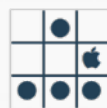


SEMINR

ANALYSE FACTORIELLE MULTI-GROUPE

CHRISTOPHE LALANNE



www.aliquote.org

“ (...) the first thing a psychologist, who has proposed a measure for a theoretical attribute, would do is to spell out the nature and form of the relationship between the attribute and its measures. The researcher would, for instance, posit a hypothesis on the structure (e.g., continuous or categorical) of the attribute, on its dimensionality, on the link between that structure and scores on the proposed measurement instruments (e.g., parametric or nonparametric), and offer an explanation of the actual workings of the instrument.” — Borsboom (2006)

RAPPELS SUR LA CFA

LAVAN:CFA

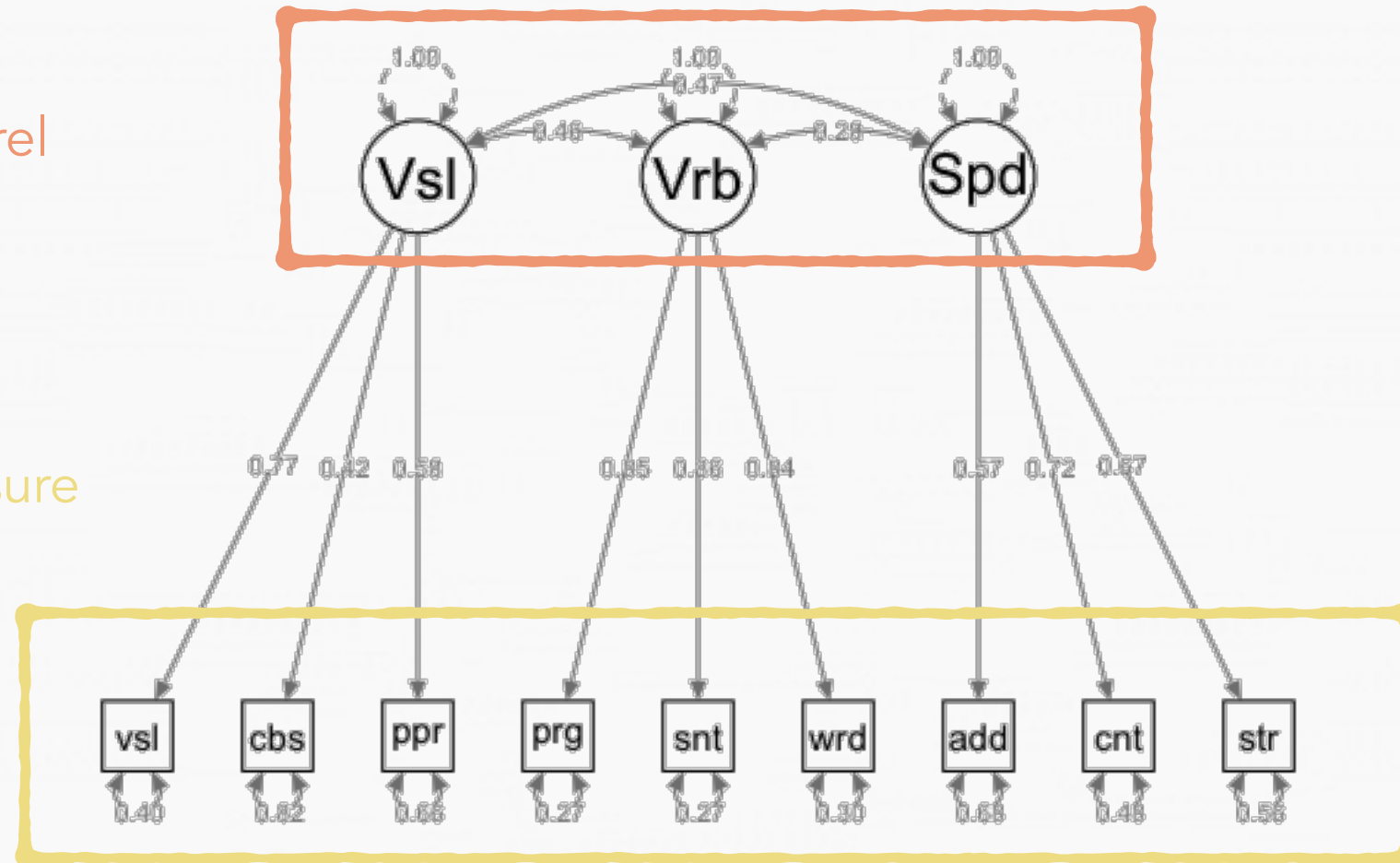
- ✓ Spécification d'un **modèle réflexif** :
 - =~ régression MV - LV
 - ~~ covariance LV-LV
 - ~ régression LV-LV
 - == contraintes (identification ou autre)
 - := construction d'un nouveau terme de modèle
- ✓ Saisie des données : données individuelles ou matrice de covariance (corrélation)
+ nombre d'observations (sample.cov= et sample.obs=)
- ✓ Méthode de standardisation (MV (1ère variable) ou LV (variance unité))
- ✓ Estimation du modèle : cfa() ou sem() (basé sur lavaan())
- ✓ Affichage des résultats : summary(), parameterEstimates()
- ✓ Diagnostic du modèle : fitMeasures(), residuals(), anova() (comparaison de modèles)

