

* 참고

- 오차 error
 - 잔차 residual
 - 편차 deviation
 - 표준편차 standard deviation
 - 표준오차 standard error
-
- RMSE root-mean-square error = standard error of regression, 회귀의 표준오차

VII. 회귀분석 심화

1. 회귀분석의 추정

- Basic format: $y_i = \beta_0 + \beta_1 x_i + u_i$
- SSE (sum of the squared residuals) = $\sum \varepsilon_i^2 = \sum (y_i - \hat{y}_i)^2 = \sum (y_i - (\beta_0 + \beta_1 x_i))^2$

1. 회귀분석의 추정

- Random variable: $y_i = \beta_0 + \beta_1 x_i + u_i$

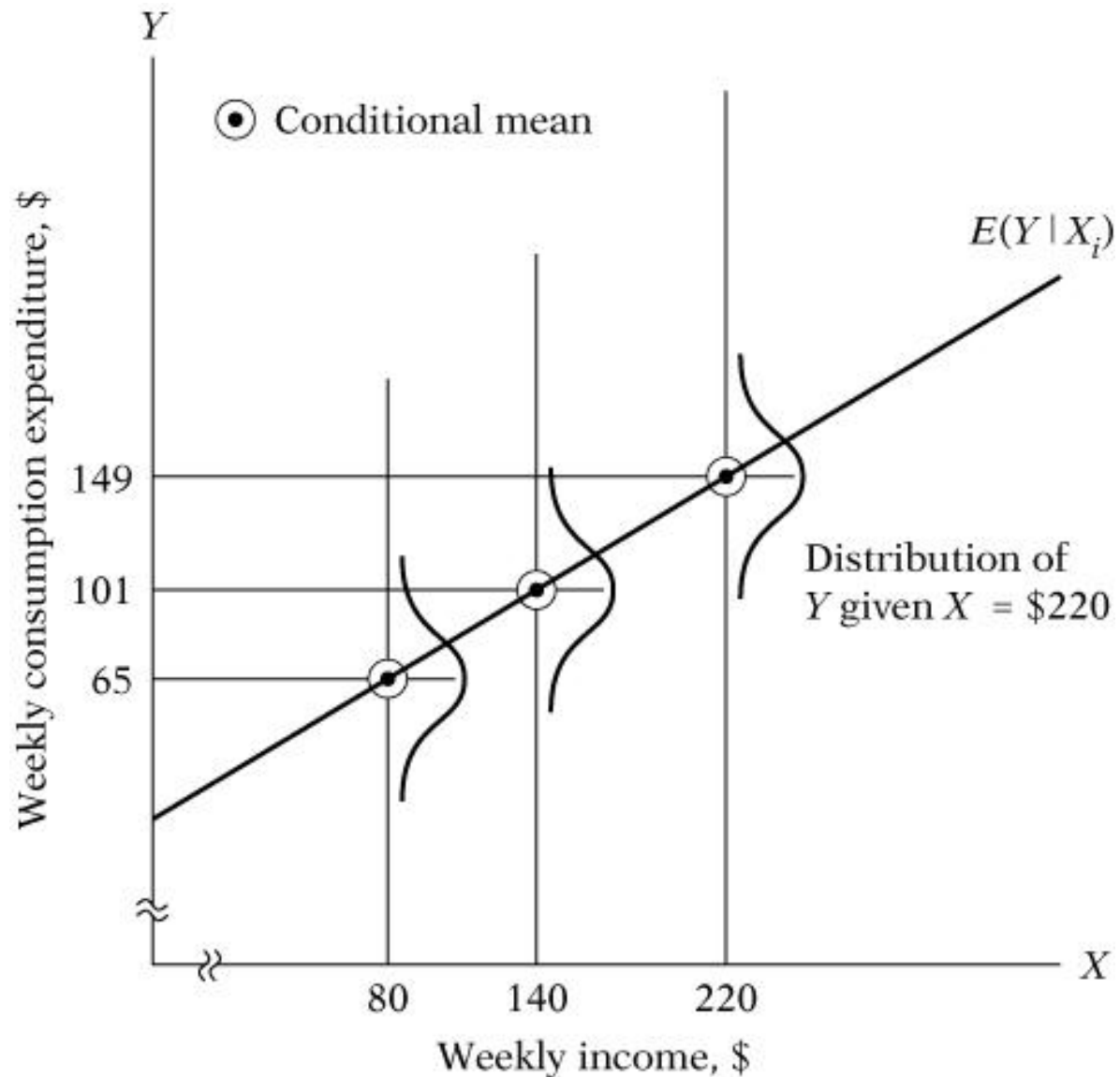
1. 회귀분석의 추정

- $E(Y|X)$: X 에 대한 조건부 평균/기댓값 conditional mean
- Unconditional mean

TABLE 2.1
Weekly Family
Income X , \$

$Y \downarrow \quad X \rightarrow$	80	100	120	140	160	180	200	220	240	260
Weekly family consumption expenditure Y , \$	55 60 65 70 75 – –	65 70 74 80 85 88 –	79 84 90 94 98 – –	80 93 95 103 108 113 115	102 107 110 116 118 125 –	110 115 120 130 135 140 –	120 136 140 144 145 – –	135 137 140 152 157 160 162	137 145 155 165 175 189 –	150 152 175 178 180 185 191
Total	325	462	445	707	678	750	685	1043	966	1211
Conditional means of Y , $E(Y X)$	65	77	89	101	113	125	137	149	161	173

