

## Q1) Implementing Dijkstra's algorithm in Python

```
PS C:\Users\chols\OneDrive\Documents\Algorithms\HW6> python -u "c:\Users\chols\OneDrive\Documents\Algorithms\HW6\Dijkstra.py"
Starting Dijkstra's algorithm...
```

```
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Node(s) with Weight: 0 is added to the 'Visited' ['s']
Relaxed: vertex[A]: OLD: Infinity, NEW: 1, PATHS: {}
Relaxed: vertex[D]: OLD: Infinity, NEW: 4, PATHS: {'A': 's'}
Relaxed: vertex[G]: OLD: Infinity, NEW: 6, PATHS: {'A': 's', 'D': 's'}
Node(A) with Weight: 1 is added to the 'Visited' ['s', 'A', 'D', 'G']
Relaxed: vertex[B]: OLD: Infinity, NEW: 3, PATHS: {'A': 's', 'D': 's', 'G': 's'}
No edge relaxation is needed for node [D]

Relaxed: vertex[E]: OLD: Infinity, NEW: 3, PATHS: {'A': 's', 'D': 's', 'G': 's', 'B': 'A'}
Node(B) with Weight: 3 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E']
Relaxed: vertex[C]: OLD: Infinity, NEW: 5, PATHS: {'A': 's', 'D': 's', 'G': 's', 'B': 'A', 'E': 'A'}
Node(E) with Weight: 3 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C']
Relaxed: vertex[F]: OLD: Infinity, NEW: 6, PATHS: {'A': 's', 'D': 's', 'G': 's', 'B': 'A', 'E': 'A', 'C': 'B'}
Relaxed: vertex[G]: OLD: 6, NEW: 4, PATHS: {'A': 's', 'D': 's', 'G': 's', 'B': 'A', 'E': 'A', 'C': 'B', 'F': 'E'}
Relaxed: vertex[H]: OLD: Infinity, NEW: 5, PATHS: {'A': 's', 'D': 's', 'G': 'E', 'B': 'A', 'E': 'A', 'C': 'B', 'F': 'E'}
Relaxed: vertex[I]: OLD: Infinity, NEW: 6, PATHS: {'A': 's', 'D': 's', 'G': 'E', 'B': 'A', 'E': 'A', 'C': 'B', 'F': 'E', 'H': 'E'}
Node(G) with Weight: 4 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I']
No edge relaxation is needed for node [H]

Node(D) with Weight: 4 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I']
No edge relaxation is needed for node [E]

No edge relaxation is needed for node [G]
```

```
Node(C) with Weight: 5 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I']
No edge relaxation is needed for node [E]

No edge relaxation is needed for node [F]

Relaxed: vertex[t]: OLD: Infinity, NEW: 9, PATHS: {'A': 's', 'D': 's', 'G': 'E', 'B': 'A', 'E': 'A', 'C': 'B', 'F': 'E', 'H': 'E', 'I': 'E'}
Node(H) with Weight: 5 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I', 't']
No edge relaxation is needed for node [I]

Node(I) with Weight: 6 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I', 't']
No edge relaxation is needed for node [t]

Node(F) with Weight: 6 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I', 't']
No edge relaxation is needed for node [I]

No edge relaxation is needed for node [t]

Node(t) with Weight: 9 is added to the 'Visited' ['s', 'A', 'D', 'G', 'B', 'E', 'C', 'F', 'H', 'I', 't']
```

### Final Shortest Path Results:

#### Visited (Shortest Distances):

```
s: 0
A: 1
D: 4
G: 4
B: 3
E: 3
C: 5
F: 6
H: 5
I: 6
t: 9
```

### Path (Predecessors):

```
A: s
D: s
G: E
B: A
E: A
C: B
F: E
H: E
I: E
t: C
```

Total Weight: 46

## Q2: Application of Dijkstra's SSSP and MST algorithms

There are 15 cities in this planning trip program:

1. Atlanta
2. Boston
3. Chicago
4. Dallas
5. Denver
6. Houston
7. LA (Los Angeles)
8. Memphis
9. Miami
10. New York (NY)
11. Philadelphia
12. Phoenix
13. San Francisco (SF)
14. Seattle
15. Washington DC (WDC)

### ❖ Dijkstra's Algorithm

- 1) Initialize our variables to be able to show what nodes were visited, what paths were taken, and a set to contain all the nodes
- 2) In the loop, the algorithm iterates over each of the nodes that have not been visited and each time the nodes are visited the node with the smallest distance is selected
- 3) The selected node is then constructed using the path dictionary
- 4) The algorithm updates the distance based on the current node and neighboring node distances
  - Which it then stores the shortest path after each iteration

