefore what dep_delay it would have. Out of the methods that we covered in class, I found gradient boosted models to provide the best performance based on having the lowest root mean squared error on the cross validations et. I believe that this makes sense because GBMs are able to capture non linear relationships between the explanatory variables and 'dep_delay' whereas linear regression cannot.

5.3 Future Work

TODo: add dep_delay vs explanatory plots. TODO: remove points that are outliers ie dep_delay > 200 or 300 etc. or remove less than x number of points. then use k-folds cross validation on cross validation set where no points were removed. can repeat k-folds for different seeds. can just try this on my quickest model, i.e. linear regression. should be bowl shape vs RMSE vs. number of points removed. theoretically

I also considered removing based on cook's distance but this took too long to compute.

5 folds with 10 different random seeds

have train, CV and test set 1/3 train, 1/3 CV, 1/3 test 2/3% train, 1/3%CV, wait for prof test set try lasso regression

6 Code

6.1 Preparing the programming environment

6.1.1 Loading Libraries

```
library(tidyverse)
## -- Attaching packages --
## v ggplot2 3.2.1
                   v purrr
                           0.3.3
## v tibble 2.1.3
                   v dplyr
                           0.8.3
## v tidyr
         1.0.0
                   v stringr 1.4.0
## v readr
         1.3.1
                   v forcats 0.4.0
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                 masks stats::lag()
```

6.2 Data Preprocessing

6.2.1 Loading the data

```
library(nycflights13)
library(Hmisc)
## Loading required package: lattice
## Loading required package: survival
## Loading required package: Formula
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
       src, summarize
##
## The following objects are masked from 'package:base':
##
##
       format.pval, units
set.seed(42)
original_data <- read_csv("fltrain.csv.gz")</pre>
## Parsed with column specification:
## cols(
```

Table 1: A table of the first few rows of the nycflights 13 data.

year.x	month	day	dep_time	$sched_dep_time$	dep_delay	arr_time	$sched_arr_time$	arr_delay	carrier f
2013	11	7	600	600	0	826	825	1	WN
2013	10	30	1252	1250	2	1356	1400	-4	AA
2013	12	18	1723	1715	8	2008	2020	-12	DL
2013	11	20	2029	2030	-1	2141	2205	-24	WN
2013	10	21	1620	1625	-5	1818	1831	-13	DL
2013	11	7	852	900	-8	1139	1157	-18	B6

```
.default = col_double(),
##
##
     carrier = col_character(),
##
     tailnum = col_character(),
     origin = col_character(),
##
##
     dest = col_character(),
     time hour = col datetime(format = ""),
##
##
     name = col_character(),
##
     dst = col_character(),
##
     tzone = col_character(),
##
     type = col_character(),
##
     manufacturer = col_character(),
##
     model = col_character(),
##
     engine = col_character()
## )
## See spec(...) for full column specifications.
DF <- original_data
turning all columns with datatype characters to factors.
DF[sapply(DF, is.character)] <- lapply(DF[sapply(DF, is.character)],</pre>
                                         as.factor)
DF$flight <- as.factor(DF$flight)</pre>
library(lubridate)
## Attaching package: 'lubridate'
## The following object is masked from 'package:base':
##
##
       date
DF$sched_arr_time_posix <- as.POSIXct(str_pad(as.character(DF$sched_arr_time), 4, pad="0"),format="%H%M
DF$sched_arr_time_hour <- hour(DF$sched_arr_time_posix)</pre>
DF$sched_arr_time_minute <- minute(DF$sched_arr_time_posix)</pre>
#num minute is number of minutes since start of day for scheduled arrival time
DF$sched_arr_time_num_minute <- 60*DF$sched_arr_time_hour + DF$sched_arr_time_minute
DF$sched_dep_time_posix <- as.POSIXct(str_pad(as.character(DF$sched_dep_time),4 , pad="0"),format="%H%M
DF$sched_dep_time_hour <- hour(DF$sched_dep_time_posix)</pre>
DF$sched_dep_time_minute <- minute(DF$sched_dep_time_posix)</pre>
#num minute is number of minutes since start of day for scheduled depival time
```

```
DF$sched_dep_time_num_minute <- 60*DF$sched_dep_time_hour + DF$sched_dep_time_minute
select(original_data, time_hour, sched_dep_time, sched_arr_time, tz, tzone)
## # A tibble: 200,000 x 5
##
      time_hour
                           sched_dep_time sched_arr_time
                                                             tz tzone
##
      <dttm>
                                    <dbl>
                                                    <dbl> <dbl> <chr>
                                                             -5 America/New_York
## 1 2013-11-07 11:00:00
                                      600
                                                     825
## 2 2013-10-30 16:00:00
                                     1250
                                                     1400
                                                             -5 America/New_York
## 3 2013-12-18 22:00:00
                                     1715
                                                    2020
                                                             -5 America/New_York
## 4 2013-11-21 01:00:00
                                     2030
                                                    2205
                                                            -6 America/Chicago
## 5 2013-10-21 20:00:00
                                     1625
                                                     1831
                                                             -5 America/New York
## 6 2013-11-07 14:00:00
                                      900
                                                     1157
                                                            -5 America/New_York
                                     1529
## 7 2013-09-29 19:00:00
                                                     1649
                                                            -6 America/Chicago
## 8 2013-12-21 20:00:00
                                     1530
                                                     1710
                                                             -6 America/Chicago
## 9 2013-11-07 21:00:00
                                     1650
                                                     1906
                                                             -5 America/New_York
## 10 2013-03-31 21:00:00
                                     1700
                                                     1821
                                                             -5 America/New_York
## # ... with 199,990 more rows
select(DF, sched arr time, sched arr time hour)
## # A tibble: 200,000 x 2
##
      sched_arr_time sched_arr_time_hour
##
               <dbl>
                                    <int>
## 1
                 825
                                        8
                                       14
## 2
                1400
## 3
                2020
                                       20
## 4
                2205
                                       22
## 5
                1831
                                       18
## 6
                1157
                                       11
## 7
                                       16
                1649
## 8
                1710
                                       17
## 9
                1906
                                       19
## 10
                1821
                                       18
## # ... with 199,990 more rows
DF$sched_air_time <- DF$sched_arr_time_posix - DF$sched_dep_time_posix
drops <- c('sched_arr_time_posix', 'sched_arr_time_hour', 'sched_dep_time_posix', 'sched_dep_time_hour'</pre>
DF <- DF[ , !(names(DF) %in% drops)]</pre>
drops <- c("dep_time", "arr_time", "air_time", "arr_delay", "year.x", 'tailnum')</pre>
DF <- DF[ , !(names(DF) %in% drops)]</pre>
## Remove columns with more than 50% NA
DF <- DF[, -which(colMeans(is.na(DF)) > 0.5)]
DF$sched_air_time <- as.numeric(DF$sched_air_time)</pre>
library(imputeMissings)
##
## Attaching package: 'imputeMissings'
## The following object is masked from 'package:Hmisc':
##
##
## The following object is masked from 'package:dplyr':
```

```
##
##
       compute
impute_model <- imputeMissings::compute(DF, method="median/mode")</pre>
impute_model
## $month
## [1] 7
##
## $day
## [1] 16
##
## $dep_delay
## [1] -2
##
## $carrier
## [1] "UA"
##
## $flight
## [1] "15"
##
## $origin
## [1] "EWR"
##
## $dest
## [1] "ATL"
##
## $distance
## [1] 872
##
## $temp
## [1] 57.2
##
## $dewp
## [1] 42.8
## $humid
## [1] 57.69
##
## $wind_dir
## [1] 220
##
## $wind_speed
## [1] 10.35702
##
## $precip
## [1] 0
##
## $pressure
## [1] 1017.5
##
## $visib
## [1] 10
##
```

