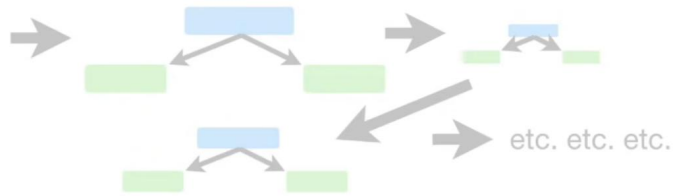
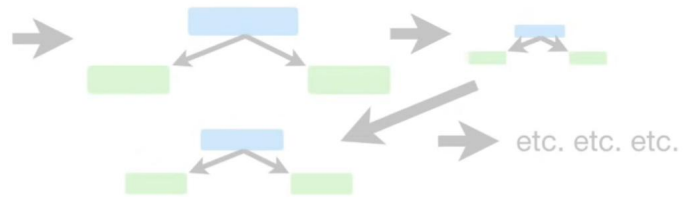


| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



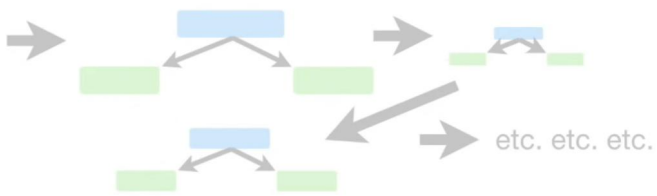
In contrast, **Gradient Boost** starts by making a single leaf, instead of a tree or stump.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



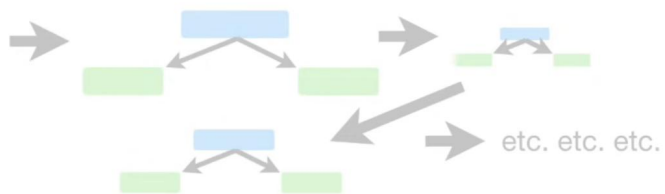
This leaf represents an initial guess for the **Weights** of all of the samples.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



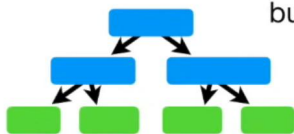
When trying to **Predict** a continuous value like **Weight**, the first guess is the the average value.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

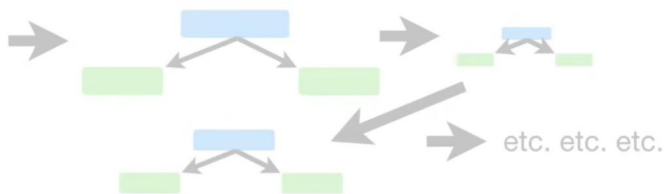


73.3

Then **Gradient Boost** builds a tree.

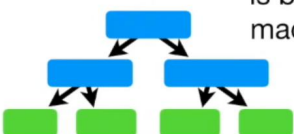


| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

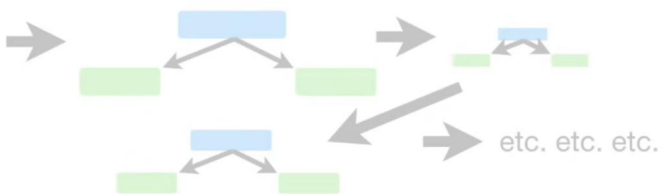


73.3

Like **AdaBoost**, this tree is based on the errors made by the previous tree...

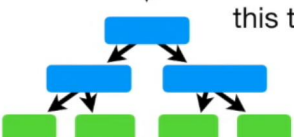


| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

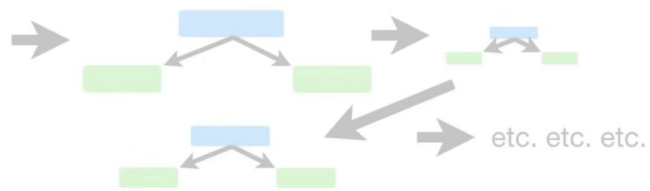


73.3

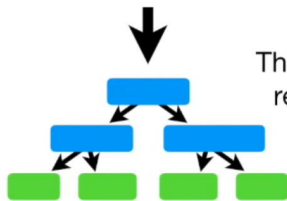
...but unlike **AdaBoost**, this tree is usually larger than a stump.



| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

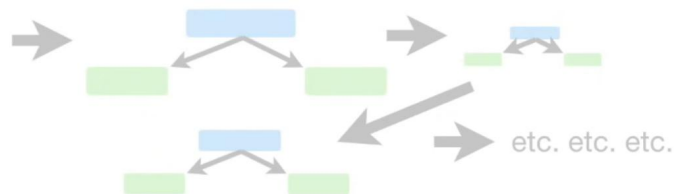


73.3

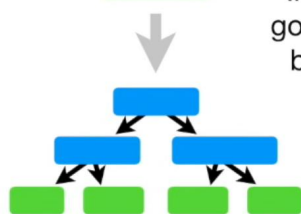


That said, **Gradient Boost** still restricts the size of the tree.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

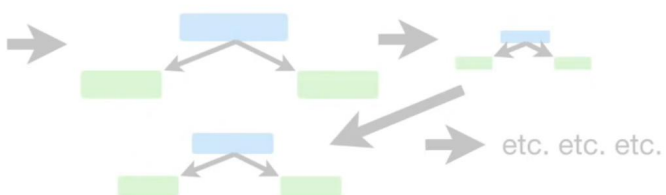


73.3

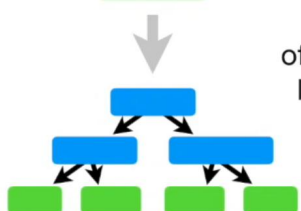


In the simple example that we will go through in this StatQuest, we will build trees with up to four leaves, but no larger.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

