

Time and Work

Rule :

If A can do a piece of work in n days, then

The work done by A in one day = $1/n$

Rule:

Chocolate Rule or unitary method

Rule :

Whosoever is more efficient will take less time

Rules and Tricks:

Rule 1: Universal Rule

This rule can be used in almost every problems.

- If M_1 persons can do W_1 work in D_1 days and M_2 persons can do W_2 works in D_2 days then we can say

$$M_1 D_1 W_2 = M_2 D_2 W_1$$

- If the persons work T_1 and T_2 hours per day respectively then the equation gets modified to

$$M_1 D_1 T_1 W_2 = M_2 D_2 T_2 W_1$$

- If the persons has efficiency of E_1 and E_2 respectively then,

$$M_1 D_1 T_1 E_1 W_2 = M_2 D_2 T_2 E_2 W_1$$

Rule :

If A can do a piece of work in X days and B can do the same work in Y days, then both of them working together will do the same work in

$$\frac{XY}{X + y} \text{ days.}$$

Rule :

Two persons A and B, working together, can complete a piece of work in X days. If A, working alone, can complete the work in Y days, then B, working alone, will complete the work in

$$\frac{XY}{Y - X} \text{ days.}$$

- salary must be divided according to efficiency
i.e number of Chocolates consumed

- IF A can complete a task in x days
- B Can Complete same task in y days
- C can Complete same task in z days
- Then in how many days A' and B' and C' will complete the same task
- No of days = $1 / ((A'/Ax) + (B'/By) + (C' / Cz))$
- Where A' B' C' new set of persons
-
- A B C previous corresponding set of persons
-
- x y z Corresponding number of days

PIPES & CISTERNS

✓ If a pipe can fill a tank in x hours, then

$$\text{Part of tank filled in 1 hour} = \frac{1}{x}$$

✓ If a pipe can empty a tank in y hours, then

$$\text{Part of tank emptied in 1 hour} = \frac{1}{y}$$

Rules and Tricks:

Rule 1:

Two pipes A and B can fill (or empty) a cistern in X and Y hours respectively, while working alone. If both the pipes are opened together, then the time taken to fill (or empty) the cistern is given by

$$\left\{ \frac{XY}{X + Y} \right\} \text{ hours.}$$

- Chocolate Rule or unitary method
- Every time **outlet** pipe is mentioned efficiency will come with **negative** sign

Rule 4:

A pipe can fill a cistern in x hours. Because of a **leak** in the bottom, it is filled in y hours. If it is full, the time taken by the leak to empty the cistern is

$$\frac{XY}{Y - X} \text{ hours.}$$



TIME & DISTANCE



✓ Speed, Time and Distance

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}} \quad \text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

$$\text{Distance} = \text{Speed} \times \text{Time}$$

✓ km/hr to m/sec conversion:

$$a \text{ km/hr} = a \times \frac{5}{18} \text{ m/sec}$$

✓ m/sec to km/hr conversion:

$$a \text{ m/sec} = a \times \frac{18}{5} \text{ km/hr}$$



- ✓ If the ratio of speeds of A and B is $a : b$, then the ratio of the time taken by them to cover the same distance will be $\frac{1}{a} : \frac{1}{b}$ or $b : a$
- ✓ Suppose a man covers a certain distance at x km/hr and an equal distance at y km/hr, then the average speed of whole journey $= \frac{2xy}{x+y}$ km/hr

- Average Speed = Total Distance / Total Time
- $S_1/S_2 = \sqrt{T_2} / \sqrt{T_1}$
- (only to be used when **after crossing** each other is mentioned in statement)

PROBLEM ON TRAINS

- ✓ Time taken by a train of length l meters to pass a pole or standing man or signal post is equal to the time taken by the train to cover l meters.
- ✓ Time taken by a train of length l meters to pass a stationary object of length b meters is equal to the time taken by the train to cover $(l + b)$ meters.
- ✓ Suppose two trains are moving in same direction at u m/s and v m/s, where $u > v$, then their relative speed will be $(u - v)$ m/s.
- ✓ Suppose two trains are moving in opposite direction at u m/s and v m/s, then their relative speed will be $(u + v)$ m/s.

- Time taken by two trains to cross each other if moving in same direction

$$T = D/S = (L_1 + L_2) / (S_1 - S_2) \quad S_1 > S_2$$

If moving in opposite direction

$$T = D/S = (L_1 + L_2) / (S_1 + S_2)$$

L_1 = Length of first Train & S_1 = Speed of First Train

L_2 = Length of Second Train & S_2 = Speed of second Train

BOATS & STREAMS

✓ **Downstream / Upstream**

In water, the direction along the stream is called Downstream and the direction against the stream is called Upstream.

- ✓ If the speed of a boat in still water is u km/hr and the speed of stream is v km/hr, then

$$\text{Speed Downstream} = (u + v) \text{ km / hr}$$

$$\text{Speed Upstream} = (u - v) \text{ km / hr}$$

- ✓ If the speed downstream is a km/hr and speed upstream is b km/hr, then:

$$\text{Speed in still water} = \frac{1}{2} (a + b) \text{ km/hr}$$

$$\text{Rate of stream} = \frac{1}{2} (a - b) \text{ km/hr}$$