### **Kearns**

# The following is not exhaustive but is a list of topics that have appeared on previous finals Basic Knowledge: Lectures, Labs, Readings, Homework

#### Vocabulary

- Graphs: directed, in-degree, out degree, weighted, path, acyclic, path length, depth, Euler path, Hamilton Path. source, sink, flow network, flow, flow value, cut, cut capacity, DFS and BFS (tree, back, forward, cross edges)
- Trees: leaf, height, spanning tree, minimal spanning tree
- Min Heap, Max Heap, sift down, sift up
- Dynamic Programming: optimal substructure, common subsequence, increasing subsequence, path in a 2 dimensional grid
- NP vs P, NP complete, problem reduction

# Sections from the text and topics from lecture and lab

#### Analysis knowledge

- Analysis framework know steps and be able to apply
- Asymptotic notations and their properties, **Formal definitions** of O(),  $\Omega$ () and  $\Theta$ ()
- Properties of logarithms, number of elements of n element set, permutations and combinations, summation formulas for arithmetic and geometric sequences, summation rules,
- Recurrence relations and their solutions using back substitution and recursion tree, Be able to use Master Theorem it will be provided if needed.

#### **Brute force**

- Traveling Salesperson and Knapsack problems
- Bread first search
- · Depth first search

## Basic data structure problems

- Topological Sort both DFS and Source removal algorithms
- Recursive algorithms for generating subsets and permutations
- Partitioning, Heaps, Heap Sort (includes construction of heap)

#### Divide and conquer

Merge Sort, Quick Sort, Closest Pair

#### **Greedy approach**

- Weighted Average Time to Completion
- Prim's algorithm MST Dijkstra's Algorithm Shortest path Cut property Proofs of correctness

# **Dynamic programming**

- Coin row problem, Robot coin collection
- Longest increasing subsequence
- Longest common subsequence
- Knapsack 0-1, Knapsack with repeats
- Matrix chain multiplication, Edit Distance

# **Iterative Improvement**

- Ford-Fulkerson Shortest Augmenting Path Algorithm, Max-Flow, Min Cut Theorem
- Stable Marriage

#### Backtracking, Branch and Bound, Approximation

- Backtracking: Subset Sum
- Branch and Bound: Knapsack Problem
- Approximations for TSP and Knapsack, Twice around the tree, proof: Twice around the Tree is a 2 approximation

#### P, NP, NP complete

- P and NP
- NP complete and Problem Reduction (Min Vert Cover, Max Clique, Max Independent Set)

# **Thought problems**

• Choose 2-3 of 3-5 problems provided. Describe and analyze the algorithms that solve the problems you select. These problems will be closely related to problems either covered in class, labs, or assignments