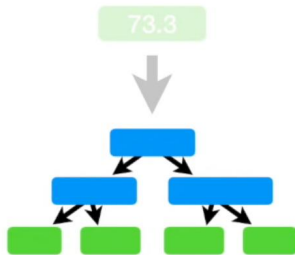
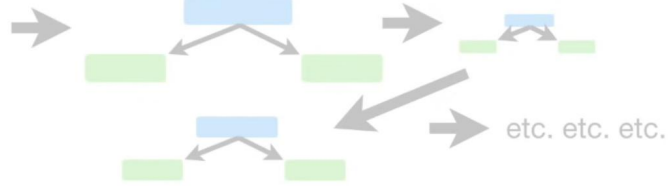


73.3



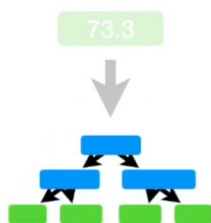
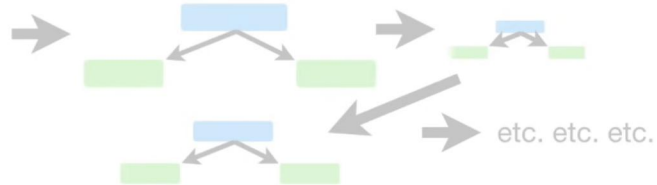
However, in practice, people often set the maximum number of leaves to be between **8** and **32**.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



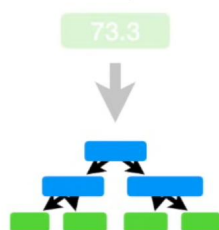
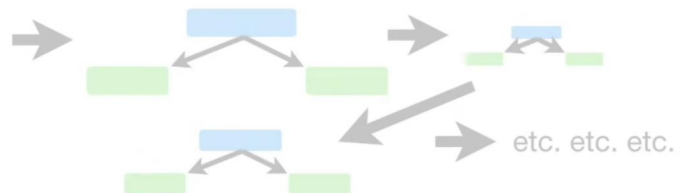
Thus, like **AdaBoost**, **Gradient Boost** builds fixed sized trees based on the previous tree's errors, but unlike **AdaBoost**, each tree can be larger than a stump.

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |

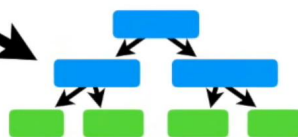


Also like **AdaBoost**, **Gradient Boost** scales the trees. However, **Gradient Boost** scales all trees by the same amount.

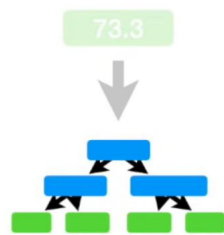
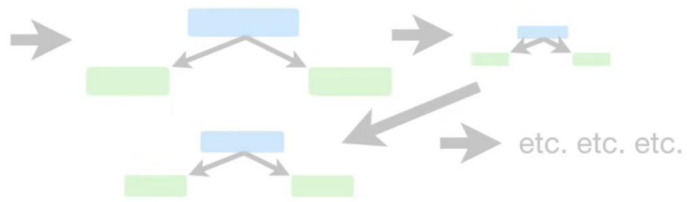
| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



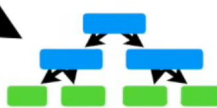
Then **Gradient Boost** builds another tree based on the errors made by the previous tree...



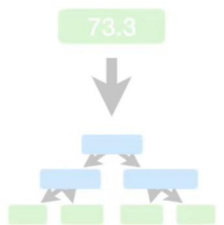
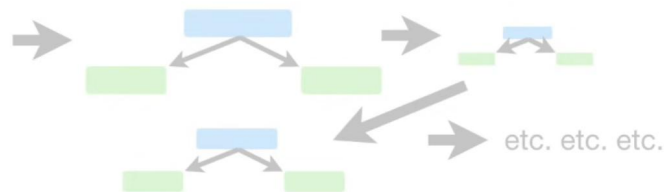
| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



...and then it scales the tree...



| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| etc... | etc... | etc... | etc... |



...and **Gradient Boost** continues to build trees in this fashion until it has made the number of trees you asked for, or additional trees fail to improve the fit.



...let's see how the most common
Gradient Boost configuration would
use this **Training Data** to **Predict**
Weight.




| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| 1.5 | Blue | Female | 56 |
| 1.8 | Red | Male | 73 |
| 1.5 | Green | Male | 77 |
| 1.4 | Blue | Female | 57 |

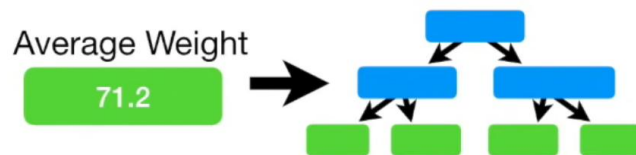
Average Weight

71.2

The first thing we do is
calculate the average
Weight.



| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| 1.5 | Blue | Female | 56 |
| 1.8 | Red | Male | 73 |
| 1.5 | Green | Male | 77 |
| 1.4 | Blue | Female | 57 |



| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| 1.5 | Blue | Female | 56 |
| 1.8 | Red | Male | 73 |
| 1.5 | Green | Male | 77 |
| 1.4 | Blue | Female | 57 |

The next thing we do is build a tree based on the errors from the first tree.