MODELE STRUCTUREL

Holzinger & Swinburne (1939)

Modèle structurel

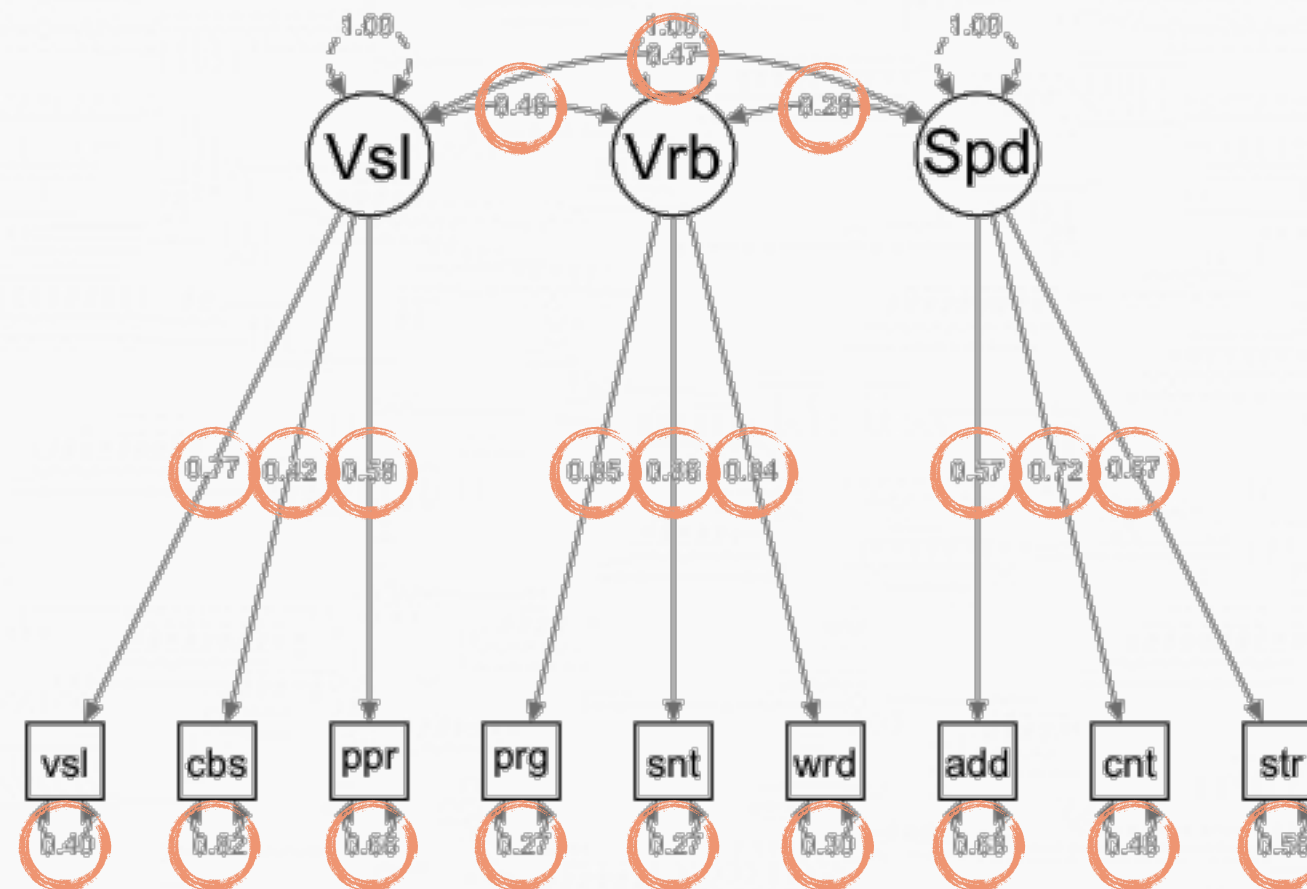
Modèle de mesure



IDENTIFICATION

Holzinger & Swinburne (1939)

