

ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT)

ORGANISATION OF ISLAMIC COOPERATION (OIC)

Department of Computer Science and Engineering (CSE)

MID SEMESTER EXAMINATION

SUMMER SEMESTER, 2017-2018

DURATION: 1 Hour 30 Minutes

FULL MARKS: 75

CSE 4203: Discrete Mathematics

Programmable calculators are not allowed. Do not write anything on the question paper.

There are 4 (four) questions. Answer any 3 (three) of them.

Figures in the right margin indicate marks.

1. a) Describe the worst-case time complexity of the odd-even sort algorithm in terms of the number of comparisons used. Express the complexity in Big-O notation. 10

The algorithm for odd-even sort algorithm is given in Figure 1.

```

procedure oddEvenSort( $a_1, \dots, a_n$  : real numbers with  $n \geq 2$ )
  isSorted := False
  while isSorted = False do
    isSorted := True
     $i := 1$ 
    while  $i < n$  do
      if  $a_i > a_{i+1}$  then
        interchange  $a_i$  and  $a_{i+1}$ 
        isSorted := False
       $i := i + 2$ 
     $i := 2$ 
    while  $i < n$  do
      if  $a_i > a_{i+1}$  then
        interchange  $a_i$  and  $a_{i+1}$ 
        isSorted := False
       $i := i + 2$ 
  return

```

Figure 1: Code listing for Question 1(a).

- b) Express the negation of the following propositions using quantifiers, and then express them in English. 15
- Some drivers do not obey the speed limit.
 - All Swedish movies are serious.
 - No one can keep a secret.
 - There is someone in this class who does not have a good attitude.
 - Every bird can fly.
2. a) Give big-O estimates (with the values of C and n_0) for the following functions: 12
- $(n^2 + 5)(n - 1)$
 - $(n \lg n + 1)^2 + (\lg n + 1)(n^2 + 1)$
 - $3n \lg(n!) + (n^2 + 4) \lg(n)$

- b) Draw Venn Diagrams showing the followings: (Identify all parts of the diagram with proper notations) 8
- $A \cup B \subset A \cup C$, but $B \cap C = \{\}$
 - $A \cap B \subset A \cap C$, but $B \cap C = \{\}$
- c) Write the following complexities in ascending order : 5
- $\theta(n^2)$, $\theta(b^n)$, $\theta(n \log n)$, $\theta(n!)$ and $\theta(1)$
- 3 a) Use logical equivalence to show that following propositions are contradiction: 6
- $\neg(p \vee \neg(p \wedge q))$
 - $\neg(((p \vee q) \wedge (\neg p \vee r)) \rightarrow (q \vee r))$
- b) Use truth table to show that: 6
- $(p \wedge (p \rightarrow q) \rightarrow \neg q)$ is a contingency.
 - $((p \rightarrow q) \wedge (q \rightarrow r) \rightarrow (p \rightarrow r))$ is a tautology.
- c) There are two restaurants next to each other. One has a sign says "Good food is not cheap" and other has a sign that says "Cheap food is not good". Are the signs saying the same thing? Justify your answer using predicates, quantification etc. 7
- d) Given that $h(x) = 3x$ and $g(t) = -2t - 2 - h(t)$ and $f(n) = -5n^2 + h(n)$, calculate $h(g(8) + f(2))$. 6
- 4 a) Show that if n is an integer and $n^2 + 5$ is odd, then n is even using 12
- A proof by contraposition.
 - A proof by contradiction
- b) Given premises : 8
- "Students who pass the course either do the homework or attend lecture;"
- "Mahid did not attend every lecture;"
- "Mahid passed the course."
- Using rules of inference prove the conclusion that "Mahid have done the homework".
- c) Theorem: If n^2 is positive, then n is positive. 5
- Proof: Suppose that n^2 is positive. Because the conditional statement "If n is positive, then n^2 is positive" is true, we can conclude that n is positive.
- Is there any problem with the proof of this theorem? Give proper arguments to support your answer.