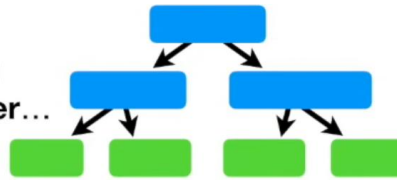


| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |
| 1.6 | Green | Female | 76 |
| 1.5 | Blue | Female | 56 |
| 1.8 | Red | Male | 73 |
| 1.5 | Green | Male | 77 |
| 1.4 | Blue | Female | 57 |

The errors that the previous tree made are the differences between the **Observed Weights** and the **Predicted Weight, 71.2**.

(Observed Weight - Predicted Weight)

Now we will build a **Tree**, using **Height**, **Favorite Color** and **Gender**...



| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | 16.8 |
| 1.6 | Green | Female | 76 | 4.8 |
| 1.5 | Blue | Female | 56 | -15.2 |
| 1.8 | Red | Male | 73 | 1.8 |
| 1.5 | Green | Male | 77 | 5.8 |
| 1.4 | Blue | Female | 57 | -14.2 |

...to **Predict the Residuals**.

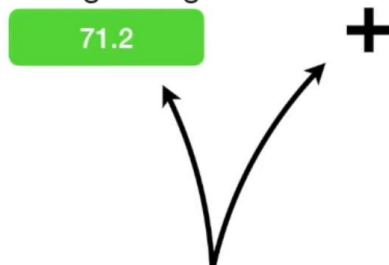
| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | 16.8 |
| 1.6 | Green | Female | 76 | 4.8 |
| 1.5 | Blue | Female | 56 | -15.2 |
| 1.8 | Red | Male | 73 | 1.8 |
| 1.5 | Green | Male | 77 | 5.8 |
| 1.4 | Blue | Female | 57 | -14.2 |



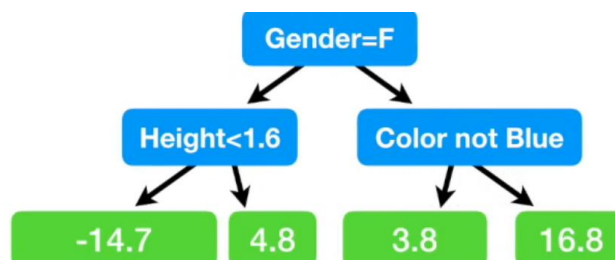
Remember, in this example we are only allowing up to four leaves...

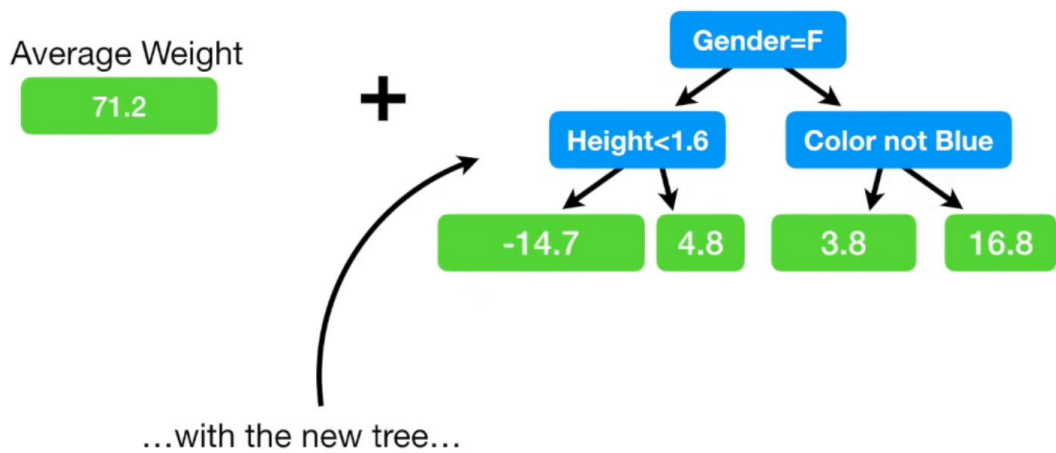
...but when using a larger dataset, it is common to allow anywhere from **8** to **32**.

Average Weight



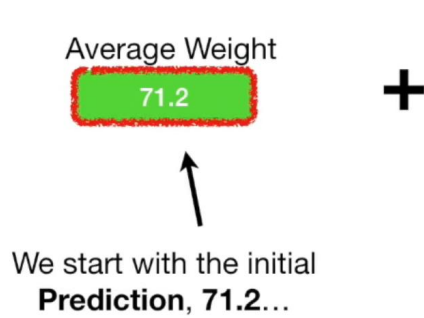
Now we can now combine the original leaf...



