Optimizations

CSCI 2021: Machine Architecture and Organization

Antonia Zhai

Department Computer Science and Engineering

University of Minnesota

http://www.cs.umn.edu/~zhai

With Slides from Bryant



Overview

- Generally Useful Optimizations
 - Code motion/precomputation
 - Strength reduction
 - Sharing of common subexpressions
 - · Removing unnecessary procedure calls
- Optimization Blockers
 - · Procedure calls
 - · Memory aliasing
- Exploiting Instruction-Level Parallelism
- · Dealing with Conditionals

Performance Realities

- There's more to performance than asymptotic complexity
- · Constant factors matter too!
 - Easily see 10:1 performance range depending on how code is written
 - Must optimize at multiple levels:
 - algorithm, data representations, procedures, and loops
- Must understand system to optimize performance
 - · How programs are compiled and executed
 - · How to measure program performance and identify bottlenecks
 - How to improve performance without destroying code modularity and generality

With Slides from Bryant

Optimizing Compilers

- · Provide efficient mapping of program to machine
 - · register allocation
 - code selection and ordering (scheduling)
 - · dead code elimination
 - · eliminating minor inefficiencies
- Don't (usually) improve asymptotic efficiency
 - · up to programmer to select best overall algorithm
 - big-O savings are (often) more important than constant factors
 - · but constant factors also matter
- · Have difficulty overcoming "optimization blockers"
 - · potential memory aliasing
 - · potential procedure side-effects

Limitations of Optimizing Compilers

- Operate under fundamental constraint
 - · Must not cause any change in program behavior
 - Often prevents it from making optimizations when would only affect behavior under pathological conditions.
- Behavior that may be obvious to the programmer can be obfuscated by languages and coding styles
 - e.g., Data ranges may be more limited than variable types suggest
- Most analysis is performed only within procedures
 - · Whole-program analysis is too expensive in most cases
- Most analysis is based only on static information
 - · Compiler has difficulty anticipating run-time inputs
- When in doubt, the compiler must be conservative

With Slides from Bryant

Generally Useful Optimizations

- Optimizations that you or the compiler should do regardless of processor / compiler
- · Code Motion
 - · Reduce frequency with which computation performed
 - · If it will always produce same result
 - · Especially moving code out of loop

```
void set_row(double *a, double *b,
    long i, long n)
{
    long j;
    for (j = 0; j < n; j++)
        a[n*i+j] = b[j];
}</pre>
long j;
int ni = n*i;
for (j = 0; j < n; j++)
    a[ni+j] = b[j];

a[ni+j] = b[j];
```

Compiler-Generated Code Motion id set row(double *a, double *b, long j; long i, long n) long ni = n*i; double *rowp = a+ni; long j; for (j = 0; j < n; j++)for (j = 0; j < n; j++)*rowp++ = b[j]; a[n*i+j] = b[j];set_row: testq %rcx, %rcx # Test n # If 0, goto done %rcx, %rax # rax = n movq # rax *= i %rdx, %rax imulq leaq (%rdi,%rax,8), %rdx # rowp = A + n*i*8\$0, %r8d # j = 0 .L3: # loop: (%rsi,%r8,8), %rax # t = b[j] %rax, (%rdx) # *rowp = t \$1, %r8 # j++ \$8, %rdx # rowp++ addq cmpq %r8, %rcx # Compare n:j .L3 # If >, goto loop .L4: # done: rep ; ret

Reduction in Strength

- · Replace costly operation with simpler one
- · Shift, add instead of multiply or divide

```
16*x --> x << 4
```

- · Utility machine dependent
- · Depends on cost of multiply or divide instruction
 - · On Intel Nehalem, integer multiply requires 3 CPU cycles
- · Recognize sequence of products

```
for (i = 0; i < n; i++)
  for (j = 0; j < n; j++)
   a[n*i + j] = b[j];

int ni = 0;
  for (i = 0; i < n; i++) {
   for (j = 0; j < n; j++)
    a[ni + j] = b[j];
   ni += n;
}</pre>
```

Share Common Subexpressions

- · Reuse portions of expressions
- Compilers often not very sophisticated in exploiting arithmetic properties

```
/* Sum neighbors of i,j */
up = val[(i-1)*n + j ];
down = val[(i+1)*n + j ];
left = val[i*n + j-1];
right = val[i*n + j+1];
sum = up + down + left + right;
```

```
up = val[inj - n];
down = val[inj + n];
left = val[inj - 1];
right = val[inj + 1];
sum = up + down + left + right;
```

