

# Lecture 8

## Prolog

Prolog is a language for *logic programming*. Its concept is based on the First Order Logic.

### 8.1 Prolog Syntax

**Constant Symbols** – a word starting with a *lowercase* letter, or numbers  
e.g. john, richard, mickey, 123.

**Variable Symbols** – a word starting with a *uppercase* letter, or an underscore, e.g. X, Person, \_.

**Predicate Symbols** – a predicate name starting with a *lowercase* letter e.g.  
male(john), likes(john,apple), larger(mickey,X).

**Connective Symbols** – a comma (,) = and, a semicolon (;) = or,  
\+ = not, -> = implies.

**Equality Symbol** – =

**Evaluation predicate** – is

### 8.2 Hello, World!

```
1 ?- write('Hello, World!').  
2 Hello, World!  
3 true.
```

## 8.3 Prolog Source File

A statement in Prolog can be categorized into two types: *fact* and *rule*.

### 8.3.1 Facts

Facts are represented by predicates. They show relations among object. Each predicate must end with a period (.).

**Example 8.1** Facts showing the family relationships from the Bible.

1	father(terach,abraham).	father(terach,nachor).
2	father(terach,haran).	father(abraham,isaac).
3	father(haran,lot).	father(haran,milcah).
4	father(haran,yiscah).	
5		
6	male(terach).    male(abraham).    male(nachor).    male(haran).	
7	male(isaac).    male(lot).	
8		
9	mother(sarah,isaac).	
10		
11	female(sarah).    female(milcah).    female(yiscah).	

### 8.3.2 Rules

Rules are statements written in form of

$$A \leftarrow B_1, B_2, \dots, B_n.$$

where  $n \geq 0$ . Here,  $A$  is the *head* of the rule, and  $B_1, \dots, B_n$  is the *body* of the rule. All  $B_i (1 \leq i \leq n)$  are connected by commas. When all  $B_i (1 \leq i \leq n)$  are true, we can conclude that  $A$  is true.

**Example 8.2** Rules for the Biblical family.

```

1 /* X is a son of Y, if Y is a father of X and X is a male */
2 son(X,Y) :- father(Y,X), male(X).
3
4 /* X is a grandfather of Y, */
5 /* if X is a father of Z and Z is a father of Y */
6 grandfather(X,Y) :- father(X,Z), father(Z,Y).

```

## 8.4 Queries

Queries are for retrieving information from the loaded program. A query can be either a single predicate or a conjunction of predicates.

```

1 Welcome to SWI-Prolog (Multi-threaded, 64 bits, Version 6.6.0)
2 Copyright (c) 1990-2013 University of Amsterdam, VU Amsterdam
3 SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software
4 and you are welcome to redistribute it under certain conditions.
5 Please visit http://www.swi-prolog.org for details.
6
7 For help, use ?- help(Topic). or ?- apropos(Word).
8
9 ?- [bible].
10 % bible compiled 0.00 sec, 20 clauses
11 true.
12
13 ?- father(abraham,isaac).
14 true.
15
16 ?- father(abraham,haran).
17 false.
18
19 ?- father(X,haran).
20 X = terach.
21
22 ?- son(abraham,terach).
23 true.
24
25 ?- son(lot,X).
26 X = haran.
27
28 ?- son(X,haran).
29 X = lot ;
30 false.
31
32 ?- father(haran,X).
33 X = lot ;
34 X = milcah ;
35 X = yiscah.

```

```

1 ?- father(X,isaac),mother(Y,isaac).
2 X = abraham,

```

```
3 Y = sarah.  
4  
5 ?- son(isaac,X), father(terach,X).  
6 X = abraham.
```

**Exercise 8.1** Translate the following English sentences into Prolog queries. Use the facts from the Biblical family.

1. Is **terach** is a father of **nachor**?
2. Is **haran** is a brother of **abraham**?
3. Who is a grandfather of **isaac**?
4. Who is a sister of **lot**?

