COMP6771 Advanced C++ Programming

Week 8
Part Two: Template Metaprogramming

2016

www.cse.unsw.edu.au/~cs6771

Metaprogramming

- Metaprogramming is the writing of computer programs with the ability to treat other program code as their data. It means that a program could be designed to read, generate, analyse or transform other programs, or do part of the work during compile time that is otherwise done at run time.
- Metalanguage: The language in which the metaprogram is written
- Reflection: The ability of a programming language to be its own metalanguage
- Object language: the language of the programs being manipulated
- Examples:
 - · compilers, lex and yacc
 - Metaprogramming involves modifying programs at run time as in Lisp, Python, Ruby and Perl
- C++ metaprogramming: static (compile time calculated values)

Computing Factorials

• Factorials: 0! = 1, 1! = 1, 2! = 2 * 1!, $3! = 3 \times 2!$...

•0000000000000

Compile-time computation of factorials using templates.

```
#include <iostream>
2
  template<int n> struct Factorial {
     static const long val = Factorial<n-1>::val * n;
5
6
  template<> struct Factorial<0> {
     static const long val = 1; // must be a compile-time constant
10
   int main() {
11
12
     std::cout << Factorial<6>::val << std::endl;
13
```

- Such programs are called template metaprograms (i.e., programs about programs)
- The compiler recursively instantiates Factorial until the specialisation is invoked
- Turing-complete (since it supports if-else and recursion)

Computing Factorials (C++11)

```
#include <iostream>

constexpr int factorial (int n) {
   return n > 0 ? n * factorial( n - 1 ) : 1;
}

int main() {
   std::cout << factorial(6) << std::endl;
}</pre>
```

- Recall the differences between const and constexpr
- Note: this is not a template metaprogram

Loop Unrolling

- Consider calculating the dot product over a large Euclidean Vector (a[0] * b[0] + a[1] * b[2]...):
- Could do this in a loop at run time:

```
double calcDotProduct(EV a, EV b, int numDim) {
   double result = 0;
   for (unsigned int i = 0; i < numDim; ++i) {
      result += ( a[i] * b[i] );
   }
   return result;
}</pre>
```

 Code sketch of Loop Unrolling by the optimiser (elimates the counter i variable):

```
double calcDotProduct(EV a, EV b) {
   double result = ( a[1] * b[1] );
   result += ( a[2] * b[2] );
   result += ( a[3] * b[3] );
   ...
   return result;
   }
}
```

Loop Unrolling with Metaprogramming

```
// primary template
  template <int DIM, typename T>
  struct DotProduct {
     static T result (T* a, T* b) \{
5
       return *a * *b + DotProduct<DIM-1,T>::result(a+1,b+1);
6
7
8
   // partial specialisation as end criteria
  template <typename T>
10
11
  struct DotProduct<1,T> {
     static T result (T* a, T* b) {
12
13
       return *a * *b;
14
15
```

Modified from: http://www.informit.com/articles/article.aspx?p=30667&seqNum=7

Loop Unrolling

Client code:

Compile-time computations:

```
DotProduct<3, int>:result(a, b)
= *a * *b + DotProduct<2, int>:result(a+1, b+1)
= *a * *b + *(a+1) * *(b+1) + DotProduct<1, int>:result(a+2, b+2)
= *a * *b + *(a+1) * *(b+1) + *(a+2) * *(b+2)
```

Used in numeric libraries such as Blitz++ and MTL

Template Recursion

- Consider the problem of trying to make a N-Dimensional grid.
- Could make a one dimension, length 10, grid using: std::vector<int> grid(10);
- To make a two dimension grid (size 10x10), we would need to create: std::vector<std::vector<int>> grid2D(10);
- But then we would need to ensure that each inner vector is also resized to 10 before use.
- Can use the following class to wrap a vector and get this behaviour right...