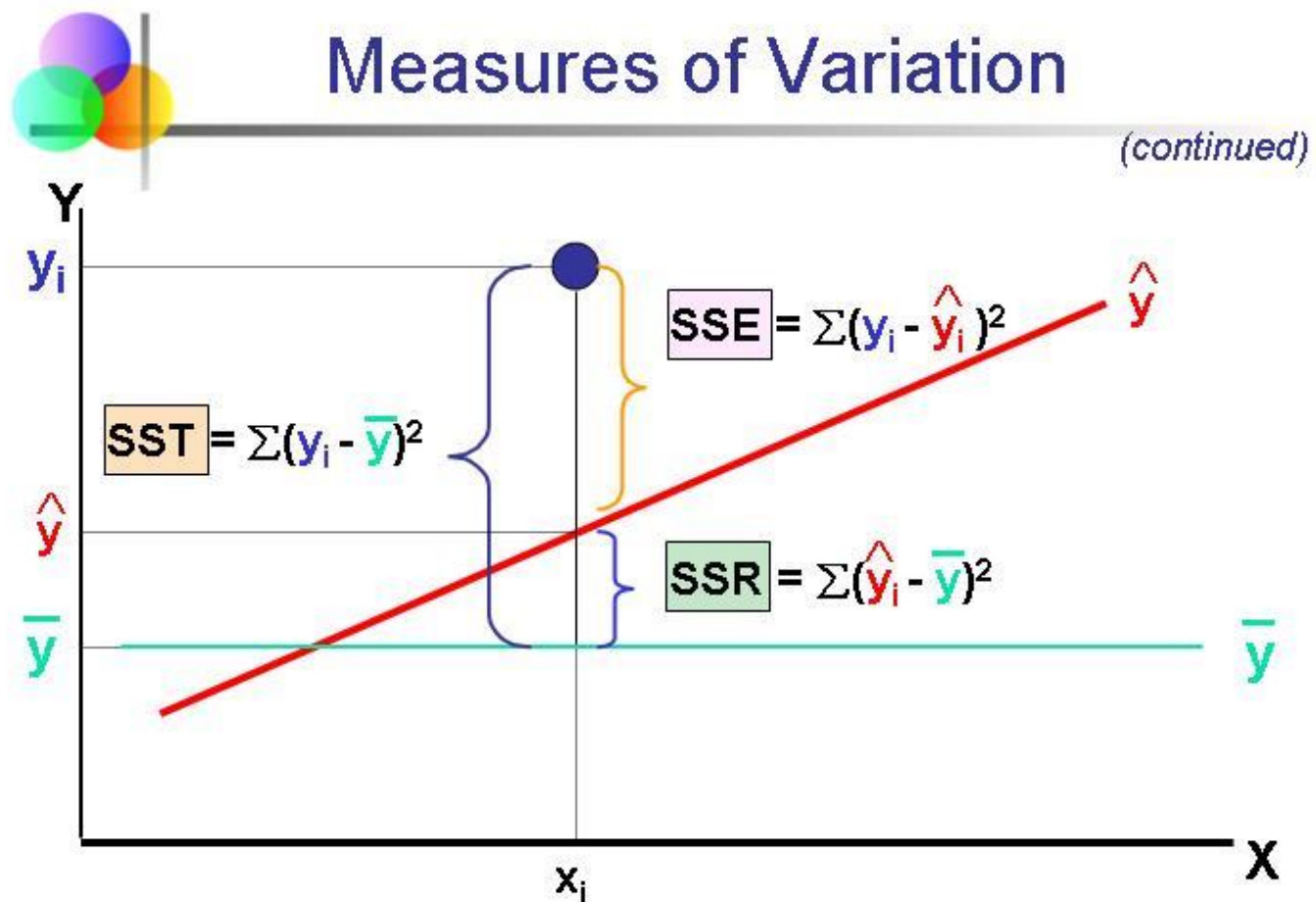
1. 회귀분석의 추정



2. 적합도_{goodness of fit}의 측정

- 총제곱합 total sum of squares $SST = \sum_{i=1}^n (y_i - \bar{Y})^2$
- 오차제곱합 error sum of squares $SSE = \sum_{i=1}^n (y_i - (b_0 + b_1 x_i))^2 = \sum_{i=1}^n (y_i - \hat{y}_i)^2 = \sum_{i=1}^n e_i^2$
- 회귀제곱합 regression sum of squares $SSR = \sum_{i=1}^n (\hat{y}_i - \bar{Y})^2 = b_1^2 \sum_{i=1}^n (x_i - \bar{X})^2$

2. 적합도_{goodness of fit}의 측정