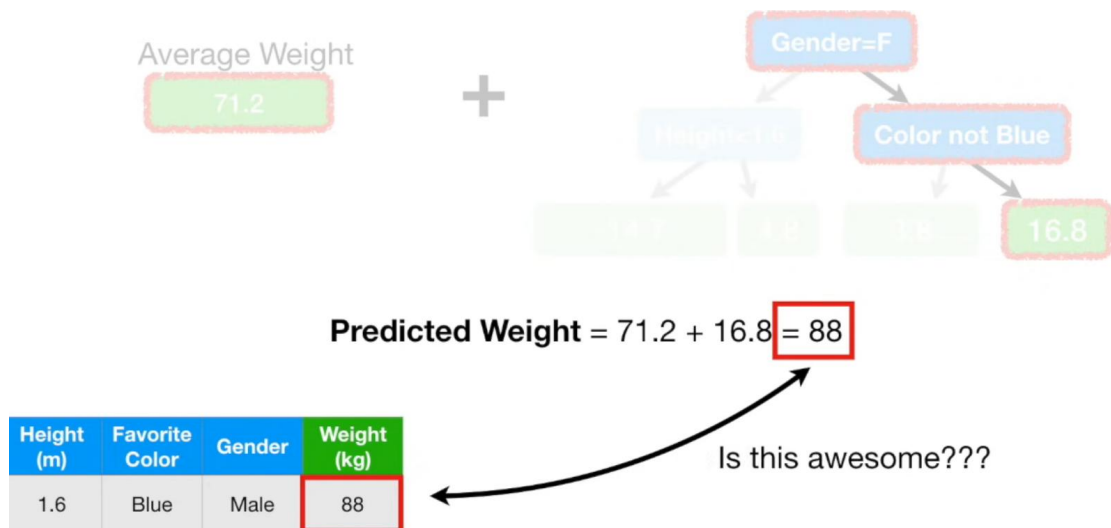
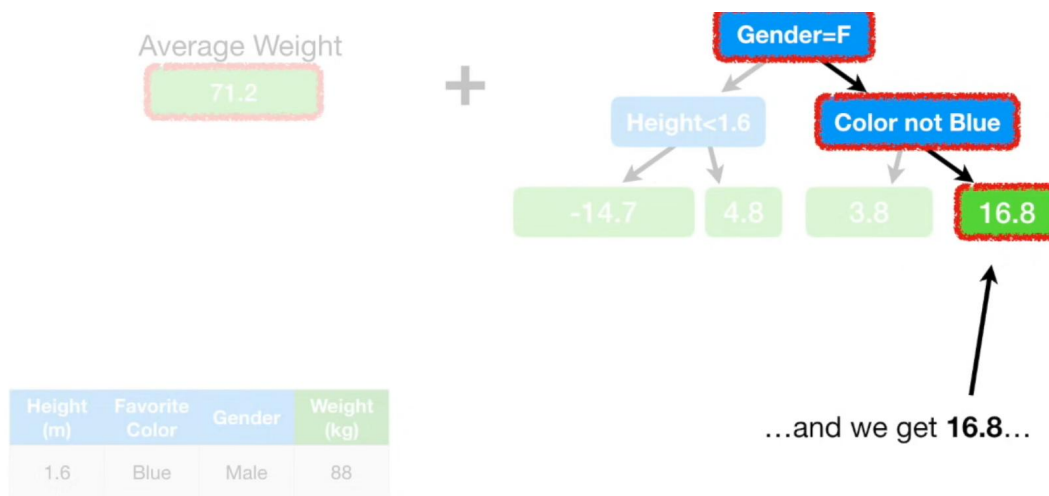
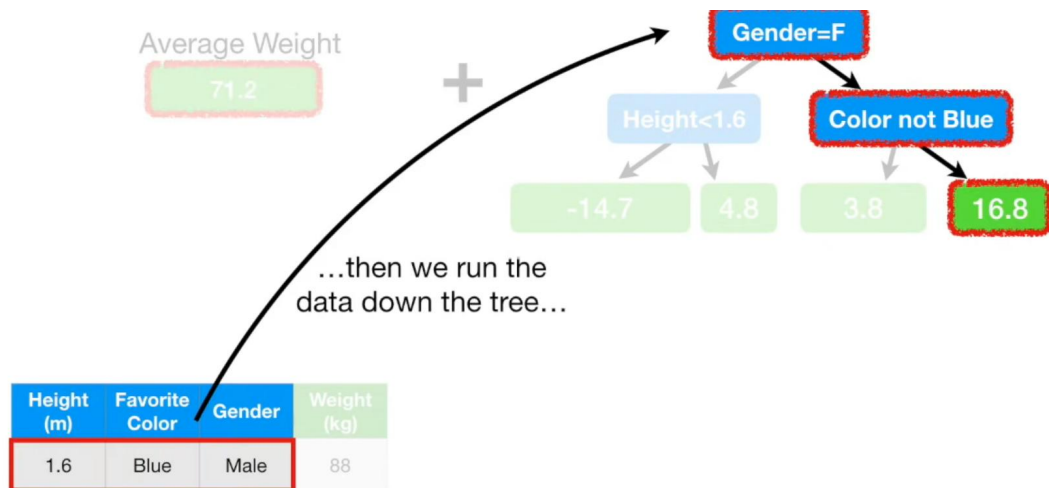


| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |

...to make a new **Prediction** of an individual's **Weight** from the **Training Data**.



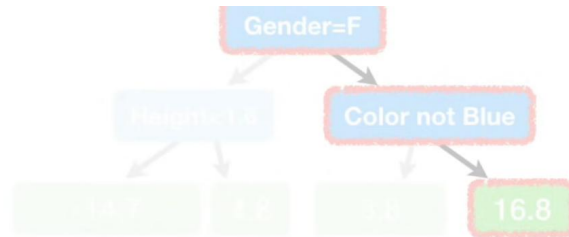
| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |



Average Weight

71.2

+



$$\text{Predicted Weight} = 71.2 + 16.8 = 88$$

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |

No. The model fits the **Training Data** too well.

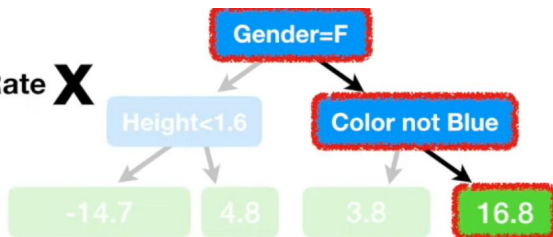
In other words, we have low **Bias**, but probably very high **Variance**.