OneDGrid.h

```
#pragma once
2
   #include <cstddef>
   #include <vector>
5
  template <typename T>
6
   class OneDGrid {
   public:
     explicit OneDGrid(size_t inSize = 10);
9
     virtual ~OneDGrid():
10
11
     T& operator[](size t x);
12
     const T& operator[](size_t x) const;
13
14
     void resize(size_t newSize);
15
     size_t getSize() const { return mElems.size(); }
16
17
18
   private:
     std::vector<T> mElems:
19
20
```

OneDGrid.h

```
template <typename T>
   OneDGrid<T>::OneDGrid(size_t inSize) {
     mElems.resize(inSize);
3
4
5
   template <typename T>
   OneDGrid<T>:: OneDGrid() {
     // Nothing to do, the vector will clean up itself.
8
9
10
  template <typename T>
11
   void OneDGrid<T>::resize(size t newSize) {
12
13
     mElems.resize(newSize);
14
15
   template <typename T>
16
   T& OneDGrid<T>::operator[](size t x) {
17
     return mElems[x]:
18
19
20
   template <typename T>
21
   const T& OneDGrid<T>::operator[](size t x) const {
22
     return mElems[x]:
23
24
```

10

User Code

```
#include "OneDGrid.h"
2
   int main() {
     OneDGrid<int> singleDGrid;
4
     OneDGrid<OneDGrid<int>> twoDGrid:
5
     OneDGrid<OneDGrid<OneDGrid<int>>> threeDGrid:
6
7
     singleDGrid[3] = 5;
8
     twoDGrid[3][3] = 5;
9
     threeDGrid[3][3][3] = 5;
10
11
```

- We have solved the resizing problem.
- N dimensional grids can be generated through recursive types.
- But, the nested types are messy, e.g.
 OneDGrid<OneDGrid<int>>> threeDGrid;
- It would be nicer to write: NDGrid<int ,3> threeDGrid;
- We can do this through a recursive template...

Recursive Template Class

```
template <typename T, size_t N>
  class NDGrid {
  public:
     explicit NDGrid(size_t inSize = 10);
     virtual ~NDGrid():
5
6
     NDGrid<T, N-1>& operator[](size_t x);
8
     const NDGrid<T, N-1>& operator[](size t x) const;
9
     void resize(size_t newSize);
10
     size_t getSize() const { return mElems.size(); }
11
12
13
  private:
     std::vector<NDGrid<T, N-1>> mElems;
14
15
```

- The private vector field is recursive on the template class!
- It creates a NDGrid class of dimension N-1.
- Also note the operator[] functions return references to NDGrid<T, N-1> objects not T objects!
- How do we stop the recursion?

Recursive Template Base Class

Stop the recursion with a partial specialization for dimension 1.

```
template <typename T>
   class NDGrid<T, 1> {
   public:
     explicit NDGrid(size t inSize = 10);
4
     virtual ~NDGrid():
5
6
7
     T& operator[](size_t x);
8
     const T& operator[](size t x) const;
9
10
     void resize(size_t newSize);
     size_t getSize() const { return mElems.size(); }
11
12
13
   private:
     std::vector<T> mElems;
14
15
```

• The private vector and operator[] types are now of type T.

Recursive Template Implementation

```
template <typename T, size t N>
   NDGrid<T, N>::NDGrid(size t inSize) {
 3
     resize(inSize);
 4
 5
   template <typename T, size t N>
   NDGrid<T, N>:: "NDGrid() {
8
      // Nothing to do, the vector will clean up itself.
9
10
11
   template <typename T, size_t N>
12
   void NDGrid<T, N>::resize(size t newSize) {
13
     mElems.resize(newSize):
14
     // Resizing the vector calls the 0-argument constructor for
15
     // the NDGrid<T, N-1> elements, which constructs
16
     // it with the default size. Thus, we must explicitly call
17
     // resize() on each of the elements to recursively resize all
     // nested Grid elements.
18
19
      for (auto& element : mElems) {
20
       element.resize(newSize);
21
22
23
24
   template <typename T, size_t N>
25
   NDGrid<T, N-1>& NDGrid<T, N>::operator[](size t x) {
26
      return mElems[x];
27
28
29
   template <typename T, size t N>
30
   const NDGrid<T, N-1>& NDGrid<T, N>::operator[](size t x) const {
31
      return mElems[x]:
32
```

Partial Specialization Implementation

```
template <typename T>
   NDGrid<T, 1>::NDGrid(size_t inSize) {
     resize(inSize);
4
5
   template <typename T>
   NDGrid<T, 1>:: NDGrid() {
     // Nothing to do, the vector will clean up itself.
8
9
10
   template <typename T>
11
   void NDGrid<T, 1>::resize(size t newSize) {
12
13
     mElems.resize(newSize);
14
15
   template <typename T>
16
   T& NDGrid<T, 1>::operator[](size t x) {
17
     return mElems[x]:
18
19
20
21
   template <typename T>
   const T& NDGrid<T, 1>::operator[](size t x) const {
22
     return mElems[x]:
23
24
```

