

Submitted in part fulfilment for the degree of BEng.

An App for Visualisation of Avalanche Hazard

Chongyang Shi

(to-be-completed)

Supervisor: Dr William Smith

Number of words = (to-be-completed), as counted by `wc -w`.
This includes the body of the report, and the title page, abstract and body of the report, but not bibliographies and appendices.

Abstract

This project produces a functional mobile application to visualise potential avalanche hazards along popular winter mountaineering routes within a 3D terrain reality, with a primary focus on Scottish mountains while providing excellent adaptability for other regions with appropriate data sources. Avalanche hazards were projected from a combination of professional avalanche forecasts and spatial analysis of mountain terrain models. Both the accuracy and the usability of the application were evaluated through various methods. The safety and ethical considerations on the application being put into real world use were also discussed.

Contents

1	Introduction	4
1.1	Overview of the project	4
1.2	Motivations behind the application	4
1.3	Stages of the project	5
1.4	Considerations and statements on ethics	6
1.5	Structure of this report	6
2	Literature Review	7
2.1	Snow avalanches	7
2.2	Avalanche forecasting	7
2.3	Modelling of avalanche hazard in GIS	9
2.4	Colour representation of risks	11
2.4.1	Saturation-based colouring	11
2.4.2	Hue-based colouring	12
2.5	Cost-based terrain pathfinding	12
2.6	Usability evaluations of a 3D model	13
3	Procurement and Processing of Data	14
4	Description of the Application	15
5	Evaluation and Testing of the Application	16
6	Conclusions	17

1 Introduction

1.1 Overview of the project

The purpose of this project is to produce a functional mobile application to visualise potential avalanche hazards along popular winter mountaineering routes within a 3D terrain reality, with a primary focus on Scottish mountains while providing excellent adaptability for other regions with appropriate data sources.

A model for projecting localised avalanche hazards based on carefully sourced and processed avalanche forecasts [1] and terrain model data [2] was produced by the project. The accuracy of the model has been evaluated against past avalanche records [3, pp. 143-151][4]. Usability and effectiveness of the application guiding the user away from hazardous locations were evaluated through experiments and test uses conducted with experienced mountaineers.

The project incorporated tools and techniques from various aspects of Computer Science, including software engineering, geographic information system (GIS) modelling, human-computer interaction, computer graphics and algorithms. Many of these tools and techniques are associated with current research in these areas.

1.2 Motivations behind the application

As a front-runner of digital avalanche forecasts, the Scottish Avalanche Information Service (SAIS) [1] have been providing frequent and reliable winter avalanche forecasts for decades in Scotland.

In addition to written observations on conditions of the snowpack and weather, a typical SAIS avalanche forecast also includes a compass rose, providing avalanche risk levels on the scale of 1 to 5 for slopes of different aspects above and below a transition threshold altitude, shown in Figure 1.1. However, while this compass rose provides a comprehensive overview on avalanche risks across the forecast region, it is not straightforward to interpret, as the user will need to work out the surface aspects and altitudes along their route, and mentally infer the risk levels of different locations along their route. This is a very complex task, and prone to errors as risk levels could vary sharply between neighbouring aspects and altitudes, as shown in Figure 1.1.

Therefore, the primary purpose of this project is to vastly simplify this process, by generating a coloured image based on the altitude and surface aspects at each point (as determined by a terrain raster model), which is then laid on top of a computer-generated terrain model in the 3D terrain viewer. Hence the information supplied by the compass rose can be visualised in the most straightforward way, allowing the user to freely navigate the 3D model and observe the hazard levels at each location along their route. The avalanche hazard of the same area mapped in Figure 1.1 is visualised as shown in Figure 1.2.

In later stages of the project, we also seek to improve hazard representation through constructing a custom risk model based on information from the compass rose and terrain spatial

data; and to improve the functionalities of the application by adding in features such as pathfinding.

