# Introduction

# **Background and Motivation**

- Parallel computing is a part of HPC.
  - HPC also includes everything else that makes the computation fast.
  - No point parallelizing without increasing performance.
  - You might want to optimize for the architecture.
  - Sometimes overhead outweighs benefits from parallelization.
- Focusing on parallel algorithms.
  - Different version of parallel algorithms suits different architecture or models.
- Many application yo.
- People made super computers throughout the 1900s
- Super computers rely on carefully designed interconnects.
- Cloud computers are just AWS instances.
- Many aspects

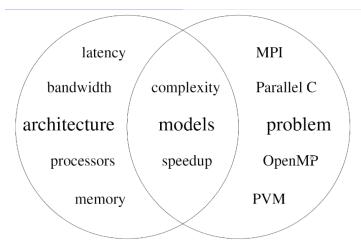


Figure: Overlapping aspects of parallel computing

## Complexity

- $f(n) = O(g(n)) \Rightarrow f$  grows no faster than g
- $f(n) = \Omega(g(n)) \Rightarrow f$  grows no slower than g
- $f(n) = o(g(n)) \Rightarrow f$  grows slower than g
- $f(n) = \omega(g(n)) \Rightarrow f$  grows faster than g
- $f(n) = \Omega(g(n)) \land f(n) = O(g(n)) \Rightarrow f(n) = \Theta(g(n))$
- Strictly speaking we should really use  $\in$  instead of =
- Some common name for complexities:
  - Constant
  - Logarithmic
  - Polylog:  $(\log(n))^c$
  - Linearithmic:  $n \log n$
  - Quadratic:  $n^2$
  - Polynomial or geometric
  - Exponential
  - Factorial
- Log factor are often ignored.

### Model

- RAM model: random access machine
  - Common model when we talk about sequential time complexity.
- Multiplying the number of computers by a constant factor doesn't change the complexity.
  - Solution: allow p, the number of processors to increase with problem size and hence reduces the complexity.

### **PRAM**

- Parallel Random Access Machine
- *p* number of RAM processors, each have private memory and share a large shared memory, all memory access takes the same amount of time.
- Does things synchronously, AKA in lock steps.
- PRAM pseudo code looks like regular pseudo code but there's this

 $\label{eq:continuous} \begin{tabular}{ll} \textbf{for } i \leftarrow 0 \begin{tabular}{ll} \textbf{to } n-1 \begin{tabular}{ll} \textbf{do in parallel} \\ \textbf{processor} \begin{tabular}{ll} \textbf{does thingy} \\ \end{tabular}$ 

Many different PRAM model

- EREW: exclusive read, exclusive write
- CREW: concurrent read, exclusive write
- CRCW: concurrent read, concurrent write
  - Concurrent write have different types
    - COMMON: Error when two processor tries to write to the same location with different value.
    - ARBITRARY: Pick a arbitrary processor if many processor writes the same time.
    - PRIORITY: Processor with lowest ID writes.
    - COMBINING: Runs a function whenever multiple processors tries to write at the same time.
      - Too powerful.
- ERCW: exclusive read, concurrent write (never used)

Power of model: expresses the set of all problems that can be solved within a certain complexity.

- A is more powerful that B if A can solve a larger set of problems within any complexities.
- A is equally powerful as B if they can solve the same set problems within any complexities.
- Partial ordering.
- COMMON, ARBITRARY, PRIORITY and COMBINING are in increasing order of power.
- Any CRCW PRIORITY PRAM can be simulated by a EREW PRAM with a complexity increase of  $\mathcal{O}(\log p)$
- *Parallel Computation Thesis*: any thing can be solved with a Turing Machine with polynomially bounded space can be solved in polynomially bounded space with unlimited processors.
  - Unbounded *word sizes* are not useful, so we limit word counts to  $\mathcal{O}(\log p)$
- *Nick's Class* (NC): Solvable in polylog time with ploy number of processors.
- Widely believed that  $\mathbf{NP} 
  eq P$