15

User Code

The following user code now works and is much cleaner than the earlier version.

```
#include "NDGrid.h"
2
   #include <iostream>
4
   int main() {
     NDGrid<int, 3> my3DGrid(3);
6
     my3DGrid[2][1][2] = 5;
7
     my3DGrid[1][1][1] = 5;
8
9
10
     std::cout << my3DGrid[2][1][2] << std::endl;
11
12
     return 0;
13
```

Compile-Time Expressions

Calculating Square Root

17

```
#include <iostream>
2
3
    // primary template to compute sgrt (N)
   template <long N, long LO=1, long HI=N>
   struct Sgrt {
     // compute the midpoint, rounded up
6
     static const long mid = (LO+HI+1)/2;
7
     // search a not too large value in a halved interval
     static const long result = (N<mid*mid) ?
9
                           (long) Sgrt<N,LO,mid-1>::result
10
                           : (long) Sart<N.mid.HI>::result;
11
12
13
14
   // partial specialisation for the case when LO equals HI
   template<long N, long M>
15
   struct Sqrt<N,M,M> {
16
     static const long result = M;
17
18
19
20
   int main() {
     std::cout << Sqrt<16>::result << std::endl;</pre>
21
22
```

Compile-Time Selection

Client code:

Template Recursion Expressions

```
std::cout << Sqrt<16>::result << std::endl;</pre>
  Compile-time computations:
    Sqrt<16>::result expanded to Sqrt<16, 1, 16>::result
   mid = (1+16+1)/2 = 9
   result = (16 < 9*9 ? Sqrt<16,1,8>::result
                        : Sqrt<16,9.16>::result
           = Sqrt<16,1,8>::result
   mid = (1+8+1)/2 = 5
   result = (16 < 5*5 ? Sqrt<16,1,4>::result
                        : Sqrt<16,5.8>::result
           = Sqrt<16,1,4>::result
    . . .
```

Finally, the specialisation Sqrt<16, 4, 4>::result=4 called

C++11 constexpr Version

```
#include <iostream>
 2
 3
     static constexpr long ct_mid(long a, long b) {
          return (a+b) / 2;
 4
 5
 6
7
     static constexpr long ct pow(long a) {
 8
          return a*a;
 9
10
11
     static constexpr long ct sgrt(long res, long lo, long hi) {
12
          return
13
               lo == hi ? hi // case when lo == hi
14
               : ct sqrt(res, ct pow(
15
                    \operatorname{ct} \operatorname{mid}(\operatorname{lo}, \operatorname{hi}) > = \operatorname{res} ? \operatorname{lo} : \operatorname{ct} \operatorname{mid}(\operatorname{lo}, \operatorname{hi}) + 1,
16
                    ct_pow(ct_mid(lo, hi)) >= res ? ct_mid(lo, hi) : hi);
17
18
19
     static constexpr long ct sgrt(long res) {
20
          return ct_sqrt(res, 1, res);
21
22
23
     int main() {
24
       std::cout << ct sqrt(16) << std::endl;
25
```

No need for the class variables storing the mid point, but can still be confusing.

C++14 constexpr Version

```
#include <iostream>
 2
3
   static constexpr long ct_sqrt(long res, long lo, long hi) {
     if(lo == hi) {
        return hi;
6
      } else {
 7
        const auto mid = (lo + hi) / 2:
8
9
        if(mid * mid >= res) {
10
          return ct_sqrt(res, lo, mid);
11
        } else {
12
          return ct sgrt (res, mid + 1, hi);
13
14
15
16
17
   static constexpr long ct_sqrt(long res) {
18
      return ct_sqrt(res, 1, res);
19
20
21
   int main() {
22
      std::cout << ct_sqrt(16) << std::endl;
23
```

- In C++14 can use if statements and loops in constexpr
- Not supported in g++ 4.9.2! Need clang++-3.5
- Example from:

Passing a Meta Template Function as a Parameter

```
// Passes a "meta template function" as a parameter at compile time.
   #include <iostream>
3
4 // Accumulates the results of F(0)..F(n)
  // class template with a template template parameter F
  template<int n, template<int> class F>
7 struct Accumulate {
     static const int val = Accumulate<n-1, F>::val + F<n>::val;
9
10
  // The stopping criterion (returns the value F(0))
11
  template<template<int> class F>
12
   struct Accumulate<0, F> {
13
     static const int val = F<0>::val;
14
  1 };
15
16 // Various "functions":
17 | template<int n> struct Identity {
18
     static const int val = n;
19
20
   template<int n> struct Square {
21
     static const int val = n*n;
22
23
   template<int n> struct Cube {
24
     static const int val = n*n*n;
25
   };
26
27
   int main() {
28
     std::cout << Accumulate<4, Identity>::val << std::endl; // 10
29
     std::cout << Accumulate<4, Square>::val << std::endl; // 30
30
     std::cout << Accumulate<4, Cube>::val << std::endl; // 100
31
```

Passing a Function as a Parameter at Compile Time

- Using a template template parameter to simulate passing a function as a parameter to another function
- What does it compute?

$$F(n) +_F(n-1) + ... F(0)$$

• For three different functions passed:

```
Identity(4) +_I Identity(3) + ... Identity(0) = 10
Square(4) + Square(3) + ... Square(0) = 30
Cube(4) + Cube(3) + ... Cube(0) = 100
```

• See http://en.cppreference.com/w/cpp/language/ template_parameters#Template_template_arguments

BubbleSort I

```
#include <iostream>
   // function to swap two values
   template<int I, int J>
   struct IntSwap {
 4
     static inline void compareAndSwap(int* data) {
 5
       if (data[I] > data[J])
6
 7
         std::swap(data[I], data[J]);
 8
9
10
   // loop to go through array
11
   template<int I, int J>
12
   class IntBubbleSortLoop {
13
14
   private:
     static const bool go = (J \le I-2);
15
   public:
16
     static inline void loop(int* data) {
17
18
       IntSwap<J, J+1>::compareAndSwap(data);
       IntBubbleSortLoop<go ? I : 0, go ? (J+1) : 0>::loop(data);
19
20
21
```

BubbleSort II

```
22
   template <>
23
24
   struct IntBubbleSortLoop<0,0> {
     static inline void loop(int*) { }
25
26
27
28
   // recursive metafunction to keep looping until sorted
   template<int N>
29
30
   struct IntBubbleSort {
     static inline void sort(int* data) {
31
       IntBubbleSortLoop<N-1,0>::loop(data);
32
33
       IntBubbleSort<N-1>::sort(data);
34
35
36
   template <>
37
   struct IntBubbleSort<1> {
38
     static inline void sort(int* data) { }
39
40
```

Client Code

```
int main() {
     int a[] = {3, 1, 2, 5};
     IntBubbleSort<4>::sort(a):
     for (int i = 0; i < 4; i++)
4
5
       std::cout << a[i] << " ";
     std::cout << std::endl;
6
7
     // sort is called at runtime
8
     // metatemplate compiles required templates at compile time.
9
     a[0] = 100;
10
     IntBubbleSort<4>::sort(a):
11
12
     for (int i = 0; i < 4; i++)
       std::cout << a[i] << " ";
13
     std::cout << std::endl;
14
15
```

Output:

```
1 1 2 3 5
2 2 3 5 100
```

Client Instantiations

 Ideally, some extensive instantiations may lead to (when N=4):

```
inline void IntBubbleSort4(int* data) {
   if (data[0] > data[1]) std::swap(data[0], data[1]);
   if (data[1] > data[2]) std::swap(data[1], data[2]);
   if (data[2] > data[3]) std::swap(data[2], data[3]);
   if (data[0] > data[1]) std::swap(data[0], data[1]);
   if (data[1] > data[2]) std::swap(data[1], data[2]);
   if (data[0] > data[1]) std::swap(data[0], data[1]);
}
```

The specialisation is several times faster than the standard algorithm

Benefits and Drawback of C++ Metaprogramming

- Compile-time versus execution-time tradeoff
- Generic programming
- Readability (can be hard to understand)
- Code bloat (due to some extensive instantiations/specialisations)