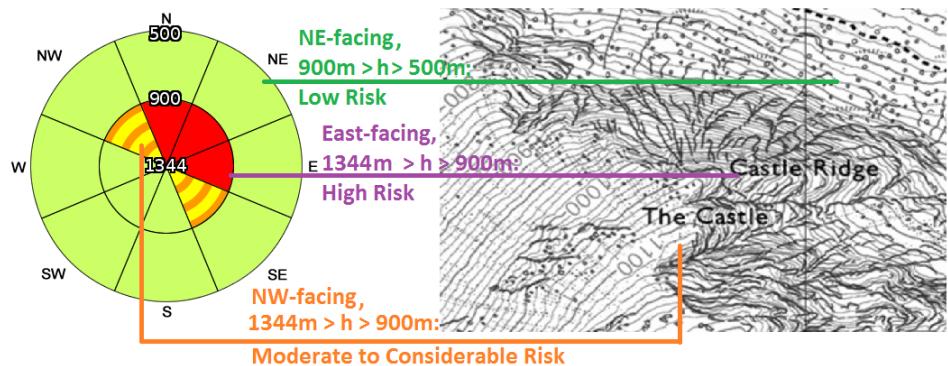


Figure 1.1: An example compass rose produced by the SAIS on January 6, 2016 for Lochaber (left), showing a steep transition of risk levels; and an example manual inference of risk levels based on the compass rose and contour lines near Ben Nevis, Lochaber (right). [5]

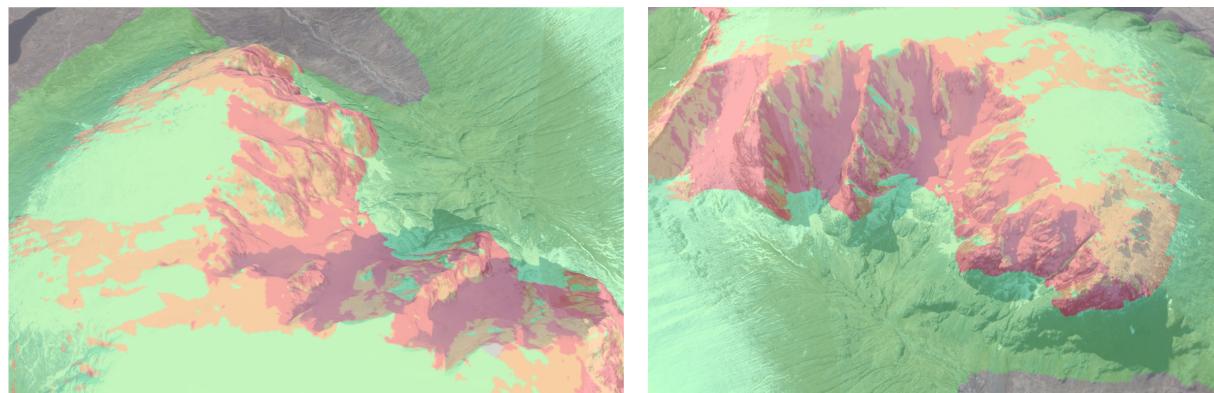


Figure 1.2: The avalanche hazard visualisation of the same area mapped in Figure 1.1, generated in the 3D terrain viewer by the initial stage product using the same avalanche forecast. The same slope is viewed from two different angles.

1.3 Stages of the project

The course of the project was divided into four development and evaluation stages, in order to effectively track and manage the workload. As the product from each stage is able to function independently of work done in other stages, risks from unforeseen difficulties encountered in research and development can be effectively mitigated. The four stages are described as followed:

Stage 1 - Basic Functionalities: The aim of this stage was to select an appropriate application framework and libraries to produce a basic but functional application – a 3D terrain viewer with a hazard map overlay, the data for which would be derived solely from forecasts by the Scottish Avalanche Information Service [1]. The WebGL framework Cesium [6] was chosen as the foundation for front-end developments, while Python was chosen to be used to develop the backend, and to interface other systems such as GIS processors with its vast range of interfacing libraries.

1 Introduction

Stage 2 - Improved Spatial Analysis and Evaluation: This stage of the project expands the data source for generating the hazard map overlay by performing surface fitting and spatial analysis on the terrain model data [2], in order to make the hazards more localised, and to better reflect the hazard posed by unique terrain features such as concave slopes. MATLAB [7] was used to perform the computations for these purposes. Evaluations on the localised hazard map against avalanche records were also conducted at this stage, with a focus on the avalanche “blackspots” of Scottish mountains.

Stage 3 - Pathfinding and Risk Calculator: With a localised hazard map obtained in Stage 2, this stage was focused on developing a pathfinding tool for the front end application, allowing the user to plot a potential hiking path with a configurable avalanche risk level. Techniques such as A* path finding [8] were utilised to develop this functionality.