# Definitions (need to remember)

- $w(n) = t(n) \times p(n)$  where w(n) is the work / cost, t(n) is the time and p(n) is the number of processors.
  - Optimal processor allocation means:  $t(n) \times p(n) = \Theta(T(n))$  where T(n) is the time taking by a sequential algorithm.
    - Equivalent to  $t(n) \times p(n) = O(T(n))$  because  $t(n) \times p(n) = \Omega(T(n))$  always.
  - Speedup $(n) = \frac{T(n)}{t(n)}$ 
    - Speedup optimal = processor optimal.
  - Optimal: processor optimal AND  $t(n) = \mathcal{O}(\log^k n)$ 
    - Processor optimal and polylog in time.
  - Efficient: Assume  $T(n) = \Omega(n) w(n) = \mathcal{O}(T(n) \log^{\alpha} n)$  AND polylog in time
    - Optimal but polylog increase in work.
- *size*: Size(n) is the total number of operations it does.
- efficiency:  $\eta(n)$  speedup per processor  $\eta(n) = \frac{T(n)}{w(n)} = \frac{\operatorname{Speedup}(n)}{p(n)}$
- You can decrease p and increase t by a factor of  $O\left(\frac{p_1}{p_2}\right)$ , w(n) doesn't increase its complexity.
  - · Can't do it the other way around.

## **Brent's Principle (important)**

• If something can be done with size x and t time with infinite processors, then it can be done in  $t + \frac{x-t}{n}$  time with p processors

#### Amdahl's Law

- Maximum speedup: if f is the fraction of time that can't be parallelized, then Speedup $(p) \to \frac{1}{f}$  as  $p \to \infty$ 
  - Honestly very obvious.

### Gustafson's Law

- s is fraction time of serial part, r is fraction time of parallel part, then Speedup $(p) = \Omega(p)$ 
  - Very obvious again...

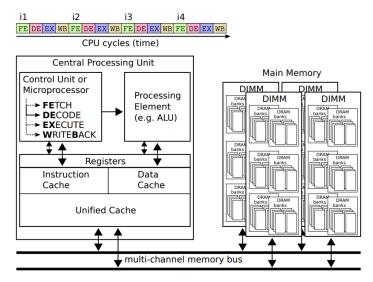
## **Algorithms**

- sum
- · logical or
- Maximum
  - $n^2$  processors all compare all elements and set is max array to false if element isn't maximum.
  - Only processor with element being max write it to the returning memory address.
- Maximum $n^2$ 
  - $\mathcal{O}(\log \log n)$
  - *n* processor on *n* elements.
  - Is efficient
  - Make elements into a square, find maximum on each row recursively.
  - Find maximum of maximum of the rows using maximum.
  - $\mathcal{O}(\log \log n)$  levels of recursion, each level takes  $\mathcal{O}(1)$  times
- Element Uniqueness
  - Have an array size of MAX INT.
  - Write processor ID to the array with the element.
  - Check if processor ID is indeed there, if not there's another element there.
- Replication

- $O(\log n)$
- · Replication optimal
  - $p = \frac{n}{\log(n)}$  and copy at the end.
- Broadcast
  - Just replicate
- Simulate PRIORITY with COMMON  $n^2$ 
  - Minimum version of Maximum
- Simulate PRIORITY with EREW
  - All processor wants to write
  - Sort array A of tuples (address, processorID) using Cole's Merge Sort.
  - For each processor k, if A[k].address  $\neq A[k-1]$ .address then A[k].processorID is the smallest ID that wants to write to that address.

# Architecture

• Fetch Decode Execute WriteBack



- Bus is a wire and everyone can see everything on that wire.
- Pipeline: let's do all of them at the same time for the next 4 instructions
  - Need to predict the next 4 instructions sometimes.
- Superpipeline: Do all of them for the next 8 (or more) instructions.
- Superscalar: Multiple pipeline in parallel
- Word size: 64 bits, 32 bits etc, various aspects:
  - Integer size
  - Float size
  - Instruction size
  - Address resolution (mostly bytes)
- Single instruction multiple data SIMD
  - Make word size more complicated
- Coprocessor
  - Used to means stuff directly connected to the CPU like a floating point processor.
  - Now can means FPGA or GPU.
- Multicore processor are just single core duplicated but they all have one extra single shared cache.