Type Relations, Type Traits and enable_if

- Recall the type_traits library from week 7.
- We can use the type_trait is_same to figure out if two variables are of the same type.

```
#include <iostream>
    #include <string>
   #include <tvpe_traits>
   template<typename T1, typename T2>
   void same (const T1& t1, const T2& t2) {
     bool sameType = std::is_same<T1, T2>::value;
      std::cout << "'" << t1 << "' and '" << t2 << "' are ";
      std::cout << (sameType ? "the same types." : "different types.") << std::endl;
10
11
12
   int main() {
13
      same(1, 32);
14
     same (1, 3.01):
15
      same(3.01, std::string("Test"));
16
```

Output:

```
'1' and '32' are the same types.
'1' and '3.01' are different types.
'3.01' and 'Test' are different types.
```

SFINAE and enable_if

- What if we want to only create a template function for certain types?
- enable_if can be used to disable certain function overloads based on type traits.
- enable_if takes two type parameters, the first is a bool indicating if to enable or disable this template.
- type_traits can be used to determine the value of the bool (i.e., metaprogramming).
- The second type parameter is passed through to the nested type ::type if the bool is true.
- If the bool is false, the second type parameter is not passed through and this can lead to compilation errors.
- But!, enable_if is an example of Substitution Failure Is Not An Error (SFINAE) which disables a function overload and backtracks to find another function overload that will compile.
 If no function is found than an error will be generated.

enable_if Example

```
template<typename T1, typename T2>
   typename std::enable if<std::is same<T1, T2>::value, bool>::type
   check type (const T1& t1, const T2& t2) {
      std::cout << "'" << t1 << "' and '" << t2 << "' ";
      std::cout << "are the same types." << std::endl;
 6
     return true;
 7
8
9
   template<typename T1, typename T2>
10
   typename std::enable_if<!std::is_same<T1, T2>::value, bool>::type
11
   check_type(const T1& t1, const T2& t2) {
      std::cout << "'" << t1 << "' and '" << t2 << "' ";
12
13
      std::cout << "are different types." << std::endl;
14
     return false:
15
16
17
   int main() {
18
     check_type(1, 32);
19
     check type(1, 3.01);
20
      check type(3.01, std::string("Test"));
21
```

- Return type of the function check_type is determined by enable_if, if the enable_if fails then no return type is provided.
- This causes an error, but because of SFINAE, the second overload will be generated.
- Leaving out either version of check_type will compile error.

Trailing return, Variadic and SFINAE template

```
#include <iostream>
2
   // this overload is always in the set of overloads
   // ellipsis parameter has the lowest ranking for overload resolution
   void test(...) {
     std::cout << "Catch-all overload called" << std::endl;
7
8
   // this overload is added to the set of overloads if
   // C is a reference-to-class type and F is a member function pointer
10
  template < class C, class F>
11 l
  auto test(C c, F f) \rightarrow decltype((void)(c.*f)(), void()) {
12
     std::cout << "Reference overload called" << std::endl;</pre>
13
14
15
16 // this overload is added to the set of overloads if
   // C is a pointer-to-class type and F is a member function pointer
17
  template < class C. class F>
18
  auto test(C c, F f) \rightarrow decltype((void)((c\rightarrow*f)()), void()) {
19
     std::cout << "Pointer overload called" << std::endl;</pre>
20
21
```

Trailing return, Variadic and SFINAE template

User code:

```
struct X { void f() {} };

int main(){
    X x;
    test( x, &X::f);
    test(&x, &X::f);
    test(42, 1337);
}
```

Output:

```
1 Reference overload called
2 Pointer overload called
3 Catch-all overload called
```

Static Assert

Consider if we want a function that operates only on classes that inherit from a particular base class or have a particular type trait?

```
#include <type_traits>
  class Base1 {};
  class Base1Child : public Base1 {};
5
  class Base2 {};
  class Base2Child : public Base2 {};
8
  template<typename T>
  void process(const T& t) {
10
    static_assert(std::is_base_of<Base1, T>::value,
11
        "Base1 should be a base for T.");
12
13
14
15
  int main(){
    process (Base1());
16
17
    process (BaselChild());
    18
19
    process(Base2Child()); // Compile Error
20
```

unique_ptr.h Implementation

- We now have all the understanding to read the implementations of the STL classes in the compiler!
- Let's look at the unique_ptr.h source
- https:
 //android.googlesource.com/platform/prebuilts/
 gcc/linux-x86/host/x86_64-w64-mingw32-4.8/+/
 l-preview/x86_64-w64-mingw32/include/c++/4.8.3/
 bits/unique_ptr.h