Stage 4 - Usability Testing: The final stage of the project focus on the human-computer interaction aspects of the application. Experienced mountaineers were consulted and invited to test use the application to provide feedbacks on usability, as well as the effectiveness of the application guiding them away from avalanches that would have occurred in real use. Some improvements were made based on the feedbacks.

1.4 Considerations and statements on ethics

The application was designed as a tool to improve winter mountaineering safety, therefore evidently the foremost consideration on ethics regarding the accuracy and robustness of avalanche hazards projected by the application. If a location with imminent avalanche threat is reported as safe by the application, a user relying on the guidance of this application could be placed in serious danger; conversely, if the application indicate avalanche warnings to users at a location where an avalanche is unlikely to occur, undue anxiety could be caused.

Due to the constraints placed on this project, it is difficult to conduct an extensive peer review process to examine the accuracy of hazard projections. And while most open source libraries utilised during the development process have been widely-used and well-tested, software errors may still occur and affect the safety assurance of the product. Furthermore, the lack of a known commercial or academic product with comparable functionalities eliminates the possibilities of cross-testing the software product.

As a result, while the application is functional and shown promise during our own evaluations, it is not considered as a product ready for real-life use – a warning of which is displayed when a user initially accesses the application.

1.5 Structure of this report

A literature review is conducted in Chapter 2 over existing research and developments in the various aspects of Computer Science involved in this project. The procurement and processing of both avalanche forecast and topographical data used across all stages of the project are discussed in Chapter 3. Chapter 4 describes in detail the features and internal architectures of the application, as well as its development process. This is followed by Chapter 5, which describes the evaluation and testing conducted on the application and the quality of its data, mainly conducted during **Stage 4**. Finally, Chapter 6 concludes the report and discusses the potential uses and future developments of the application.

2 Literature Review

As an application designed to improve the usability of snow avalanche forecasts, it is necessary to first consider and evaluate past research and efforts made to understand and predict avalanches. While the term avalanche can be applied to various types of moving substances, such as rock and mud [9, p. 1], only snow avalanches are studied by this project.

2.1 Snow avalanches

Accumulated snow covers generally are not stable structures – snow found in avalanches are usually 80s% air, and cover structures gradually deform as environment temperature approaches the melting point of snow [10, p. 16]. This instability allows avalanches to occur easily.

Snow avalanches occur when large masses of snow or ice move rapidly down a mountainside or over a precipice, often triggered from the snow cover [9, p. 1]. Avalanches can either be triggered naturally due to combinations of certain geographical [9, p. 17] and meteorological [9, p. 23] conditions, or triggered by human activities nearby [11]. Often the latter is constructive to the former when an avalanche is triggered [10, p. 17][3, p .48].

McClung and Schaerer [10, p. 73] classified snow avalanches into two general types: loose snow avalanches, which usually involves surface snow and starts from a single area of the slope; and slab avalanches which are due to failures in the snow cover, resulting in blocks of snow to fall down the slope destructively. This classification is in agreement with most schemes, such as the avalanche classification by the UNESCO [12], which also diversifies the classification by types of originating zones, paths and deposition zones. The diversified classification has been further improved by more recent researches [9].

Regardless of type and triggering source, avalanches are often deadly to human present nearby, especially when travelling outside areas with built-up defense [9], as it often occurs to mountaineers. During the 45 years leading up to 1999, a total of 440 fatalities from avalanche incidents were recorded in the United States [13]; while in the UK, avalanches in Scottish mountains alone claimed at least 73 lives during a similar time period [3].

With a prosperous winter sport industry bringing millions to mountains and resorts every year[14], accurate forecasting of avalanches is becoming increasingly critical.

2.2 Avalanche forecasting

Avalanche forecasting is defined as predictions of current and future snow instability in space and time relative to a given triggering level for avalanche initiation [15, p. 131]. When applied, the main concerns of such predictions are of risk to humans or property.