**Exercise 8.2** Write the output for the following queries using the given program.

```
1 isa(mickey,mouse). isa(minnie,mouse). isa(kitty,cat).
2 isa(doraemon,cat). isa(doraemon,robot). isa(nobita,boy).
3 isa(shizuka,girl).
4
5 isa(X,human) :- isa(X,boy).
6 isa(X,human) :- isa(X,girl).
7
8 eat(cat,meat). eat(mouse,cheese). eat(human,meat).
9 eat(human,vegetable). eat(doraemon,dorayaki).
10 eat(human,chicken).
11
12 carnivore(X) :- isa(X,Y), (eat(Y,meat) ; eat(Y,chicken)).
```

1. ?- isa(doraemon,cat).

2. ?- isa(nobita,X).

3. ?- carnivore(mickey).

4. ?- isa(X,human).

5. ?- isa(X,robot), isa(X,cat).

## 8.5 Query Evaluation

Prolog evaluates a query based on *matching between two terms* and *depth-first search*.

**Example 8.3** Write the output of the following queries using the given program.

```

1 input(0).    input(1).
2
3 and(0,0,0).  and(0,1,0).  and(1,0,0).  and(1,1,1).
4 or(0,0,0).   or(0,1,1).   or(1,0,1).   or(1,1,1).
5 xor(0,0,0).  xor(0,1,1).  xor(1,0,1).  xor(1,1,0).
6
7 circuit(In1,In2,Out1,Out2) :- input(In1), input(In2),
8                               xor(In1,In2,Out1), and(In1,In2,Out2).
```

1. ?- circuit(1,1,X,Y).

```

1 Resolvent = [circuit(1,1,X,Y)]
2 Choose circuit(1,1,X,Y)
3   Match with circuit(In1,In2,Out1,Out2) :-
4       input(In1), input(In2),
5       xor(In1,In2,Out1), and(In1,In2,Out2).
6
7 Resolvent = [input(1), input(1), xor(1,1,X), and(1,1,Y)]
8 Choose input(1)
9   Match with input(1).
10
11 Resolvent = [input(1), xor(1,1,X), and(1,1,Y)]
12 Choose input(1)
13   Match with input(1).
14
15 Resolvent = [xor(1,1,X), and(1,1,Y)]
16 Choose xor(1,1,X).
17   Match with xor(1,1,0). (X=0)
18
19 Resolvent = [and(1,1,Y)]
20 Choose and(1,1,Y).
21   Match with and(1,1,1). (Y=1)
22
23 Resolvent = []
24 Return X=0, Y=1
```

2. ?- circuit(1,0,0,1).

```

1 Resolvent = [circuit(1,0,0,1)]
2 Choose circuit(1,0,0,1)
3   Match with circuit(In1,In2,Out1,Out2) :-
4       input(In1), input(In2),
5       xor(In1,In2,Out1), and(In1,In2,Out2).
6
7 Resolvent = [input(1), input(0), xor(1,0,0), and(1,0,1)]
8 Choose input(1)
9   Match with input(1)
10
11 Resolvent = [input(0), xor(1,0,0), and(1,0,1)]
12 Choose input(0)
13   Match with input(0)
14
15 Resolvent = [xor(1,0,0), and(1,0,1)]
16 Choose xor(1,0,0)
17   Unable to match
18
19 Return false

```

3. ?- circuit(X,Y,1,0).

```

1 Resolvent = [circuit(X,Y,1,0)]
2 Choose circuit(X,Y,1,0)
3   Match with circuit(In1,In2,Out1,Out2) :-
4       input(In1), input(In2),
5       xor(In1,In2,Out1), and(In1,In2,Out2).
6
7 Resolvent = [input(X), input(Y), xor(X,Y,1), and(X,Y,0)]
8 Choose input(X)
9   Match with input(0) (X=0)
10
11 Resolvent = [input(Y), xor(0,Y,1), and(0,Y,0)]
12 Choose input(Y)
13   Match with input(0) (Y=0)
14
15 Resolvent = [xor(0,0,1), and(0,0,0)]
16 Choose xor(0,0,1)
17   Unable to match
18
19 Backtrack
20 Resolvent = [input(Y), xor(0,Y,1), and(0,Y,0)]
21 Choose input(Y)
22   Match with input(1) (Y=1)
23
24 Resolvent = [xor(0,1,1), and(0,1,0)]
25 Choose xor(0,1,1)
26   Match with xor(0,1,1)
27
28 Resolvent = [and(0,1,0)]
29 Choose and(0,1,0)
30   Match with and(0,1,0)
31
32 Resolvent = []
33 Return X=0, Y=1