- Classification of parallel architectures
  - SISD regular single core.
  - SIMD regular modern single core.
  - MIMD regular multicore.
  - MISD doesn't exist.
- · SIMD vs MIMD
  - Effectively SIMD vs non-SIMD
  - Most processor have multicore and SIMD on each core.
    - So a balance between the two.
  - SIMD cores are larger so less of them fit on a die.
  - SIMD is faster at vector operations.
  - SIMD is not useful all the time so sometimes the SIMD part sit idle.
  - SIMD is harder to program.
- Shared memory: All memory can be accessed by all processors.
  - All memory access truly equal time: symmetric multi-processor.
    - Only can have so many cores when the bus is only so fast.
    - Making more buses doesn't help cause space also slows things down.
    - Sometimes can be done with switching interconnect network.
  - Some processor access some memory faster.
    - More complex network.
  - Distributed shared memory: each processor have its own memory but interconnect network exist so you can read other people's memory.
    - non-uniform memory access NUMA
    - Static interconnect network: each node connect to some neighbors.
      - *degree*: just like degree in graphs.
      - diameter: just like in graphs.
      - $cost = degree \times diameter$
- Distributed memory: Each processor have its own memory. Each process live on one processor.
- Blade contains Processor / Package / Socket which contains Core which contains ALU.
- Implicit vs explicit: explicit  $\rightarrow$  decision made by programmer
  - Parallelism: Can I write a sequential algorithm.
  - Decomposition: Can I pretend threads processes doesn't exist.
  - Mapping: Can I pretend all cores are the same.
  - Communication.
- Single Program Multiple Data: one exe
- Multiple Program Multiple Data: multiple exe

### Other HPC considerations

- · Cache friendliness
- Processor-specific code
- Compiler optimization.
  - Compiler from CPU maker are usually better.
  - So Intel compiler is better than both clang and gcc.

### Memory interleaving

• Memory module takes a while to recharge, so we interleave a page on different memory module.

## Automatic Vectorization

- Sometimes compilers automatically insert SIMD instructions in place of loops.
  - Depends on the availabilities of a lot of things, including the OS.
- Manual SIMD:

```
multiply_and_add(const float* a, const float* b, const float* c, float* d) {
   for(int i=0; i < 8; i++) {
      d[i] = a[i] * b[i];
      d[i] = d[i] + c[i];
   }
}
--m256 multiply_and_add(--m256 a, --m256 b, --m256 c) {
   return _mm256_fmadd_ps(a, b, c);
}</pre>
```

• AVX have to be aligned: i.e. 256 bits SIMD have to be 256 bits aligned - address is multiple of 256 bits.

### Multithreading

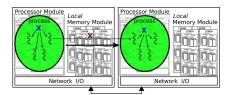
- Synchronization is more expensive if threads are on cores further away.
  - It's expensive in general.
- Instruction reordering: thread continues with other instructions while it waits on earlier instructions.
- Speculative execution: don't wait on instructions, just go for it and if it fails then unroll.
- Some programming patterns are more friendly to NUMA.

Message passing considerations

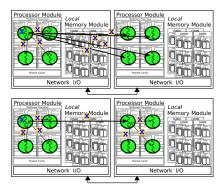
- Multi processing have to pass messages around because processes don't share address space.
- Hard to predict performance.

Wants good communication patterns

• For multithread multiprocess:



• For single thread multiprocess:



# **OpenMP**

• Abstracts single process, multithreaded program execution on a single machine.

- Abstracts: Multi-socket, multi-core, threads, thread synchronization, memory hierarchy, SIMD, NUMA.
- Everything OMP does are hints.
- *internal control variable*: ICV: OMP\_NUM\_THREADS, OMP\_THREAD\_LIMIT, OMP\_PLACES, OMP\_MAX\_ACTIVE\_LEVELS.
- Can also be set with functions in #include "omp.h"

#### **Execution Model**

- There's an implicit parallel region on the outside.
- There's by default an implicit barrier at the end of each parallel region.
  - no-wait removes the implicit barrier
- If a parallel region is encountered, then the threads split and a new team is created.
- A lot of parallel region nested can create a lot of thread very quickly.
  - Can limit nesting by OMP\_MAX\_ACTIVE\_LEVELS.