2. 적합도_{goodness of fit}의 측정

- $R^2 = SSR/SST = 1 - SSE/SST$
= 회귀제곱합/총제곱합 = 1-오차제곱합/총제곱합

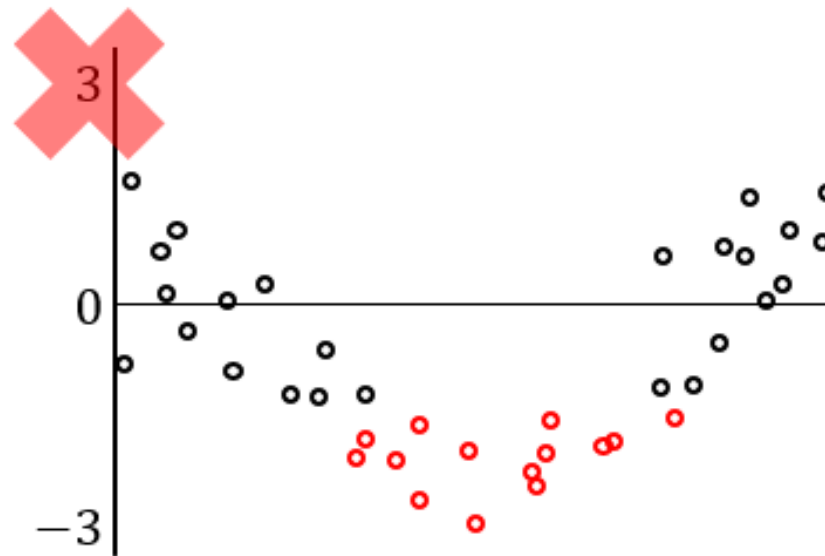
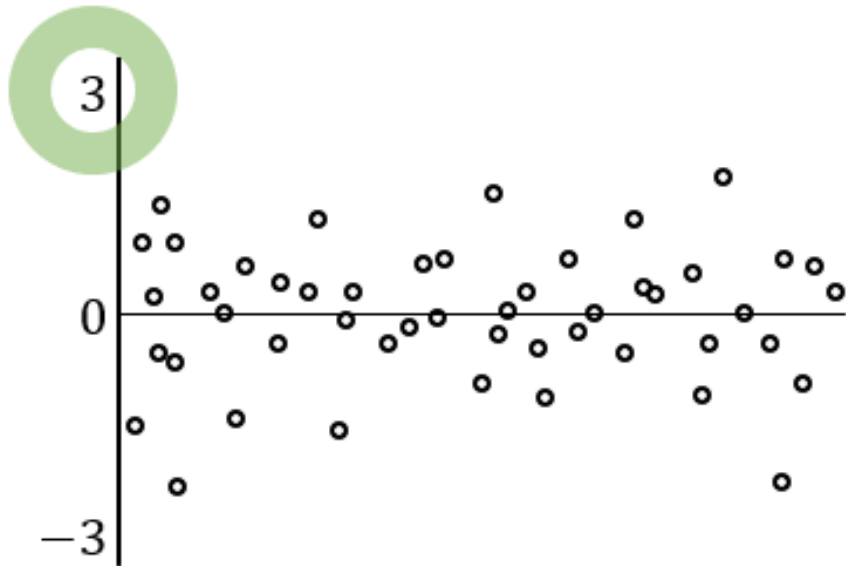
$$SSR = \sum_{i=1}^n (\hat{y}_i - \bar{Y})^2 = b_1^2 \sum_{i=1}^n (x_i - \bar{X})^2$$

3. 회귀분석의 가정

- OLS의 추정치 estimator
 - 불편성(unbiasedness)
 - 효율성(efficiency)
 - 선형성(linearity)
 - 일관성(consistency)
- Best Linear Unbiased Estimator: BLUE