21 paramètres estimés

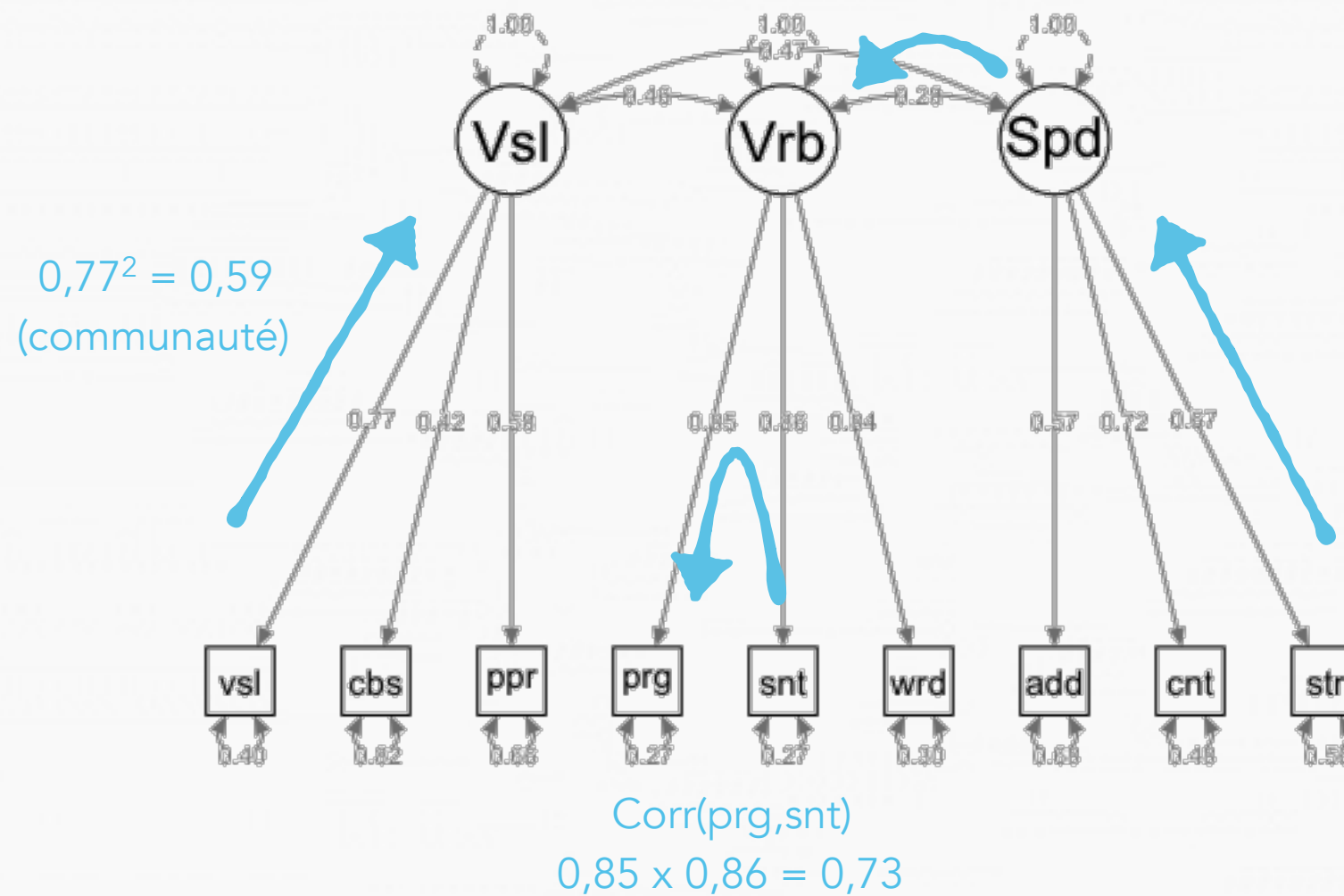


$p(p+1)/2 (+m)$
termes
non redondants

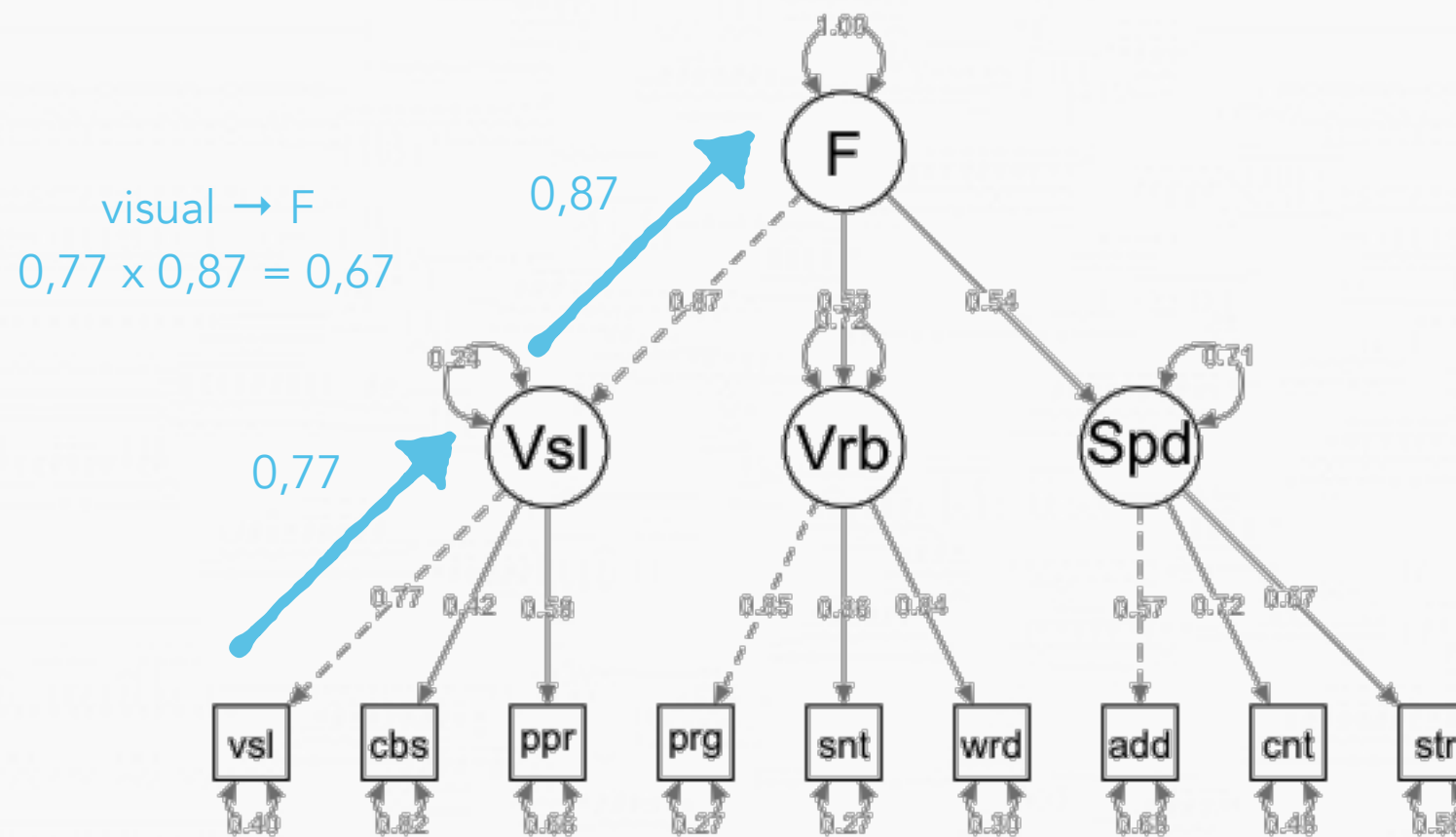
INTERPRETATION

« tracing rules »

straight → Verbal
 $0,67 \times 0,28 = 0,19$



MODELE DE 2ND ORDRE



COVARIANCE-BASED MODELS

cfa2.R

données

```
Console ~/Desktop/SEMinR/
> cov(d)
      visual  cubes  paper  paragra  sentence  wordm  addition  counting  straight
visual  1.363  0.4087 0.5818   0.507   0.442 0.456   0.0850   0.265   0.460
cubes   0.409  1.3864 0.4526   0.210   0.212 0.248  -0.0971   0.110   0.245
paper   0.582  0.4526 1.2791   0.209   0.113 0.245   0.0886   0.213   0.375
paragra 0.507  0.2096 0.2089   1.355   1.101 0.899   0.2205   0.126   0.244
sentence 0.442  0.2118 0.1127   1.101   1.665 1.018   0.1435   0.181   0.296
