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Q3

Exercise 7.6 of the textbook (page 244-245)

1) Estimate  $\mu$ .

$$\hat{\mu} = \frac{\sum \text{observations}}{n} = \frac{12.00+11.97+\dots+12.02+12.04}{36} = \frac{430.04}{36} \approx 11.9456$$

Thus, the estimation of  $\mu$  is 11.9456 (ounces).

2) Place a bound on the error of estimation. Assume  $N = 1800$ .

$$Var(s^2) = \frac{(X_i - \hat{\mu})^2}{n-1} = \frac{(12.00-11.9456)^2 + (11.97-11.9456)^2 + \dots + (12.02-11.9456)^2 + (12.04-11.9456)^2}{36-1} \approx 0.0058$$

$$\hat{Var}(\hat{\mu}) = \left(1 - \frac{n}{N}\right) \frac{s^2}{n} = \left(1 - \frac{36}{1800}\right) \frac{0.0058}{36} \approx 0.000159$$

The bound of error of estimation is

$$B = 2\sqrt{\hat{Var}(\hat{\mu})} = 2\sqrt{0.000159} \approx 0.02513.$$

Therefore, the average amount of fill lies within the bound of error 0.02513 (ounces) of the estimation.