knit

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- 3. Methods
- 4. Results
- 5. Conclusions and Discussion

1 Introduction

The goal of this project is to predict the response variable, departure delays for a particular flight given the explanatory variables.

2 Data

The dataset consists of information about all the flights leaving from New York City in 2013. The dataset contains 43 variables in total. The dataset is an algamation of several datasets including datasets containing information on weather, the airports, the flights, and the models of airplanes. The training dataset provided to us contains 200,000 observations.

3 Methods:

3.1 Data Preprocessing

I performed data preprocessing. My data preprocessing steps include the following: 1. Dropping columns that contain data from after the planes' departure which may leak information about the response variable dep_delay. 2. Dropping columns with too many NAs. 3. Impute NAs for the remaining columns. 4. Scaling the data to work well with methods like lasso regression. 5. Only kept data which had a departure delay of less than 30 minutes late, which reduced the dataset from 200,000 rows to approximately 170,000.

3.2 Modelling

Initially, I used the most basic cross validation technique where I have a training dataset and a holdout test dataset. I split the original data into a ratio of 2/3 train and 1/3 of the data for test. I believe that this split gives enough data for the models to learn while 1/3 is enough data for me to get an accurate assessment of the error. k-folds cross validation was not initially used in order to save on compute time as I was only exploring the models. k-folds cross validation would increase training time for the models by a factor of k.

3.3 Basic Models

dep_delay is the number of minutes that the plane either departs early or late. Negative numbers are for early departures and positive numbers are for the number of minutes the plane is late. First, I used a basic model of simply predicting the dep_delay to always be 0. This was done to establish baseline performance. This model had an root mean squared error (RMSE) of 8.30571. TODO The model in which I predicted the mean for all the predictions had an RMSE of TODO.

3.4 Linear Regression

Then I tried linear regression with dep_delay as the response variables and all the other remaining variables as the explanatory variables. This model was better than predicting the mean with an RMSE of TODO. This suggests that there is some relationship between the dep_delay and the explanatory variables.

3.5 GBM

Aftewards, I tried a Generalized Boosted Regression Model (GBM). This model had the lowest RMSE on the test dataset after I tuned it to have a shrinkage of 0.01 and around 16,000 trees. Shrinkage is proportional to the learning rate. 16,000 trees is the number of trees used in the model. Each iteration uses 1 tree, so 16,000 trees also refers to the number of iterations. According to the vignette, the rmse can always be improved by decreasing shrinkage but this provides diminishing returns. A good strategy would be to pick a small shrinkage that balances performance and compute time. Then with this fixed shrinkage value, increase the number of trees until you get diminishing returns.

4 Results

In regression and gbm, I found different features to be important. For the best gbm model, dest which refers to which airport a given plane is going to was the most important feature. However, the one hot encoding versions of carrier were the most important features for regression. On the other hand, dest does appear as an important feature in linear regression as well but it is not the most important feature. I surmise that if we can somehow sum up all the contributions from each of the one hot encoded variables derived from dest then, it might appear as the most important feature for linear regression as well. We can try Anova in order to measure the statistical significance of dest. Performing anova on comparing linear regression model with and without dest, it was determined that due to the low p-value of 0.0001863 associated with having dest that keeping at least one of the one hot categorical variables derived from dest is beneficial for the linear regression model.

TODO: try interaction terms, try anova.

5 Conclusion and Discussion

Conclusion: In conclusion, out of the methods that we covered in class, I found gradient boosted models to provide the best performance based on having the lowest root mean squared error on the hold out test set.

Based on the relative influence scores provided by the gbm, some of the most important feature variables include dest, model, and sched_dep_time_num_minute.

The dest column contains the airport code for where a given flight is flying to. Based on my run of gbm with a shrinkage of 0.01 and 16834 trees, dest was the most important feature with 49.56 relative influence. ("Gradient Boosting Machines · UC Business Analytics R Programming Guide" 2019).

TODO; think about removing points that are outliers aka points with high cook's distance consider removing outliers in train but not in test, then use k-folds cross validation on test.

TODO: remove points that are outliers ie dep_delay > 200 or 300 etc. or remove less than x number of points, then use k-folds cross validation on cross validation set where no points were removed, can repeat k-folds for different seeds, can just try this on my quickest model, ie linear regression, should be bowl shape vs rmse vs. number of points removed, theoretically

I also considered removing based on cook's distance but this took too long to compute.

5 folds with 10 different random seeds

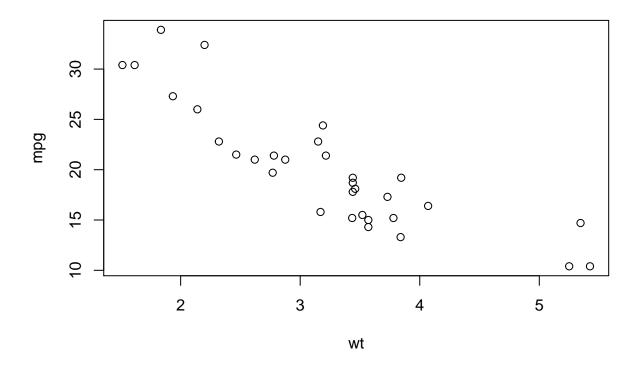
- 6 have train, CV and test setå
- 7 1/3 train, 1/3 CV, 1/3 test
- 8 2/3% train, 1/3%CV, wait for prof test set

try lasso regression

9 Code

9.1 Loading Libraries

```
library(tidyverse)
## -- Attaching packages -----
                                                                   ----- tidyverse 1.2.1
## v ggplot2 3.2.1
                  v purrr
                            0.3.3
## v tibble 2.1.3
                            0.8.3
                   v dplyr
                 v stringr 1.4.0
## v tidyr
          1.0.0
## v readr
           1.3.1
                  v forcats 0.4.0
## -- Conflicts ----- tidyverse_conflicts()
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
attach(mtcars)
## The following object is masked from package:ggplot2:
##
##
      mpg
plot(wt, mpg)
```