A conventionally approach to avalanche forecasting involves extensive field observations and testings of the snow cover by experienced forecasters and mountain guides, cross-

2 Literature Review

referencing of historic meteorological and avalanche records, and utilisation of statistical and information theory methods on data collected to reduce decision uncertainties, as summarised by LaChapelle [16] in 1980. This is still very similar to the approach the Scottish Avalanche Information Service (SAIS) use today [17, p. 5]. In this style of approach, final decisions on hazard levels are heavily reliant on the experience and judgement of the experienced forecasters. LaChapelle noted [16, p. 76] that while inaccuracies do occur in forecasters' decisions, complete failures are rare. McClung [10] further analysed the influence of human perceptions in avalanche forecasting, and gave a formalised decision-making process to eliminate biases and improve accuracy.

While human decision-making still plays a dominant role in forecasting avalanche hazard levels, computational models have been developed to improve data analysis and to provide supplementary opinions through machine learning methods, backed by a vast increase in accessible computing power, as McClung [18] has explored as early as in 1994. Numerous models have since been developed, with computations performed on different types of data.

SNOWPACK, a snow profile comparison method was first published by Lehning *et al.* [19] in 2001. The method attempts to establish a numerical profile of snow cover conditions based on various measured properties of the cover, such as the size and type of snow grains, temperature and density of the environments. A agreement score could then be established by comparing the numerical profile with an observed profile in the field, with high agreement scores reached by the experiments, indicating that the numerical profile would be suitable for use in avalanche forecasts.

However, attempts to apply SNOWPACK to other regions with different snow conditions have identified weaknesses in the assumptions made in the model, which was originally developed for the Swiss Alps. A notable attempt was made by Hirashima *et al.* [20] from 2005 to 2006 in Tsunan, Japan. While numerical profiles computed were in reasonable agreement with the observed snow profiles in Tsunan, it was found that the stability index estimators embedded in the model was not suitable for the shear strength Japanese snow, and an alternative method for calculating the index had to be adopted. This suggests adaptation of SNOWPACK to a new region may require appropriate changes to the model based on local snow conditions.

While SNOWPACK was developed as a specialised method for analysis of snow covers, more generalised models such as the Nearest Neighbours (NN) method have also been developed. The NN model was initially developed by Buser [21] in 1983, which has been improved and supplemented by various studies, such as Purves *et al.* in 2003, and Singh and Ganju [22] [23] since 2004. The NN method applies a machine learning approach on historic avalanche and meteorological records, as well as spatial data to estimate the likelihood of an avalanche under the current conditions of a location. As the NN method has difficulties with high dimensional data, an alternative method based on Support Vector Machines (SVMs) have been proposed and developed [19] [24].

The most notable application of the NN method is by the SAIS. Avalanche forecasts from the SAIS partially dependent on the NN method achieved a weighted accuracy of between 71% and 82% on visible winter days between 1988 and 2002 [25, p. 351]. With up to 205 avalanches reported by mountaineers during the winter season of 2015-2016 [1] (as partly shown in Figure 2.1), the SAIS plays a very significant role in saving lives from avalanches. Data from SAIS forecasts would also be a critical component in data sourcing and hazard modelling during this project, and is directly used to derive the hazard map overlay in **Stage 1** of the project.

In addition to analysis of snow and terrain conditions and past avalanche records, studies of

2.3 Modelling of avalanche hazard in GIS

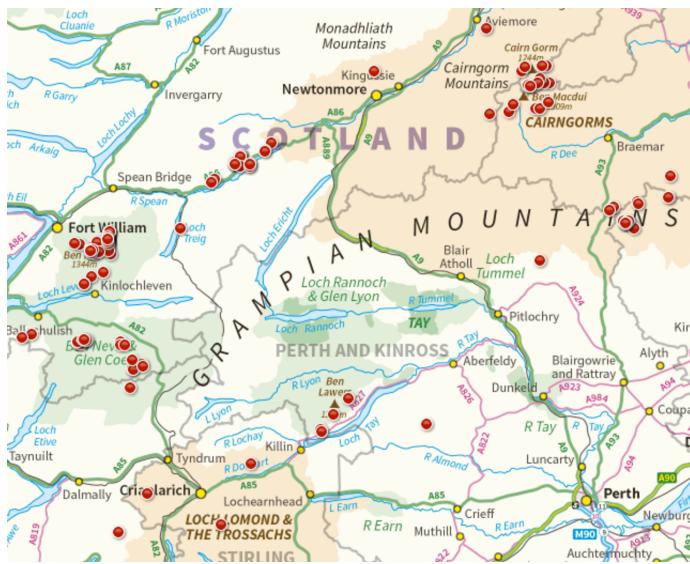


Figure 2.1: User-reported avalanches in the Cairngorms and the Glencoe regions during winter sports season of 2015-2016, generated by the SAIS.[4]