### Memories: global, stack, heap

• Threads have their own stack but share global and heap.

#### **Directives**

- The #pragma omp thingy.
- Allows specifying parallelism and still allow the base language to be the same.
  - Theoretically, simply remove the directives and program will just run like a sequential program.
- Syntax:

```
#pragma omp <directive name> [[,]<clause> [[,]<clause> [...]]]
<statement / block>
```

- Multiple directives can be applied to one following block
- Some directives are *stand alone*, they don't have structured block following them.

### Synchronization

- thread team is a group of threads.
- barrier will block threads in a team that reach it early.
- flush will enforce consistency between different thread's view of memory.
- critical ensures a critical region where only one thread can be in it at a time.
- atomic is faster than critical but only for simple operations.
- simd make use of SIMD instructions.
- *places*: specify how processing units on the architecture are partitioned.
- Thread encounters a parallel directive -> split itself into the number of threads.
- #pragma omp parallel
  - create some number of threads and do its thing.
  - clauses:
    - num threads(int) overrides ICV, limited by OMP THREAD LIMIT
    - private(list of variables) each thread will have own memory allocated to private variable.
      - Default for variables on stack.
    - shared(list of variables) all thread share the same variables, same piece of memory.
      - OpenMP will add locks.
    - threadprivate(list of variables) variable stay with the thread if all threadprivate directives are identical.
  - Can combine with for, loop, sections and workshare.

- #pragma omp for
  - clauses:
    - schedule([modifier[, modifier]:]kind[, chunk\_size])
      - · kind:
        - static: divided into chunk\_size (default  $\frac{iterations}{num \ threads}$ ) and distributed round-robin over the threads
        - dynamic: chunks of chunk size (default 1) distributed to threads as they complete them.
        - guided: like dynamic but varying chunk\_size, large chunks at the start and small chunks at the end.
        - auto: default.
        - runtime: determined by sched-var ICV.
      - · modifier:
        - monotonic: chunks are given in increasing logical iteration
        - nonmonotonic: default, allows work stealing: I finished early, I will now take your work.
        - simd: try to make the loop into SIMD constructs.
    - collapse(n): n nested loops are combined into one large logical loop.
    - ordered[(n)]: There are operations in the loop that must be executed in their logical order.
    - reduction([reduction-modifier, ] reduction-modifier:list): a list of variable that will be used in a reduction operation.
      - Allowed operations: +, -, \*, &, ^, &&, ||, max, min
      - Example: #pragma omp parallel for reduction(+:x), x is the result, + is the operation.
        - x starts as a private variable initialized to the identity value.
        - global x will be assigned to the sum of all xs at the end.
- #pragma omp loop
  - Work for any loop, not just for.
  - Main diff to for is bind
- #pragma omp sections
  - Have #pragma omp section inside.
  - Each #pragma omp section gets executed by one thread.
  - clauses:
    - private(list of variables): each thread will have its own version of the variable.
    - firstprivate(list of variables): same as private but memory is initialized to the global version.
    - lastprivate(list of variables): copy the private variables to the global version for the "lexically last" private variables.
      - A variable can be firstprivate and lastprivate at the same time.
- #pragma omp single
  - Only do it in a single thread in the team, used inside #pragma omp parallel
    - private(list of variables): each thread will have its own version of the variable.
    - firstprivate(list of variables): same as private but memory is initialized to the global version.
- #pragma omp workshare
  - Here's a bunch of independent statements / blocks, figure out how to parallelize it.
- #pragma omp atomic
  - critical for read, write, update (x += 1), compare (if (expr < x) x = expr;).
- #pragma omp critical [(name) [[,] hint(hint-expression)]]
  - clauses
    - (name): two critical region with the same name can't happen at the same time.
      - All no name critical region are treated as having the same name.