9.2 Loading the data

```
library(nycflights13)
library(Hmisc)
## Loading required package: lattice
## Loading required package: survival
## Loading required package: Formula
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
       src, summarize
## The following objects are masked from 'package:base':
##
##
       format.pval, units
set.seed(42)
original_data <- read_csv("fltrain.csv.gz")</pre>
## Parsed with column specification:
## cols(
     .default = col_double(),
##
##
     carrier = col_character(),
     tailnum = col_character(),
##
     origin = col_character(),
##
##
     dest = col_character(),
     time_hour = col_datetime(format = ""),
##
     name = col_character(),
```

```
## dst = col_character(),
## tzone = col_character(),
## type = col_character(),
## manufacturer = col_character(),
## model = col_character(),
## engine = col_character()
## )
## See spec(...) for full column specifications.
DF <- original_data</pre>
```

10 turning all columns with datatype characters to factors.

```
DF[sapply(DF, is.character)] <- lapply(DF[sapply(DF, is.character)],</pre>
                                      as.factor)
DF$flight <- as.factor(DF$flight)</pre>
str(DF)
## Classes 'spec_tbl_df', 'tbl_df', 'tbl' and 'data.frame': 200000 obs. of 43 variables:
## $ year.x
                   : num 2013 2013 2013 2013 ...
## $ month
                   : num 11 10 12 11 10 11 9 12 11 3 ...
                          7 30 18 20 21 7 29 21 7 31 ...
## $ day
                   : num
                   : num
## $ dep_time
                          600 1252 1723 2029 1620 ...
## $ sched_dep_time: num
                          600 1250 1715 2030 1625 ...
## $ dep_delay
                   : num
                          0 2 8 -1 -5 -8 -10 -4 0 -8 ...
## $ arr_time
                   : num
                          826 1356 2008 2141 1818 ...
## $ sched_arr_time: num 825 1400 2020 2205 1831 ...
## $ arr_delay
                : num 1 -4 -12 -24 -13 -18 -10 -16 4 -11 ...
## $ carrier
                   : Factor w/ 16 levels "9E", "AA", "AS", ...: 15 2 5 15 5 4 6 6 1 13 ...
                   : Factor w/ 3672 levels "1","2","3","4",..: 1525 147 1400 2343 1860 24 3083 3351 20
## $ flight
## $ tailnum
                   : Factor w/ 3957 levels "D942DN", "NOEGMQ",...: 1437 1226 836 565 756 2459 204 2890 6
## $ origin
                   : Factor w/ 3 levels "EWR", "JFK", "LGA": 3 2 3 1 3 1 1 3 2 3 ...
## $ dest
                   : Factor w/ 104 levels "ABQ", "ACK", "ALB", ...: 5 12 54 55 33 54 59 59 27 29 ...
                   : num 123 44 133 107 90 136 110 118 101 47 ...
## $ air time
                   : num 762 187 950 711 502 937 725 738 589 214 ...
## $ distance
                   : num
                          6 12 17 20 16 9 15 15 16 17 ...
## $ minute
                          0 50 15 30 25 0 29 30 50 0 ...
                   : num
                   : POSIXct, format: "2013-11-07 11:00:00" "2013-10-30 16:00:00" ...
## $ time_hour
## $ temp
                          63 59 34 37 63 ...
                   : num
## $ dewp
                   : num
                          55.9 46.9 17.1 18 41 ...
## $ humid
                   : num
                          77.8 64.2 49.5 45.6 44.5 ...
## $ wind_dir
                          210 240 270 20 160 240 180 190 320 140 ...
                   : num
## $ wind_speed
                          13.81 9.21 17.26 5.75 13.81 ...
                   : num
## $ wind_gust
                          NA NA 21.9 NA NA ...
                   : num
                          0 0 0 0 0 0 0 0 0 0 ...
## $ precip
                   : num
## $ pressure
                   : num 1011 1025 1020 1036 1017 ...
## $ visib
                   : num 10 10 10 10 10 10 10 10 10 ...
                   : Factor w/ 100 levels "Akron Canton Regional Airport",..: 37 31 67 17 26 67 32 32
## $ name
## $ lat
                   : num 33.6 42.4 28.4 41.8 42.2 ...
## $ lon
                   : num -84.4 -71 -81.3 -87.8 -83.4 ...
## $ alt
                   : num 1026 19 96 620 645 ...
                   : num -5 -5 -5 -6 -5 -5 -6 -6 -5 -5 ...
## $ tz
```

```
## $ dst
                    : Factor w/ 2 levels "A", "N": 1 1 1 1 1 1 1 1 1 1 ...
## $ tzone
                    : Factor w/ 7 levels "America/Anchorage",..: 5 5 5 2 5 5 2 2 5 5 ...
## $ year.y
                    : num 2001 NA 2002 2006 1992 ...
## $ type
                     : Factor w/ 3 levels "Fixed wing multi engine",..: 1 NA 1 1 1 1 1 1 1 1 ...
   $ manufacturer : Factor w/ 35 levels "AGUSTA SPA", "AIRBUS",..: 10 NA 2 10 3 2 18 11 11 3 ...
## $ model
                    : Factor w/ 126 levels "150", "172E", "172M", ...: 37 NA 80 37 84 88 106 98 99 79 ...
## $ engines
                    : num 2 NA 2 2 2 2 2 2 2 2 ...
## $ seats
                     : num 140 NA 145 140 182 200 55 80 95 179 ...
##
    $ speed
                     : num NA NA NA NA NA NA NA NA NA ...
##
                     : Factor w/ 6 levels "4 Cycle", "Reciprocating",..: 3 NA 3 3 4 3 3 3 3 3 ...
   $ engine
   - attr(*, "spec")=
##
     .. cols(
##
          year.x = col_double(),
##
     . .
          month = col_double(),
##
          day = col_double(),
##
          dep_time = col_double(),
     . .
##
         sched_dep_time = col_double(),
##
          dep delay = col double(),
     . .
##
         arr_time = col_double(),
##
     . .
         sched_arr_time = col_double(),
##
         arr_delay = col_double(),
     . .
##
         carrier = col_character(),
     . .
##
         flight = col_double(),
##
          tailnum = col_character(),
     . .
##
          origin = col_character(),
##
         dest = col_character(),
     . .
##
          air_time = col_double(),
##
         distance = col_double(),
     . .
##
         hour = col_double(),
##
         minute = col_double(),
     . .
##
     . .
         time_hour = col_datetime(format = ""),
##
         temp = col_double(),
     . .
##
          dewp = col_double(),
     . .
##
         humid = col_double(),
##
          wind dir = col double(),
     . .
##
         wind_speed = col_double(),
     . .
##
     . .
          wind gust = col double(),
##
         precip = col_double(),
##
          pressure = col_double(),
     . .
##
         visib = col_double(),
         name = col_character(),
##
     . .
##
         lat = col_double(),
##
         lon = col_double(),
     . .
##
         alt = col_double(),
##
         tz = col_double(),
     . .
##
          dst = col_character(),
     . .
##
          tzone = col_character(),
     . .
##
          year.y = col_double(),
##
          type = col_character(),
##
          manufacturer = col_character(),
     . .
##
         model = col_character(),
     . .
##
     . .
         engines = col_double(),
##
     . .
         seats = col_double(),
##
          speed = col_double(),
     . .
```

```
## .. engine = col_character()
## .. )
```

