

1 Beta Distribution

1.1 Notation

$Beta(\alpha, \beta)$ where $\alpha, \beta > 0$ are the shape parameters.

1.2 Denstiy Function

$$f(x) = \frac{x^{\alpha-1}(1-x)^{\beta-1}}{B(\alpha, \beta)} \text{ where } B(\alpha, \beta) = \frac{\Gamma(\alpha)\Gamma(\beta)}{\Gamma(\alpha+\beta)}.$$

1.3 Mean and Variance

$$E[X] = \frac{\alpha}{\alpha+\beta}$$
$$Var[X] = \frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$$

2 Uniform Distribution

2.1 Notation

$U(a, b)$ where $-\infty < a < b < \infty$.

2.2 Density Function

$$f(x) = \frac{1}{b-a}$$

2.3 Mean and Variance

$$E[X] = \frac{1}{2}(a+b)$$
$$Var[X] = \frac{1}{12}(b-a)^2$$