Machine-Level Programming II: **Arithmetic and Control**

CSci 2021: Machine Architecture and Organization Lectures #8-9, February 6th-9th, 2015 Your instructor: Stephen McCamant

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Arithmetic and Control

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops
- Switch statements

Complete Memory Addressing Modes

- Most General Form
- D(Rb,Ri,S) Mem[Reg[Rb]+S*Reg[Ri]+D]
 - D: Constant "displacement" 1, 2, or 4 bytes
 - Rb: Base register: Any of 8 integer registers
 - Ri: Index register: Any, except for %esp
 - Unlikely you'd use %ebp, either
 - S: Scale: 1, 2, 4, or 8 (why these numbers?)
- Special Cases
- (Rb,Ri) Mem[Reg[Rb]+Reg[Ri]]
- D(Rb,Ri) Mem[Reg[Rb]+Reg[Ri]+D]
- (Rb,Ri,S) Mem[Reg[Rb]+S*Reg[Ri]]

Address Computation Examples

%edx	0xf000
%ecx	0x0100

Expression	Address Computation	Address
0x8 (%edx)		
(%edx,%ecx)		
(%edx,%ecx,4)		
0x80(,%edx,2)		

Address Computation Instruction

- leal Src,Dest
 - Src is address mode expression.
 - Set Dest to address denoted by expression
- Uses
 - Computing addresses without a memory reference
 - E.g., translation of p = &x[i];
 - Computing arithmetic expressions of the form x + k*y
 - k = 1, 2, 4, or 8

■ Example

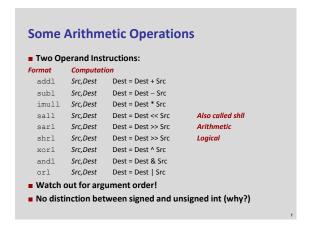
int mul12(int x) return x*12;

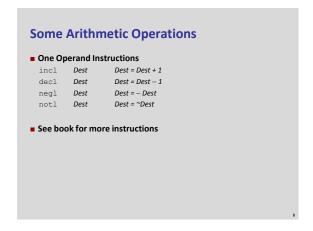
Converted to ASM by compiler:

leal (%eax, %eax, 2), %eax ;t <- x+x*2 sall \$2, %eax ;return t<<

Arithmetic and Control

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops
- Switch statements





```
Arithmetic Expression Example
                                   arith:
                                      pushl %ebp
int arith(int x, int y, int z)
                                      movl %esp, %ebp
  int t1 = x+y;
                                      movl
                                              8(%ebp), %ecx
  int t2 = z+t1:
                                              12(%ebp), %edx
(%edx,%edx,2), %eax
                                      movl
  int t3 = x+4;
                                      leal
  int t4 = y * 48;
int t5 = t3 + t4;
int rval = t2 * t5;
                                      sall
                                            $4, %eax
                                      leal
                                              4(%ecx,%eax), %eax
                                      addl %ecx, %edx
addl 16(%ebp), %edx
imull %edx, %eax
  return rval;
                                      popl
                                             %ebp
                                                                     Finish
                                      ret
```

```
Understanding arith
int arith(int x, int y, int z)
                                            Offset
  int t1 = x+y;
                                              16
                                                      z
  int t2 = z+t1:
  int t3 = x+4;
                                              12
  int t4 = y * 48;
int t5 = t3 + t4;
int rval = t2 * t5;
                                               8
  return rval;
                                                   Old %ebp
                                               Ω
                                                                -%ebp
  movl 8(%ebp), %ecx
  movl 12(%ebp), %edx
  leal
         (%edx,%edx,2), %eax
         $4, %eax
  sall
  leal
         4(%ecx,%eax), %eax
         %ecx, %edx
16(%ebp), %edx
  add1
  imull %edx, %eax
```

```
Stack
Understanding arith
int arith(int x, int y, int z)
                                                          16
  int t1 = x+v:
                                                                    z
  int t2 = z+t1;
                                                          12
                                                                    У
  int t3 = x+4;
  int t4 = v * 48
                                                                    х
  int t5 = t3 + t4;
int rval = t2 * t5;
                                                               Rtn Addr
  return rval;
                                                               Old %ebp
                                                           0
                                                                                -%ebp
           8(%ebp), %ecx
                                         \# ecx = x
  movl
                                         # edx = y
# eax = y*3
# eax *= 16 (t4)
           12(%ebp), %edx
                                        # eax = t4 +x+4 (t5)
# edx = x+y (t1)
# edx += z (t2)
# eax = t2 * t5 (rval)
  leal 4(%ecx,%eax), %eax
addl %ecx, %edx
addl 16(%ebp), %edx
  imull %edx, %eax
```

```
Observations about arith

    Instructions in different

int arith(int x, int y, int z)
                                                   order from C code

    Some expressions require

  int t1 = x+v:
  int t2 = z+t1;
                                                   multiple instructions
  int t3 = x+4;

    Some instructions cover

  int t4 = v * 48:
                                                  multiple expressions
  int t5 = t3 + t4;
int rval = t2 * t5;
                                                 • Get exact same code when
  return rval;
                                                   compile:
                                                 (x+y+z) * (x+4+48*y)
          8(%ebp), %ecx
                                       \# ecx = x
  movl
          12(%ebp), %edx
                                       # edx = y
 leal 4(%ecx, %eax), %eax
addl %ecx, %edx
addl 16(%ebp), %edx
imull %edx, %eax
                                       # eax = t4 +x+4 (t5)
# edx = x+y (t1)
# edx += z (t2)
                                       \# eax = t2 * t5 (rval)
```

```
Another Example
                                     logical:
                                         pushl %ebp
                                         movl %esp,%ebp
int logical(int x, int y)
                                         movl 12(%ebp),%eax
  int t1 = x^y;
                                         xorl 8(%ebp),%eax
  int t2 = t1 >> 17;
int mask = (1<<13) - 7;
int rval = t2 & mask;
                                         sarl $17,%eax
                                                                    Body
  return rval;
                                         popl %ebp
ret
                                                                     Finish
     movl 12(%ebp),%eax
                                 \# eax = y
                                 # eax = x^y (t1)
# eax = t1>>17 (t2)
# eax = t2 & mask (rval)
     xorl 8(%ebp),%eax
      sarl $17.%eax
     andl $8185,%eax
```

```
Another Example
                                      logical:
                                           pushl %ebp
                                                                     } Set Up
                                           movl %esp,%ebp
int logical(int x, int y)
                                           movl 12(%ebp),%eax
   int t1 = x^y;
                                           xorl 8(%ebp),%eax
sarl $17,%eax
  int t2 = t1 >> 17;
int mask = (1<<13) - 7;
int rval = t2 & mask;
                                                                        - Body
                                           andl $8185,%eax
  return rval;
                                           popl %ebp
                                           ret
                                                                        Finish
      movl 12(%ebp),%eax
                                  # eax = y
# eax = x^y
# eax = t1>>17
                                                          (t1)
      xorl 8(%ebp),%eax
sarl $17.%eax
                                                          (t2)
                                   # eax = t2 & mask (rval)
      andl $8185,%eax
```

```
Another Example
                                       logical:
                                          push1 %ebp
mov1 %esp,%ebp
                                                                      } Set Up
int logical(int x, int y)
                                           movl 12(%ebp),%eax
  int t1 = x^y;
  int t2 = t1 >> 17;
int mask = (1<<13) - 7;
int rval = t2 & mask;</pre>
                                           xorl 8(%ebp),%eax
                                           sarl $17.%eax

    Body

                                           andl $8185,%eax
  return rval:
                                           popl %ebp
                                                                          Finish
                                           ret
      movl 12(%ebp),%eax
                                   \# eax = y
                                   # eax = x^y (t1)
# eax = t1>>17 (t2)
# eax = t2 & mask (rval)
      xorl 8(%ebp),%eax
      sarl $17,%eax
      andl $8185,%eax
```