\$name

```
## [1] "Hartsfield Jackson Atlanta Intl"
##
## $lat
## [1] 36.09775
## $lon
## [1] -83.35339
##
## $alt
## [1] 433
## $tz
## [1] -5
##
## $dst
## [1] "A"
##
## $tzone
## [1] "America/New_York"
## $year.y
## [1] 2002
##
## $type
## [1] "Fixed wing multi engine"
## $manufacturer
## [1] "BOEING"
##
## $model
## [1] "A320-232"
##
## $engines
## [1] 2
## $seats
## [1] 149
##
## $engine
## [1] "Turbo-fan"
## $sched_arr_time_minute
## [1] 30
##
## $sched_arr_time_num_minute
## [1] 957
## $sched_dep_time_minute
## [1] 29
## $sched_dep_time_num_minute
## [1] 839
##
## $sched_air_time
```

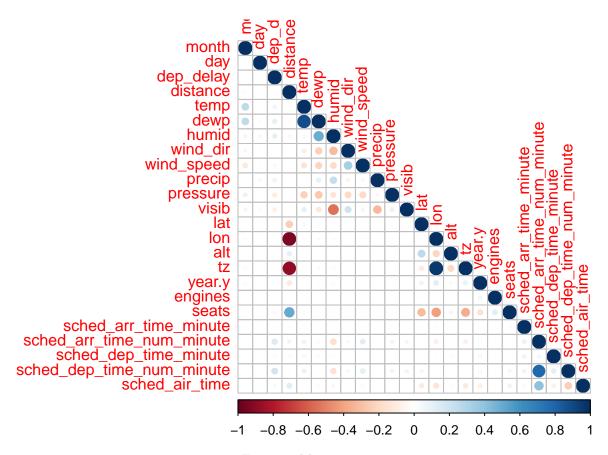


Figure 1: My caption

```
## [1] 139

DF <- impute(DF, object=impute_model, flag=TRUE)

DF <- DF[!duplicated(as.list(DF))] #remove all redundant flag columns that are identical to each other

numeric_only_df <- dplyr::select_if(DF, is.numeric)
library(corrplot)</pre>
```