wordm   0.456  0.2484 0.2449   0.899   1.018 1.200   0.1446   0.166   0.237
addition 0.085 -0.0971 0.0886   0.220   0.143 0.145   1.1871   0.537   0.375
counting 0.265  0.1100 0.2130   0.126   0.181 0.166   0.5370   1.025   0.459
straight 0.460  0.2448 0.3751   0.244   0.296 0.237   0.3745   0.459   1.018

> resid(r)
$type
[1] "raw"

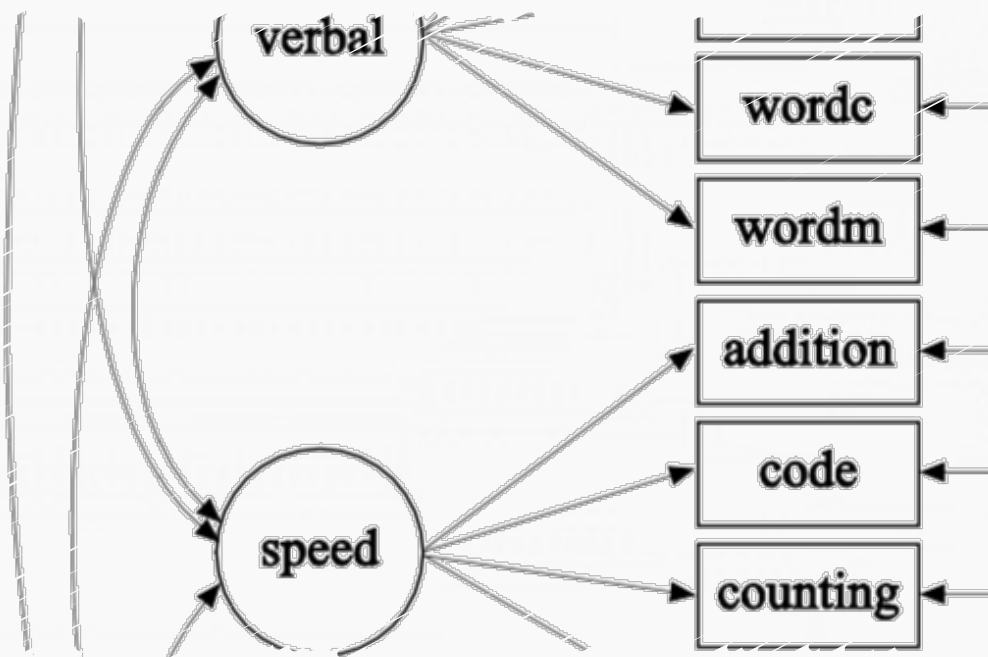
$cov
      visual  cubes  paper  pargrp  sentnc  wordm  additn  contng  strght
visual  0.000
cubes   0.275  0.000
paper   0.452  0.386  0.000
paragra 0.002 -0.046 -0.040  0.000
sentence -0.112 -0.070 -0.160  0.030  0.000
wordm   -0.013  0.010  0.014 -0.008  0.021  0.000
addition -0.015 -0.148  0.039  0.026 -0.070 -0.036  0.000
counting 0.160  0.057  0.161 -0.075 -0.040 -0.021  0.495  0.000
straight 0.301  0.164  0.296 -0.061 -0.040 -0.047  0.313  0.394  0.000
```