- hint(hint-expression):
  - omp\_sync\_hint\_uncontended
  - omp\_sync\_hint\_contended
  - omp\_sync\_hint\_speculative: try to speculate.
  - omp\_sync\_hint\_nonspeculative: don't try to speculate.
- #pragma omp ordered
  - Inside loops so that they're executed in their logical order.
- #pragma omp barrier
  - Explicit barrier.
- #pragma omp flush
  - Sync cache.
  - Be aware of code reordering.
- #pragma omp task
  - The *Task Model*: specify work without allocating work to threads.
  - Task is a unit of work.
  - Task have dependencies such as completion of other tasks.
  - Task may generate other tasks.
  - Uses many same clauses such as private, shared and firstprivate.
  - Task can have data affinity.
  - clauses:
    - depend([depend-modifier,] dependence-type:locator-list).
    - priority(int): hint of order of execution.
    - affinity([aff-modifier :] locator-list)
- #pragma omp taskloop
  - clauses:
    - num\_tasks([strict:]num-tasks): specify the number of tasks that will be generated.
    - grainsize([strict:]grainsize): how many iteration per task.
- #pragma omp taskwait
  - · Wait for all current child tasks to finish

### Places

- OMP\_PLACES: list of power units by their identifiers
  - {0,1,2,3}, {4,5,6,7}: specify two places each with 4 processing units.
    - use hwloc-ls to find processing unit number.
  - threads(8): 8 places on 8 hardware threads
  - cores(4): 4 places on 4 cores.
  - ll\_caches(2): 2 places on 2 set of cores where all the cores in a set shares their last level cache.
  - numa\_domains(2): 2 places on 2 set of cores whose closes memory is the same or similar distance.
  - sockets(2): 2 places on two sockets
  - OMP\_PLACES partition power units into places. Which can then be referred to by proc\_bind(type) clause in parallel directives.
- proc\_bind(type): overrides OMP\_PROC\_BIND, only in parallel directives.
  - primary: All threads created in the team are in the same place.
  - close: Threads are allocated to places in a round-robin fashion first thread in place i, second thread in place i+1, third thread in place i+2
  - spread: Place thread in a way so that the distance between the power unit ID are as far as possible.

### Memory

- Sending memory to other numa domains cost cache as well because the send operation needs to be done by a CPU which means cache.
- OpenMP memory classification:
  - omp\_default\_mem\_space: DRAM
  - omp\_large\_cap\_mem\_space: SSD
  - omp const mem space: optimized for read only
  - omp high bw mem space: high bandwidth
  - omp\_low\_lat\_mem\_space: low latency.
- Memory allocator have traits:
  - sync\_hint: expected concurrency contended (default), uncontended, serialized, private
  - alignment: default byte.
  - access: which thread can access the memory, all (default), cgroup, pteam, thread
  - pool\_size: total amount of memory the allocator can allocate.
  - fallback: on error return null or exit, default is first try standard allocator and return null if fail.
  - partition: environment (default), nearest, blocked, interleaved. How is the allocated memory partitioned over the allocator's storage resource.

## **Prefix Sum**

- Doesn't have to be sum, can also be any other associative operations (like prod, min, max).
- The only way to reduce depth is to increase size (hopefully only slightly).

# Upper/Lower parallel prefix algorithm

- Divide array into two parts and compute their prefix sum.
- Add the sum of the first part to the second part.
- $\Theta(\log n)$  time complexity
- $\Theta(n \log n)$  work
- $\Theta(n \log n)$  size
- Half of the processors are idle all time except first iteration. (can probably be easily fixed)

# Odd/Even parallel prefix algorithm

- Divide array into odd and even indices parts.
- Add odd indices to even indices.
- Compute prefix of even part recursively.
  - Now the even part contains the correct prefix.
- Compute the odd part in one parallel step.
- Same complexity as Upper/Lower, but 2 times slower.

# Ladner and Fischer's parallel prefix algorithm.

- Optimal possible time.
- Split array into two parts and use odd even for the first part, upper lower for the second part.
  - Odd even for the first part is beneficial because the last element is available one step earlier.

## Pointer jumping

• All processor replace next with next next, so you start going in  $2^n$  steps for each iteration.

# **Sorting**

- Merge sort parallelized is O(n) because last merge is sequential.
- Quick sort parallelized is O(n) because the first split is sequential.

