

Refactoring Laws for Colorful Alloy

The refactored laws of our colorful Alloy is present in the form of an equation of two Alloy template. we can apply a refactoring whenever either side template is matched by a piece of Alloy code and when it satisfies the preconditions. A matching is an assignment of all the variables in the left/right hand side templates to concrete values from the source annotated Alloy code.

Restriction of Colorful Alloy:

$\textcircled{a} \cap \textcircled{b} = \perp$, which means there's no common product in \textcircled{a} and \textcircled{b} .

The meaning of Symbols:

p denotes a set of signatures, predicates, or facts, p may contain feature annotations;

ds denotes a set of Field declarations, ds may contain features;

\textcircled{a} , \textcircled{b} , \textcircled{c} denote a set of features combination that can be marked on the Alloy elements;

\textcircled{k} represent a concrete feature k is selected, while $\bullet k$ means the de-selection of k .

r represent a Field relation.

Law 1,2,3,?? are rules for signatures.

Law 1 (Remove abstract Attribute) [1]

$$\begin{array}{|l}
 \textcircled{a} \textbf{abstract sig} A \{ ds \} \textcircled{a} \\
 \textcircled{a} \textbf{sig} A_1 \textbf{extends} A \{ ds_1 \} \textcircled{a} \\
 \dots \\
 \textcircled{a} \textbf{sig} A_n \textbf{extends} A \{ ds_n \} \textcircled{a}
 \end{array}
 =
 \begin{array}{|l}
 \textcircled{a} \textbf{sig} A \{ ds \} \textcircled{a} \\
 \textcircled{a} \textbf{sig} A_1 \textbf{extends} A \{ ds_1 \} \textcircled{a} \\
 \dots \\
 \textcircled{a} \textbf{sig} A_n \textbf{extends} A \{ ds_n \} \textcircled{a} \\
 \textcircled{a} \textbf{fact} \{ A = A_1 + \dots + A_n \} \textcircled{a}
 \end{array}$$

Law 2 (Remove the Multiplicity of Sig) [1]

$$\textcircled{a} m \textbf{sig} A \{ ds \} \textcircled{a} = \textcircled{a} \textbf{sig} A \{ ds \} \textcircled{a} \textcircled{a} \textbf{fact} \{ m A \} \textcircled{a}$$

where $m \in \{ \textit{none}, \textit{one}, \textit{some} \}$;

If we have signatures with abstract and multiplicity, we can always remove them with law 1 and law 2 before the refactoring .

Law 3 (Introduce generalization) [1]

$$\textcircled{a} \textbf{sig} A \{ ds \} \textcircled{a} = \begin{array}{|l} \textcircled{a} \textbf{abstract sig} U \{ \} \textcircled{a} \\ \textcircled{a} \textbf{sig} A \textbf{extends} U \{ ds \} \textcircled{a} \end{array}$$

→ no paragraphs and field declarations named U ;

← U does not appear in paragraphs and Field declarations.

Law 4 (Separate feature annotations)

$$\textcircled{a} p \textcircled{a} = \begin{array}{|l} \textcircled{a} \textcircled{k} p \textcircled{k} \textcircled{a} \\ \textcircled{a} \bullet k p \bullet k \textcircled{a} \end{array}$$

Law 5 (Separate feature annotations For Field)

$$\boxed{\begin{array}{l} \textcircled{a} \textcircled{k} \text{ sig } A \{ \text{ds}_0, \text{ds}_1 \dots \text{ds}_k \} \textcircled{k} \textcircled{a} \\ \textcircled{a} \textcircled{k} \text{ sig } A \{ \text{ds}'_0, \text{ds}'_1 \dots \text{ds}'_l \} \textcircled{k} \textcircled{a} \end{array}} = \boxed{\begin{array}{l} \textcircled{a} \text{ sig } A \{ \\ \textcircled{k} \text{ds}_0 \textcircled{k}, \textcircled{k} \text{ds}_1 \textcircled{k} \dots, \textcircled{k} \text{ds}_k \textcircled{k}, \\ \textcircled{k} \text{ds}'_0 \textcircled{k}, \textcircled{k} \text{ds}'_1 \textcircled{k} \dots, \textcircled{k} \text{ds}'_l \textcircled{k} \\ \} \textcircled{a} \end{array}}$$

Law 6 (Reorder) put features in the right order to merge

$$\boxed{\textcircled{a} \textcircled{k} \text{ p } \textcircled{k} \textcircled{a}} = \boxed{\textcircled{k} \textcircled{a} \text{ p } \textcircled{a} \textcircled{k}}$$

\leftrightarrow \textcircled{k} not appear in \textcircled{a}

our implementation does not care about the order of the feature

Law 7 (Combine Building Expressions)

$$\boxed{\begin{array}{l} \textcircled{a} \text{ r: set } T \textcircled{a}, \\ \textcircled{b} \text{ r: set } U \textcircled{b} \end{array}} = \boxed{\text{r: set } \textcircled{a} T \textcircled{a} \ \& \ \textcircled{b} U \textcircled{b}}$$

Laws for relation declarations: law7-10

Law 8 (Remove disj qualifier)

$$\boxed{\textcircled{a} \text{ disj } \text{r}', \text{r}'': \text{set } T \textcircled{a}} = \boxed{\begin{array}{l} \textcircled{a} \text{r}', \text{r}'': \text{set } T \textcircled{a} \\ \textcircled{a} \text{ fact } \{ \text{no } \text{r}' \ \&\& \ \text{r}'' \} \textcircled{a} \end{array}}$$

Law 9 (Separate Relation Declarations) [1]

$$\boxed{\textcircled{a} \text{r}', \text{r}'': \text{set } T \textcircled{a}} = \boxed{\textcircled{a} \text{r}': \text{set } T, \text{r}'': \text{set } T \textcircled{a}}$$

Law 10 (Remove Relation Qualifier) [1]

$$\boxed{\textcircled{a} \text{ sig } A \{ \text{r: } m T \} \textcircled{a}} = \boxed{\begin{array}{l} \textcircled{a} \text{ sig } A \{ \text{r: set } T \} \textcircled{a} \\ \textcircled{a} \text{ fact } \{ \text{all } a:A \mid m \text{ a.r } \} \textcircled{a} \end{array}}$$

also apply to binary expressions such as (some- \rightarrow one)

For expressions:

Law 11 ("and" expression)

$$\boxed{\textcircled{a} \text{R in } \phi \textcircled{a} \text{ and } \textcircled{b} \text{R in } \psi \textcircled{b}} = \boxed{\text{R in } \textcircled{a} \phi \textcircled{a} \ \& \ \textcircled{b} \psi \textcircled{b}}$$

References

[1] R. Gheyi. A refinement theory for alloy. 2007.