6.3 try features scaling

corrplot 0.84 loaded

```
dep_delay_vec <- DF$dep_delay</pre>
DF$dep_delay <- NULL</pre>
head(DF)
##
     month day carrier flight origin dest distance temp dewp humid wind_dir
## 1
        11
             7
                     WN
                           1716
                                   LGA ATL
                                                  762 62.96 55.94 77.83
                                                                               210
## 2
        10
            30
                     AA
                           178
                                   JFK
                                        BOS
                                                  187 59.00 46.94 64.22
                                                                               240
## 3
                     DL
                          1585
                                   LGA MCO
                                                  950 33.98 17.06 49.51
                                                                               270
        12
           18
## 4
        11
            20
                     WN
                          3494
                                   EWR MDW
                                                  711 37.04 17.96 45.58
                                                                                20
                          2231
                                                  502 62.96 41.00 44.47
                                                                               160
## 5
        10
            21
                     DL
                                   LGA
                                        DTW
## 6
        11
                     B6
                             27
                                   EWR
                                        MCO
                                                  937 64.40 55.40 77.29
                                                                               240
     wind_speed precip pressure visib
                                                                                   lat
                                                                        name
```

```
## 1
       13.80936
                          1011.0
                                           Hartsfield Jackson Atlanta Intl 33.63672
## 2
        9.20624
                          1024.9
                                    10 General Edward Lawrence Logan Intl 42.36435
                     0
## 3
       17.26170
                          1019.8
                                                              Orlando Intl 28.42939
        5.75390
                          1035.6
## 4
                                                       Chicago Midway Intl 41.78597
                      \cap
                                    10
## 5
       13.80936
                          1016.9
                                    10
                                                    Detroit Metro Wayne Co 42.21244
## 6
       16.11092
                     0
                          1017.5
                                    10
                                                              Orlando Intl 28.42939
           lon alt tz dst
                                       tzone year.y
                                                                         type
## 1 -84.42807 1026 -5
                          A America/New York
                                                2001 Fixed wing multi engine
## 2 -71.00518
                 19 -5
                          A America/New York
                                                2002 Fixed wing multi engine
## 3 -81.30899
                          A America/New_York
                 96 -5
                                                2002 Fixed wing multi engine
## 4 -87.75242
               620 -6
                          A America/Chicago
                                                2006 Fixed wing multi engine
## 5 -83.35339
                645 -5
                          A America/New_York
                                                1992 Fixed wing multi engine
## 6 -81.30899
                 96 - 5
                          A America/New_York
                                                2006 Fixed wing multi engine
         manufacturer
                          model engines seats
                                                  engine sched_arr_time_minute
## 1
               BOEING 737-7H4
                                      2
                                          140 Turbo-fan
                                                                             25
                                      2
## 2
               BOEING A320-232
                                          149 Turbo-fan
                                                                              0
## 3
               AIRBUS A319-114
                                      2
                                          145 Turbo-fan
                                                                             20
                                      2
## 4
               BOEING 737-7H4
                                          140 Turbo-fan
                                                                              5
## 5 AIRBUS INDUSTRIE A320-211
                                      2
                                          182 Turbo-jet
                                                                             31
                                      2
               AIRBUS A320-232
                                          200 Turbo-fan
                                                                             57
##
     sched_arr_time_num_minute sched_dep_time_minute sched_dep_time_num_minute
## 1
                            505
                                                     0
## 2
                            840
                                                    50
                                                                              770
## 3
                           1220
                                                    15
                                                                             1035
## 4
                                                    30
                           1325
                                                                             1230
## 5
                           1111
                                                    25
                                                                              985
## 6
                            717
                                                     0
                                                                              540
     \verb|sched_air_time_dep_delay_flag_temp_flag_wind_dir_flag_wind_speed_flag|
## 1
                145
                                  0
                                             0
                                                           0
                                                                            0
## 2
                                  0
                                                                            0
                 70
                                             0
                                                           0
## 3
                185
                                  0
                                             0
                                                           0
                                                                            0
## 4
                 95
                                  0
                                             0
                                                           0
                                                                            0
                                  0
                                             0
                                                                            0
## 5
                126
                                                           0
                177
## 6
                                  0
                                             0
                                                           0
                                                                            0
     precip_flag pressure_flag name_flag year.y_flag type_flag
## 1
               0
                              0
                                        0