# Parallel merge

- $\mathcal{O}\left(\frac{n}{p} + \log p\right)$  or  $\mathcal{O}(\log n)$  where p = n
- Two sorted list, assume all value are below n where n is the length of the resulting array.
- Count unique value for both of them.
- Write the sum of count for both array to result array with index X.
- Now the count is sorted.
- Compact the result array.
- Use prefix sum to space the resulting array evenly so that there are count -1 null element after even element.
- Use distribution to fill out the rest of the array.

### Compaction

- Move all non null element to the first part of the array.
- Use prefix sum to count the index of each empty element.
- Move each non empty element to its index.

## **Unique Counts**

- Sorted array to (value, count) element.
- Find all places where the adjacent values are different.
- Use prefix sum to find their index.
- · Reverse engineer their count with old indices.

#### Distribution

- Array with some null value, fill with the closest non null value to the left.
- Best complexity is achieved with simple broadcast.
- 1. Use prefix sum and unique count to figure out how many empty element are after each non empty one.
- 2. Do sequential distribute with each processor.
- 3. For the processors where their first element is null:
  - 1. Still need to fill
  - 2. Use info obtained previously at the very first step to calculate how long does this null sequence last.
  - 3. All processor involved in the null sequence, broadcast!

#### Rank sort

- Count the number of element smaller and number of element bigger, and just write this element to the array.
- Use  $n^2$  processors. Can count the index in  $\mathcal{O}(\log n)$  time.
- With a combine PRAM, it can be done in  $\mathcal{O}(1)$  time.

### Rank Merge

• Much simpler than Parallel merge, just use binary search to find the ranks.

### **Bitonic MergeSort**

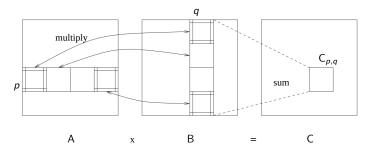
- Bitonic is a sequence is two monotonic sequences but one up and one down.
- · You can find the pivot and turn this into a regular merge.
- Alternatively:
  - compare and maybe swap each two pair of element in two part of the array (none of them reversed.)
  - You end up getting two bitonic array.
  - · Keep doing this and you sort it.

• Same time complexity.

You can use bitonic sort to do bitonic merge sort, by keep constructing bitonic lists and merging them with bitonic sort.

# **Matrix Multiplication**

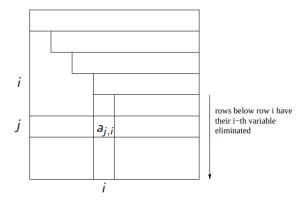
- Matrix multiplication doesn't have dependencies between them, so easy to parallelize with less than  $n^2$  processors.
- Pretty trivial to parallelize in ideal conditions, so we will focus on practical side of matrix multiplication.
- For huge matrices, we can divide them into smaller one, multiply the smaller ones, and then sum the smaller ones.



• You can divide the matrices into 4 parts recursively, until the matrix is small enough to fit into the cache.

## Gaussian elimination

- Common for matrix to be sparse, aka mostly zero.
- Gaussian elimination is for dense matrix.
- Solving system of linear equation by getting rid of variables one by one by rewriting them in terms of other variables.

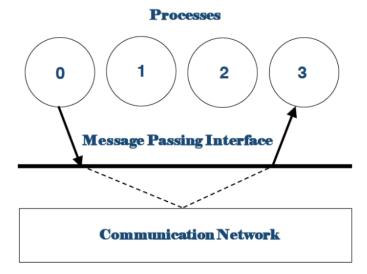


- If a coefficient of a variables is close to zero, then we run into numerical problems.
  - We can swap this row with the rows below to fix this. This is called *partial pivoting* 
    - Partial because the columns aren't being swapped.
    - Can be done in  $\mathcal{O}(\log_2 n)$
    - We will ignore partial pivoting to simplify our problem. (make it more theoretical)
- The eliminate step can be parallelized. Resulting in time complexity of  $\mathcal{O}(n^2)$  with p=n
  - We can more better utilize processor if there are less than n processor by using *cyclic-striped* partitioning.

processor 1
processor 2
processor 3
processor 1
processor 2
processor 3
processor 1
processor 2

## **MPI**

• Pass messages between processes.



