

Model on Montpellier rainfall

2025-01-07

COMEPHORE data

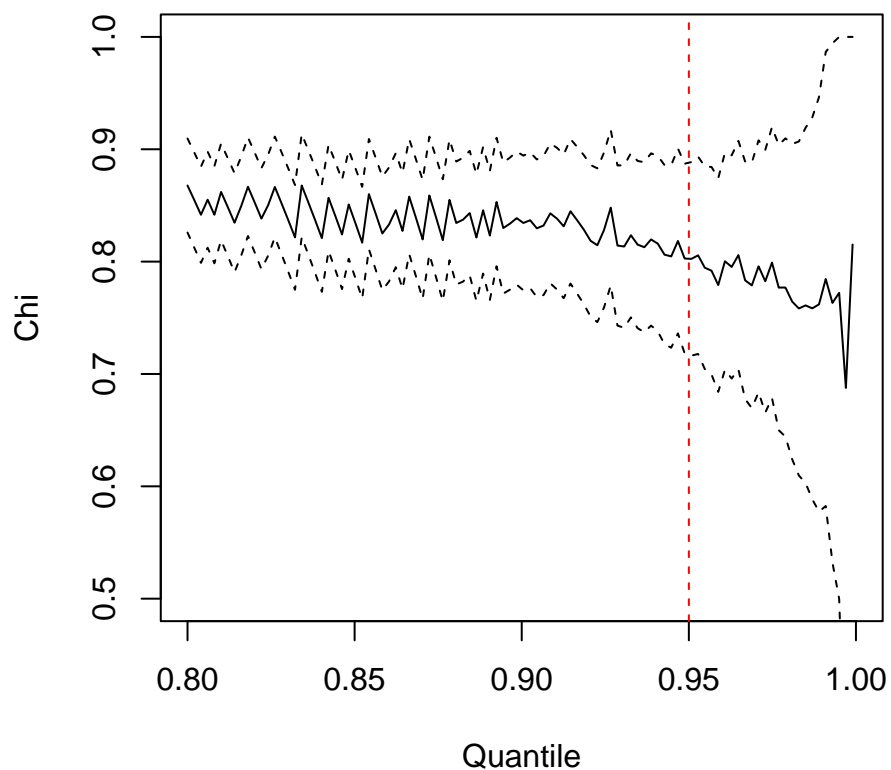
An other dataset is considered, the COMEPHORE radar renalysis data from Météo France. We consider 59 pixels in the Montpellier area.

Quantile choice

```
# Remove lines with just zeros
comephore_nozeros <- comephore[rowSums(comephore) > 0, ]

# Choose two site and remove zeros
comephore_pair <- comephore_nozeros[, c(1,15)]
comephore_pair <- comephore_pair[rowSums(comephore_pair) > 0, ]
chiplot(comephore_pair, xlim = c(0.8, 1), ylim1 = c(0.5, 1), which = 1,
        qlim = c(0.8, 0.999))
abline(v = 0.95, col = "red", lty = 2)
```