11 Methods

11.1 Preprocessing

5 2013-10-21 20:00:00

6 2013-11-07 14:00:00

7 2013-09-29 19:00:00

Data preprocessing steps include the following: - Dropping columns that contain data from after the planes' departure which may leak information about the response variable dep_delay. - Dropping columns with too many NAs. - Impute NAs for the remaining columns. - Scaling the data to work well with methods like lasso regression.

11.2 - Dropping columns that contain data from after the planes' departure which may leak information about the response variable dep_delay.

dropping the columns "dep_time", "arr_time", "air_time", "arr_delay", because that leaks the response variable. dropping column "year.x" because all the values are 2013 dropping tailnum because it produces too many dummy variable columns for one hot encoding.

```
library(lubridate)
##
## Attaching package: 'lubridate'
## The following object is masked from 'package:base':
##
##
       date
DF$sched arr time posix <- as.POSIXct(str pad(as.character(DF$sched arr time), 4, pad="0"),format="%H%M
DF$sched_arr_time_hour <- hour(DF$sched_arr_time_posix)</pre>
DF$sched_arr_time_minute <- minute(DF$sched_arr_time_posix)</pre>
#num minute is number of minutes since start of day for scheduled arrival time
DF$sched_arr_time_num_minute <- 60*DF$sched_arr_time_hour + DF$sched_arr_time_minute
DF$sched_dep_time_posix <- as.POSIXct(str_pad(as.character(DF$sched_dep_time),4 , pad="0"),format="%H%M
DF$sched_dep_time_hour <- hour(DF$sched_dep_time_posix)</pre>
DF$sched_dep_time_minute <- minute(DF$sched_dep_time_posix)</pre>
#num minute is number of minutes since start of day for scheduled depival time
DF$sched_dep_time_num_minute <- 60*DF$sched_dep_time_hour + DF$sched_dep_time_minute
select(original_data, time_hour, sched_dep_time, sched_arr_time, tz, tzone)
## # A tibble: 200,000 x 5
                          sched_dep_time sched_arr_time
##
      time_hour
                                                             tz tzone
##
      <dttm>
                                    <dbl>
                                                    <dbl> <dbl> <chr>
   1 2013-11-07 11:00:00
                                      600
                                                     825
                                                             -5 America/New_York
##
   2 2013-10-30 16:00:00
                                     1250
                                                     1400
                                                             -5 America/New_York
    3 2013-12-18 22:00:00
                                                     2020
                                                             -5 America/New York
##
                                     1715
  4 2013-11-21 01:00:00
                                                     2205
                                                             -6 America/Chicago
##
                                     2030
```