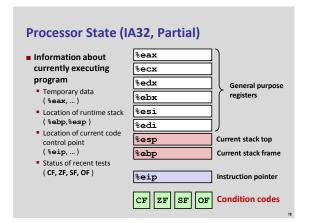
```
Another Example
                                      logical:
                                          pushl %ebp
movl %esp,%ebp
                                                                     } Set Up
int logical(int x, int y)
                                           movl 12(%ebp),%eax
   int t1 = x^y;
                                           xorl 8(%ebp),%eax
   int t2 = t1 >> 17:
  int mask = (1<<13) - 7;
int rval = t2 & mask;
                                           sarl $17.%eax

    Body

                                           andl $8185,%eax
  return rval:
                                           popl %ebp
                                                                         Finish
                                           ret
 2<sup>13</sup> = 8192, 2<sup>13</sup> - 7 = 8185
      movl 12(%ebp), %eax
                                   \# eax = y
      xorl 8(%ebp),%eax
                                  # eax = t1>>17 (t2)
# eax = t2 & mask (rval)
      sarl $17,%eax
andl $8185,%eax
```

```
Arithmetic and Control

Complete addressing mode, address computation (leal)
Arithmetic operations
Control: Condition codes
Conditional branches
Loops
Switch statements
```



Condition Codes (Implicit Setting) ■ Single bit registers ■CF Carry Flag (for unsigned) SF Sign Flag (for signed) ■ ZF Zero Flag OF Overflow Flag (for signed) ■ Implicitly set (think of it as side effect) by arithmetic operations Example: add1/addq Src,Dest ⇔ t = a+b CF set if carry out from most significant bit (unsigned overflow) ZF set if t == 0 SF set if t < 0 (as signed) OF set if two's-complement (signed) overflow (a>0 && b>0 && t>0 | | (a<0 && b<0 && t>=0) ■ Not set by lea instruction ■ Intel documentation, others, have full details

```
Condition Codes (Explicit Setting: Compare)

■ Explicit Setting by Compare Instruction

■ cmp1 / cmpq Src2, Src1

■ cmp1 b, a like computing a-b without setting destination

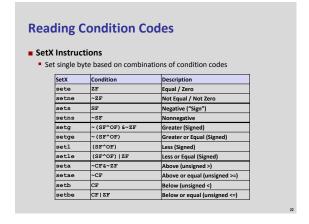
■ CF set if carry out from most significant bit (used for unsigned comparisons)

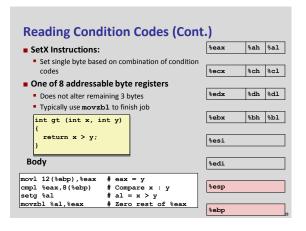
■ ZF set if (a-b) < 0 (as signed)

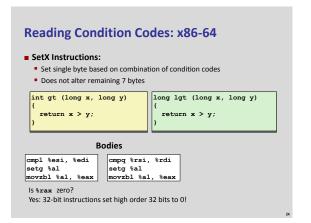
■ OF set if two's-complement (signed) overflow

(a>0 && b<0 && (a-b)<0) || (a<0 && b>0 && (a-b)>0)
```

Condition Codes (Explicit Setting: Test) ■ Explicit Setting by Test instruction ■test1/testq Src2, Src1 test1 b, a like computing a&b without setting destination ■Sets condition codes based on value of Src1 & Src2 ■Useful to have one of the operands be a mask ■ZF set when a&b == 0 ■SF set when a&b < 0







Exercise Break: More Conditions

- Every condition can be negated by putting "n" in the mnemonic, for "not"
 - We skipped some of these conditions in the previous tables, because they were equivalent to others
- Which other conditions are these equivalent to?
- 1. setng: not greater than
- 2. setnbe: not below or equal

Equivalents of More Conditions

- Intuition: cover three cases: <, =, >
- setng not greater than (signed)
- If not greater, than either less than or equal: setle
- Check conditions:
- ~(~(SF ^ OF) & ~ZF) = ~~(SF ^ OF) | ~~ZF = (SF ^ OF) | ZF ✓
- setnbe not below or equal (unsigned)
- If not below or equal, must be above: seta
- Check conditions:
- ~(CF | ZF) = ~CF & ~ZF ✓

Arithmetic and Control

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- **■** Control: Condition codes
- Conditional branches & Moves
- Loops
- Switch statements