                                                     0
## 2
               0
                              0
                                        0
                                                     1
                                                                1
## 3
               0
                              0
                                        0
                                                     0
                                                                0
## 4
               0
                              0
                                        0
                                                     0
                                                                0
                                                     0
                                                               0
## 5
               0
                              0
                                        Λ
## 6
                                        0
                                                                0
library(dplyr)
DF <- DF %>% mutate if(is.numeric, scale)
head(DF)
                    day carrier flight origin dest
##
                                                       distance
       month
## 1 1.30322 -0.9929373
                                   1716
                                           LGA ATL -0.3777852 0.3339858
## 2 1.01019 1.6325235
                                            JFK BOS -1.1644742 0.1127815
                                    178
                              AA
## 3 1.59625 0.2627179
                              DL
                                   1585
                                                 MCO -0.1205721 -1.2848272
                                           T.GA
## 4 1.30322 0.4910188
                              WN
                                           EWR MDW -0.4475611 -1.1138966
                                   3494
## 5 1.01019 0.6051693
                              DL
                                   2231
                                           LGA DTW -0.7335054 0.3339858
## 6 1.30322 -0.9929373
                              B6
                                     27
                                           EWR MCO -0.1383581 0.4144237
##
           dewp
                     humid
                              wind_dir wind_speed
                                                        precip
                                                                   pressure
                                                                                visib
## 1 0.7418623 0.9315583 0.07717317 0.4871566 -0.1492223 -0.96830167 0.3664282
```

```
## 2 0.2753242 0.2375566 0.36735789 -0.3415806 -0.1492223 1.01596006 0.3664282
## 3 -1.2735821 -0.5125364 0.65754261 1.1087096 -0.1492223 0.28792159 0.3664282
## 4 -1.2269283 -0.7129351 -1.76066338 -0.9631336 -0.1492223 2.54341334 0.3664282
## 5 -0.0325909 -0.7695363 -0.40646802 0.4871566 -0.1492223 -0.12606108 0.3664282
## 6 0.7138700 0.9040226 0.36735789 0.9015253 -0.1492223 -0.04040949 0.3664282
##
                                   name
                                              lat
                                                         lon
        Hartsfield Jackson Atlanta Intl -0.4207546 0.3298674 0.48364704
## 2 General Edward Lawrence Logan Intl 1.1190951 1.2378347 -0.60619417
                           Orlando Intl -1.3395034 0.5408516 -0.52285973
## 4
                    Chicago Midway Intl 1.0170501 0.1049977 0.04424731
## 5
                 Detroit Metro Wayne Co 1.0922942 0.4025621 0.07130394
## 6
                           Orlando Intl -1.3395034 0.5408516 -0.52285973
##
            tz dst
                               tzone
                                          year.y
## 1 0.6826595
                 A America/New_York -0.08500492 Fixed wing multi engine
## 2 0.6826595
                 A America/New_York 0.08617407 Fixed wing multi engine
                 A America/New_York 0.08617407 Fixed wing multi engine
## 3
     0.6826595
                 A America/Chicago 0.77089000 Fixed wing multi engine
## 4 -0.2514221
     0.6826595
                 A America/New York -1.62561576 Fixed wing multi engine
## 6 0.6826595
                 A America/New York 0.77089000 Fixed wing multi engine
##
        manufacturer
                        model
                                engines
                                              seats
                                                        engine
## 1
              BOEING 737-7H4 0.05879311 0.02232546 Turbo-fan
              BOEING A320-232 0.05879311 0.15869100 Turbo-fan
              AIRBUS A319-114 0.05879311 0.09808410 Turbo-fan
## 3
              BOEING 737-7H4 0.05879311 0.02232546 Turbo-fan
## 5 AIRBUS INDUSTRIE A320-211 0.05879311 0.65869797 Turbo-jet
              AIRBUS A320-232 0.05879311 0.93142905 Turbo-fan
##
     sched_arr_time_minute sched_arr_time_num_minute sched_dep_time_minute
               -0.2348938
                                         -1.4325947
## 1
                                                               -1.36042229
## 2
               -1.6716145
                                         -0.3129587
                                                               1.23408583
               -0.5222379
                                           0.9570761
                                                               -0.58206985
## 4
               -1.3842703
                                           1.3080068
                                                                0.19628258
## 5
                0.1099192
                                          0.5927766
                                                               -0.06316823
## 6
                1.6041087
                                         -0.7240489
                                                               -1.36042229
     sched_dep_time_num_minute sched_air_time dep_delay_flag temp_flag
## 1
                   -1.6236293
                                 0.14883297
                                                           0
## 2
                   -0.1673447
                                  -0.24317221
                                                           0
                                                                     0
## 3
                     0.7739125
                                  0.35790240
                                                           0
## 4
                     1.4665357
                                  -0.11250381
                                                           0
                                                                     0
## 5
                     0.5963168
                                   0.04952499
## 6
                   -0.9842849
                                   0.31608852
                                                           Λ
     wind_dir_flag wind_speed_flag precip_flag pressure_flag name_flag year.y_flag
## 1
                                0
                                            0
                                                           0
                                                                     0
                 0
                                                                                 0
## 2
                 0
                                0
                                            0
                                                           0
                                                                     0
                                                                                 1
## 3
                 0
                                0
                                            0
                                                          0
                                                                     0
                                                                                 0
## 4
                                0
                                             0
                                                          0
## 5
                 0
                                0
                                            0
                                                          0
                                                                     0
                                                                                 0
                                0
## 6
     type_flag
## 1
            0
## 2
            1
## 3
            0
## 4
## 5
            0
## 6
```