erreurs
(écarts au
modèle)

Modèle = données + erreurs

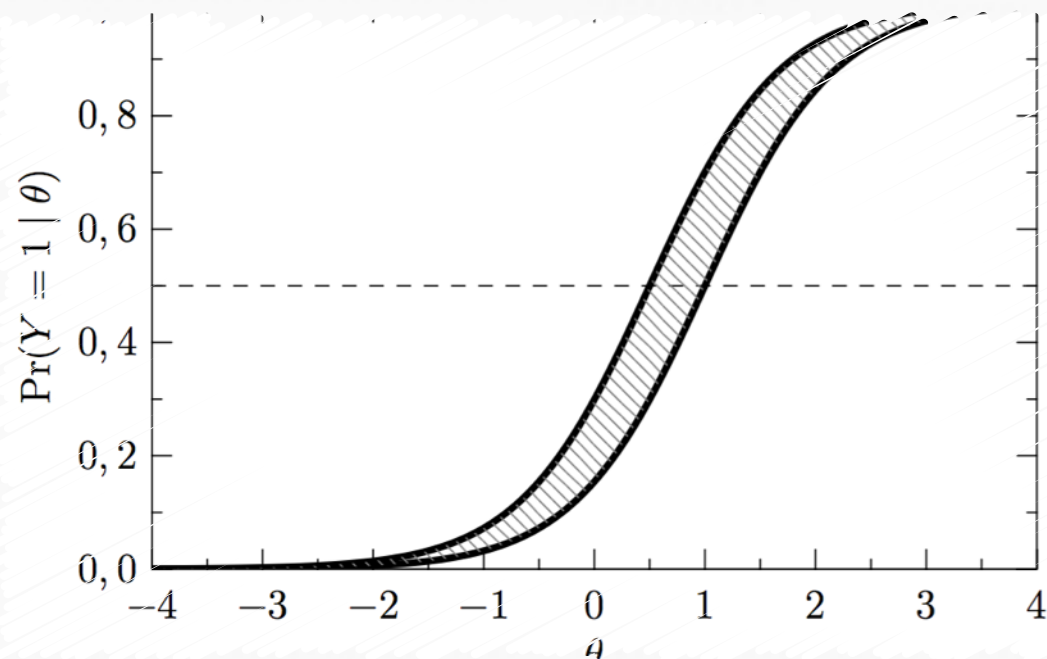
(matrice de covariance avec dénominateur à N, méthode ML)

QUALITE DU MODELE



SPECIFICATION

- comparaison de modèles (RMSEA, CFI, R^2 , etc.)
- indices de modification (erreurs corrélées, EPC)
- interprétation, modèle structurel



INVARIANCE DE MESURE

- équivalence du modèle de mesure dans des sous-populations
- biais de fonctionnement différentiel des items