3 multiplications: i*n, (i-1)*n, (i+1)*n

```
leaq 1(%rsi), %rax # i+1
leaq -1(%rsi), %r8 # i-1
imulq %rcx, %rsi # i*n
imulq %rcx, %rax # (i+1)*n
imulq %rcx, %r8 # (i-1)*n
addq %rdx, %rsi # i*n+j
addq %rdx, %rax # (i+1)*n+j
addq %rdx, %r8 # (i-1)*n+j
```

1 multiplication: i*n

long inj = i*n + j;

```
imulq %rcx, %rsi # i*n
addq %rdx, %rsi # i*n+j
movq %rsi, %rax # i*n+j
subq %rcx, %rax # i*n+j-n
leaq (%rsi,%rcx), %rcx # i*n+j+n
```

With Slides from Bryant

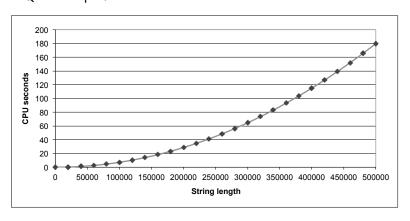
Optimization Blocker #1: Procedure Calls

• Procedure to Convert String to Lower Case

```
void lower(char *s)
{
  int i;
  for (i = 0; i < strlen(s); i++)
    if (s[i] >= 'A' && s[i] <= 'Z')
       s[i] -= ('A' - 'a');
}</pre>
```

Lower Case Conversion Performance

- · Time quadruples when double string length
- · Quadratic performance



With Slides from Bryant

Convert Loop To Goto Form

```
void lower(char *s)
{
   int i = 0;
   if (i >= strlen(s))
     goto done;
loop:
   if (s[i] >= 'A' && s[i] <= 'Z')
        s[i] -= ('A' - 'a');
   i++;
   if (i < strlen(s))
     goto loop;
done:
}</pre>
```

strlen executed every iteration

Calling Strlen

```
/* My version of strlen */
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
        s++;
        length++;
    }
    return length;
}
```

- Strlen performance
 - Only way to determine length of string is to scan its entire length, looking for null character.
- · Overall performance, string of length N
 - · N calls to strlen
 - Require times N, N-1, N-2, ..., 1
 - Overall O(N2) performance

With Slides from Bryant

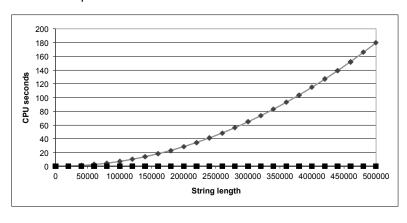
Improving Performance

```
void lower(char *s)
{
  int i;
  int len = strlen(s);
  for (i = 0; i < len; i++)
    if (s[i] >= 'A' && s[i] <= 'Z')
       s[i] -= ('A' - 'a');
}</pre>
```

- Move call to strlen outside of loop
- · Since result does not change from one iteration to another
- · Form of code motion

Lower Case Conversion Performance

- · Time doubles when double string length
- · Linear performance



With Slides from Bryant

Optimization Blocker: Procedure Calls

- Why couldn't compiler move strlen out of inner loop?
 - · Procedure may have side effects
 - Alters global state each time called
 - · Function may not return same value for given arguments
 - · Depends on other parts of global state
 - Procedure lower could interact with strlen
- Warning:
 - · Compiler treats procedure call as a black box
 - · Weak optimizations near them
- · Remedies:
 - Use of inline functions
 - GCC does this with -O2
 - · See web aside ASM:OPT
 - · Do your own code motion

```
int lencnt = 0;
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
        s++; length++;
    }
    lencnt += length;
    return length;
}
```

Memory Matters

```
/* Sum rows is of n X n matrix a
    and store in vector b */
void sum_rows1(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}</pre>
```

```
# sum_rows1 inner loop
.L53:

addsd (%rcx), %xmm0 # FP add
addq $8, %rcx
decq %rax
movsd %xmm0, (%rsi,%r8,8) # FP store
jne .L53
```

- Code updates b[i] on every iteration
- · Why couldn't compiler optimize this away?