Chi Plot



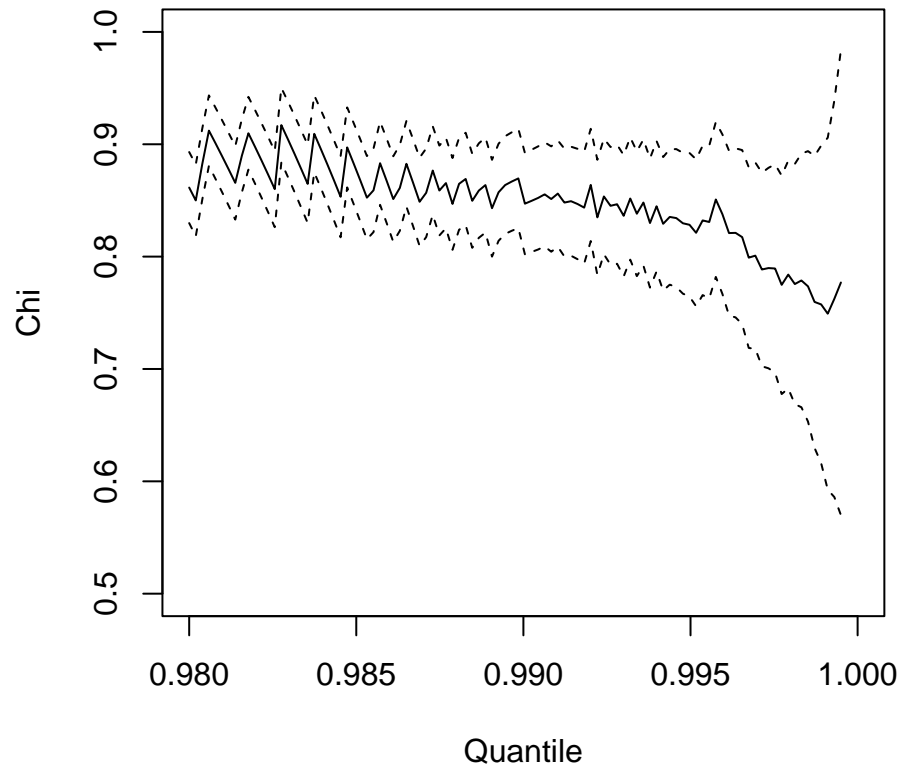
```
# count conjoint excesses
q <- 0.95
# uniformize the data
n <- nrow(comephore_pair)
data_unif <- cbind(rank(comephore_pair[, 1]) / (n + 1),
                   rank(comephore_pair[, 2]) / (n + 1))

count_excesses <- sum(data_unif[, 1] > q & data_unif[, 2] > q)
print(count_excesses)
```

```
## [1] 509
```

```
# With all zeros
comephore_pair <- comephore[, c(1,10)]
chiplot(comephore_pair, xlim = c(0.98, 1), ylim1 = c(0.5, 1), which = 1,
        qlim = c(0.98, 0.9995))
```

Chi Plot

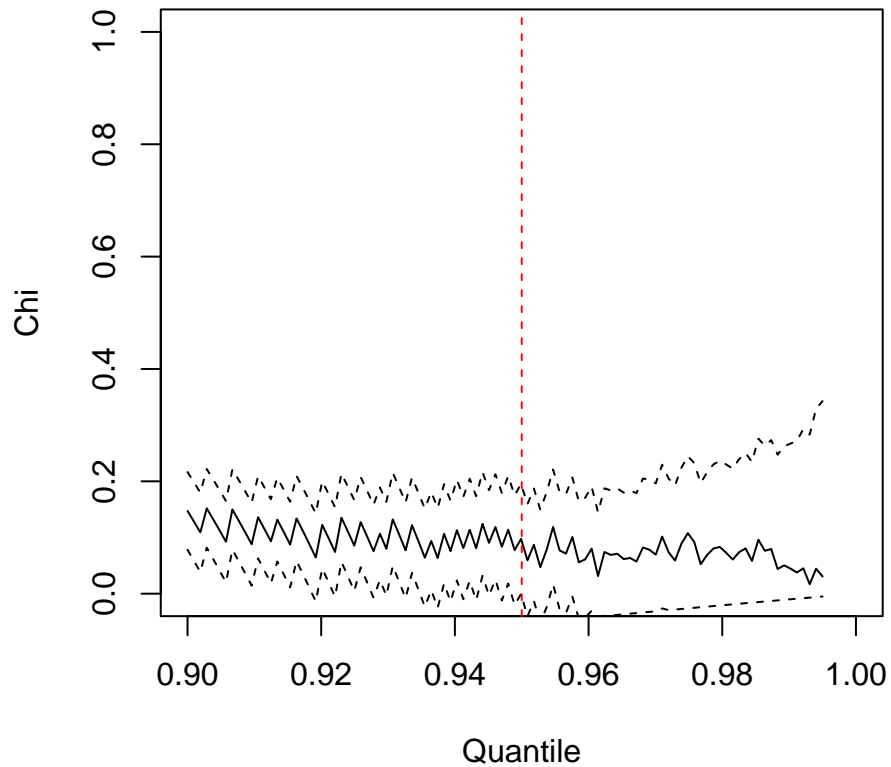


```
threshold <- quantile(comephore$p102, probs = 0.998, na.rm = T)
# get the quantile from threshold in the data without 0 when the quantile is
# 0.998 with zeros inside data
empirical_cdf <- ecdf(comephore_pair$p102)
quantile_in_nozeros <- empirical_cdf(threshold)
print(quantile_in_nozeros)
```

```
## [1] 0.9980013
```

```
# Temporal chi
rain_nolag <- comephore_nozeros$p142[1:(length(comephore_nozeros$p142) - 5)]
rain_lag <- comephore_nozeros$p142[6:length(comephore_nozeros$p142)]
comephore_pair <- cbind(rain_nolag, rain_lag)
comephore_pair <- comephore_pair[rowSums(comephore_pair) > 0, ]
chiplot(comephore_pair, xlim = c(0.9, 1), ylim1 = c(0, 1), which = 1,
        qlim = c(0.9, 0.995))
abline(v = 0.95, col = "red", lty = 2)
```