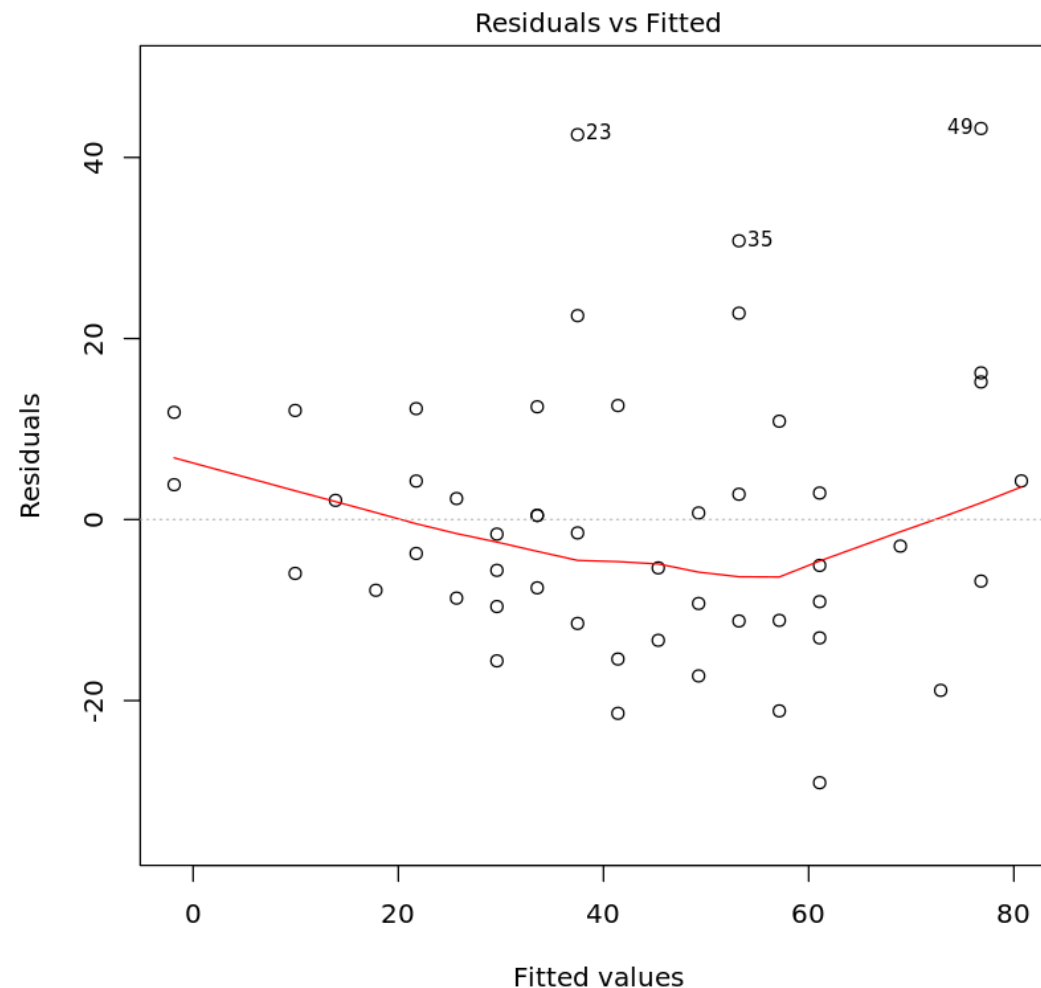
3. 회귀분석의 가정

1) 선형성 $y_i = \beta_0 + \beta_1 x_i + u_i$



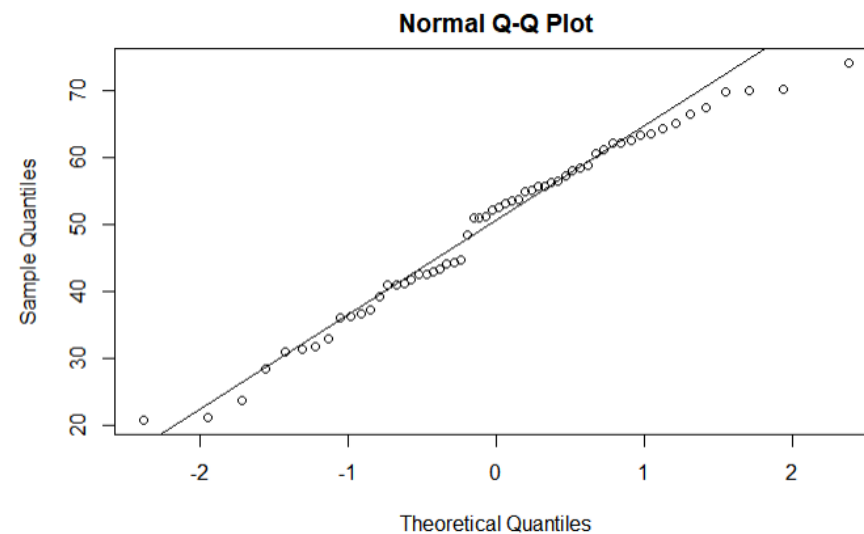
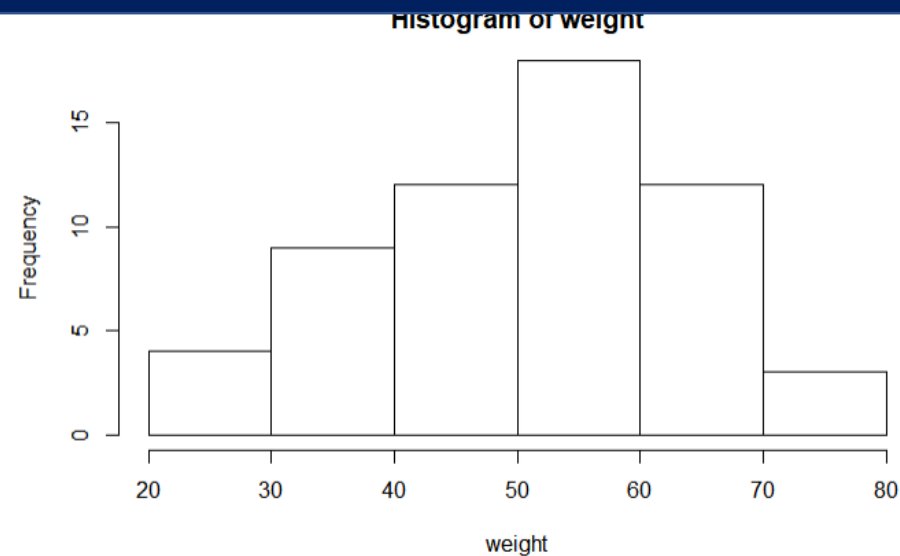