- Provide consistent interface to have portable code on different architectures.
- Can be sync or async
  - sync: returns after message being read by receiver process.
  - async: returns asap and have some other thread or the kernel do the sending.
- MPI is a language.

### Communicator

- Communicators: a set of processes.
  - $\bullet$  MPI\_COMM\_WORLD: all processes.
- Rank: 0 based index of your processes given a communicator.
- Size: size of the communicator.

## **Functions**

- int MPI\_Init(int \*argc, char \*\*\*argv): first MPI call, initialize the MPI execution environment, takes away the MPI arguments by modifying argc and argv.
- int MPI\_Finalize(): last MPI call.
- int MPI\_Send(void \*buf, int count, MPI\_Datatype datatype, int dest, int tag, MPI\_Comm comm)

- int MPI\_Recv(void \*buf, int count, MPI\_Datatype datatype, int source, int tag, MPI\_Comm comm,
  - MPI\_Status \*status)
  - For send and receive to succeed, rank must be valid, communicator must be same, tags must be same (or say idk what tag), message datatype must be compatible.
- int MPI\_Bcast(void \*buf, int count, MPI\_Datatype, int root, MPI\_Comm comm)
- int MPI\_Scatter(void \*buf, int sendcount, MPI\_Datatype sendtype, void \*recvbuf, int recvcount, MPI Datatype recvtype, int root, MPI Comm comm)
  - One node send different data to other nodes.
- int MPI\_Gather(void \*buf, int sendcount, MPI\_Datatype sendtype, void \*recvbuf, int recvcount, MPI\_Datatype recvtype, int root, MPI\_Comm comm)
  - Opposite of scatter.
- int MPI\_Allgather(void \*sendbuf, int sendcount, MPI\_Datatype sendtype, void \*recvbuf, int recvcount, MPI\_Datatype recvtype, MPI\_Comm comm)
- int MPI\_Alltoall(void \* sendbuf, int sendcount, MPI\_Datatype sendtype, void \* recvbuf, int recvcount, MPI\_Datatype recvtype, MPI\_Comm comm)
- int MPI\_Alltoallv(void \* sendbuf, int \* sendcounts, int \* sdispls, MPI\_Datatype sendtype, void \* recvbuf, int \* recvcounts, int \* rdispls, MPI\_Datatype recvtype, MPI Comm comm)
- int MPI\_Reduce(void \* sendbuf, void \* recvbuf, int count, MPI\_Datatype datatype, MPI\_Op op, int root, MPI\_Comm comm)
  - MPI\_Op can be: MPI\_MAX, MPI\_MIN, MPI\_SUM, MPI\_PROD, MPI\_LAND, MPI\_BAND, MPI\_LOR, MPI\_BOR, MPI\_LXOR, MPI\_BXOR.
- int MPI Barrier(MPI Comm comm)
  - Mostly used to share OS resource are not controlled by MPI.
- MPI Ssend: sync
  - MPI\_Send can be sync or async
  - Sync send can deadlock if the receiver is waiting for a message with a different tag.
- MPI\_Bsend: Async
  - Many other type of MPI\_Send
  - Async send can be out of order.
  - Can check status to check tag.
- MPI Comm split(MPI Comm comm, int color, int key, MPI Comm \*newcomm)
- int MPI\_Cart\_create(MPI\_Comm comm\_old, int ndims, int \*dims, int \*periods, int reorder, MPI Comm \*comm cart)
  - Create cartesian topology
- int MPI\_Dims\_create(int nnodes, int ndims, int \*dims)
  - Will fill in the zeros in dims, will try to make dimensions as close to each other as possible.
- int MPI\_Cart\_rank(MPI\_Comm comm, int \*coords, int \*rank)
  - Map coordinates to rank.
- int MPI\_Cart\_coords(MPI\_Comm comm, int rank,, int maxdims, int \*coords)
  - Map rank to coordinates.
- int MPI\_Cart\_shift(MPI\_Comm comm, int direction, int disp, int \*rank\_source, int \*rank\_dest)