Table 2: proportion of variance explained by each principal component

	X
PC1	0.1352687
PC2	0.1061946
PC3	0.0862791
PC4	0.0688860
PC5	0.0605903
PC6	0.0582950

```
DF$dep_delay <- dep_delay_vec
```

6.4 Exploratory Data Analysis

```
numeric_DF <- dplyr::select_if(DF, is.numeric) %>% scale()

prcomp_res <- prcomp(numeric_DF)
sdev <- prcomp_res$sdev
sdev

## [1] 1.801791e+00 1.596455e+00 1.438992e+00 1.285793e+00 1.205889e+00
## [6] 1.182827e+00 1.096174e+00 1.028253e+00 1.017278e+00 9.998650e-01
## [11] 9.870519e-01 9.598095e-01 9.527413e-01 9.302188e-01 8.722020e-01
## [16] 8.678655e-01 8.004108e-01 7.322880e-01 7.049102e-01 6.392628e-01
## [21] 2.137689e-01 1.418198e-01 5.881124e-02 1.734179e-14</pre>
```

6.4.1 all four components at same time

proportion of variance explained by each component

```
pve <- colSums(prcomp_res$x^2)/sum(numeric_DF^2)

rotation <- as.data.frame(prcomp_res$rotation)
rotation[order(-abs(rotation$PC1)),]</pre>
```

```
##
                                PC1
                                           PC2
                                                      PC3
                                                                  PC4
## lon
                         ## distance
                        -0.5303215501 -0.013672653 0.042091019 0.0006060091
## tz
                         0.5152320734 0.003918041 -0.003819370 -0.0093898478
## seats
                        -0.3267974610 -0.021806698 0.092397836 0.0075811906
                        ## alt
                        -0.1269319210 -0.059262301 -0.046756285 -0.0535120057
## sched_air_time
## year.y
                        ## sched_arr_time_num_minute -0.0808327463 -0.139515851 -0.548184284 -0.2068187847
## lat
                        0.0722096939 0.032190638 -0.080234329 0.0246355126
                        -0.0345819273 \quad 0.539843580 \ -0.222885964 \quad 0.1989663082
## dewp
                        -0.0291750632 0.384082292 -0.336092763 0.3735114971
## temp
## month
                        -0.0237188202  0.182298459  -0.084197143  0.3005556332
                        -0.0215092361 -0.015025384 -0.089818353 -0.0429715263
## sched_arr_time_minute
## humid
                        -0.0203751852 0.453383850 0.144953536 -0.3156006821
```

```
-0.0127603053 0.004264643 0.001902439 0.0110691777
## engines
## wind_speed
                     -0.0082656281 -0.253349116 -0.146083514 -0.2029687361
                      ## dep delay
                      0.0071744619 -0.280198624 -0.146006623 0.5175332824
## visib
               0.0051374481 -0.127426965 0.233410657 0.1117576955

-0.0032312124 0.177264013 0.017625071 -0.4019773885

0.0031602295 -0.294478266 -0.112869407 0.0491076591

nute -0.0026413644 0.003439200 -0.121374246 -0.0057857207
                      0.0051374481 -0.127426965 0.233410657 0.1117576955
## pressure
## precip
## wind dir
## sched_dep_time_minute
## dav
                       0.0004234420 -0.029084254 -0.002485255 0.0805143860
## sched_dep_time_num_minute 0.0003538067 -0.107997556 -0.550807880 -0.1834313382
                             PC5
                                       PC6
                                                 PC7
                      ## lon
## distance
                      -0.042941576 -0.005942745 -0.122735618 0.043705253
                      ## tz
                     -0.299154868 -0.009581806 -0.206563161 -0.144397469
## seats
                      0.466078117 -0.062307363 0.241777658 -0.082760758
## alt
## sched_arr_time_num_minute -0.104506952  0.310826773  0.201433129 -0.047918183
                      0.662475235 -0.078116941 0.239929946 -0.075262096
## dewp
                      -0.078261453 -0.121386482 0.033430978 0.007641409
## temp
                     -0.092120074 -0.132315189 0.049043959 0.010668654
                     ## month
0.003708481 -0.016414325 -0.017906587 -0.005803837
## humid
## engines
                     -0.044314253 0.009660787 -0.123433154 -0.848006590
## wind_speed
                     -0.061901823 -0.437801958 0.009361381 -0.047218482
                      0.045376993 -0.018945452 -0.127408457 0.067633220
## dep_delay
                    -0.007702427 -0.018742792 -0.026418970 0.024830862
## visib
                    ## pressure
## precip
## wind_dir
## sched_dep_time_minute
                      0.092015290 0.054589781 -0.390804984 0.021989590
                      -0.001689151 0.020937857 -0.047272003 0.037610315
## sched_dep_time_num_minute 0.092202353
                                 0.227284354 -0.259042906 0.070884810
##
                             PC9
                                      PC10
                                                PC11
                                                          PC12
## lon
                      ## distance
                      0.020078457 -0.041564282 0.11149965 -0.041739208
## tz
                      0.038322354
                      ## seats
## alt
                      -0.138469996  0.146822298  -0.29987639  0.092299979
## sched_air_time
                      ## year.y
                      -0.034976443 -0.155852739 0.66240241 -0.262765846
## sched_arr_time_num_minute 0.053926504 -0.020110402 0.04077386 -0.025711336
## lat
                       ## dewp
                       ## temp
                      0.006200971 -0.013446913 -0.02987388 -0.002801481
                      -0.120787905 -0.156460256 0.19154435 0.625378579
## month
## sched_arr_time_minute
                      ## humid
                      0.132086910 0.104896992 -0.32454087 0.021879150
## engines
                  -0.071625458 -0.057666857 0.10354898 0.185290272
0.200325467 0.111865346 -0.09362580 -0.081177009
## wind_speed
                      ## dep_delay
## visib
                      0.032108130 -0.048673404 -0.05950128 -0.052108675
```

```
0.010837763 -0.093446997 0.03191945 0.236585784
## pressure
                       0.010837763 -0.093446997 0.03191945 0.230000764
-0.076608798 -0.105843585 0.08898224 0.535791873
## precip
                        -0.088916746 -0.037067781 0.09755445 0.208042591
## wind dir
                         ## sched_dep_time_minute
                          0.213140360 0.886240079 0.33176453
                                                           0.184965679
## sched_dep_time_num_minute 0.158656717 -0.045621287 -0.09049849
                                                           0.070227231
##
                                PC13
                                            PC14
                                                       PC15