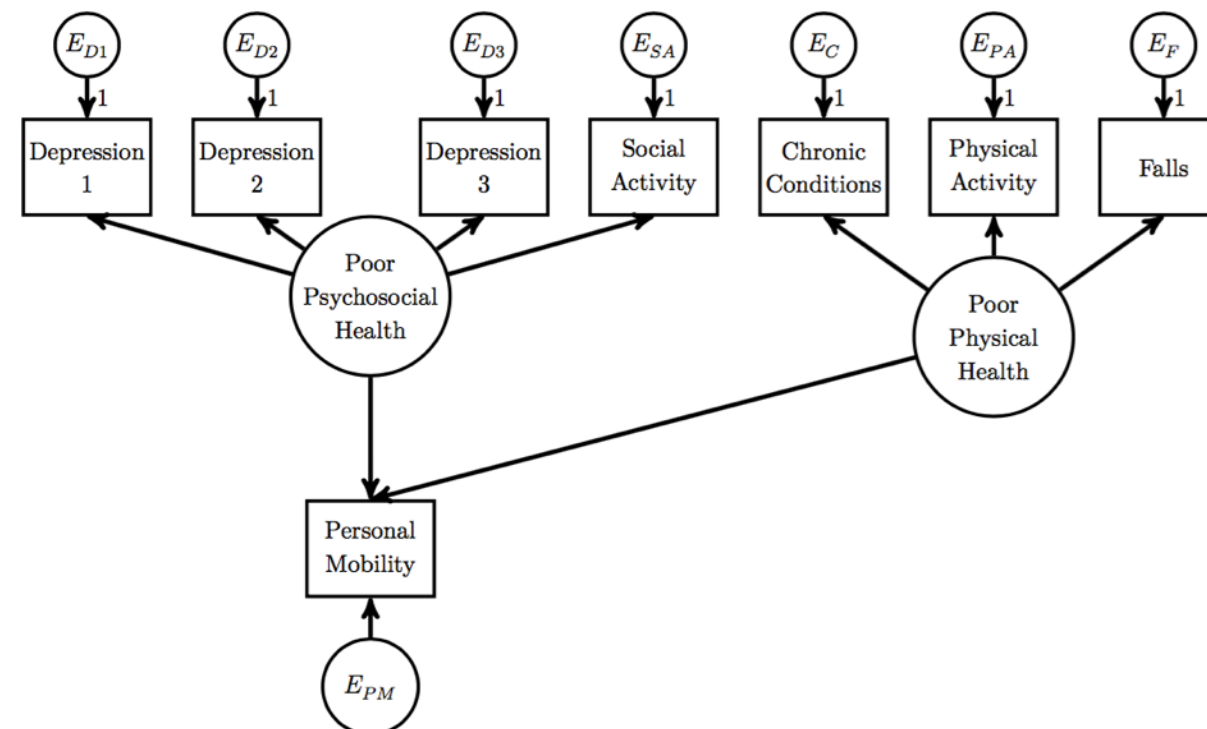
APPLICATION

Beaujean (2014)

	D1	D2	D3	SA	F	CC	PA	PM
Depression 1	0.77	0.38	0.39	-0.25	0.31	0.24	-3.16	-0.92
Depression 2	0.38	0.65	0.39	-0.32	0.29	0.25	-3.56	-0.88
Depression 3	0.39	0.39	0.62	-0.27	0.26	0.19	-2.63	-0.72
Social Activity	-0.25	-0.32	-0.27	6.09	-0.36	-0.18	6.09	0.88
Falls	0.31	0.29	0.26	-0.36	7.67	0.51	-3.12	-1.49
Chronic Conditions	0.24	0.25	0.19	-0.18	0.51	1.69	-4.58	-1.41
Physical Activity	-3.16	-3.56	-2.63	6.09	-3.12	-4.58	204.79	16.53
Personal Mobility	-0.92	-0.88	-0.72	0.88	-1.49	-1.41	16.53	7.24

Data taken from Umstattd-Meyer et al. (2013, pp. 4-5)

Les facteurs psychosociaux et de santé physiques sont-ils prédictifs de la mobilité ?



INVARIANCE DE MESURE

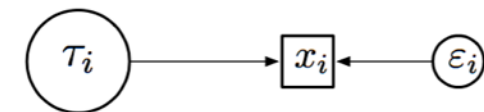
THEORIE DES TESTS

(a₁) τ -equivalence, $\tau_i = \tau_j$

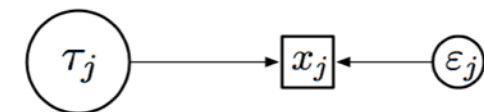
(a₂) essential τ -equivalence, $\tau_i = \tau_j + \lambda_{ij}$, $\lambda_{ij} \in \mathbb{R}$

(a₃) τ -congenerity, $\tau_i = \lambda_{ij0} + \lambda_{ij1}\tau_j$, $\lambda_{ij0}, \lambda_{ij1} \in \mathbb{R}, \lambda_{ij1} > 0$

(b) uncorrelated errors, $\text{cov}(\varepsilon_i, \varepsilon_j) = 0, \forall i \neq j$



(c) equal error variances, $\mathbb{V}(\varepsilon_i) = \mathbb{V}(\varepsilon_j)$



A1, B ET C = TESTS PARALLELES

A2 ET B = TESTS TAU-EQUIVALENT

A3 ET B = TESTS CONGENERIQUES

INVARIANCE DE MESURE

MODELE DE MESURE

- ✓ Invariance configurale : structure factorielle identique entre groupes
- ✓ Invariance faible : égalité des charges factorielles entre groupes
- ✓ Invariance forte : égalité des moyennes (ordonnées à l'origine) entre groupes
- ✓ Invariance stricte : égalité des erreurs (variances) entre groupes
- ✓ Invariance stricte + égalité des variances LV
- ✓ Invariance stricte + égalité des variances LV + égalité des moyennes LV
- ✓ Invariance partielle : conditions non vérifiées pour l'ensemble des MV

MODELE STRUCTUREL

	Type of Invariance	Constraints	Between-Groups Comparisons Allowed
1	Configural	Same model. No parameter constraints.	None
2	Weak	1 + all loadings constrained to be equal between groups (but can vary within a group). Latent (co)variances allowed to vary between groups.	Latent (co)variances [weak evidence]
3	Strong	2 + all intercepts are constrained to be equal between groups (but can vary within a group). Latent means allowed to vary between groups.	Latent means, latent (co)variances [strong evidence]
4	Strict	3 + error variances are constrained to be the same between groups (but can vary within a group).	

Models with larger numbers are nested within the models with smaller numbers.