1831

1157

1649

-5 America/New York

-5 America/New York

-6 America/Chicago

1625

1529

900

```
8 2013-12-21 20:00:00
                                      1530
                                                     1710
                                                              -6 America/Chicago
## 9 2013-11-07 21:00:00
                                                     1906
                                                              -5 America/New_York
                                      1650
## 10 2013-03-31 21:00:00
                                      1700
                                                     1821
                                                              -5 America/New York
## # ... with 199,990 more rows
select(DF, sched_arr_time, sched_arr_time_hour)
## # A tibble: 200,000 x 2
##
      sched_arr_time sched_arr_time_hour
##
               <dbl>
                                     <int>
##
                 825
                                        8
    1
                1400
                                        14
##
    2
##
   3
                2020
                                        20
##
   4
                2205
                                        22
##
    5
                1831
                                        18
##
    6
                1157
                                        11
##
   7
                1649
                                        16
##
   8
                1710
                                        17
##
    9
                1906
                                        19
## 10
                                        18
                1821
## # ... with 199,990 more rows
DF$sched_air_time <- DF$sched_arr_time_posix - DF$sched_dep_time_posix
drops <- c('sched_arr_time_posix', 'sched_arr_time_hour', 'sched_dep_time_posix', 'sched_dep_time_hour'</pre>
DF <- DF[ , !(names(DF) %in% drops)]</pre>
drops <- c("dep_time", "arr_time", "air_time", "arr_delay", "year.x", 'tailnum')</pre>
DF <- DF[ , !(names(DF) %in% drops)]</pre>
DF
  # A tibble: 200,000 x 37
##
##
              day dep_delay carrier flight origin dest distance temp dewp humid
      month
      <dbl> <dbl>
                       <dbl> <fct>
                                                              <dbl> <dbl> <dbl> <dbl> <
##
                                      <fct>
                                             <fct>
                                                    <fct>
                           O WN
                                             LGA
                                                                     63.0 55.9
                                                                                 77.8
##
    1
         11
                7
                                      1716
                                                    ATL
                                                                762
    2
                                     178
                                             JFK
                                                                     59
                                                                           46.9
##
         10
               30
                           2 AA
                                                    BOS
                                                                187
                                                                                  64.2
##
    3
         12
               18
                           8 DL
                                     1585
                                             LGA
                                                    MCO
                                                                950
                                                                     34.0 17.1
                                                                                  49.5
##
    4
         11
               20
                          -1 WN
                                     3494
                                             EWR
                                                    MDW
                                                                711
                                                                     37.0 18.0
                                                                                  45.6
                                      2231
                                                                     63.0 41
##
    5
         10
               21
                          -5 DL
                                             LGA
                                                    DTW
                                                                502
                                                                                  44.5
##
    6
         11
                7
                          -8 B6
                                     27
                                             EWR
                                                    MCO
                                                                937
                                                                     64.4 55.4 77.3
##
    7
          9
               29
                         -10 EV
                                     4580
                                             EWR
                                                    MKE
                                                                725 69.1 53.1 56.7
    8
         12
                                     5207
                                                                738 57.9
                                                                           46.0 64.5
##
               21
                          -4 EV
                                             LGA
                                                    MKE
##
    9
         11
                7
                           0 9E
                                      2910
                                             JFK
                                                    CVG
                                                                589
                                                                     53.6
                                                                          48.2
                                                                                  81.9
## 10
          3
               31
                          -8 US
                                     2183
                                             LGA
                                                    DCA
                                                                214 51.1 36.0 56.0
    ... with 199,990 more rows, and 26 more variables: wind_dir <dbl>,
       wind_speed <dbl>, wind_gust <dbl>, precip <dbl>, pressure <dbl>,
## #
       visib <dbl>, name <fct>, lat <dbl>, lon <dbl>, alt <dbl>, tz <dbl>,
## #
## #
       dst <fct>, tzone <fct>, year.y <dbl>, type <fct>, manufacturer <fct>,
       model <fct>, engines <dbl>, seats <dbl>, speed <dbl>, engine <fct>,
       sched_arr_time_minute <int>, sched_arr_time_num_minute <dbl>,
## #
       sched_dep_time_minute <int>, sched_dep_time_num_minute <dbl>,
## #
       sched air time <drtn>
## #
## Remove columns with more than 50% NA
DF <- DF[, -which(colMeans(is.na(DF)) > 0.5)]
```

```
DF$sched_air_time <- as.numeric(DF$sched_air_time)</pre>
library(imputeMissings)
##
## Attaching package: 'imputeMissings'
## The following object is masked from 'package:Hmisc':
##
##
       impute
## The following object is masked from 'package:dplyr':
##
##
       compute
impute_model <- imputeMissings::compute(DF, method="median/mode")</pre>
impute_model
## $month
## [1] 7
##
## $day
## [1] 16
##
## $dep_delay
## [1] -2
##
## $carrier
## [1] "UA"
##
## $flight
## [1] "15"
##
## $origin
## [1] "EWR"
##
## $dest
## [1] "ATL"
##
## $distance
## [1] 872
##
## $temp
## [1] 57.2
##
## $dewp
## [1] 42.8
##
## $humid
## [1] 57.69
##
## $wind_dir
## [1] 220
##
## $wind_speed
## [1] 10.35702
```

```
##
## $precip
## [1] 0
##
## $pressure
## [1] 1017.5
## $visib
## [1] 10
##
## $name
## [1] "Hartsfield Jackson Atlanta Intl"
## $lat
## [1] 36.09775
##
## $lon
## [1] -83.35339
##
## $alt
## [1] 433
## $tz
## [1] -5
##
## $dst
## [1] "A"
## $tzone
## [1] "America/New_York"
## $year.y
## [1] 2002
##
## $type
## [1] "Fixed wing multi engine"
##
## $manufacturer
## [1] "BOEING"
##
## $model
## [1] "A320-232"
## $engines
## [1] 2
##
## $seats
## [1] 149
## $engine
## [1] "Turbo-fan"
## $sched_arr_time_minute
## [1] 30
```

```
##
## $sched_arr_time_num_minute
## [1] 957
##
## $sched_dep_time_minute
## [1] 29
## $sched_dep_time_num_minute
## [1] 839
##
## $sched_air_time
## [1] 139
DF <- impute(DF, object=impute_model, flag=TRUE)</pre>
DF <- DF[!duplicated(as.list(DF))] #remove all redundant flag columns that are identical to each other
numeric_only_df <- dplyr::select_if(DF, is.numeric)</pre>
library(corrplot)
## corrplot 0.84 loaded
corrplot(cor(numeric_only_df), type = 'lower')
                          month
                             day
                      dep_delay
                        distancé
                           temp
                           dewp
                          humid
                        wind_dir
                    wind_speed
                          precip
                       pressure
                            visib
                              lat
                              Ion
                              alt
                               tz
                          year.y
                        engines
                           šeats
       sched_arr_time_minute
sched_arr_time_num_minute
sched_dep_time_minute
sched_dep_time_num_minute
                sched_air_time
                                      -0.8 -0.6 -0.4 -0.2
                                                                  0.2
                                                            0
                                                                       0.4
```