```



```
34
35 ----User inputs ';'
36 Backtrack
37 Resolvent = [input(Y), xor(0,Y,1), and(0,Y,0)]
38 Choose input(Y)
39     No more option
40
41 Backtrack
42 Resolvent = [input(X), input(Y), xor(X,Y,1), and(X,Y,0)]
43 Choose input(X)
44     Match with input(1) (X=1)
45
46 Resolvent = [input(Y), xor(1,Y,1), and(1,Y,0)]
47 Choose input(Y)
48     Match with input(0) (Y=0)
49
50 Resolvent = [xor(1,0,1), and(1,0,0)]
51 Choose xor(1,0,1)
52     Match with xor(1,0,1)
53
54 Resolvent = [and(1,0,0)]
55 Choose and(1,0,0)
56     Match with and(1,0,0)
57
58 Resolvent = []
59 Return X=1, Y=0
60
61 ----User inputs ';'
62 ...
```



**Exercise 8.3** Answer the questions from the following Prolog program.

1. Write the output of `?- circuit(1,0,X,Y).`
  
2. Write the output of `?- circuit(1,1,1,Y).`
  
3. Write the output of `?- circuit(X,Y,0,1).`
  
4. Write a rule `dosth(X,Y,Z)` where  $Z = (X \wedge Y) \vee X$ .

## 8.6 Recursive Rules

Some rules may need to use themselves recursively to describe a more general concept. From the Biblical family data, we can write a set of rules for representing the ancestors as:

```

1  parent(X,Y) :- father(X,Y).
2  parent(X,Y) :- mother(X,Y).
3  grandparent(X,Y) :- parent(X,Z), parent(Z,Y).
4  greatgrandparent(X,Y) :- parent(X,Z), grandparent(Z,Y).
5  greatgreatgrandparent(X,Y) :- parent(X,Z), greatgrandparent(Z,Y).
```

We can define rules of the general concept of ancestors by using recursion.

```

1  ancestor(X,Y) :- parent(X,Y).           /* base case */
2  ancestor(X,Y) :- parent(X,Z), ancestor(Z,Y). /* recursive case */
```

**Example 8.4** Define rules for `factorial(N,F)` which is a predicate “ $N!$  is  $F$ ”.

```
1 factorial(0,1) :- !.  
2 factorial(N,F) :- M is N-1, factorial(M,G), F is N*G.
```

Note: `!` is the cut operator. It forces Prolog to stop backtracking when the operator is encountered.

**Exercise 8.4** Write rules for `pow(X,Y,Z)` which is a predicate “ $X^Y$  is  $Z$ ”.

**Example 8.5** A predicate **edge(X,Y)** is a fact representing a directed edge from node  $X$  to node  $Y$ . For example, **edge(a,b)** shows an edge from  $a$  to  $b$ , but not from  $b$  to  $a$ . The following program shows some example facts.

1	<b>edge(a,b).</b> <b>edge(a,c).</b> <b>edge(b,c).</b> <b>edge(b,d).</b>
2	<b>edge(c,e).</b> <b>edge(c,f).</b> <b>edge(c,g).</b>

Write rules for **path(P,Q)** which is a predicate “There is a directed path from node  $P$  to node  $Q$ ”. For example, **path(a,b)** is true, **path(a,e)** is true, but **path(d,f)** is false.

**Example 8.6** From the previous path, write rules for **path(P,Q,R)** which is an extension of **path(P,Q)** with **R** showing how to get to **Q** from **P**. Here are some expected query results:

```
1 ?- path(a,b,go(a,b)).  
2 true .  
3  
4 ?- path(a,c,X).  
5 X = go(a, c) ;  
6 X = go(a, b, go(b, c)) ;  
7 false.
```

## References

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