

# Math

$\log_k(x)$  is the number of times we have to divide  $x$  by  $k$  to get to 1.

$$\log_k(ab) = \log_k(a) + \log_k(b)$$

$$\log_k(x^n) = n \cdot \log_k(x)$$

$$\log_k\left(\frac{a}{b}\right) = \log_k(a) - \log_k(b)$$

$$\log_u(x) = \frac{\log_k(x)}{\log_k(u)}$$

The natural logarithm  $\ln(x)$  of a number  $x$  is a logarithm whose base is  $e \approx 2.71828$ .

The number of digits of an integer  $x$  in base  $b$  is  $\lfloor \log_b(x) + 1 \rfloor$ .

## Time complexity

We can use time complexity to estimate if a particular algorithm is going to be efficient enough.

Assuming time limit is 1 second:

Input size	Required time complexity
$n \leq 10$	$O(n!)$
$n \leq 20$	$O(2^n)$
$n \leq 500$	$O(n^3)$
$n \leq 5000$	$O(n^2)$
$n \leq 10^6$	$O(n \log n)$
$n \geq 10^6$	$O(\log n)$

It is important to remember that time complexity is only an estimate.