12 try features scaling

```
dep_delay_vec <- DF$dep_delay
DF$dep_delay <- NULL
head(DF)</pre>
```

```
month day carrier flight origin dest distance temp dewp humid wind_dir
                          1716
                                  LGA ATL
                                                 762 62.96 55.94 77.83
             7
                    WN
## 2
                           178
                                       BOS
                                                 187 59.00 46.94 64.22
        10
            30
                    AA
                                  JFK
                                                                             240
## 3
                          1585
                                       MCO
                                                 950 33.98 17.06 49.51
        12
            18
                    DL
                                  LGA
                                                                             270
## 4
                    WN
                          3494
                                  EWR
                                       MDW
                                                 711 37.04 17.96 45.58
        11
            20
                                                                              20
## 5
        10
            21
                    DL
                          2231
                                  LGA
                                       DTW
                                                 502 62.96 41.00 44.47
                                                                             160
                                                 937 64.40 55.40 77.29
                                                                             240
## 6
        11
             7
                    B6
                            27
                                  EWR
                                       MCO
##
     wind_speed precip pressure visib
                                                                       name
                                                                                  lat
       13.80936
                      0
                          1011.0
                                           Hartsfield Jackson Atlanta Intl 33.63672
## 2
        9.20624
                      0
                          1024.9
                                    10 General Edward Lawrence Logan Intl 42.36435
                                                               Orlando Intl 28.42939
## 3
       17.26170
                      0
                          1019.8
                                    10
## 4
                          1035.6
                                                       Chicago Midway Intl 41.78597
        5.75390
                      0
                                    10
## 5
       13.80936
                          1016.9
                                    10
                                                    Detroit Metro Wayne Co 42.21244
## 6
       16.11092
                      0
                          1017.5
                                    10
                                                               Orlando Intl 28.42939
           lon alt tz dst
                                       tzone year.y
                                                                         type
## 1 -84.42807 1026 -5
                                                2001 Fixed wing multi engine
                          A America/New_York
## 2 -71.00518
                          A America/New_York
                 19 -5
                                                2002 Fixed wing multi engine
## 3 -81.30899
                          A America/New_York
                 96 -5
                                                2002 Fixed wing multi engine
## 4 -87.75242 620 -6
                          A America/Chicago
                                                2006 Fixed wing multi engine
## 5 -83.35339
                645 -5
                          A America/New_York
                                                1992 Fixed wing multi engine
## 6 -81.30899
                 96 -5
                          A America/New_York
                                                2006 Fixed wing multi engine
                          model engines seats
                                                  engine sched_arr_time_minute
##
         manufacturer
## 1
               BOEING 737-7H4
                                      2
                                          140 Turbo-fan
                                      2
                                          149 Turbo-fan
                                                                              0
## 2
               BOEING A320-232
## 3
               AIRBUS A319-114
                                      2
                                          145 Turbo-fan
                                                                             20
## 4
               BOEING 737-7H4
                                      2
                                          140 Turbo-fan
                                                                              5
## 5 AIRBUS INDUSTRIE A320-211
                                      2
                                          182 Turbo-jet
                                                                             31
                                      2
               AIRBUS A320-232
                                          200 Turbo-fan
                                                                             57
     sched_arr_time_num_minute sched_dep_time_minute sched_dep_time_num_minute
##
## 1
                            505
## 2
                            840
                                                    50
                                                                              770
## 3
                           1220
                                                    15
                                                                             1035
                                                                             1230
## 4
                           1325
                                                    30
## 5
                                                    25
                           1111
                                                                              985
## 6
                            717
                                                                              540
                                                     0
     sched_air_time dep_delay_flag temp_flag wind_dir_flag wind_speed_flag
## 1
                145
                                  0
                                             0
## 2
                 70
                                  0
                                             0
                                                           0
                                                                            0
                                                                            0
## 3
                185
                                  0
                                             0
                                                           0
## 4
                 95
                                  0
                                             0
                                                           0
                                                                            0
## 5
                126
                                  0
                                             0
                                                           0
                                                                            0
## 6
                177
                                  0
                                             0
                                                           0
                                                                            0
     precip_flag pressure_flag name_flag year.y_flag type_flag
## 1
               0
                              0
                                        0
                                                                0
                                                     0
## 2
               0
                              0
                                        0
                                                     1
                                                                1
## 3
               0
                              0
                                        0
                                                     0
                                                                0
## 4
               0
                              0
                                        0
                                                     0
                                                                0
## 5
               0
                              0
                                        0
                                                     0
                                                                0