Chi Plot



```
n <- nrow(comephore_pair)
data_unif <- cbind(rank(comephore_pair[, 1]) / (n + 1),
                  rank(comephore_pair[, 2]) / (n + 1))
q <- 0.95
count_excesses <- sum(data_unif[, 1] > q & data_unif[, 2] > q)
print(count_excesses)
```

```
## [1] 91
```

```
# We choose q = 0.95
q <- 0.95
```

Empirical chi and WLSE

Temporal chi

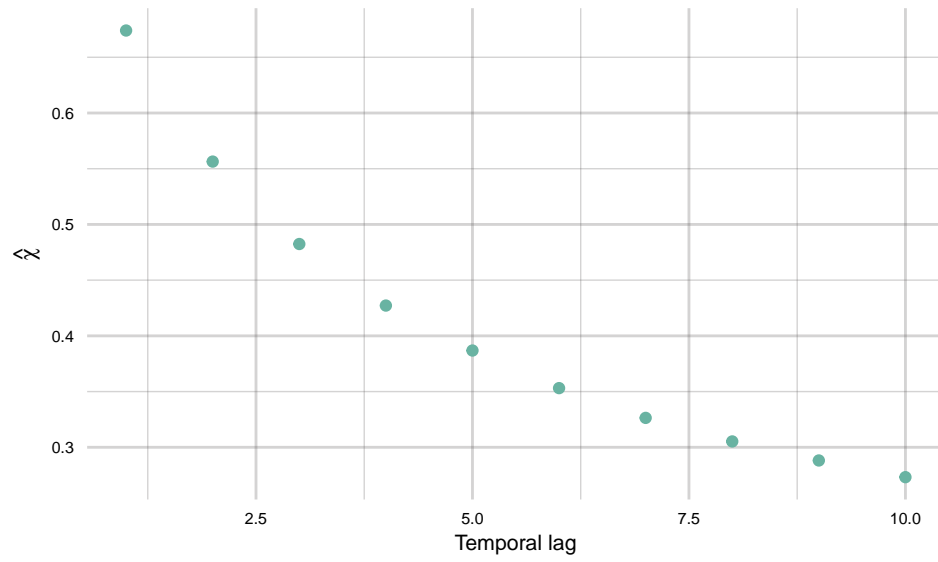


Figure 1: Empirical temporal extremogram

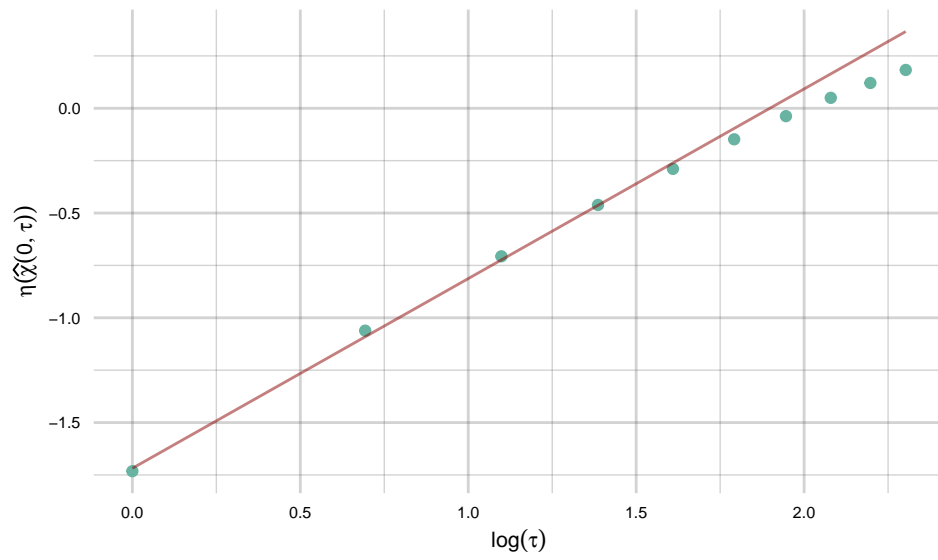


Figure 2: Empirical temporal extremogram with eta transformation and WLSE

Spatial chi

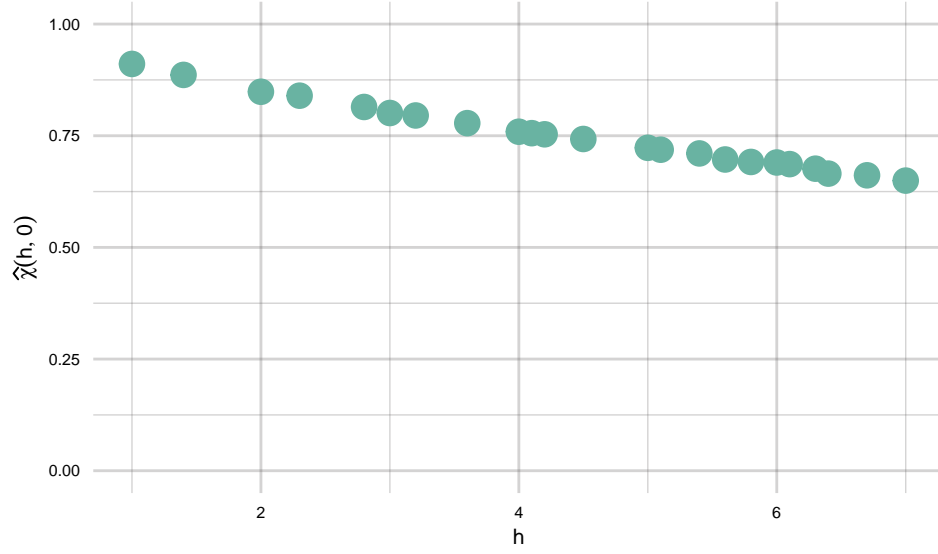


Figure 3: Empirical spatial extremogram

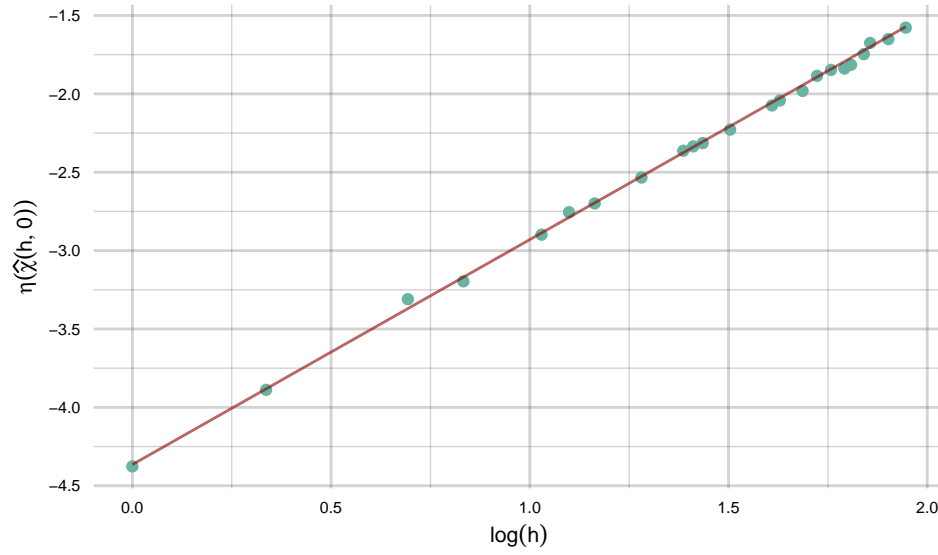


Figure 4: Empirical spatial extremogram with eta transformation and WLSE

Results of the WLSE method on the COMEPHORE data are:

beta1	beta2	alpha1	alpha2
0.0127182	0.1794025	1.435095	0.9052191

Optimization of the composite likelihood

Choose conditional points

```
# Get coords
sites_coords <- loc_px[, c("Longitude", "Latitude")]

# remove 0
rain_new <- comephore
quantile <- 0.998
min_spatial_dist <- 2 # in km
min_time_dist <- 5 # in hours

selected_points <- choose_conditional_points(
  sites_coords = sites_coords,
  data = rain_new,
  quantile = quantile,
  min_spatial_dist = min_spatial_dist,
  min_time_dist = min_time_dist
)

# Extract s0 and t0
s0_list <- lapply(selected_points, `[[`, "s0")
t0_list <- lapply(selected_points, `[[`, "t0")
```

We have 23 conditional points.

Get corresponding lags and excesses

Optimization results

We initialize the parameters with the values obtained from the WLSE method and we consider an advection of 0.1 for both directions. It converges and the results of the optimization on the COMEPHORE data are:

beta1	beta2	alpha1	alpha2	adv1	adv2
0.0241322	0.0775136	1.434925	0.836116	-0.038373	-0.0384274

