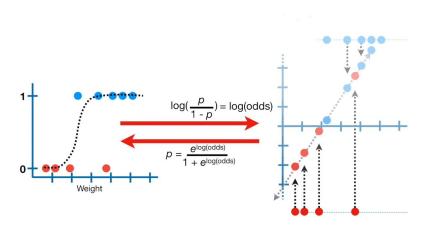
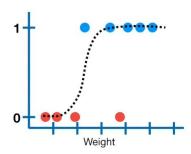
Logistic Regression, Details Part 3: R² and p-values

R-squared Calculation



However, we ended with a little bit of a cliff-hanger. We know that the line is the "best fit", but how do we know if it is useful?



In other words, how do we calculate R^2 and a p-value for the relationship between weight and obesity?

Even though pretty much everyone agrees on how to calculate R^2 and the associated p-value for Linear Models...

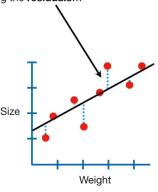
...there is no consensus on how to calculate R^2 for Logistic Regression. There are more than 10 different ways to do it!!!

For this StatQuest, rather than describe every single R^2 for Logistic Regression, I'm focusing on one that is commonly used and is easily calculated from the output that R gives you.

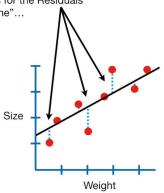
Just so you know, this R^2 is called "McFadden's Pseudo R^2 "

Another bonus is that this method is very similar to how R^2 is calculated for regular old Linear Models.

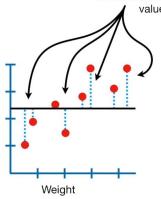
In Linear Regression (and other linear models), R^2 and the related p-value are calculated using the **residuals**...



In brief, we square the residuals and then add them up. I call this **SS(fit)**, for "sum of squares for the Residuals around the best fitting line"...

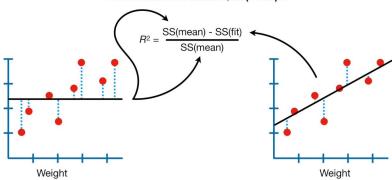


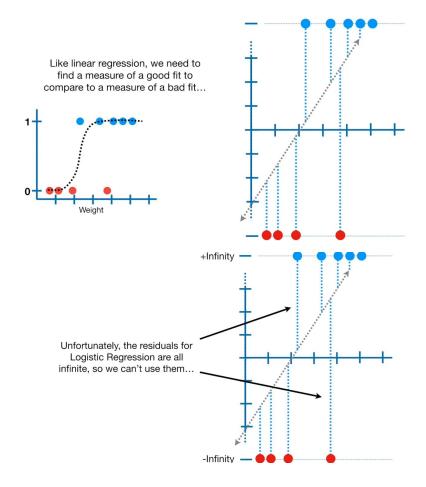
...and we compare that to the sum of squared residuals around the worst fitting line, the mean of the y-axis values. This is called **SS(mean)**.



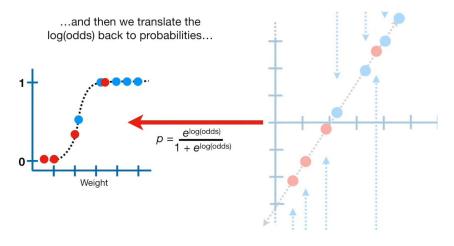


R² compares a measure of a good fit, **SS(fit)**... ...to a measure of a bad fit, **SS(mean)**...

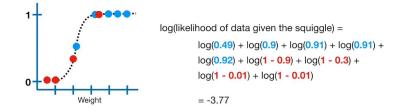




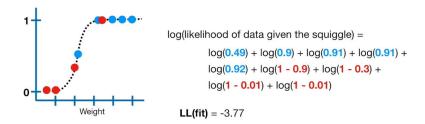
...but we can project the data onto the best fitting line...



...and lastly, calculate the log-likelihood of the data given the best fitting squiggle.



We can call this **LL(fit)**, for the log-likelihood of the fitted line, and use it as a substitute for **SS(fit)**.