Beaujean (2014)

DONNEES CATEGORIELLES

CATEGORIES ET DIMENSIONS

- ✓ Analyse factorielle : MV et LV supposées continues.
- ✓ Cas des MV catégorielles ? Deux types : dichotomiques (oui/non) ou polytomiques (type Likert).
- ✓ Solution : modèle de type IRT ou CFA sur matrice de corrélation appropriée (IFA ; package R polycor, psych::fa.poly, psych::irt.fa), choix d'un estimateur approprié (WLSM(V)/DWLS et paramétrisation theta ; Muthén, 1993).
- ✓ Le package lavaan permet de traiter le cas des variables catégorielles et fournit des modèles à seuils (Beaujean, 2014 ; chap. 6).

ESTIMATEURS WLS

Table A.2 Robust Estimators Available in lavaan.

Estimator Variant	Description
<i>Maximum Likelihood (ML)</i>	
MLM	Estimation with robust standard errors and Satorra-Bentler scaled test statistic. For complete data only.
MLMVS	Estimation with robust standard errors and a mean- and variance-adjusted test statistic (Satterthwaite approach). For complete data only.
MLMV	Estimation with robust standard errors and a mean- and variance-adjusted test statistic (scale-shifted approach). For complete data only.
MLF	Estimation with standard errors based on the first-order derivatives and a conventional test statistic. For both complete and incomplete data.
MLR	Estimation with robust (Huber-White) standard errors and a scaled test statistic that is asymptotically equal to the Yuan-Bentler test statistic. For both complete and incomplete data.
<i>Least-Squares (DWLS/ULS)</i>	
WLSM ^{a,b}	Weighted least squares estimation with robust standard errors and a mean-adjusted test statistic. For complete data only.
WLSMVS ^{a,b}	Weighted least squares estimation with robust standard errors and a mean- and variance-adjusted test statistic (Satterthwaite approach). For complete data only.
WLSMV ^{a,b}	Weighted least squares estimation with robust standard errors and a mean- and variance-adjusted test statistic (scale-shifted approach). For complete data only.
ULSM	Unweighted least squares estimation with robust standard errors and a mean-adjusted test statistic. For complete data only.
ULSMVS	Unweighted least squares estimation with robust standard errors and a mean- and variance-adjusted test statistic (Satterthwaite approach). For complete data only.
ULSMV	Unweighted least squares estimation with robust standard errors and a mean- and variance-adjusted test statistic (scale-shifted approach). For complete data only.

^a For the robust weighted least squares variants (WLSM, WLSMVS, WLSMV), lavaan uses the diagonal of the weight matrix for estimation, but uses the full weight matrix to correct the standard errors and to compute the test statistic.

^b As of version 05.15 in lavaan, categorical data can have missing data using missing="pairwise" argument.

Mplus, lavaan
(≠ EQS, Stata)

Beaujean (2014)