Variogram

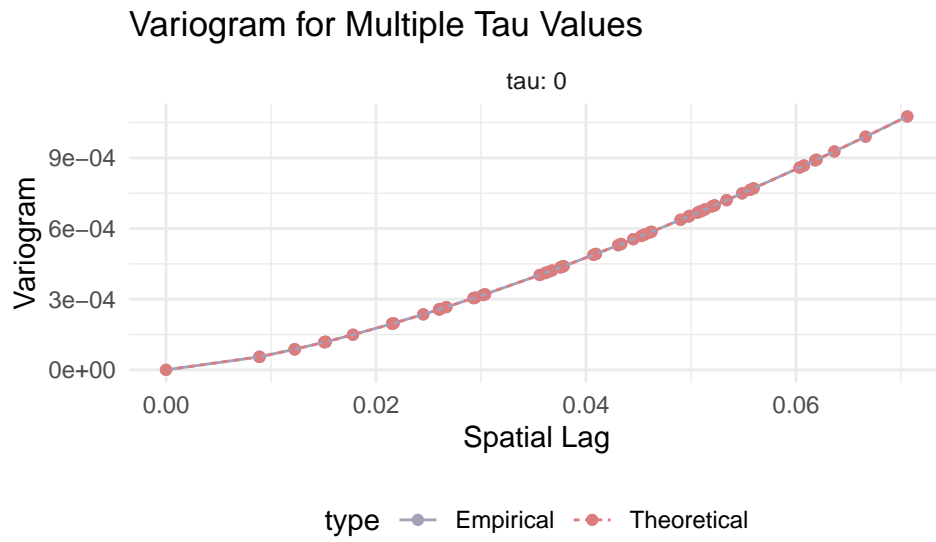


Figure 5: Variogram estimate

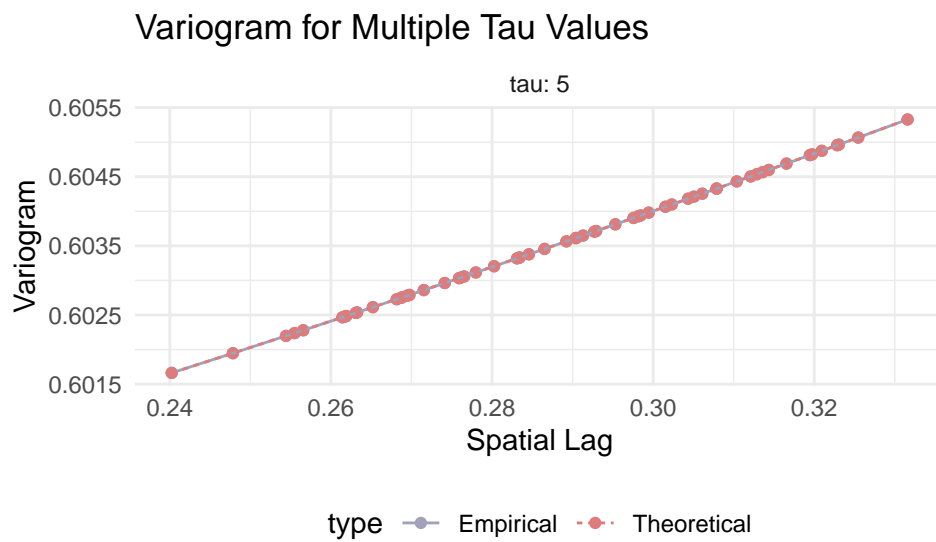


Figure 6: Variogram estimate

Variogram for Multiple Tau Values

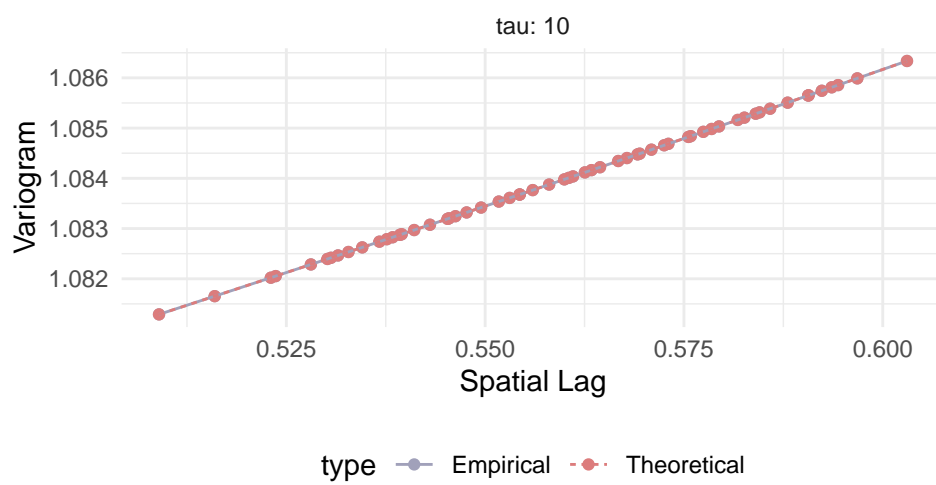


Figure 7: Variogram estimate