vegetations in mountainous areas can also provide important information on recurrence of avalanches. Christophe *et al.* [26] developed a model based on observation of tree-rings. As avalanches affect the growth of trees and other vegetations on the mountain slopes, growth condition of trees would provide useful insight into the magnitude and frequency of past avalanches in the area. One downside of the model is its unsuitableness for direct use in temporal avalanche forecasts, as the formation of general vegetation conditions requires a long period of time. However, for the purpose of this project this model could potentially be used for establishing a static risk level for each point in the terrain, to be included in the overall risk model.

2.3 Modelling of avalanche hazard in GIS

In order to effectively store large amounts of geographical data for computing hazard map overlays for the project, a geographic information system (GIS) [27] is the most suitable method of organising avalanche hazard data.

While a majority of implemented avalanche forecasting methods – such as those discussed in Section – provide a generalised risk level with respect to unique sets of environmental conditions, these generalised risk levels cannot be easily converted into localised hazards in a GIS, as these forecasting methods only operate on smaller subsets of parameters contributing to an avalanche. To evaluate the avalanche hazard of a specific location (e.g. Red Ben in Ben Nevis, Lochaber), it is necessary to develop a systematic method of calculating risk for each point in the region, taking into account of as many hazard parameters as possible. Computations of per-point risk will also provide the improved hazard map used in **Stage 2** of the project.

According to Bühler *et al.* [28], parameters influencing avalanche hazards can generally be placed in one of the three categories: (a) terrain topography features at each point in the modelled area; (b) meteorological data of the general area; and (c) characteristics of the snow cover in the area.

2 Literature Review

Terrain topography features, such as aspect and slope [29, pp. 17-18], convexity and concavity [30, p. 267], and roughness [31, p. 12] can be computed directly from a terrain height-map raster. For the main area of study in this project (Scotland), the government owned Ordnance Survey has mapped the entire terrain of the British Isles (excluding Republic of Ireland) into a raster with resolution of 5 meters [32]. The data is updated frequently, and has a root-mean-square error of 2.5 meters in mountainous area, which is sufficient for the need of this project. As terrain features outside urban areas are not subject to frequent change, once the aforementioned terrain features are computed, they do not need to be re-computed until the source terrain data updates.

Meteorological and snow profile data, on the other hand, are largely dependent on the current and recent weather conditions in the forecasting regions. Commonly examined parameters by past researches include temperature change, snow accumulation [33], humidity[34], and wind direction [35]; as well as snow profile parameters such as snow grain size and density (as analysed in the SNOWPACK model [19]). However, as most past researches relied on weather forecasts in the regions in which they were conducted, not all parameters they used are available in Scotland. Fortunately, each SAIS avalanche forecast is also accompanied by a snow profile, containing measured meteorological and snow conditions observed during the field work of that forecast [36].

A number of efforts have been made to produce GIS models of avalanche hazards based on some or all of the aforementioned hazard parameters.