Average Weight

71.2

+

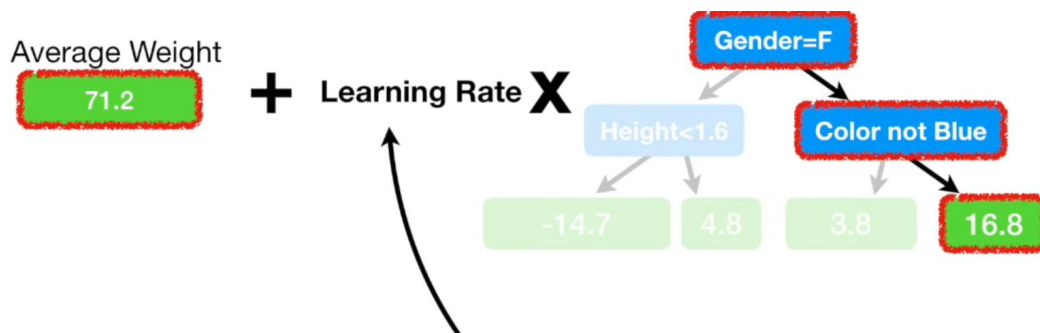
Learning Rate X



| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |

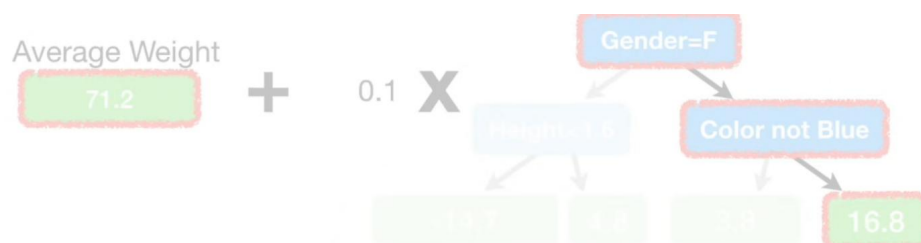
Gradient Boost deals with this problem by using a **Learning Rate** to scale the contribution from the new tree.

The **Learning Rate** is a value between **0** and **1**.



In this case, we'll set the **Learning Rate** to **0.1**.

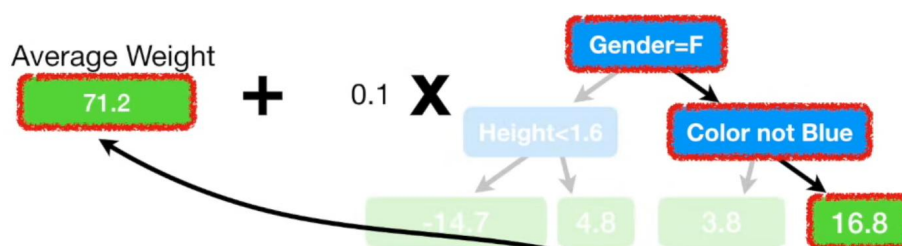
| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |



$$\text{Predicted Weight} = 71.2 + (0.1 \times 16.8) = 72.9$$

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |

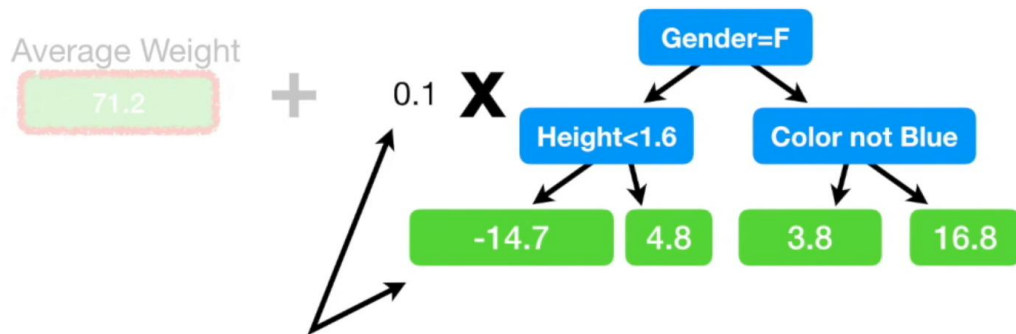
With the **Learning Rate** set to **0.1**, the new **Prediction** isn't as good as it was before...



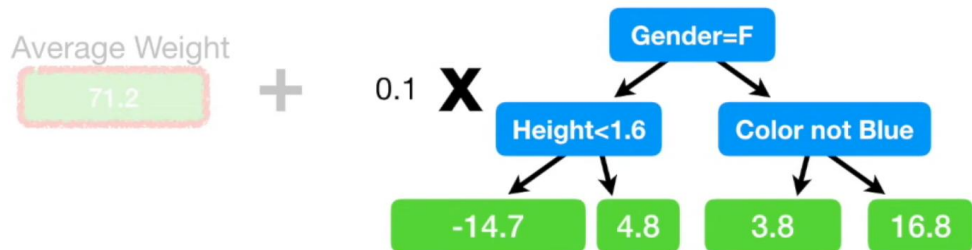
$$\text{Predicted Weight} = 71.2 + (0.1 \times 16.8) = 72.9$$

| Height (m) | Favorite Color | Gender | Weight (kg) |
|------------|----------------|--------|-------------|
| 1.6 | Blue | Male | 88 |