## 6
               0
                              1
                                         0
                                                                0
```

```
library(dplyr)
DF <- DF %>% mutate_if(is.numeric, scale)
head(DF)
##
       month
                   day carrier flight origin dest
                                                    distance
## 1 1.30322 -0.9929373
                            WN
                                 1716
                                         LGA ATL -0.3777852
                                                              0.3339858
## 2 1.01019
            1.6325235
                            AA
                                  178
                                          JFK
                                              BOS -1.1644742
                                                              0.1127815
## 3 1.59625
             0.2627179
                            DL
                                 1585
                                         LGA
                                              MCO -0.1205721 -1.2848272
## 4 1.30322 0.4910188
                            WN
                                         EWR MDW -0.4475611 -1.1138966
                                 3494
## 5 1.01019 0.6051693
                            DL
                                 2231
                                         LGA DTW -0.7335054 0.3339858
## 6 1.30322 -0.9929373
                            B6
                                   27
                                         EWR MCO -0.1383581 0.4144237
##
          dewp
                    humid
                             wind_dir wind_speed
                                                     precip
                                                               pressure
     0.7418623 0.9315583
                           ## 2 0.2753242 0.2375566
                           0.36735789 -0.3415806 -0.1492223 1.01596006 0.3664282
## 3 -1.2735821 -0.5125364
                           0.65754261
                                       1.1087096 -0.1492223
                                                            0.28792159 0.3664282
## 4 -1.2269283 -0.7129351 -1.76066338 -0.9631336 -0.1492223 2.54341334 0.3664282
## 5 -0.0325909 -0.7695363 -0.40646802 0.4871566 -0.1492223 -0.12606108 0.3664282
                                       0.9015253 -0.1492223 -0.04040949 0.3664282
## 6 0.7138700 0.9040226
                          0.36735789
##
                                  name
                                              lat
                                                        lon
                                                                    alt.
## 1
       Hartsfield Jackson Atlanta Intl -0.4207546 0.3298674
                                                             0.48364704
## 2 General Edward Lawrence Logan Intl 1.1190951 1.2378347 -0.60619417
                          Orlando Intl -1.3395034 0.5408516 -0.52285973
## 3
## 4
                   Chicago Midway Intl 1.0170501 0.1049977 0.04424731
## 5
                Detroit Metro Wayne Co 1.0922942 0.4025621 0.07130394
## 6
                          Orlando Intl -1.3395034 0.5408516 -0.52285973
##
                               tzone
                                         year.y
                                                                   type
## 1 0.6826595
                 A America/New_York -0.08500492 Fixed wing multi engine
     0.6826595
                 A America/New York 0.08617407 Fixed wing multi engine
## 3
     0.6826595
                 A America/New_York 0.08617407 Fixed wing multi engine
## 4 -0.2514221
                 A America/Chicago 0.77089000 Fixed wing multi engine
     0.6826595
                 A America/New_York -1.62561576 Fixed wing multi engine
## 5
     0.6826595
                 A America/New York 0.77089000 Fixed wing multi engine
##
                                 engines
         manufacturer
                        model
                                              seats
                                                       engine
## 1
              BOEING
                      737-7H4 0.05879311 0.02232546 Turbo-fan
## 2
              BOEING A320-232 0.05879311 0.15869100 Turbo-fan
              AIRBUS A319-114 0.05879311 0.09808410 Turbo-fan
              BOEING 737-7H4 0.05879311 0.02232546 Turbo-fan
## 5 AIRBUS INDUSTRIE A320-211 0.05879311 0.65869797 Turbo-jet
              AIRBUS A320-232 0.05879311 0.93142905 Turbo-fan
     sched_arr_time_minute sched_arr_time_num_minute sched_dep_time_minute
## 1
               -0.2348938
                                         -1.4325947
                                                              -1.36042229
## 2
                -1.6716145
                                         -0.3129587
                                                               1.23408583
## 3
               -0.5222379
                                          0.9570761
                                                              -0.58206985
## 4
                                          1.3080068
                -1.3842703
                                                               0.19628258
## 5
                0.1099192
                                          0.5927766
                                                              -0.06316823
## 6
                1.6041087
                                         -0.7240489
                                                              -1.36042229
     sched_dep_time_num_minute sched_air_time dep_delay_flag temp_flag
## 1
                   -1.6236293
                                  0.14883297
                                                          0
                                                                    0
## 2
                   -0.1673447
                                 -0.24317221
                                                          0
                                                                    0
## 3
                                                          0
                                                                    0
                    0.7739125
                                  0.35790240
## 4
                     1.4665357
                                 -0.11250381
                                                          0
                                                                    0
## 5
                                                          0
                                                                    0
                    0.5963168
                                  0.04952499
## 6
                   -0.9842849
                                  0.31608852
                                                          0
     wind_dir_flag wind_speed_flag precip_flag pressure_flag name_flag year.y_flag
```

```
0
                                                                  0
                                                                                           0
## 1
                                     0
                                                                  0
## 2
                   0
                                     0
                                                  0
                                                                              0
                                                                                           1
## 3
                                                  0
                                                                  0
                                                                              0
                                                                                           0
                   0
                                     0
## 4
                   0
                                     0
                                                  0
                                                                  0
                                                                             0
                                                                                           0
## 5
                   0
                                     0
                                                  0
                                                                  0
                                                                              0
                                                                                           0
## 6
                   0
                                     0
                                                  0
                                                                              0
                                                                                           0
     type_flag
## 1
              0
## 2
              1
## 3
              0
## 5
              0
## 6
              0
DF$dep_delay <- dep_delay_vec
#take out extreme departure delays
DF<-DF[DF$dep_delay < 30,]</pre>
set.seed(42)
DF$flight <- NULL
train_index <- sample(1:nrow(DF),size=2*nrow(DF)/3,replace=FALSE)</pre>
train_df <- DF[train_index,]</pre>
test_df <- DF[-train_index,]</pre>
```