Jumping

- jX Instructions
 - Jump to different part of code depending on condition codes

jΧ	Condition	Description
jmp	1	Unconditional
je	ZF	Equal / Zero
jne	~ZF	Not Equal / Not Zero
js	SF	Negative
jns	~SF	Nonnegative
jg	~(SF^OF) &~ZF	Greater (Signed)
jge	~(SF^OF)	Greater or Equal (Signed)
j1	(SF^OF)	Less (Signed)
jle	(SF^OF) ZF	Less or Equal (Signed)
ja	~CF&~ZF	Above (unsigned)
jb	CF	Below (unsigned)

Conditional Branch Example

```
int absdiff(int x, int y)
                                    pushl
                                            %ebp
                                                               Setup
     int result:
                                            %esp, %ebp
8(%ebp), %edx
                                    movl
    if (x > y) {
                                    movl
                                            12(%ebp), %eax
%eax, %edx
       result = x-y;
                                    movl
    } else {
                                    cmpl
                                                                Body1
       result = y-x;
                                    subl
                                            %eax, %edx
    return result;
                                    movl
                                            %edx, %eax
                                                                Body2a
                                    jmp .L7
                                 .L6
                                    subl %edx, %eax
                                  L7:
                                    popl %ebp
                                                             Finish
```

```
Conditional Branch Example (Cont.)
```

```
int goto_ad(int x, int y)
                                       pushl
                                                                   Setup
                                               %esp, %ebp
8(%ebp), %edx
   if (x <= y) goto Else;
result = x-y;</pre>
                                       movl
                                       movl
                                               12(%ebp), %eax
%eax, %edx
   goto Exit;
                                       movl
                                       cmpl
                                                                    Body1
  result = y-x;
                                       subl
                                               %eax, %edx
                                       movl
                                               %edx, %eax
                                                                    Body2a
   return result;
                                       jmp .L7
                                   .L6:
C allows "goto" as means of
                                       subl %edx, %eax
                                    . L7 :
  transferring control
                                       popl %ebp

    Closer to machine-level

                                                                 Finish
    programming style
■ Generally considered bad
  coding style
```

```
Conditional Branch Example (Cont.)
int goto_ad(int x, int y)
   int result;
                                   pushl
                                                             Setup
                                          %esp, %ebp
8(%ebp), %edx
  if (x <= y) goto Else;
result = x-y;</pre>
                                   movl
  goto Exit;
                                   movl
                                          12(%ebp), %eax
Else:
                                   cmpl
                                           %eax, %edx
                                                             Body1
 result = y-x;
                                           . 16
Exit
                                   subl
                                         %eax, %edx
                                                             Body2a
                                          %edx, %eax
  return result;
                                   movl
                                   jmp .L7
                                .L6:
                                   subl %edx, %eax
                                . ъ7 :
                                   popl %ebp
                                                           Finish
                                   ret
```

```
Conditional Branch Example (Cont.)
int goto_ad(int x, int y)
                                    pushl
   int result;
                                                                Setup
                                            %esp, %ebp
8(%ebp), %edx
  if (x <= y) goto Else;
result = x-y;</pre>
                                     movl
                                     movl
   goto Exit;
                                    movl
                                            12(%ebp), %eax
%eax, %edx
 Else:
                                     cmpl
                                                                Body1
 result = y-x;
                                             .L6
Ewite
                                     subl
                                            %eax, %edx
                                                                Body2a
                                            %edx, %eax
  return result;
                                    movl
                                     jmp .L7
                                 .L6:
                                    subl %edx, %eax
                                  . ъ7 :
                                    popl %ebp
                                                             Finish
```

```
Conditional Branch Example (Cont.)
int goto_ad(int x, int y)
                               absdiff:
                                  pushl
                                                           Setup
                                          %esp, %ebp
  if (x <= y) goto Else;
result = x-y;</pre>
                                  movl
                                          8(%ebp), %edx
  goto Exit;
                                  movl
                                         12(%ebp), %eax
Else:
                                  cmpl
                                          %eax, %edx
                                                           Body1
 result = y-x;
                                          .L6
                                         %eax. %edx
Exit:
                                  subl
                                                            Body2a
                                         %edx, %eax
  return result:
                                  movl
                                   jmp .L7
                               . L6:
                                  subl %edx, %eax
                               т.7 -
                                  popl %ebp
                                                         Finish
```

```
General Conditional Expression Translation
C Code
val = Test ? Then_Expr : Else_Expr;
      val = x>y ? x-y : y-x;

    Test is expression returning integer

    = 0 interpreted as false

Goto Version
                                    • ≠ 0 interpreted as true
  nt = !Test;

    Create separate code regions for

  if (nt) goto Else;
                                    then & else expressions
  val = Then_Expr;

    Execute appropriate one

  goto Done;
 val = Else Expr;
Done:
```

```
Using Conditional Moves

    Conditional Move Instructions

  Instruction supports:
    if (Test) Dest ← Src

    Supported in post-1995 x86 processors

    GCC does not always use them

                                           val = Test
    • For compatibility with ancient
                                              ? Then_Expr
      processors
                                               : Else_Expr;

    Enabled for x86-64

                                          Goto Version
    • Use switch -march=686 for IA32
                                            tval = Then_Expr;
■ Why?
                                            result = Else_Expr;

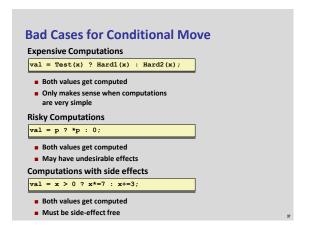
    Branches are very disruptive to

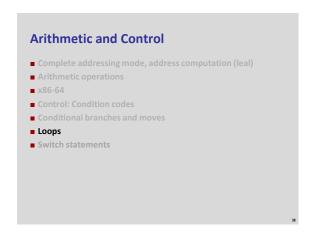
                                            t = Test;
   instruction flow through pipelines
                                            if (t) result = tval;

    Conditional move do not require control

                                            return result;
   transfer
```

```
Conditional Move Example: x86-64
int absdiff(int x, int y)
    int result;
    if (x > y) {
        result = x-y;
        result = y-x;
    return result;
                     absdiff:
x in %edi
                      movl
                      subl
                              %esi, %edx
                                          # tval = x-y
y in %esi
                      movl
                              %esi, %eax
                      subl
                              %edi, %eax
                                          # result = y-x
                      cmpl
                              %esi, %edi
                                          # Compare x:y
# If >, result = tval
                      cmovq
                             %edx, %eax
```