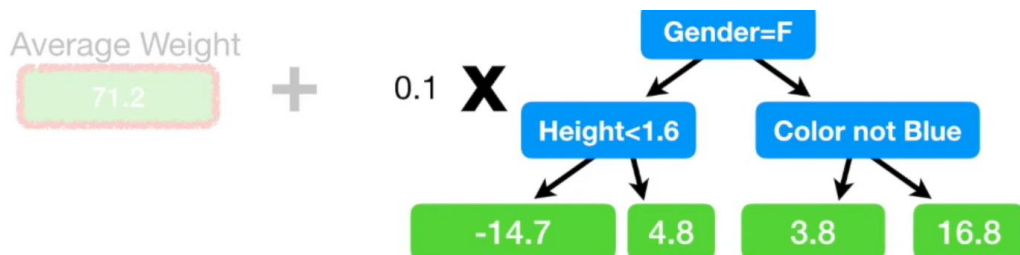
...but it's a little bit better than the **Prediction** made with just the original leaf, which predicted that all samples would weigh **71.2**.



In other words, scaling the tree by the **Learning Rate** results in a small step in the right direction.



According to the dude that invented **Gradient Boost**, Jerome Friedman, empirical evidence shows that taking lots of small steps in the right direction results in better **Predictions** with a **Testing Dataset**, i.e. lower **Variance**.



So let's build another tree so we can take another small step in the right direction.

Just like before, we calculate the **Pseudo Residuals**, the difference between the **Observed Weights** and our latest **Predictions**.

| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | |
| 1.6 | Green | Female | 76 | |
| 1.5 | Blue | Female | 56 | |
| 1.8 | Red | Male | 73 | |
| 1.5 | Green | Male | 77 | |
| 1.4 | Blue | Female | 57 | |

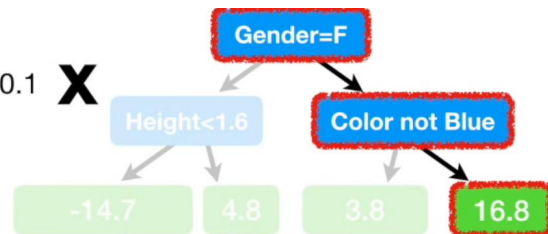
← **Residual = (Observed - Predicted)**

Average Weight

71.2

+

0.1 X



| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | |
| 1.6 | Green | Female | 76 | |
| 1.5 | Blue | Female | 56 | |
| 1.8 | Red | Male | 73 | |
| 1.5 | Green | Male | 77 | |
| 1.4 | Blue | Female | 57 | |

$$\text{Residual} = (88 - (71.2 + 0.1 \times 16.8)) = 15.1$$

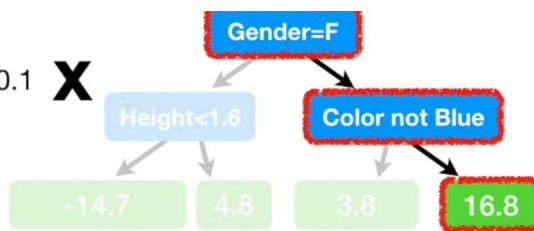
...and we get **15.1**...

Average Weight

71.2

+

0.1 X

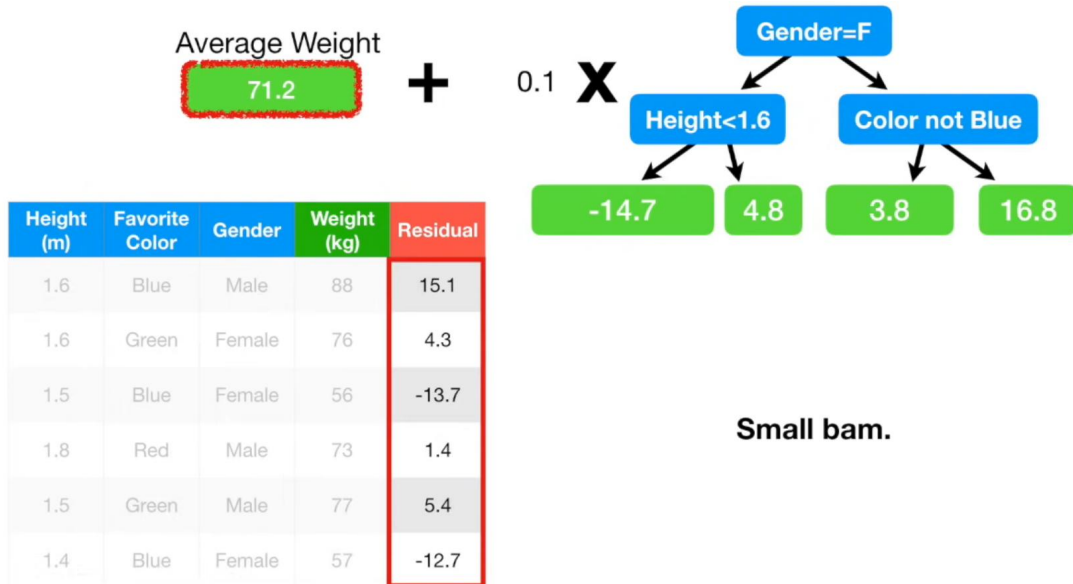


| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | |
| 1.6 | Green | Female | 76 | |
| 1.5 | Blue | Female | 56 | |
| 1.8 | Red | Male | 73 | |
| 1.5 | Green | Male | 77 | |
| 1.4 | Blue | Female | 57 | |

$$\text{Residual} = (88 - (71.2 + 0.1 \times 16.8)) = 15.1$$

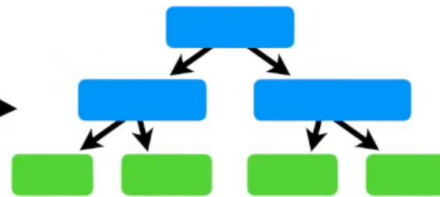
...and we save that in the column for **Pseudo Residuals**.