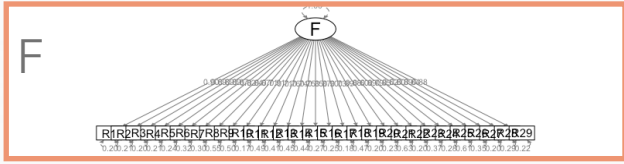
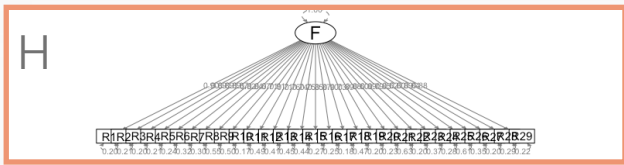
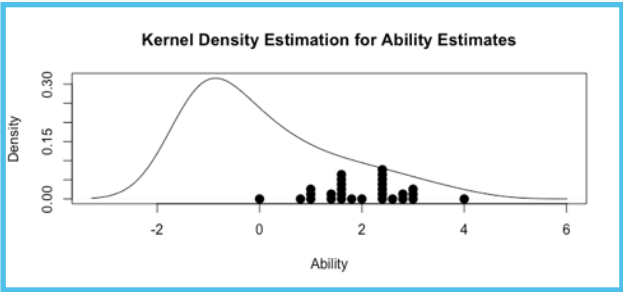
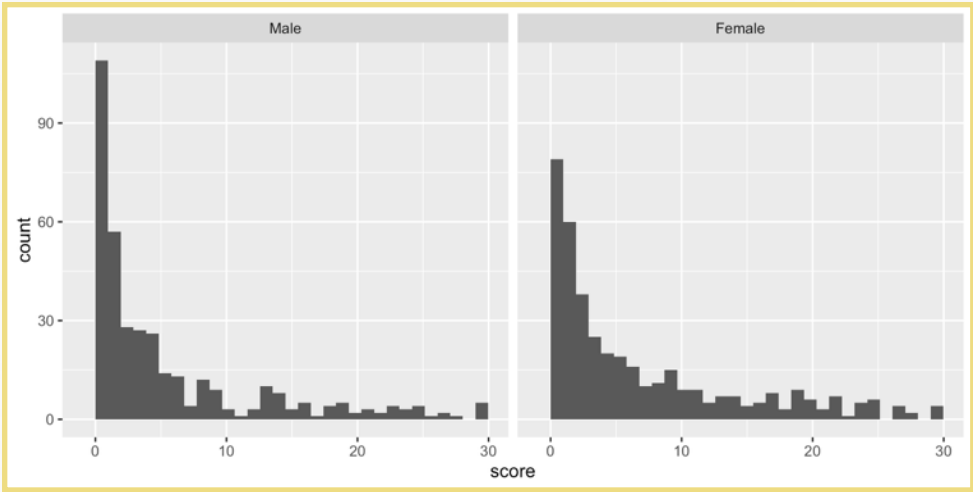
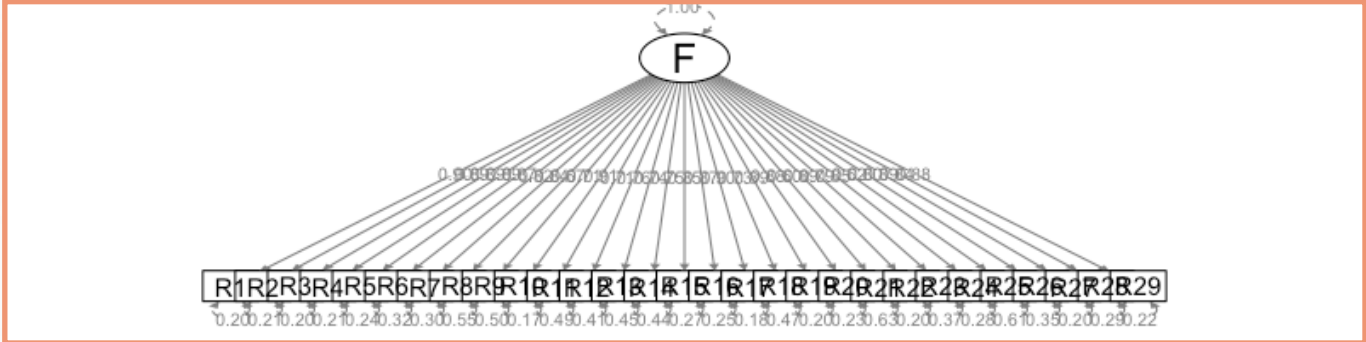
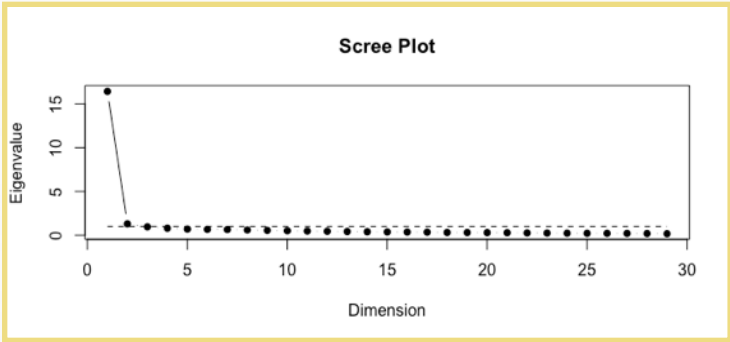
<http://lavaan.ugent.be/tutorial/est.html>

Choi et al. (2011) ; Pilkonis et al. (2011)

- | | |
|-----------------------------------------------------|----------------------------------------------------------------|
| 1. I felt fearful | 16. I felt worried |
| 2. I felt frightened | 17. I felt terrified |
| 3. It scared me when I felt nervous | 18. I worried about other people's reactions to me |
| 4. I felt anxious | 19. I found it hard to focus on anything other than my anxiety |
| 5. I felt like I needed help for my anxiety | 20. My worries overwhelmed me |
| 6. I was concerned about my mental health | 21. I had twitching or trembling muscles |
| 7. I felt upset | 22. I felt nervous |
| 8. I had a racing or pounding heart | 23. I felt indecisive |
| 9. I was anxious if my normal routine was disturbed | 24. Many situations made me worry |
| 10. I had sudden feelings of panic | 25. I had difficulty sleeping |
| 11. I was easily startled | 26. I had trouble relaxing |
| 12. I had trouble paying attention | 27. I felt uneasy |
| 13. I avoided public places or activities | 28. I felt tense |
| 14. I felt fidgety | 29. I had difficulty calming down |
| 15. I felt something awful would happen | |

1 = 'Never', 2 = 'Rarely', 3 = 'Sometimes', 4 = 'Often', 5 = 'Always'

PEUT-ON METTRE EN EVIDENCE UNE DIFFERENCE DE SCORES ENTRE LES HOMMES ET LES FEMMES ?



anxiety.R

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2. Choi, S., Gibbons, L. and Crane, P. (2011). lordif: An R package for detecting differential item functioning using iterative hybrid ordinal logistic regression/Item Response Theory and monte carlo simulations. *Journal of Statistical Software*, 39(8), 2011.
3. Beaujean, A.A. *Latent Variable Modeling Using R, A Step-by-Step Guide*. New York: Routledge, 2014.
4. Muthén, B.O. Goodness of fit with categorical and other nonnormal variables. In K.A. Bollen, & J.S. Long (eds.), *Testing structural equation Models* (pp. 205-234). Newbury Park, CA: Sage, 1993.