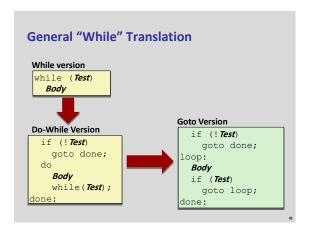
```
"Do-While" Loop Example
                                Goto Version
int pcount_do(unsigned x)
                                int pcount_do(unsigned x)
   int result = 0;
                                  int result = 0;
  do {
                                 loop:
    result += x & 0x1;
                                  result += x & 0x1;
  x >>= 1;
} while (x);
                                   x >>= 1;
                                  if (x)
                                    goto loop;
  return result;
                                   return result;
■ Count number of 1's in argument x ("popcount")
■ Use conditional branch to either continue looping or to exit
 loop
```

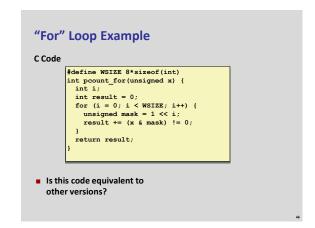
```
"Do-While" Loop Compilation
 Goto Version
int pcount_do(unsigned x) {
  int result = 0;
 loop:
  result += x & 0x1;
  x >>= 1:
  if (x)
    goto loop;
  return result;
                            $0. %ecx
                                         # result = 0
                     movl
                    .L2:
                            # loop:
Registers:
                     movl
                           %edx, %eax
$1, %eax
%edx
                                             t = x & 1
                     andl
         result
%есх
                            %eax, %ecx
                                            result += t
                                            x >>= 1
If !0, goto loop
                     shrl
                            %edx
```