3. 회귀분석의 가정

1) 선형성 $y_i = \beta_0 + \beta_1 x_i + u_i$



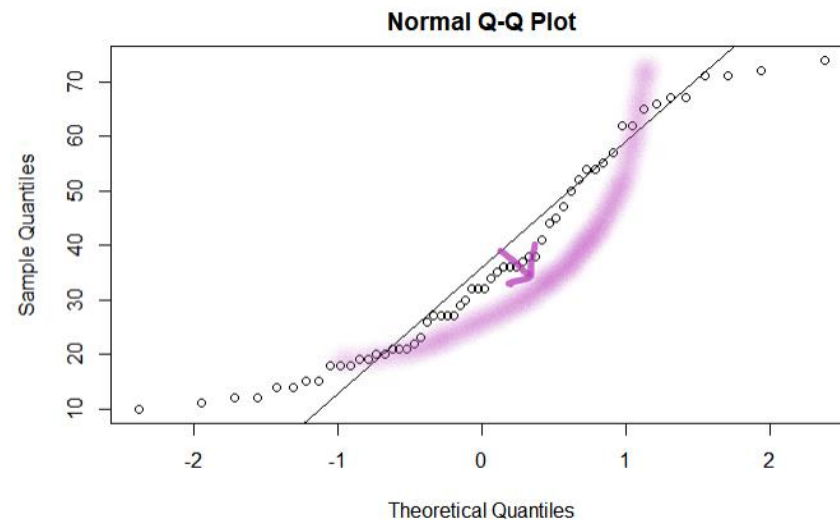
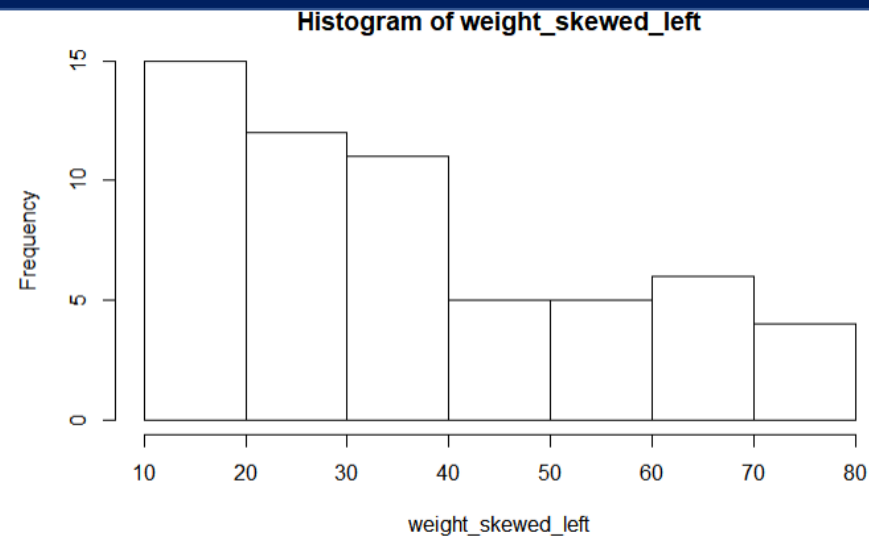
3. 회귀분석의 가정

