

1. Assume the runners in a race have run times which follow a normal distribution with a mean of 122 seconds and a sd of 6 seconds. Answer the following.

- (a) What are the subject, variable and variable type?

The subject is a runner, the run time is the variable, and it is a quantitative / numeric variable.

- (b) What is the chance of three randomly selected runners all having a time of less than 122 seconds?

Since it's normal, we have a 50% chance of being below 122. Consider that this happens independently and we need this to happen three times, so $\frac{1}{2}^3 = \frac{1}{8}$

Independence guarantees that the probability can be calculated by multiplication.

- (c) What is the chance of a randomly selected runner having a time of greater than 128 seconds?

z-score = 1, $P(Z > 1) = 0.16$

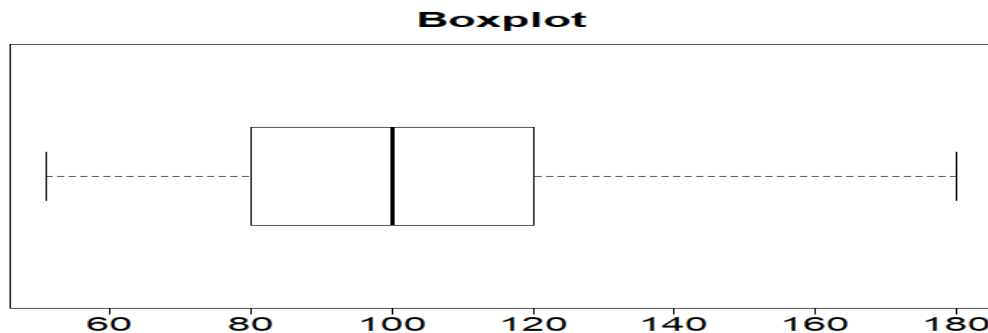
Use the formula $z - \text{score} = \frac{\text{Observation} - \text{Average}}{SD}$. And then use z-table to check the quantile.

- (d) What is the chance that, if we randomly selected two runners, exactly one will have a run time greater than 128 seconds?

*$2 * 0.16 * (1 - 0.16) = 0.27$*

We could interpret this as follows: the first one has a run time greater than 128 seconds and the second one has a run time smaller than 128 seconds or the second one has a run time greater than 128 seconds and the first one has a run time smaller than 128 seconds. Then, we can calculate the chance for this two possible situations.

2. Examine the following boxplot. The underlying data set has a sd of 40.



- (a) Can we conclude that 68% of the data is in the interval [60, 140]? Why or why not?

No, we can't assume it's normal. It specifically looks not normal, because it seems to be right skewed.

Note: if some data is normally distributed, then we could use z-score to calculate its distribution.

- (b) What is the probability that a randomly chosen value is in the interval 120 to 180?

This is between the third quartile and the maximum, so it contains 25% of the data and we have a 25% chance of finding a value there.

If without the boxplot and assuming the distribution to be normal, then we could use z-score to compute it.

- (c) Will the mean be less than, greater than, or about equal to the median?

Likely greater than, as the data appears to be skewed right.