                         -0.039446447 -0.011082224 -0.095304541 0.077597524
## lon
                          0.039795147 \quad 0.002647274 \quad 0.039897734 \quad -0.004261933
## distance
## tz
                         -0.063720131 -0.035598494 -0.136768637
                                                            0.126354681
## seats
                         -0.027325189 0.020728319 -0.252623268 0.247686911
                         -0.170421919 -0.125274181 -0.455475123 0.483583152
## alt
## sched_air_time
                         -0.164479367 -0.208946245 0.041593996 -0.030363222
## year.y
                         0.197515002  0.011913488  -0.161597312  0.354827113
## sched_arr_time_num_minute -0.077917477 0.109167190 -0.088599384 -0.027228430
## lat
                          0.035792204 0.086517293 0.199298954 -0.284868167
                         -0.017049314 0.049682409 0.061863302 0.060756471
## dewp
## temp
                         0.118816359 -0.207210166 -0.371210630 -0.334318394
## month
## sched_arr_time_minute
                         0.556752791 0.125447499 0.111052124 -0.001069467
## humid
                         ## engines
                         -0.057545879  0.002619518  0.178322651  -0.213145500
                         0.003326375 -0.006229440 -0.077318196 -0.076182657
## wind speed
                         0.290573141 -0.828553616 0.116709581 0.042342062
## dep delay
## visib
                         0.056744264 -0.097207648 0.203736898 0.193394671
## pressure
                         0.027199545 -0.128666719 0.184057892 0.108434211
## precip
                        0.042744908 -0.080419991 -0.006239399 -0.069929842
## wind_dir
                         -0.670765113 -0.241104191 0.085424899 -0.145499061
## sched_dep_time_minute
                         -0.079973980 0.072516223 0.018126851 0.001947757
## day
## sched_dep_time_num_minute 0.028967986 0.258010080 -0.122424720 -0.008303141
##
                                 PC17
                                             PC18
                                                         PC19
                                                                    PC20
## lon
                         0.0205984456 -0.007328044 -0.1825459698 0.002448852
## distance
## tz
                         -0.0051770963 0.018809032 0.0334504287 -0.017652697
## seats
                        -0.0560405964 0.016440667 0.7255605863 0.013581073
## alt
                         -0.0034980154 -0.004840517 0.0992775830 -0.034805534
## sched_air_time
                         0.0096125145 -0.009443594 0.0894488451 0.039095520
## year.y
## sched_arr_time_num_minute 0.0562858424 0.035350187 0.0356674787 -0.080371931
                         -0.0520614544 -0.012599070 0.5277297074 -0.001035736
## lat
                         ## dewp
## temp
                         -0.1050475638 0.211514725 -0.0068747953 0.258118643
                          0.0289369124 -0.245815406 -0.0116573597 0.055270714
## month
                         -0.0117347846 -0.001681325 -0.0254211838 0.016161871
## sched_arr_time_minute
                         ## humid
## engines
                         0.0086998591 -0.003776375 -0.2195595169 -0.011263309
                        ## wind_speed
## dep_delay
                        -0.0005171053 -0.022901277 0.0568514930 0.061563276
                       -0.0735870801 -0.324502693 0.0148202229 -0.645786881
-0.2197533179 0.626620074 0.0007539589 -0.115345022
## visib
## pressure
## precip
                        0.1120149351 -0.238971520 0.0196643203 -0.093284192
## wind dir
                         0.5566040091 0.499155917 0.0416506799 -0.142598451
                      0.0036919766 -0.018413525 0.0629338235 -0.020942773
## sched dep time minute
```

```
-0.0242345214 -0.001266925 0.0008713042 -0.029416910
## day
## sched_dep_time_num_minute 0.0621948131 0.040857801 -0.0295601569 -0.061762457
##
                              PC21
                                          PC22
                                                     PC23
## lon
                        ## distance
                        ## tz
                       -0.692935877 -0.3885478079 -2.387247e-03
## seats
                        0.035356839 -0.0141846176 3.536570e-05
                        0.004741932 0.0333354457 1.708179e-04
## alt
## sched air time
                        -0.011013975 0.0180351813 6.012199e-04
                        0.005825894 -0.0149597542 -4.767877e-04
## year.y
## sched_arr_time_num_minute -0.006289146  0.0065552063 -1.225185e-03
                        ## lat
                        ## dewp
                        -0.005663154 0.0002352898 6.113164e-01
## temp
## month
                        ## sched_arr_time_minute
                        0.004516970 0.0014876945 2.250719e-05
## humid
                        0.009389784 -0.0061721256 3.494391e-01
## engines
                       ## wind speed
                        0.001061596 -0.0025257566 -5.755781e-04
                       ## dep delay
## visib
                       0.003848279 -0.0010054753 3.640126e-02
## pressure
                       0.002485028 -0.0027882656 1.438635e-03
## precip
                       ## wind dir
                        0.003375411 -0.0014023794 -3.540807e-04
## sched_dep_time_minute
                        0.001530860 -0.0004536717 -2.571908e-04
## sched_dep_time_num_minute 0.000800948 -0.0052895688 -1.710632e-03
##
                               PC24
## lon
                        1.073158e-14
## distance
                        6.778678e-15
                        -7.737005e-16
## tz
## seats
                        2.744135e-16
## alt
                        -8.633487e-17
                        -4.221606e-01
## sched_air_time
## year.y
                        4.918863e-16
## sched_arr_time_num_minute 6.602011e-01
## lat
                        2.167659e-15
## dewp
                        -1.348152e-15
## temp
                        -8.870884e-16
## month
                        2.656342e-16
## sched arr time minute
                       -1.997126e-15
## humid
                        2.401847e-15
## engines
                        -1.067216e-16
## wind_speed
                       -2.446632e-15
## dep_delay
                        5.015833e-17
## visib
                        5.676978e-16
## pressure
                        1.661713e-15
## precip
                       -8.702010e-16
## wind_dir
                        1.569069e-15
## sched_dep_time_minute
                        1.336574e-15
## day
                        -3.738223e-16
## sched_dep_time_num_minute -6.212206e-01
```