Then we repeat for the all of the other individuals in the **Training Dataset**.

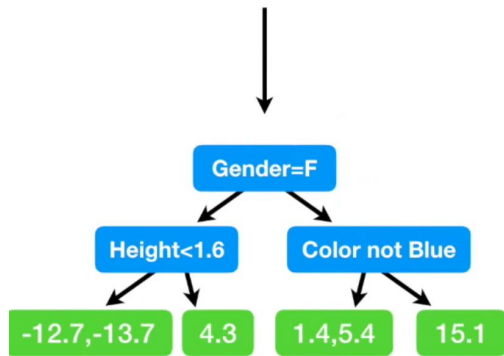


Now let's build a new tree to predict the new **Residuals**.

| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | 15.1 |
| 1.6 | Green | Female | 76 | 4.3 |
| 1.5 | Blue | Female | 56 | -13.7 |
| 1.8 | Red | Male | 73 | 1.4 |
| 1.5 | Green | Male | 77 | 5.4 |
| 1.4 | Blue | Female | 57 | -12.7 |



And here's the new tree!



Average Weight

71.2

NOTE: We scale all of the **Trees** by the **Learning Rate**, which we set to **0.1...**

0.1 **X**

0.1 **X**

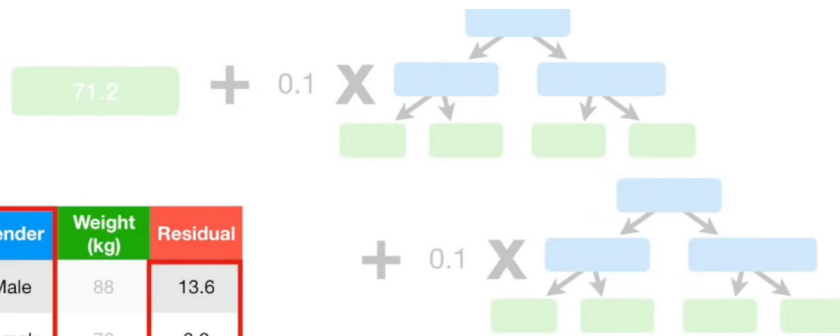
Average Weight

71.2

...and add everything together.

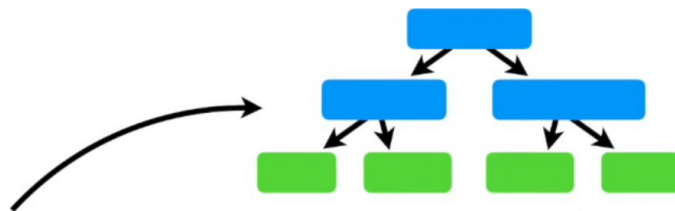
+ 0.1 **X**

+ 0.1 **X**



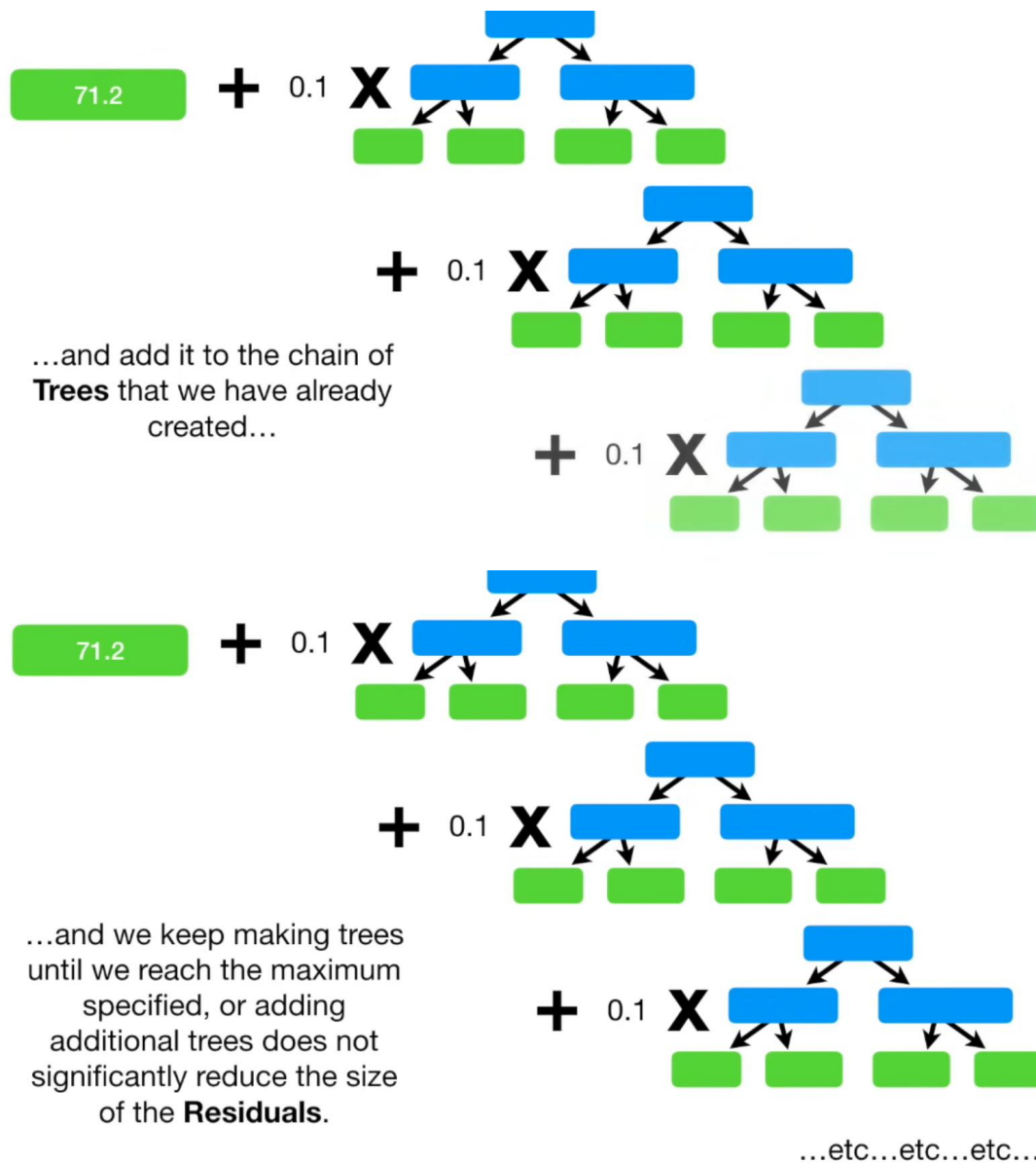
| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | 13.6 |
| 1.6 | Green | Female | 76 | 3.9 |
| 1.5 | Blue | Female | 56 | -12.4 |
| 1.8 | Red | Male | 73 | 1.1 |
| 1.5 | Green | Male | 77 | 5.1 |
| 1.4 | Blue | Female | 57 | -11.4 |