Struct template in unique_ptr.h

```
/// Primary template, default_delete.
  template<typename _Tp>
  struct default delete {
     constexpr default_delete() noexcept = default;
5
     template<typename _Up, typename = typename
6
         enable_if<is_convertible<_Up*, _Tp*>::value>::tvpe>
7
       default_delete(const default_delete<_Up>&) noexcept { }
8
9
10
     void operator()(_Tp* __ptr) const {
       static assert(sizeof(Tp)>0,
11
         "can't delete pointer to incomplete type");
12
       delete ptr;
13
14
15
```

In one struct: constexpr, noexcept, enable_if, type traits, functors, static assert

Template Specialization in unique_ptr.h

```
// DR 740 - omit specialization for array objects with a
   // compile time length
   /// Specialization, default_delete.
  template<tvpename Tp>
  struct default delete < Tp[]> {
    // ...
6
     void operator()(_Tp* __ptr) const {
8
         static assert(sizeof(Tp)>0,
           "can't delete pointer to incomplete type");
9
10
         delete [] __ptr;
11
12
       template<typename _Up>
13
       typename enable if < is derived Tp < Up >:: value >:: type
14
15
       operator()(_Up*) const = delete;
16
```

Template specialization and deleting a function based on enable_if

Inner class in Unique_ptr class in unique_ptr.h

```
/// 20.7.1.2 unique_ptr for single objects.
  template <typename _Tp, typename _Dp = default_delete<_Tp> >
  class unique ptr {
     // use SFINAE to determine whether _Del::pointer exists
    class Pointer {
5
6
7
      template<tvpename Up>
8
       static typename Up::pointer test(typename Up::pointer*)
9
      template<typename _Up>
10
      static Tp* test(...);
11
12
13
      typedef typename remove reference < Dp>::type Del;
     public:
14
      typedef decltype( test< Del>(0)) type;
15
     };
16
17
```

Default arguments, Inner classes, SFINAE, decltype

Constructors in Unique_ptr class in unique_ptr.h

```
// Constructors.
     constexpr unique ptr() noexcept : M t()
     { static assert(!is pointer<deleter type>::value,
       "constructed with null function pointer deleter"); }
5
6
     unique_ptr(pointer __p,
     typename remove_reference<deleter_type>::type&& __d) noexcept
7
     : M t(std::move( p), std::move( d))
     { static_assert(!std::is_reference<deleter_type>::value,
       "rvalue deleter bound to reference"); }
10
11
     constexpr unique_ptr(nullptr_t) noexcept : unique_ptr()
12
13
14
     // Move constructors.
     unique_ptr(unique_ptr&& __u) noexcept
15
16
     : _M_t(__u.release(), std::forward<deleter_type>(__u.get_deleter())
17
```

Constructors, Member initialization lists, std::move, Delegating Constructors

Operators in Unique_ptr class in unique_ptr.h

```
// Destructor.
     ~unique_ptr() noexcept {
       auto& ptr = std::get<0>( M t);
       if ( ptr != nullptr)
4
         get_deleter()(__ptr);
5
       __ptr = pointer();
6
7
8
9
     // Assignment.
10
     unique_ptr& operator=(unique_ptr&& __u) noexcept {
11
       reset( u.release());
       get_deleter() = std::forward<deleter_type>(__u.get_deleter());
12
13
       return *this:
14
15
     unique ptr& operator=(nullptr t) noexcept {
16
       reset():
17
18
       return *this:
19
```

Destructors, Operator overloading, r-value references, std::forward, Function overloading

Member functions in Unique_ptr class

```
void reset(pointer __p = pointer()) noexcept {
       using std::swap;
2
       swap(std::get<0>(_M_t), __p);
3
       if (__p != pointer())
4
         get_deleter()(__p);
5
6
7
     void swap(unique_ptr& __u) noexcept {
       using std::swap;
9
       swap(_M_t, __u._M_t);
10
11
12
13
```

Member functions, using statements, namespaces, STL algorithms

Reading

- Metaprogramming http://www.ibm.com/developerworks/linux/library/ l-metaprog1/index.html
- Chapter 5, Thinking in C++ (Eckel)
- Chapter 15, C++ Templates (Vandevoorde and Josuttis)
- C++ Template Metaprogramming (David Abrahams and Aleksey Gurtovoy), 2005.