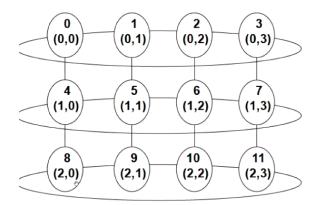
- Source is who will send to me
- Dest is who will I send to
- int MPI\_Sendrecv\_replace(void \*buf, int count, MPI\_Datatype datatype, int dest, int sendtag, int source, int recvtag, MPI\_Comm comm, MPI\_Status \*status)
  - Take the result of my source and replace my data which will be send to my dest.
  - Can use with MPI\_Cart\_shift but not necessary.
- MPI\_PROC\_NULL: send or receive from and to MPI\_PROC\_NULL does nothing so we don't have to move forward.

# Multithreading

- 4 levels options of support:
  - 0, MPI\_THREAD\_SINGLE: only one thread will execute.
  - 1, MPI\_THREAD\_FUNNELED: only one thread will make MPI calls.
  - 2, MPI\_THREAD\_SERIALIZED: calls well never be concurrent.
  - 3, MPI\_THREAD\_MULTIPLE: No restrictions.
- Call MPI\_Init\_thread(int \*argc, char \*\*\*argv, int required, int \*provided) instead of MPI\_Init to declare you need multithreading.

# **Topologies**

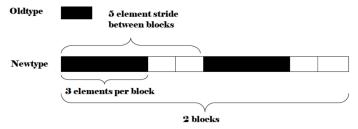
- Examples: ring.
- MPI have function that allows you to refer to "node below me" which will calculate the rank for you.
- Cylinder:



- Cartesian: a grid that might or might not be cyclic with each dimensions.
- Graph topologies: explicitly list neighbours of each node

# **Derived Types**

- Can define new MPI\_Datatype.
- Can be used in place of any MPI\_Datatype can.
- Types are defined with other list of types and displacements (in bytes).
- int MPI\_Type\_contiguous(int count, MPI\_Datatype oldtype, MPI\_Datatype \*newtype): just an array of the same type.
- Vector Datatype:



- $\bullet \ count = 2$
- stride = 5
- blocklength = 3
- Good for sub blocks of a matrix.
- int MPI\_Type\_vector(int count, int blocklength, int stride, MPI\_Datatype oldtype, MPI\_Datatype \*newtype)
- int MPI\_Type\_create\_struct(int count, const int array\_of\_blocklengths[], const MPI\_Aint array\_of\_displacements[], const MPI\_Datatype array\_of\_types[], MPI\_Datatype \*newtype)
  - Can represent any struct.
- After create datatype, must call int MPI\_Type\_commit(MPI\_Datatype \*datatype)
  - Can use uncommited datatype to build other data type.
- int MPI\_Type\_free(MPI\_Datatype \*datatype)
  - Free a committed type's memory.
- Count  $\times$  Fundamental data type count must match for send and receive.

## **GPU**

- GPGPU: General purpose GPU
- Many CUDA core / Streaming processor make up of Streaming multiprocessor.
- GPU have:
  - Threads: smallest execution entity, each have their own id.
  - Block / warp made up of threads that execute in a single multiprocessor in sync. Every thread runs the same line of code at the same time.
    - Blocks are SIMD.
  - Grid: a bunch of blocks that execute a kernel function (kinda like a regular function).
    - Blocks are running the same code but not in lock step.
    - Blocks are independent to each other, can go in any order.
- GPU have memory that's high throughput.
  - Global memory: main memory 100ms
    - · IO for grid
  - Shared memory 128kB: shared memory 5ns about the speed of L1 cache.
    - per block
    - Can use for collaboration within a block.
  - Register and local memory: fastest, around 10x faster than shared memory, not as fast as registers on CPU.
    - Per thread
    - · Store stack vars.
- Compared with CPU
  - CPU wants to run one thread very fast: Sophisticated control, powerful ALU, Large cache.
  - GPU wants high throughput: simple control, small caches, many efficient ALU.
- CUDA: Compute Unified Device Architecture.
  - Extends C/C++, can run on both GPU and CPU.
  - Abstract from the hardware, same code run on many GPU.

- Auto thread management.
- Vendor-lock to Nvidia.
- Hard to debug, don't have printf in early versions.