With Slides from Bryant

Memory Aliasing

```
/* Sum rows is of n X n matrix a
    and store in vector b */
void sum_rows1(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}
double A[9] =</pre>
```

{ 0, 1, 2, 4, 8, 16}, 32, 64, 128};
double B[3] = A+3;

sum_rows1(A, B, 3);

Value of B:

```
init: [4, 8, 16]

i = 0: [3, 8, 16]

i = 1: [3, 22, 16]

i = 2: [3, 22, 224]
```

- Code updates b[i] on every iteration
- Must consider possibility that these updates will affect program behavior $$_{\rm With\ Slides\ from\ Bryant}$$

Removing Aliasing

```
/* Sum rows is of n X n matrix a
    and store in vector b */
void sum_rows2(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        double val = 0;
        for (j = 0; j < n; j++)
            val += a[i*n + j];
        b[i] = val;
    }
}</pre>
```

```
# sum_rows2 inner loop
.L66:
    addsd (%rcx), %xmm0 # FP Add
    addq $8, %rcx
    decq %rax
    jne .L66
```

· No need to store intermediate results

With Slides from Bryant

Optimization Blocker: Memory Aliasing

- · Aliasing
 - Two different memory references specify single location
 - Easy to have happen in C
 - · Since allowed to do address arithmetic
 - Direct access to storage structures
 - · Get in habit of introducing local variables
 - · Accumulating within loops
 - · Your way of telling compiler not to check for aliasing

Exploiting Instruction-Level Parallelism

- · Need general understanding of modern processor design
 - · Hardware can execute multiple instructions in parallel
- · Performance limited by data dependencies
- Simple transformations can have dramatic performance improvement
 - · Compilers often cannot make these transformations
 - Lack of associativity and distributivity in floating-point arithmetic

With Slides from Bryant

Benchmark Example: Data Type for Vectors

```
/* data structure for vectors */
typedef struct{
  int len;
  double *data;
} vec;
len
0 1 len-1
data

.....
```

```
/* retrieve vector element and store at val */
double get_vec_element(*vec, idx, double *val)
{
    if (idx < 0 || idx >= v->len)
        return 0;
    *val = v->data[idx];
    return 1;
}
```

Benchmark Computation

```
void combinel(vec_ptr v, data_t *dest)
{
    long int i;
    *dest = IDENT;
    for (i = 0; i < vec_length(v); i++) {
        data_t val;
        get_vec_element(v, i, &val);
        *dest = *dest OP val;
    }
}</pre>
```

Compute sum or product of vector elements

Data Types

- Use different declarations for data t
- int
- float
- double

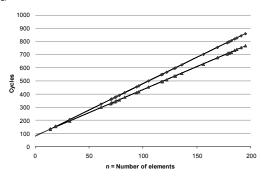
With Slides from Bryant

Operations

- Use different definitions of OP and IDENT
- + / 0
- * / 1

Cycles Per Element (CPE)

- Convenient way to express performance of program that operates on vectors or lists
- Length = n
- In our case: CPE = cycles per OP
- T = CPE*n + Overhead
 - · CPE is slope of line



Benchmark Performance

```
void combine1(vec_ptr v, data_t *dest)
{
    long int i;
    *dest = IDENT;
    for (i = 0; i < vec_length(v); i++) {
        data_t val;
        get_vec_element(v, i, &val);
        *dest = *dest OP val;
    }
}</pre>
```

Compute sum or product of vector elements

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Combine1 unoptimized	29.0	29.2	27.4	27.9
Combine1 -01	12.0	12.0	12.0	13.0

With Slides from Bryant

Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
{
  int i;
  int length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}</pre>
```

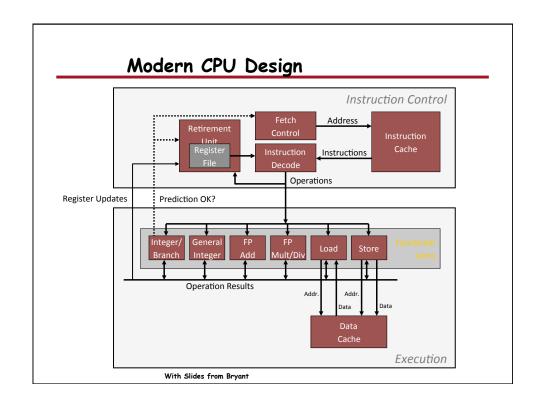
- Move vec_length out of loop
- Avoid bounds check on each cycle
- Accumulate in temporary

Effect of Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
{
  int i;
  int length = vec_length(v);
  data_t *d = get_vec_start(v);
  data_t t = IDENT;
  for (i = 0; i < length; i++)
    t = t OP d[i];
  *dest = t;
}</pre>
```