13 predicting 0

```
rmse = mean((test_df$dep_delay-0)^2) %>% sqrt()
rmse
## [1] 8.30571
```

14 predicting the mean

```
rmse = mean((test_df$dep_delay-mean(train_df$dep_delay))^2)%>% sqrt()
rmse
## [1] 8.299767
```

15 predicting the median

```
rmse = mean((test_df$dep_delay-median(train_df$dep_delay))^2)%>% sqrt()
rmse
## [1] 8.469257
```

16 linear regression with dep

```
model <- lm(dep_delay ~ ., data=train_df)</pre>
model_without_dep <- lm(dep_delay ~ .-dest, data=train_df)</pre>
anova(model, model_without_dep)
## Analysis of Variance Table
## Model 1: dep_delay ~ month + day + carrier + origin + dest + distance +
##
       temp + dewp + humid + wind_dir + wind_speed + precip + pressure +
##
       visib + name + lat + lon + alt + tz + dst + tzone + year.y +
##
      type + manufacturer + model + engines + seats + engine +
##
       sched_arr_time_minute + sched_arr_time_num_minute + sched_dep_time_minute +
##
       sched_dep_time_num_minute + sched_air_time + dep_delay_flag +
       temp_flag + wind_dir_flag + wind_speed_flag + precip_flag +
##
##
       pressure_flag + name_flag + year.y_flag + type_flag
## Model 2: dep_delay ~ (month + day + carrier + origin + dest + distance +
##
       temp + dewp + humid + wind_dir + wind_speed + precip + pressure +
##
       visib + name + lat + lon + alt + tz + dst + tzone + year.y +
##
       type + manufacturer + model + engines + seats + engine +
       sched_arr_time_minute + sched_arr_time_num_minute + sched_dep_time_minute +
##
       sched_dep_time_num_minute + sched_air_time + dep_delay_flag +
##
       temp_flag + wind_dir_flag + wind_speed_flag + precip_flag +
##
       pressure_flag + name_flag + year.y_flag + type_flag) - dest
     Res.Df
               RSS Df Sum of Sq
                                    F
                                         Pr(>F)
## 1 113488 7240975
                        -1263.7 6.602 0.0001863 ***
## 2 113491 7242239 -3
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary <- round(summary(model)$coefficients,6)</pre>
sorteddf <- summary[order(summary[,ncol(summary)]),]</pre>
head(sorteddf)
##
              Estimate Std. Error
                                    t value Pr(>|t|)
## carrierFL 4.615319 0.887510 5.200301
## carrierUA 2.440853 0.484369 5.039237
                                                     0
## originJFK 1.037568 0.117779
                                   8.809419
                                                     0
## wind speed 0.291278 0.027929 10.429081
                                    7.068777
                                                     0
## precip
              0.206814 0.029257
             -0.294549
## pressure
                         0.027059 -10.885462
head(sorteddf)
              Estimate Std. Error
                                    t value Pr(>|t|)
## carrierFL 4.615319 0.887510
                                   5.200301
## carrierUA
              2.440853 0.484369
                                   5.039237
                                                     0
## originJFK
              1.037568 0.117779
                                                     0
                                     8.809419
## wind_speed 0.291278
                         0.027929 10.429081
                                                     0
## precip
              0.206814
                         0.029257
                                    7.068777
                                                     0
## pressure -0.294549
                          0.027059 -10.885462
                                                     0
lm_test_df <- test_df</pre>
in_test_but_not_train <- setdiff(unique(lm_test_df$model), unique(train_df$model))</pre>
```

```
lm_test_df <- lm_test_df[!lm_test_df$model %in% in_test_but_not_train, ]</pre>
in_test_but_not_train <- setdiff(unique(lm_test_df$dest), unique(train_df$dest))</pre>
lm_test_df <- lm_test_df[ !lm_test_df$dest %in% in_test_but_not_train, ]</pre>
preds = predict(model, newdata=lm_test_df)
## Warning in predict.lm(model, newdata = lm_test_df): prediction from a rank-
## deficient fit may be misleading
rmse = sqrt(mean((lm_test_df$dep_delay - preds)^2))
## [1] 7.989994
17
      gbm
set.seed(42)
library(gbm)
## Loaded gbm 2.1.5
model <- gbm(dep_delay ~ ., data=train_df,</pre>
              n.trees=1000, shrinkage=0.003) # default shrinkage = 0.1
## Distribution not specified, assuming gaussian ...
preds = predict(model, newdata=test_df, n.trees=1000)
rmse = sqrt(mean((test_df$dep_delay - preds)^2))
rmse
## [1] 8.087401
summary(model)
dest
humid
4
seats
```

30

40

20

Relative influence

0

10

```
##
                                                          rel.inf
                                                   var
## sched_dep_time_num_minute sched_dep_time_num_minute 40.6986232
                                                 model 31.6301128
## model
## carrier
                                               carrier 10.3426814
## dest
                                                  dest 8.9487938
## sched arr time num minute sched arr time num minute 3.1929834
## origin
                                                origin 2.1249675
## month
                                                 month
                                                       1.8339690
## dewp
                                                  dewp 0.9995901
## precip
                                                precip 0.2282788
## day
                                                   day
                                                        0.0000000
## distance
                                                        0.0000000
                                              distance
## temp
                                                  temp 0.0000000
## humid
                                                 humid 0.000000
## wind_dir
                                              wind_dir 0.0000000
## wind_speed
                                            wind_speed 0.0000000
## pressure
                                              pressure 0.0000000
## visib
                                                 visib 0.0000000
                                                  name 0.0000000
## name
## lat
                                                   lat 0.0000000
                                                   lon 0.0000000
## lon
## alt
                                                   alt 0.0000000
## tz
                                                    tz 0.0000000
## dst
                                                   dst 0.0000000
## tzone
                                                 tzone 0.0000000
## year.y
                                                year.y 0.0000000
                                                        0.0000000
## type
                                                  type
## manufacturer
                                          manufacturer 0.0000000
## engines
                                               engines 0.0000000
## seats
                                                 seats 0.0000000
## engine
                                                engine
                                                        0.0000000
## sched_arr_time_minute
                                 sched_arr_time_minute
                                                        0.0000000
                                 sched_dep_time_minute
## sched_dep_time_minute
                                                        0.0000000
## sched_air_time
                                        sched_air_time
                                                        0.0000000
## dep delay flag
                                        dep_delay_flag
                                                        0.0000000
## temp_flag
                                             temp_flag 0.0000000
## wind dir flag
                                         wind dir flag 0.0000000
## wind_speed_flag
                                       wind_speed_flag
                                                        0.0000000
## precip_flag
                                           precip_flag 0.0000000
## pressure_flag
                                         pressure_flag 0.0000000
## name flag
                                             name flag
                                                        0.0000000
## year.y_flag
                                           year.y flag
                                                        0.0000000
## type_flag
                                             type flag
                                                        0.0000000
```

Here, you can see the relative influence for each variable for gbm.

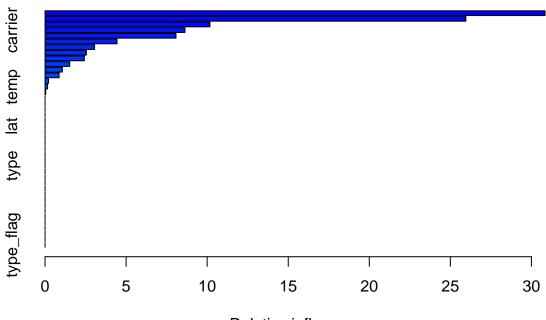
For a gbm, the improvement in the splitting criterion (which is mean squared error for regression) for a given variable is calculated at each step. The relative influence for a given variable is the average of these improvements over all the trees where the aforementioned variable is used.

