

# CSDS 440: Assignment 8

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Due and submitted on 10/30/2020

Fall 2020, Dr. Ray

## Problem 36

Known that the 95% CI are  $[x_B, y_B]$  and  $[x_N, y_N]$  respectively for two datasets, we may deduce the error rates to be  $e_B = \frac{x_B + y_B}{2}$  and  $e_N = \frac{x_N + y_N}{2}$  for their respective dataset.

Assume Prof. Bob's dataset has  $n_B$  examples and Prof. Nan has  $n_N$  examples, Prof. Scoop may simply derive his version of error rate to be a combination of the both, which is  $e_S = \frac{n_B e_B + n_N e_N}{n_B + n_N}$ . This implies  $n_S = n_B + n_N$ , we may get this  $n_S$  (and also  $n_B, n_N$ ) by doing:

$$\begin{aligned}x_B &= e_B - 2\sigma_B \\2\sqrt{\frac{e_B(1 - e_B)}{n_B}} &= e_B - x_B \\ \frac{4e_B(1 - e_B)}{n_B} &= (e_B - x_B)^2 \\ \implies n_B &= \frac{4e_B(1 - e_B)}{(e_B - x_B)^2}\end{aligned}$$

By doing the same calculation for  $n_N$  we have:

$$\begin{aligned}n_N &= \frac{4e_N(1 - e_N)}{(e_N - x_N)^2} \\ \implies n_S &= \frac{4e_B(1 - e_B)}{(e_B - x_B)^2} + \frac{4e_N(1 - e_N)}{(e_N - x_N)^2}\end{aligned}$$

Since  $e_B, n_B, e_N, n_N, n_S$  are now all known, we can calculate  $e_S$  accordingly. Now, assume Prof. Scoop will land with a 95% CI of  $[x_S, y_S]$ , then there must be:

$$\begin{aligned}
 x_S &= e_S - 2\sigma_S \\
 &= e_S - 2\sqrt{\frac{e_S(1 - e_S)}{n_S}} \\
 y_S &= e_S + 2\sigma_S \\
 &= e_S + 2\sqrt{\frac{e_S(1 - e_S)}{n_S}}
 \end{aligned}$$

The above two equations suggest we may derive  $x_S$  and  $y_S$  with just  $e_S$  and  $n_S$ , which are two known value to us and also to Prof. Scoop. So Prof. Scoop – while not doing any experiment – may derive his 95% CI base on Prof. Bob and Prof. Nan’s results at the cost of his academic integrity.