...to calculate new **Residuals**.

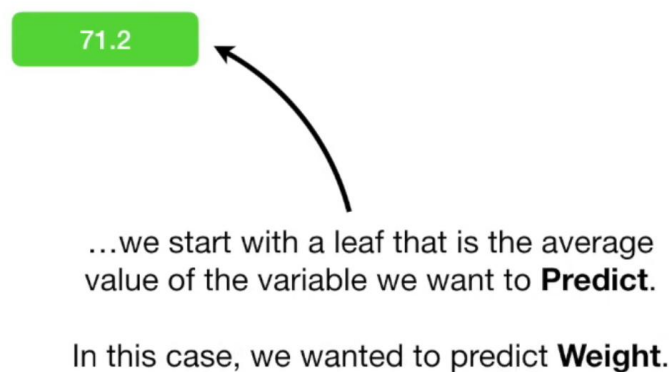


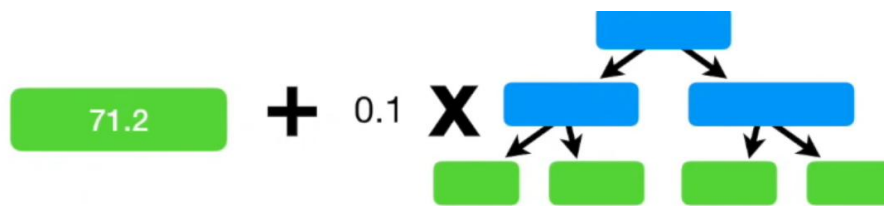
| Height (m) | Favorite Color | Gender | Weight (kg) | Residual |
|------------|----------------|--------|-------------|----------|
| 1.6 | Blue | Male | 88 | 13.6 |
| 1.6 | Green | Female | 76 | 3.9 |
| 1.5 | Blue | Female | 56 | -12.4 |
| 1.8 | Red | Male | 73 | 1.1 |
| 1.5 | Green | Male | 77 | 5.1 |
| 1.4 | Blue | Female | 57 | -11.4 |

Now we build a another tree to predict the new **Residuals**...



In summary, when **Gradient Boost** is used for **Regression**...

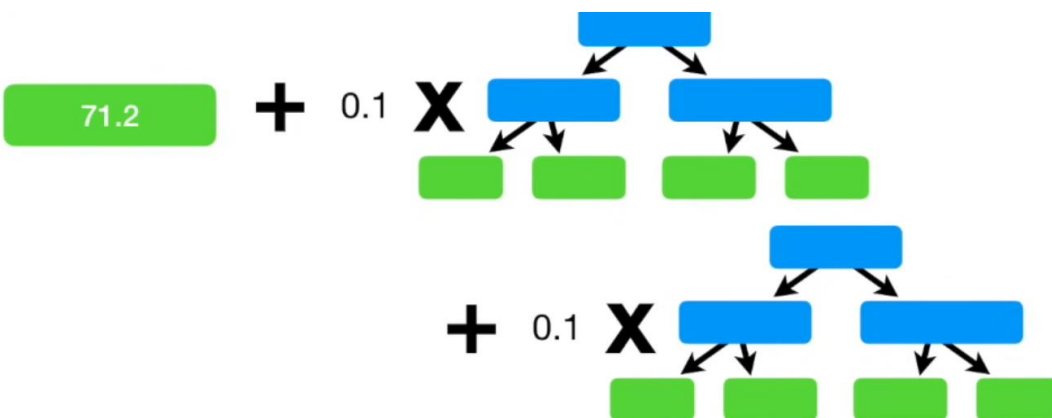




Then we add a tree based on the **Residuals**, the difference between the **Observed** values and the **Predicted** values...



...and we scale the tree's contribution to the final **Prediction** with a **Learning Rate**.



Then we add another tree based on the new **Residuals**...