2) 정규성 $\varepsilon_i \sim N(0, \delta^2)$



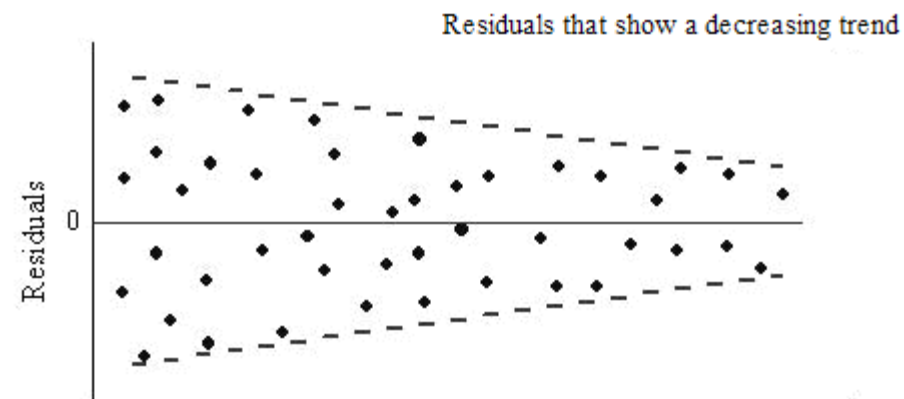
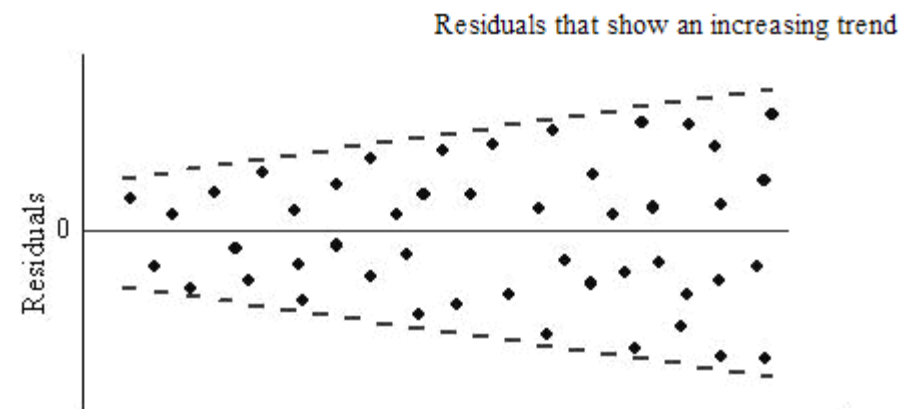
3. 회귀분석의 가정