Table 3: coefficients for each variable on each principal component

	PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8	
dewp	-0.0345819	0.5398436	-0.2228860	0.1989663	-0.0782615	-0.1213865	0.0334310	0.0076414	0
humid	-0.0203752	0.4533838	0.1449535	-0.3156007	0.0037085	-0.0164143	-0.0179066	-0.0058038	-(
$_{\mathrm{temp}}$	-0.0291751	0.3840823	-0.3360928	0.3735115	-0.0921201	-0.1323152	0.0490440	0.0106687	(
wind _dir	0.0031602	-0.2944783	-0.1128694	0.0491077	-0.0627922	-0.4851444	0.0127712	-0.0479663	-(
visib	0.0071745	-0.2801986	-0.1460066	0.5175333	-0.0077024	-0.0187428	-0.0264190	0.0248309	0
${\rm wind_speed}$	-0.0082656	-0.2533491	-0.1460835	-0.2029687	-0.0619018	-0.4378020	0.0093614	-0.0472185	-(

```
pca_rotation <- head(rotation[order(-abs(rotation$PC2)),])</pre>
```

6.4.2 take out extreme departure delays

```
DF<-DF[DF$dep_delay < 30,]

set.seed(42)
DF$flight <- NULL
train_index <- sample(1:nrow(DF),size=2*nrow(DF)/3,replace=FALSE)
train_df <- DF[train_index,]
test_df <- DF[-train_index,]

# pre-allocate space
preallocate_df <- function(n){
    df <- data.frame(model_description = character(n), rmse = numeric(n), stringsAsFactors = FALSE)
    for(i in 1:n){
        df$model_description[i] <- i
        df$rmse[i] <- toString(i)
    }
    df
}</pre>
```

7 predicting 0

```
benchmark_df <- data.frame(model_description = character(), rmse = numeric(), stringsAsFactors = FALSE)
rmse = mean((test_df$dep_delay-0)^2) %>% sqrt()
model_description = "predicting 0"
benchmark_df <- rbind(benchmark_df, data.frame(model_description = model_description, rmse=rmse))</pre>
```

8 predicting the mean

```
rmse = mean((test_df$dep_delay-mean(train_df$dep_delay))^2)%>% sqrt()
rmse
## [1] 8.299767
```

```
benchmark_df
## model_description rmse
## 1 predicting 0 8.30571
```

9 predicting the median

```
rmse = mean((test_df$dep_delay-median(train_df$dep_delay))^2)%>% sqrt()
rmse
## [1] 8.469257
model_description <- 'predicting the median'
benchmark_df <- rbind(benchmark_df, data.frame(model_description = model_description, rmse=rmse))</pre>
```

10 linear regression with dep

```
model <- lm(dep_delay ~ ., data=train_df)</pre>
model_without_dep <- lm(dep_delay ~ .-dest, data=train_df)</pre>
anova(model, model_without_dep)
## Analysis of Variance Table
##
## Model 1: dep_delay ~ month + day + carrier + origin + dest + distance +
       temp + dewp + humid + wind_dir + wind_speed + precip + pressure +
##
##
       visib + name + lat + lon + alt + tz + dst + tzone + year.y +
##
       type + manufacturer + model + engines + seats + engine +
##
       sched_arr_time_minute + sched_arr_time_num_minute + sched_dep_time_minute +
##
       sched dep time num minute + sched air time + dep delay flag +
       temp_flag + wind_dir_flag + wind_speed_flag + precip_flag +
##
       pressure_flag + name_flag + year.y_flag + type_flag
##
## Model 2: dep_delay ~ (month + day + carrier + origin + dest + distance +
##
       temp + dewp + humid + wind_dir + wind_speed + precip + pressure +
##
       visib + name + lat + lon + alt + tz + dst + tzone + year.y +
##
       type + manufacturer + model + engines + seats + engine +
##
       sched_arr_time_minute + sched_arr_time_num_minute + sched_dep_time_minute +
       sched_dep_time_num_minute + sched_air_time + dep_delay_flag +
##
       temp_flag + wind_dir_flag + wind_speed_flag + precip_flag +
##
       pressure_flag + name_flag + year.y_flag + type_flag) - dest
                RSS Df Sum of Sq
     Res.Df
## 1 113488 7240975
## 2 113491 7242239 -3
                        -1263.7 6.602 0.0001863 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary <- round(summary(model)$coefficients,6)</pre>
sorteddf <- summary[order(summary[,ncol(summary)]),]</pre>
head(sorteddf)
               Estimate Std. Error
                                      t value Pr(>|t|)
##
                          0.887510
                                     5.200301
## carrierFL
               4.615319
```

```
## carrierUA
              2.440853
                         0.484369
                                    5.039237
## originJFK 1.037568 0.117779
                                   8.809419
                                                     0
## wind speed 0.291278 0.027929 10.429081
                                                     0
                                                     0
## precip
              0.206814
                         0.029257
                                    7.068777
## pressure
             -0.294549
                         0.027059 -10.885462
                                                     0
head(sorteddf)
              Estimate Std. Error
                                    t value Pr(>|t|)
## carrierFL 4.615319 0.887510 5.200301
## carrierUA 2.440853 0.484369 5.039237
                                                     0
## originJFK
              1.037568 0.117779
                                   8.809419
                                                     0
## wind_speed 0.291278 0.027929 10.429081
                                                     0
## precip
              0.206814 0.029257
                                   7.068777
                                                     0
## pressure -0.294549 0.027059 -10.885462
                                                     Λ
lm_test_df <- test_df</pre>
in_test_but_not_train <- setdiff(unique(lm_test_df$model), unique(train_df$model))</pre>
lm_test_df <- lm_test_df[!lm_test_df$model %in% in_test_but_not_train, ]</pre>
in_test_but_not_train <- setdiff(unique(lm_test_df$dest), unique(train_df$dest))</pre>
lm_test_df <- lm_test_df[ !lm_test_df$dest %in% in_test_but_not_train, ]</pre>
preds = predict(model, newdata=lm_test_df)
## Warning in predict.lm(model, newdata = lm_test_df): prediction from a rank-
## deficient fit may be misleading
rmse = sqrt(mean((lm_test_df$dep_delay - preds)^2))
rmse
## [1] 7.989994
model_description <- 'linear regression'</pre>
benchmark_df <- rbind(benchmark_df, data.frame(model_description = model_description, rmse=rmse))
```

