ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT) ORGANISATION OF ISLAMIC COOPERATION (OIC)

Department of Computer Science and Engineering (CSE)

MID SEMESTER EXAMINATION

WINTER SEMESTER, 2017-2018

FULL MARKS: 100

18

16

9.11

PARATION: 1 Hour 30 Minutes

Math 4141: Geometry and Differential Calculus

Programmable calculators are not allowed. Do not write anything on the question paper.

There are 4 (four) questions. Answer any 3 (three) of them.

Figures in the right margin indicate marks.

- 12 Find the domain and range of the following functions $f(x) = \sqrt{x^2 - 11x + 30}$ ii. $g(x) = \sec x$ iii. $F(x) = \frac{x - 3}{|x - 3|}$ iv. $h(x) = \sin^{-1} x$
- Express the function f'(x) = x + |x + 1| in piecewise form and graph the function.
- Graph the function $f(x) = 3\sin\frac{\pi}{2}x + 1$ using period and amplitude and write their domain and range.
- 6.33 d) Find the inverse of the function $f(x) = \ln(x-3) + 1$ and graph the f and f^{-1} in the same plane.
- Write down the precise definition of limit. Using formal definition of limit prove that $\lim_{x\to 2} \sqrt{9x-2} = 4$
- Find the Limit of the following functions:
 - i. $\lim_{x\to 2^+} \frac{1}{|2-x|}$ ii. $\lim_{x\to 0} \frac{\tan 3x^2 + \sin^2 5x}{x^2}$
 - iii. $\lim_{t\to\infty} \frac{6-t^3}{7t^4+3}$ iv. $\lim_{t\to\infty} \frac{1-e^x}{1+e^x}$
- Discuss the Limit and Continuity of the following function at, x = 3

 $f(x) = \begin{cases} 4 - x^2 & x < 3 \\ 6 & x = 3 \\ x - 8 & x > 3 \end{cases}$

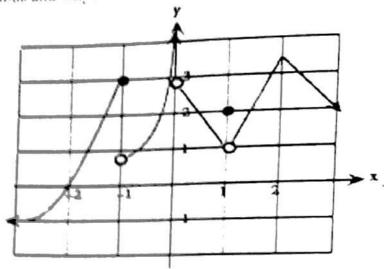
and draw the graph.

3. a) State Sandwich theorem and using this theorem show that

i. $\lim_{x\to 0} \frac{\sin x}{x} + 1$ ii. $\lim_{x\to 0} x^2 \sin \frac{1}{x} = 0$

b) Whether the following function / graphed is continuous on [-3, 3] or not. If not where does

it fail to be continuous and why? What is the $\lim_{x\to 1} f(x)$?



Use Limit to determine for all horizontal and oblique asymptotes from following equations:

i. $F(x) = \frac{x^3 - 2}{|x|^3 + 1}$

ii. $h(x) = \frac{x^2 - 4}{x - 1}$

- a) Find the tangent line to the curve $f(x) = \sqrt{x-1} + 2$ at x = 3.
 - b) At what points do the graph of the function $g(x) = x^2 7x + 12$ have horizontal tangent line and show in your graph.
 - The power P, in Watts, supplied to a circuit by a battery is given by the formula $P = 61 - 0.57^2$ where I is the current in amperes.
 - i. What is the average rate of change of power when current is 1 to 4 amperes?
 - ii. What is the approximate instantaneous rate of change of power when current is 4 amperes?
 - Show that f(x) = |2x + 1| continuous everywhere.