Method	Inte	ger	Double FP	
Operation	Add Mult		Add	Mult
Combine1 -O1	12.0	12.0	12.0	13.0
Combine4	2.0	3.0	3.0	5.0

· Eliminates sources of overhead in loop



Superscalar Processor

- Definition: A superscalar processor can issue and execute multiple instructions in one cycle. The instructions are retrieved from a sequential instruction stream and are usually scheduled dynamically.
- Benefit: without programming effort, superscalar processor can take advantage of the *instruction level parallelism* that most programs have
- Most CPUs since about 1998 are superscalar.
- Intel: since Pentium Pro

With Slides from Bryant

Nehalem CPU

- Multiple instructions can execute in parallel
 - 1 load, with address computation
 - 1 store, with address computation
 - 2 simple integer (one may be branch)
 - 1 complex integer (multiply/divide)
 - 1 FP Multiply
 - 1 FP Add
- Some instructions take > 1 cycle, but can be pipelined

Instruction	Latency	Cycles/Issue
Load / Store	4	1
Integer Multiply	3	1
Integer/Long Divide	1121	1121
Single/Double FP Multiply	4/5	1
Single/Double FP Add	3	1
Single/Double FP Divide	1023	1023

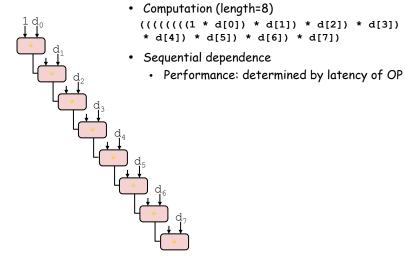
×86-64 Compilation of Combine4

• Inner Loop (Case: Integer Multiply)

Method	Integer Double FP		le FP	
Operation	Add Mult		Add	Mult
Combine4	2.0	3.0	3.0	5.0
Latency Bound	1.0	3.0	3.0	5.0

With Slides from Bryant

Combine4 = Serial Computation (OP = *)



Loop Unrolling

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
   int length = vec_length(v);
   int limit = length-1;
   data_t *d = get_vec_start(v);
   data_t x = IDENT;
   int i;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i+=2) {
        x = (x OP d[i]) OP d[i+1];
   }
   /* Finish any remaining elements */
   for (; i < length; i++) {
        x = x OP d[i];
   }
   *dest = x;
}</pre>
```

• Perform 2x more useful work per iteration

With Slides from Bryant

Effect of Loop Unrolling

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Latency Bound	1.0	3.0	3.0	5.0

- Helps integer multiply
 - · below latency bound
 - · Compiler does clever optimization
- Others don't improve. Why?
 - · Still sequential dependency

```
x = (x OP d[i]) OP d[i+1];
```

Loop Unrolling with Reassociation

```
void unroll2aa_combine(vec_ptr v, data_t *dest)
{
    int length = vec_length(v);
    int limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x = IDENT;
    int i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
        x = x OP (d[i] OP d[i+1]);
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
        x = x OP d[i];
    }
    *dest = x;
}</pre>
Compare to before

x = (x OP d[i]) OP d[i+1];
```

- Can this change the result of the computation?
- Yes, for FP. Why?

With Slides from Bryant

Effect of Reassociation

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

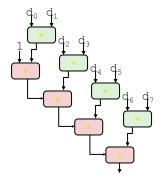
- Nearly 2x speedup for Int *, FP +, FP *
 - · Reason: Breaks sequential dependency

```
x = x OP (d[i] OP d[i+1]);
```

· Why is that? (next slide)

Reassociated Computation

x = x OP (d[i] OP d[i+1]);



- What changed:
 - Ops in the next iteration can be started early (no dependency)
- · Overall Performance
 - N elements, D cycles latency/op
 - Should be (N/2+1)*D cycles:
 CPE = D/2
 - Measured CPE slightly worse for FP mult

With Slides from Bryant

Loop Unrolling with Separate Accumulators

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
    int length = vec_length(v);
    int limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x0 = IDENT;
    data_t x1 = IDENT;
    int i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
        x0 = x0 OP d[i];
        x1 = x1 OP d[i+1];
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
        x0 = x0 OP d[i];
    }
    *dest = x0 OP x1;
}</pre>
```