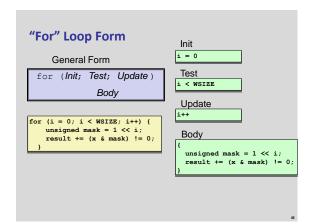
```
General "Do-While" Translation
C Code
                           Goto Version
                            loop:
    Bodv
                               Body
    while (Test);
                               if (Test)
                                 goto loop
■ Body: {
           Statement<sub>1</sub>;
           Statement<sub>2</sub>;
           Statementn;
■ Test returns integer
= = 0 interpreted as false
■ ≠ 0 interpreted as true
```

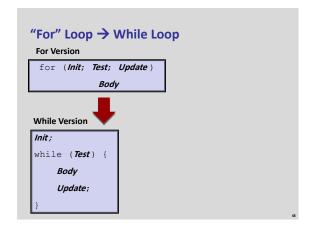
```
"While" Loop Example
 C Code
                                 Goto Version
int pcount_while(unsigned x) {
                                   int pcount_do(unsigned x) {
  int result = 0;
                                    int result = 0;
  while (x) {
                                     if (!x) goto done;
    result += x & 0x1:
                                   loop:
    x >>= 1;
                                     result += x & 0x1;
                                     x >>= 1;
if (x)
  return result;
                                      goto loop;
                                   done:
                                     return result;
 ■ Is this code equivalent to the do-while version?

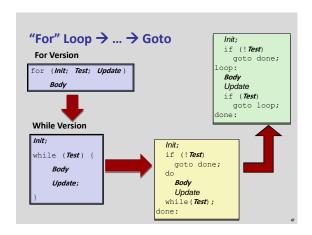
    Must jump out of loop if test fails
```

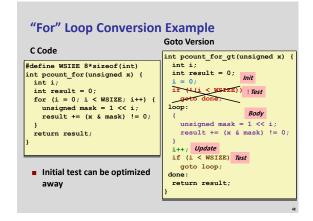












Announcement Break: Bomb Lab Now Out Analyze malicious software with a debugger Reverse engineering based on instructions, observation, and experiment

- Find inputs to "defuse" a bomb program so it does not "explode"
 We've covered enough material for you to start working
 - . E.g., control flow structure and arithmetic
 - Will also cover in discussion sections tomorrow
- Like data lab, difficulty increases between parts
 - Last phase especially complex
 - Start early!

Arithmetic and Control Complete addressing mode, address computation (leal) Arithmetic operations x86-64 Control: Condition codes Conditional branches and moves Loops Switch statements

```
long switch_eg
                                 Switch Statement
   (long x, long y, long z)
                                  Example
    long w = 1:
    switch(x) {
    case 1:
w = y*z;
                                    ■ Multiple case labels
        break;

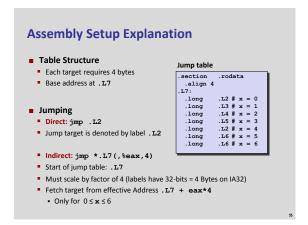
    Here: 5 & 6

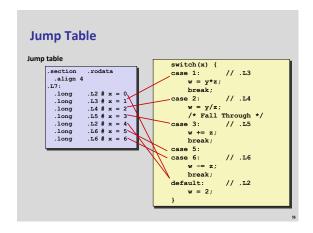
    case 2:
                                    ■ Fall through cases
        w = y/z;
/* Fall Through */
                                       Here: 2
    case 3:
w += z;
                                    Missing cases
        break;
                                       Here: 4
    case 5:
    case 6:
        break:
    default:
        w = 2;
    return w;
```

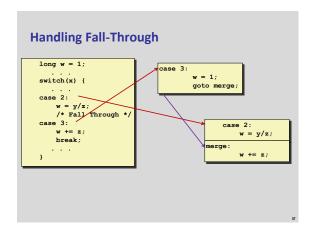
```
Jump Table Structure
                                                       Jump Targets
                            Jump Table
Switch Form
                                               Targ0:
switch(x) {
                       jtab: Targ0
                                                         Code Block
  case val_0:
                                                             n
                                Targ1
    Block 0
  case val_1:
Block 1
                                Targ2
                                               Targ1:
                                                         Code Block
  case val n-1:
                                               Targ2:
    Block n-1
                                                         Code Block
                               Targn-1
Approximate Translation
target = JTab[x];
goto *target;
                                            Targn-1:
                                                         Code Block
                                                            n-1
```