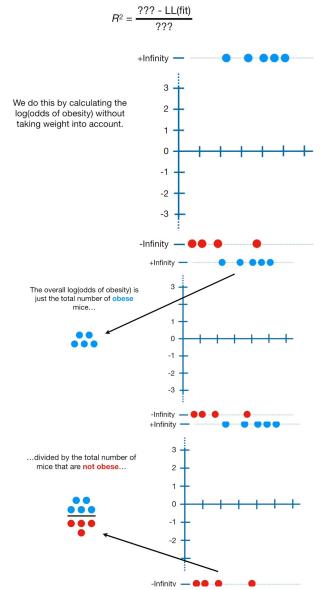


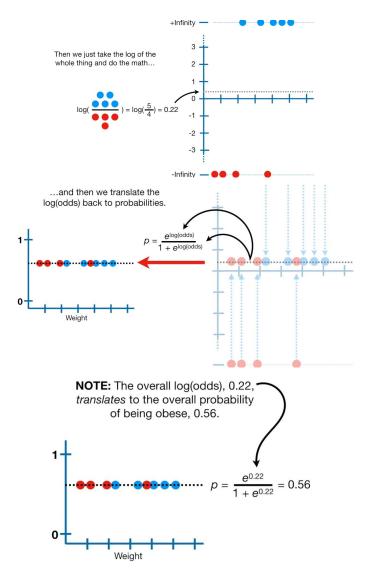
Now we need a measure of a poorly fitted line that is analogous to SS(mean)...

$$R^{2} = \frac{SS(mean) - SS(fit)}{SS(mean)}$$

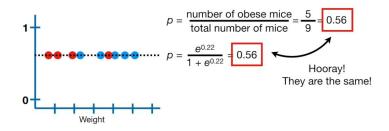
$$Vs$$

$$2?? - LL(fit)$$

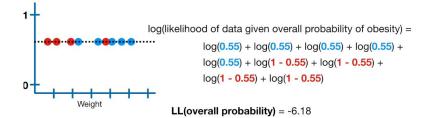


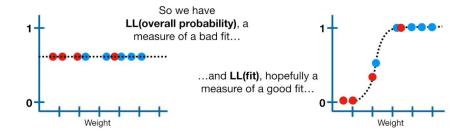


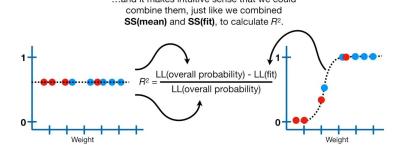
In other words, we can arrive at the same solution by calculating the overall probability of obesity.



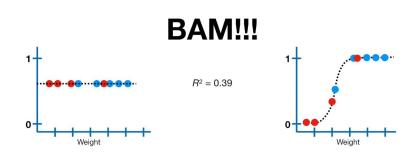
We'll call this **LL(overall probability)** and use it as a substitute for **SS(mean)**.







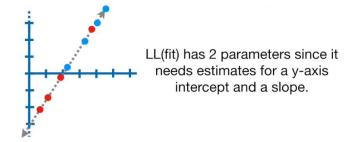
...and it makes intuitive sense that we could

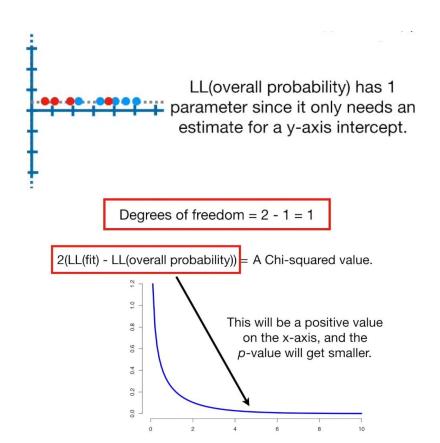


P-value Calculation

The good news is that calculating the *p*-value is pretty straight forward.

A Chi-squared value with degrees of 2(LL(fit) - LL(overall probability)) = A Chi-squared value with degrees of freedom equal to the difference in the number of parameters in the two models.





P-value is the area under the curve on the right of the Chi-squared value