2) 정규성 $\varepsilon_i \sim N(0, \delta^2)$



3. 회귀분석의 가정

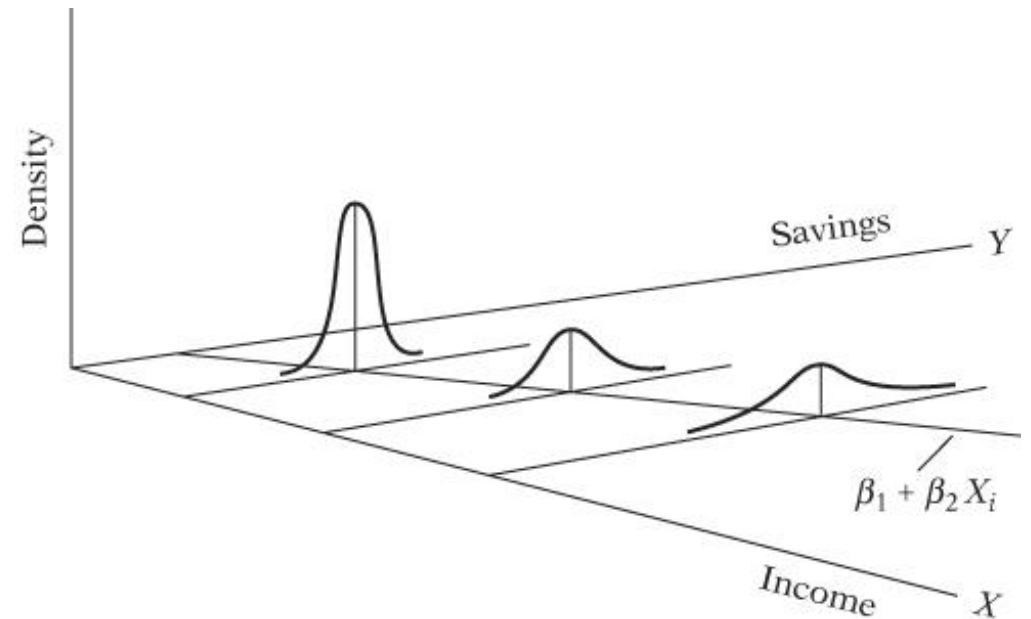
3) 등분산성 $\text{var}(\varepsilon_i) = \delta^2$