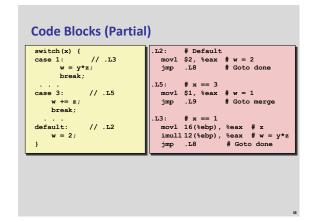
```
Switch Statement Example (IA32)
long switch_eg(long x, long y, long z)
     long w = 1;
     switch(x) {
     return w;
Setup:
  switch_eg:
    pushl %ebp
                           # Setup
                            # Setup
    movl
            %esp, %ebp
           8(%ebp), %eax # %eax = x
$6, %eax # Compare x
.L2 # If unsign
    movl
                           # Compare x to 6
    cmpl
                           # If unsigned > goto default
           *.L7(,%eax,4) # Goto *JTab[x]
                                                Note that w not
                                                initialized here
```

```
Switch Statement Example (IA32)
 long switch_eg(long x, long y, long z)
      switch(x) {
                                                  Jump table
                                                   .section
.align 4
      return w:
                                                     .long
.long
.long
.long
Setup:
       switch_eg:
                                   # Setup
# Setup
          pushl %ebp
          movl
                  %esp, %ebp
                  8(%ebp), %eax #
          movl
                                     eax = x
                                     Compare x:6
          cmpl
                  $6, %eax
                  .L2  # If unsigned > goto default *.L7(,%eax,4) # Goto *JTab[x]
jump 🔳
         qmp
```

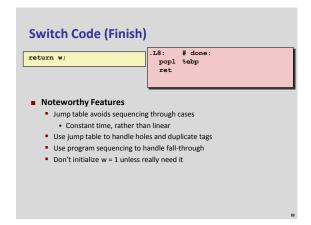


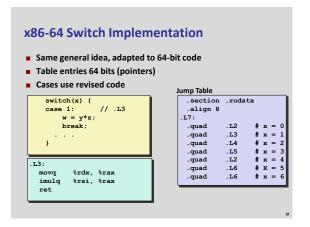






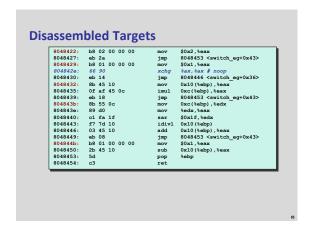
```
Code Blocks (Rest)
switch(x) {
                                  .L4:
                                            # x == 2
                                     movl 12(%ebp), %edx
   case 2: // .L4
                                     movl %edx, %eax
sarl $31, %edx
  case 2: // .L4
w = y/z;
/* Fall Through */
merge: // .L9
w += z;
                                     idivl 16(%ebp) # w = y/z
                                     addl 16(%ebp), %eax # w += z
jmp .L8 # goto done
       break:
   case 5:
   case 6: // .L6
       w -= z;
                                           # x == 5, 6
                                   .L6:
                                     movl $1, %eax
       break;
                                     subl 16(%ebp), %eax # w = 1-z
```

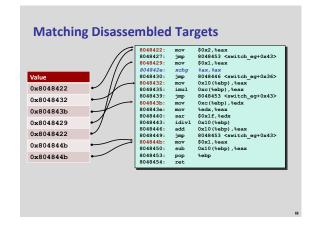












Exercise Break: switch Bounds ■ Every jump table needs to check that the index is in bounds • For each of these code patterns, what indexes are allowed? \$5, %eax Unsigned <= 5: 0 .. 5 .Ldefault jа jmp *.L1(,%eax,4) andl \$7, %eax Low 3 bits: 0 .. 7 *.L2(,%eax,4) jmp movzbl 8(%ebp), %eax Low 8 bits: 0 .. 255 *.L3(,%eax,4) jmp

Summarizing C Control If then-else do-while while, for switch Assembler Control Conditional jump Conditional move Indirect jump Standard Techniques Loops converted to do-while form Large switch statements use jump tables

Sparse switch statements may use decision trees

Summary

■ These slides

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches & conditional moves
- Loops
- Switch statements

■ Next Up

- Stack
- Call / return
- Procedure call discipline

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