#### Dijkstra's Algorithm Results:

```
-----
Distance from Denver to Denver: 0 with path (Denver)
Distance from Denver to Dallas: 1064 with path (Denver to Dallas)
Distance from Denver to LA: 1335 with path (Denver to LA)
Distance from Denver to Memphis: 1411 with path (Denver to Memphis)
Distance from Denver to Houston: 1426 with path (Denver to Dallas to Houston)
Distance from Denver to Chicago: 1474 with path (Denver to Chicago)
Distance from Denver to SF: 1894 with path (Denver to LA to SF)
Distance from Denver to Atlanta: 2221 with path (Denver to Dallas to Atlanta)
Distance from Denver to Washington: 2395 with path (Denver to Washington)
Distance from Denver to Phoenix: 2486 with path (Denver to Dallas to Phoenix)
Distance from Denver to Philadelphia: 2594 with path (Denver to Washington to Philadelphia)
Distance from Denver to NY: 2619 with path (Denver to Chicago to NY)
Distance from Denver to Boston: 2839 with path (Denver to Boston)
Distance from Denver to Seattle: 2879 with path (Denver to LA to Seattle)
Distance from Denver to Miami: 3194 with path (Denver to Dallas to Atlanta to Miami)
```

#### ❖ Prim's Algorithm (MST)

- 1) Initialize the variables to have one that stores the minimum edge weight, one to store the parent node for each node, and one to track if a node is included in the MST
- 2) In the loop, the algorithm selected the node with the smallest key and have not been included in the MST
- 3) It then updates the key and parent values based on what was selected

#### Prim's Algorithm Results:

	Edge	Weight
Denver is selected. Distance: 0	LA	LA .....1335
Dallas is selected. Distance: 1064	Houston	Houston .....362
Houston is selected. Distance: 362	Memphis	Memphis .....675
Memphis is selected. Distance: 675	Phoenix	Phoenix .....1422
Atlanta is selected. Distance: 1157	Washington	Washington .....199
Miami is selected. Distance: 973	Miami	Miami .....973
LA is selected. Distance: 1335	Atlanta	Atlanta .....1157
SF is selected. Distance: 559	Dallas	Dallas .....1064
Seattle is selected. Distance: 1092	SF	SF .....559
Philadelphia is selected. Distance: 1413	Chicago	Chicago .....1474
Washington is selected. Distance: 199	Denver	Denver .....0
Phoenix is selected. Distance: 1422	Philadelphia	Philadelphia .....1413
Chicago is selected. Distance: 1474	Seattle	Seattle .....1092
NY is selected. Distance: 1145	NY	NY .....1145
Boston is selected. Distance: 306	Boston	Boston .....306
Total MST:		13176

#### Q3: TinyZip and TinyUnzip

```
PS C:\Users\chols\OneDrive\Documents\Algorithms\HW6> python -u "c:\Users\chols\OneDrive\Documents\Algorithms\HW6\TinyUnZip.py"
Enter a file name to encode: King.txt
```

```
-----
Character      Weight      Huffman Code
-----
r              413          0000
s              419          0001
I              23          00100000
C              6          0010000100
P              3          00100001010
Y              3          00100001011
L              12         001000011
N              24         00100010
q              6          0010001100
z              6          0010001101
M              7          0010001110
€              1          001000111100
-              2          001000111101
:              2          001000111110
;              2          001000111111
k              51         0010010
'\n'           58         0010011
f              220        00101
n              450        0011
e              885         010
b              110        011000
y              124        011001
d              254        01101
a              539        0111
i              542        1000
T              14         100100000
!              8          1001000010
```

```
'              8          1001000011
?              1          1001000100000
D              1          1001000100001
E              1          1001000100010
H              1          1001000100011
B              4          10010001001
F              4          10010001010
J              1          1001000101100
R              1          1001000101101
â              1          1001000101110
”              1          1001000101111
S              8          1001000110
G              9          1001000111
,              71         1001001
w              146        100101
.              75         1001100
A              18         100110100
W              18         100110101
j              20         100110110
O              4          10011011100
x              5          10011011101
"              12         1001101111
g              167        100111
o              604        1010
t              656        1011
l              328        11000
v              81         1100100
p              93         1100101
u              175        110011
c              176        110100
m              181        110101
h              385        11011
```