· Different form of reassociation

Effect of Separate Accumulators

Method	Integer		Doub	le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Unroll 2x Parallel 2x	1.5	1.5	1.5	2.5
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

- 2x speedup (over unroll2) for Int *, FP +, FP *
 - Breaks sequential dependency in a "cleaner," more obvious way

$$x0 = x0 \text{ OP d[i]};$$

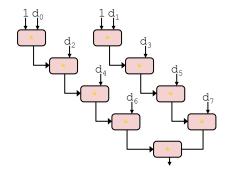
 $x1 = x1 \text{ OP d[i+1]};$

With Slides from Bryant

Separate Accumulators

$$x0 = x0 \text{ OP d[i];}$$

 $x1 = x1 \text{ OP d[i+1];}$



- What changed:
 - Two independent "streams" of operations
- Overall Performance
 - N elements, D cycles latency/op
 - Should be (N/2+1)*D cycles: CPE = D/2
 - CPE matches prediction!

What Now?

Unrolling & Accumulating

- Idea
 - · Can unroll to any degree L
 - · Can accumulate K results in parallel
 - · L must be multiple of K
- Limitations
 - · Diminishing returns
 - · Cannot go beyond throughput limitations of execution units
 - · Large overhead for short lengths
 - · Finish off iterations sequentially

With Slides from Bryant

Unrolling & Accumulating: Double *

- Case
 - Intel Nehelam (Shark machines)
 - Double FP Multiplication
 - · Latency bound: 5.00. Throughput bound: 1.00

FP*	Unrolling Factor L							
K	1	2	3	4	6	8	10	12
1	5.00	5.00	5.00	5.00	5.00	5.00		
2		2.50		2.50		2.50		
3			1.67					
4				1.25		1.25		
6					1.00			1.19
8						1.02		
10							1.01	
12								1.00

Unrolling & Accumulating: Int +

- Case
 - Intel Nehelam (Shark machines)
 - · Integer addition
 - Latency bound: 1.00. Throughput bound: 1.00

FP*		Unrolling Factor L						
K	1	2	3	4	6	8	10	12
1	2.00	2.00	1.00	1.01	1.02	1.03		
2		1.50		1.26		1.03		
3			1.00					
4				1.00		1.24		
6					1.00			1.02
8						1.03		
10							1.01	
12								1.09

With Slides from Bryant

Achievable Performance

Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Scalar Optimum	1.00	1.00	1.00	1.00
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	1.00	1.00	1.00	1.00

- Limited only by throughput of functional units
- Up to 29X improvement over original, unoptimized code

Using Vector Instructions

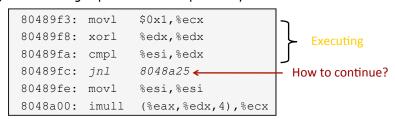
Method	Integer		Double FP	
Operation	Add	Mult	Add	Mult
Scalar Optimum	1.00	1.00	1.00	1.00
Vector Optimum	0.25	0.53	0.53	0.57
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	1.00	1.00	1.00	1.00
Vec Throughput Bound	0.25	0.50	0.50	0.50

- · Make use of SSE Instructions
 - · Parallel operations on multiple data elements
 - See Web Aside OPT:SIMD on CS:APP web page

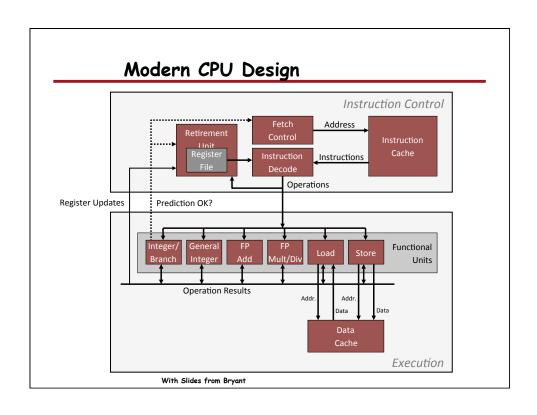
With Slides from Bryant

What About Branches?