3. 회귀분석의 가정

3) 등분산성 $\text{var}(\varepsilon_i) = \delta^2$

- Breusch-Pagan test
- weighted least square
- Transformation of variables



3. 회귀분석의 가정

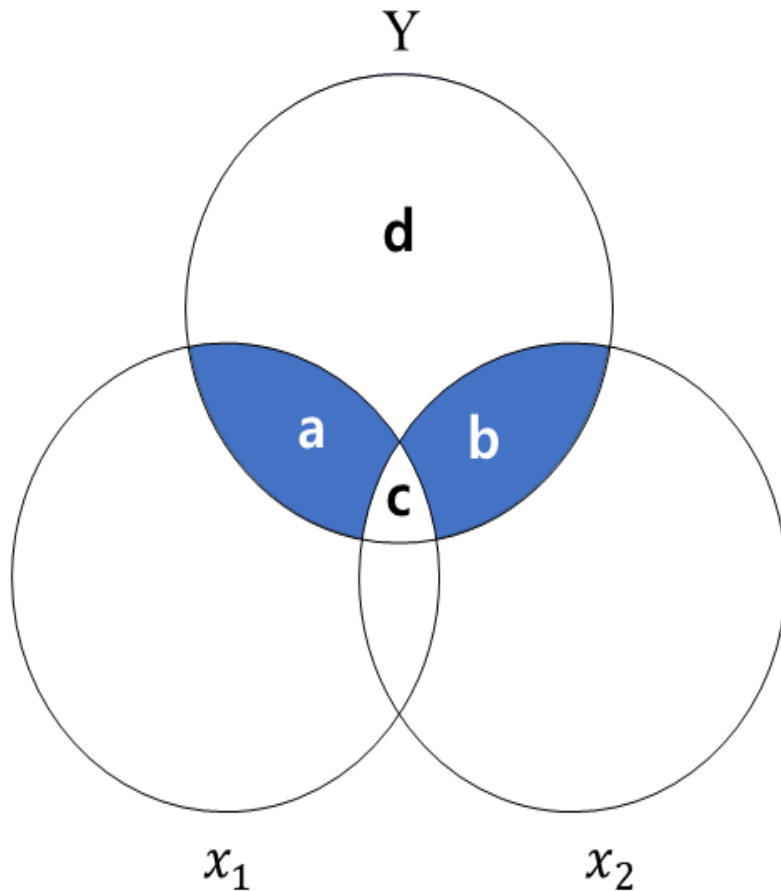
4) 잔차의 독립성 $E(\varepsilon_i)=0$

3. 회귀분석의 가정

5) 비상관성 $\text{Cov}(\varepsilon_i, \varepsilon_j) = 0$

- Durbin-watson test
- generalized least square

4. 다중공선성 multicollinearity



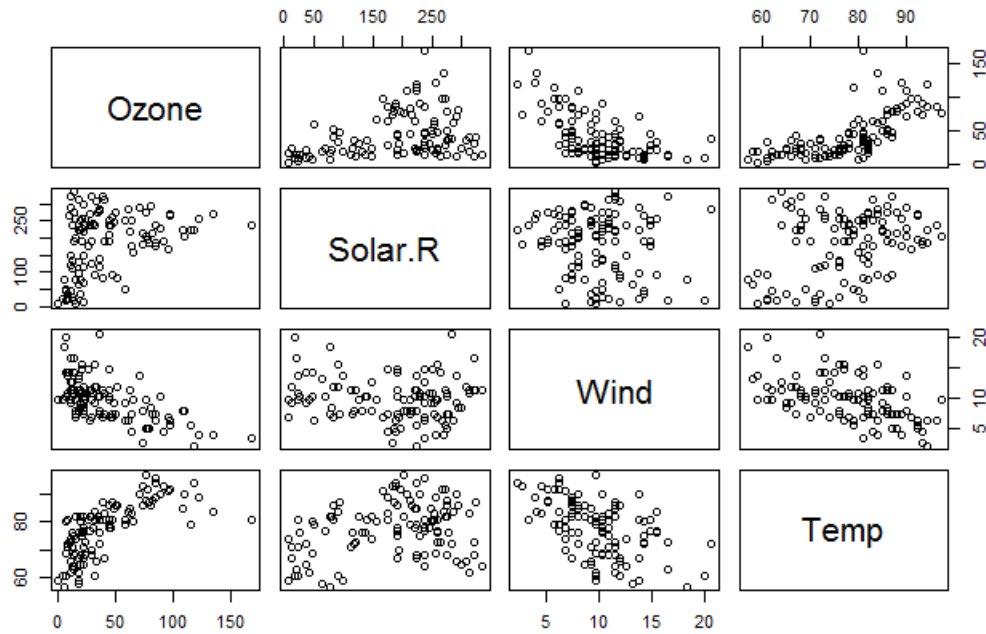
a: x_1 에 의해 설명되는 고유 분산

b: x_2 에 의해 설명되는 고유 분산

c: x_1, x_2 에 의해 설명되는 공유분산

d: x_1, x_2 의해 설명되지 않는 분산

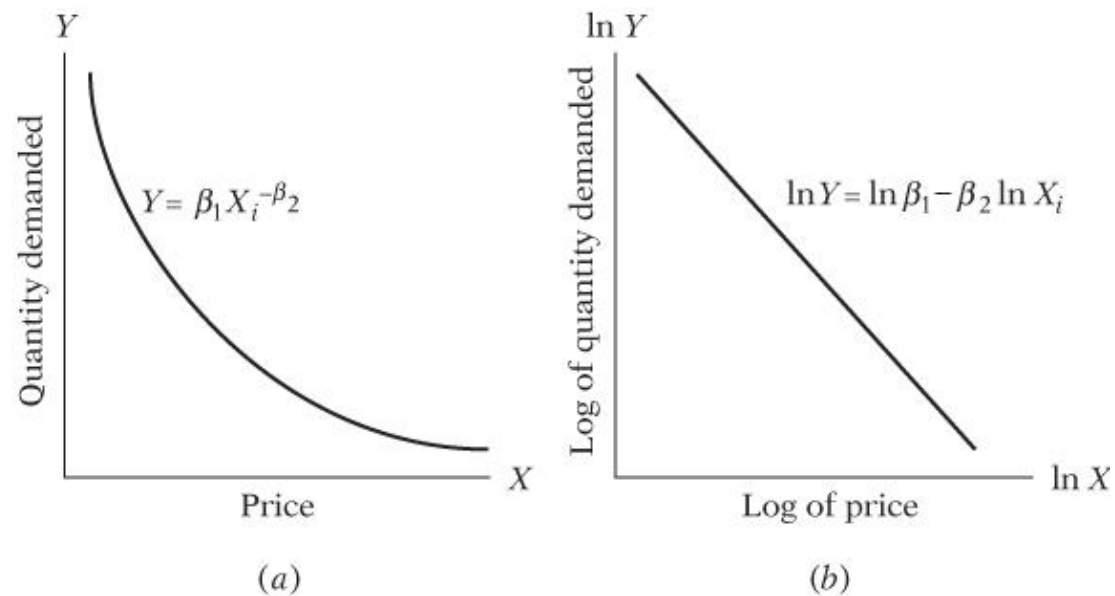
4. 다중공선성 multicollinearity



- Tolerance 공차한계 = $1 - R^2$
- VIF 분산팽창계수 = $1 / (1 - R^2)$

5. 비선형관계

- Log-log model: 탄력성 모델
- $Y = b_1 X^{b_2} e^u$
- $\ln(Y) = \ln(b_1) + b_2 \ln(X) + u$



5. 비선형관계

- Log-lin model: growth rate model
- $Y_t = Y_0(1+r)^t$
- $\ln(Y_t) = \ln(Y_0) + t\ln(1+r)$.

5. 비선형관계

- Lin-log model: absolute change model
- $Y = b_1 + b_2 \ln(X) + u$