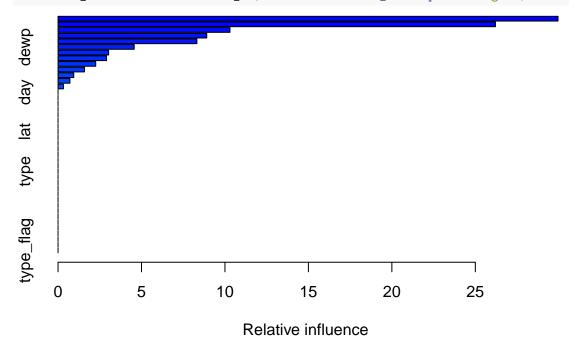
11 gbm

Table 4: gbm relative influence

	var	rel.inf
sched_dep_time_num_minute model dest carrier month	sched_dep_time_num_minute model dest carrier month	29.955850 26.206955 10.299706 8.907853 8.317570
dewp	dewp	4.563640

```
if (!file.exists(destfile)) {
   train_gbm(destfile)
}
model <- readRDS(destfile)</pre>
```

benchmark_df <- rbind(benchmark_df, data.frame(model_description = 'gbm', rmse=7.94458))



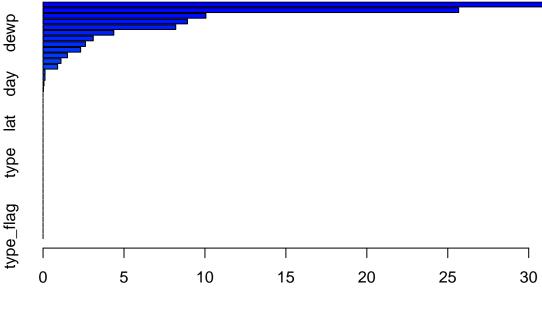
Here, you can see the relative influence for each variable for gbm.

For a gbm, the improvement in the splitting criterion (which is mean squared error for regression) for a given variable is calculated at each step. The relative influence for a given variable is the average of these improvements over all the trees where the aforementioned variable is used.

```
model <- gbm(dep_delay ~ ., data=train_df,</pre>
              n.trees=1000, shrinkage=0.01) # default shrinkage = 0.1
## Distribution not specified, assuming gaussian ...
preds = predict(model, newdata=test_df, n.trees=1000)
rmse = sqrt(mean((test_df$dep_delay - preds)^2))
rmse
```

[1] 7.980282

summary(model)



Relative influence

```
rel.inf
                                                    var
## sched_dep_time_num_minute sched_dep_time_num_minute 30.88424567
## model
                                                  model 25.67333688
## dest
                                                   dest 10.06233500
## carrier
                                                carrier 8.92374891
## month
                                                  month
                                                         8.19668822
## dewp
                                                   dewp
                                                        4.37183782
                                                 origin
                                                         3.10232960
## sched_arr_time_num_minute sched_arr_time_num_minute
                                                         2.61899718
## precip
                                                 precip
                                                         2.32288426
                                               pressure
## pressure
                                                        1.50793482
## humid
                                                  humid
                                                        1.10879519
## dep_delay_flag
                                        dep_delay_flag
                                                         0.90034697
## temp
                                                         0.12324130
                                                   temp
## pressure_flag
                                         pressure_flag
                                                         0.11994578
## day
                                                    day
                                                         0.05664389
## sched_dep_time_minute
                                 sched_dep_time_minute
                                                         0.02668850
## distance
                                               distance
                                                         0.00000000
## wind_dir
                                               wind_dir
                                                         0.00000000
## wind_speed
                                             wind_speed
                                                         0.00000000
## visib
                                                         0.0000000
                                                  visib
                                                         0.00000000
## name
                                                   name
                                                         0.00000000
## lat
                                                    lat
## lon
                                                    lon 0.00000000
## alt
                                                    alt
                                                         0.00000000
## tz
                                                     tz 0.00000000
## dst
                                                    dst 0.00000000
                                                  tzone 0.00000000
## tzone
                                                         0.00000000
## year.y
                                                 year.y
                                                         0.00000000
## type
                                                   type
## manufacturer
                                           manufacturer 0.0000000
```

Table 5: benchmark comparing all the models that we tried

model_description	rmse
predicting 0 predicting the median	8.305710 8.469257
linear regression gbm	7.989994 7.944580

```
## engines
                                              engines 0.00000000
## seats
                                                seats 0.00000000
## engine
                                               engine 0.00000000
## sched_arr_time_minute
                                sched_arr_time_minute 0.00000000
## sched_air_time
                                       sched_air_time 0.00000000
## temp_flag
                                             temp_flag 0.00000000
## wind_dir_flag
                                        wind_dir_flag 0.00000000
## wind_speed_flag
                                      wind_speed_flag 0.00000000
## precip_flag
                                          precip_flag   0.0000000
## name_flag
                                            name_flag 0.00000000
## year.y_flag
                                          year.y_flag 0.00000000
## type_flag
                                            type_flag 0.00000000
rmse = sqrt(mean((test_df$dep_delay - preds)^2))
rmse
```

[1] 7.980282

References

"Gradient Boosting Machines · UC Business Analytics R Programming Guide." 2019. http://uc-r.github.io/gbm_regression#h2o.