- Challenge
 - Instruction Control Unit must work well ahead of Execution Unit to generate enough operations to keep EU busy

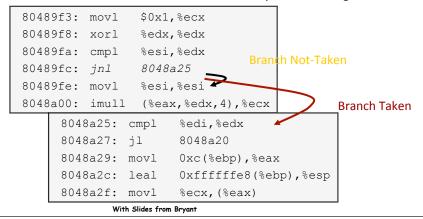


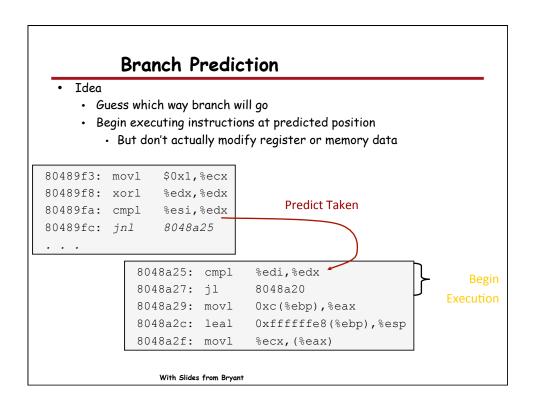
• When encounters conditional branch, cannot reliably determine where to continue fetching

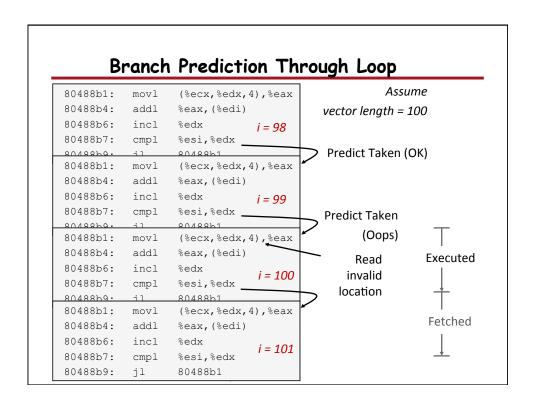


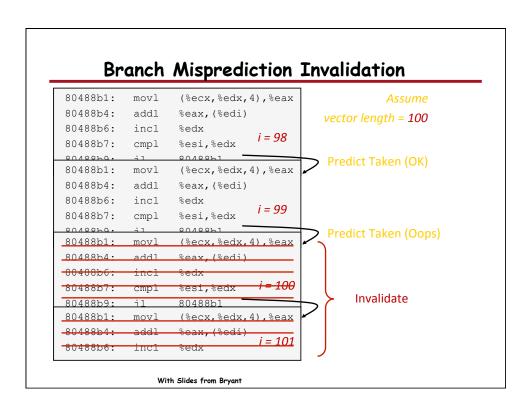


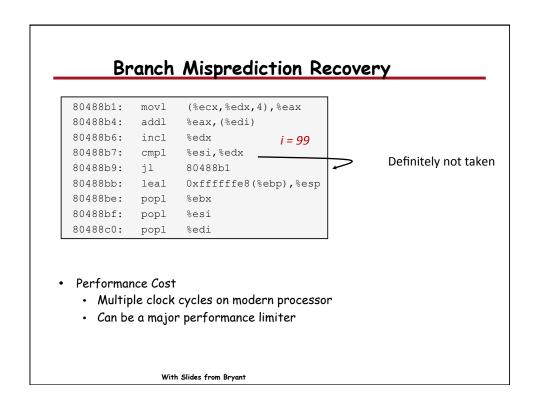
- When encounter conditional branch, cannot determine where to continue fetching
 - Branch Taken: Transfer control to branch target
 - Branch Not-Taken: Continue with next instruction in sequence
- · Cannot resolve until outcome determined by branch/integer unit











Effect of Branch Prediction

- Loops
 - Typically, only miss when hit loop end
- · Checking code
 - Reliably predicts that error won't occur

Method	Integer		Doub	le FP
Operation	Add Mult		Add	Mult
Combine4	2.0	3.0	3.0	5.0
Combine4b	4.0	4.0	4.0	5.0

With Slides from Bryant

Getting High Performance

- · Good compiler and flags
- Don't do anything stupid
 - · Watch out for hidden algorithmic inefficiencies
 - · Write compiler-friendly code
 - Watch out for optimization blockers: procedure calls & memory references
 - Look carefully at innermost loops (where most work is done)
- Tune code for machine
 - · Exploit instruction-level parallelism
 - · Avoid unpredictable branches
 - Make code cache friendly (Covered later in course)