Distribution not specified, assuming gaussian ...

```
preds = predict(model, newdata=test_df, n.trees=1000)
rmse = sqrt(mean((test_df$dep_delay - preds)^2))
rmse
```

[1] 7.980812

summary(model)



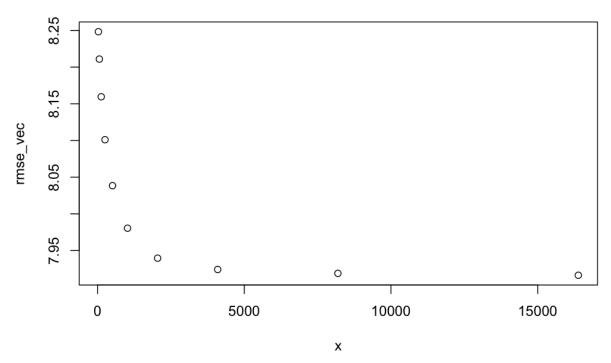
Relative influence

```
rel.inf
## sched_dep_time_num_minute sched_dep_time_num_minute 30.83853917
## model
                                                 model 25.95730577
## dest
                                                  dest 10.17043661
## carrier
                                               carrier 8.62897727
## month
                                                 month 8.07615687
## dewp
                                                  dewp 4.43848169
## origin
                                                origin 3.05562665
## sched_arr_time_num_minute sched_arr_time_num_minute
                                                        2.54883378
## precip
                                                        2.42172931
                                                 precip
## pressure
                                              pressure 1.52135832
## humid
                                                 humid 1.06685951
## dep_delay_flag
                                        dep_delay_flag 0.86763349
## pressure_flag
                                         pressure_flag
                                                        0.21490352
## temp
                                                  temp
                                                        0.15460862
## day
                                                   day
                                                        0.03854943
## distance
                                              distance
                                                        0.00000000
## wind_dir
                                              wind_dir
                                                        0.00000000
## wind_speed
                                            wind_speed 0.00000000
## visib
                                                 visib
                                                        0.00000000
## name
                                                        0.00000000
                                                  name
## lat
                                                   lat
                                                        0.00000000
## lon
                                                   lon 0.00000000
## alt
                                                    alt 0.00000000
                                                    tz 0.00000000
## tz
```

```
## dst
                                                      dst 0.00000000
## tzone
                                                    tzone 0.00000000
## year.y
                                                   year.y
                                                           0.00000000
## type
                                                           0.00000000
                                                     type
## manufacturer
                                            manufacturer
                                                           0.00000000
                                                  engines 0.00000000
## engines
## seats
                                                    seats 0.00000000
## engine
                                                   engine 0.00000000
                                   sched_arr_time_minute 0.00000000
## sched_arr_time_minute
## sched_dep_time_minute
                                   sched_dep_time_minute 0.0000000
                                          sched_air_time 0.00000000
## sched_air_time
## temp_flag
                                                temp_flag 0.00000000
## wind_dir_flag
                                           wind_dir_flag 0.00000000
## wind_speed_flag
                                         wind_speed_flag 0.00000000
## precip_flag
                                             precip_flag 0.0000000
## name_flag
                                                name_flag 0.00000000
## year.y_flag
                                             year.y_flag 0.00000000
## type_flag
                                                type_flag
                                                           0.0000000
rmse = sqrt(mean((test_df$dep_delay - preds)^2))
rmse
## [1] 7.980812
set.seed(42)
x <- 2^seq(5,14, by=1) rmse vec <- numeric(length(x)) count <- 1 for (val in x) { hboost <- gbm( dep delay
~., data = train_df, n.trees = val, distribution = 'gaussian', shrinkage = 0.01 ) preds = predict(hboost, n.trees
= val, newdata = test\_df) mse = mean((test\_df\$dep\_delay - preds) ^ 2) rmse <- sqrt(mse) rmse\_vec[count]
<- rmse
print(val) print(rmse) count = count + 1 
plot(x, rmse vec)
summary(hboost) class(summary(hboost)) summary <- summary(hboost) write.csv(summary, '16384trees gbm.csv')
gbm_benchmark<-read_csv('shrinkage_Opoint01_numtrees_32_to_16384_gbm_benchmark.csv')</pre>
## Warning: Missing column names filled in: 'X1' [1]
## Parsed with column specification:
##
     X1 = col_double(),
     num_trees = col_double(),
##
##
     rmse = col_double()
## )
gbm_benchmark
## # A tibble: 10 x 3
         X1 num trees rmse
##
##
      <dbl>
                 <dbl> <dbl>
##
   1
          1
                    32 8.25
##
    2
          2
                    64 8.21
##
    3
          3
                   128 8.16
##
   4
          4
                   256 8.10
##
   5
          5
                   512 8.04
                  1024 7.98
##
    6
          6
```

```
7
##
    7
                   2048
                          7.94
    8
           8
                   4096
                          7.92
##
                   8192
##
    9
           9
                          7.92
                  16384
## 10
          10
                          7.92
```

Above values are for gbm with shrinkage of 0.01 Analysis:



Tuning gbm

Here I plotted root mean squared error (rmse) vs the number of trees for shrinkage of 0.01 and all other variables as default for gbm. You can see that after around 5000 trees, increasing the number of trees further gives diminishing returns.

library(EZtune) response <- DF $dep_delayeztune_df < -DFeztune_df$ dep_delay <- NULL eztune_obj <- eztune(eztune_df, response, method = "gbm", optimizer = "hjn", fast = TRUE, cross = NULL)

\$n.trees [1] 2001

 $\frac{10}{10}$

\$n.minobsinnode [1] 7

\$shrinkage [1] 0.001

\$mse [1] 72.68835

 $modelgbm :: gbm(formula = y ., distribution = "gaussian", data = dat, n.trees = results n.trees, interaction.depth = results interaction.depth, n.minobsinnode = results n.minobsinnode, shrinkage = results \shrinkage) A gradient boosted model with gaussian loss function. 2001 iterations were performed. There were 42 predictors of which 24 had non-zero influence.$

References

"Gradient Boosting Machines · UC Business Analytics R Programming Guide." 2019. http://uc-r.github.io/gbm_regression#h2o.