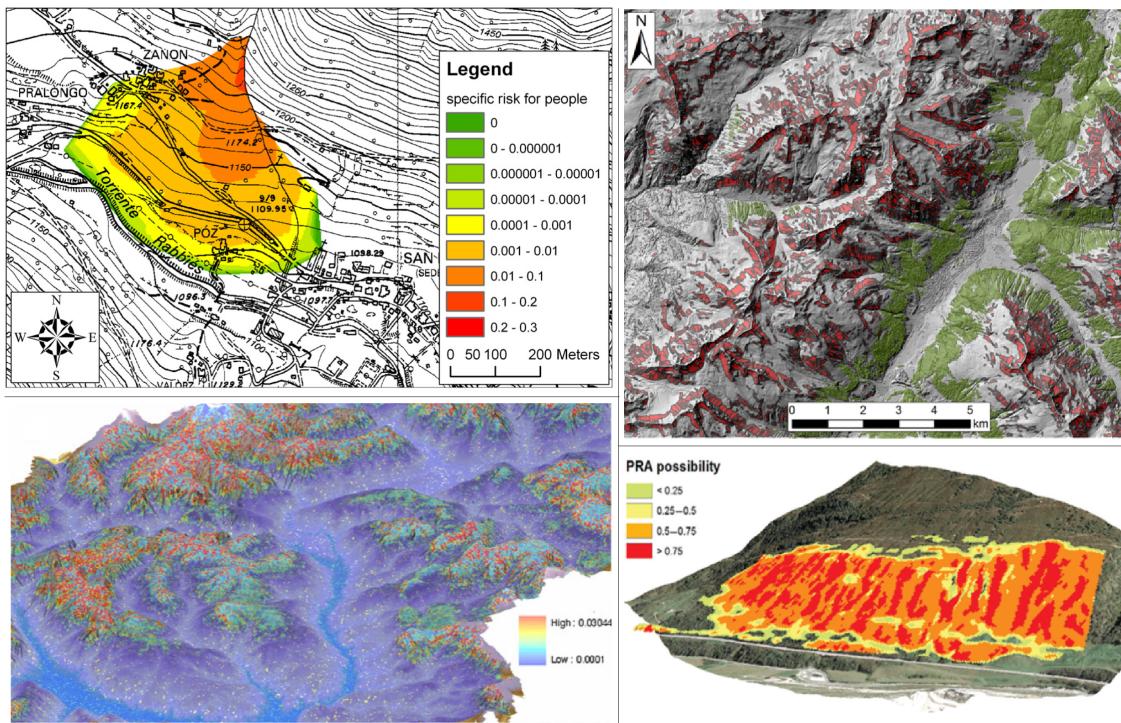


Figure 2.2: Hazard maps produced by prior efforts in visualising avalanche hazards: flow model and snow profile analysis by Cappabianca *et al.* (top-left) [37]; data-driven analysis by Pistocchi and Notarnicola (bottom-left) [38]; terrain topography analysis by Bühler *et al.* (top-right) [28]; and terrain topography and wind shelter analysis by Veitinger *et al.* (bottom-right) [39].

Grêt-Regamey and Straub [40] utilised a Bayesian network to study the relation between snow accumulation and flow model of avalanches, and visualised [41] risks of avalanche

impacts in an area with the trained network. A more comprehensive risk model was used by Cappabianca *et al.* (top-left) [37] to produce a similar visualisation, as shown in Figure 2.2 (top-left).

However, neither of the two studies above considered the full topography features of the triggering zones (e.g. convexity and terrain roughness), which significantly affect the probability of release, as shown by Ghinoi and Chung [42]. Bühler *et al.* [28] devised a considerably accurate release zone identification algorithm based on terrain topography features alone, as visualised in Figure 2.2 (top-right).

More recent researches have also included meteorological analysis in the risk model. A notable example is by Veitinger *et al.* [39] in 2016. In addition to topography features such as slope and roughness, wind sheltering effects of terrain was computed based on the direction of wind, and included in the fuzzy logic computations of per-point risk. The algorithm's visualisation of avalanche release risk on a slope where a real avalanche took place is shown in Figure 2.2 (bottom-right). While evaluations showed that little accuracy improvement was achieved in the general case due to potential mapping errors, the algorithm was significantly more accurate than its predecessor in locating frequent avalanche release areas.

Most hazard map visualisations of the aforementioned studies are in 2D only and are static once computed, providing no interactive capabilities. To our knowledge, only Pistocchi and Notarnicola [38] constructed a static 3D model with an avalanche risk overlay, as shown in Figure 2.2 (bottom-left), similar to the 3D model constructed in this project. The interactive 3D model proposed by this project would also provide capabilities of displaying additional image layers and map features (such as a planned route) "on the fly", and the ability to observe from different angles and distances.

2.4 Colour representation of risks

While a realistic imagery of the surface can be produced in the 3D viewer by covering with corresponding aerial photographs, an appropriate colour representation scheme needs to be chosen for the hazard map overlay, which visualises the risk level at each point in the terrain model. Considerations need to be made regarding the choice of the colouring scheme, as well as in what form the colours are displayed. While all colouring schemes should have an unique representation for each distinct level of risk, how well an average user of the application perceives the colouring scheme is a usability issue. The two main colouring schemes proposed by existing researches and some attempts of applying them will be discussed in this section.

2.4.1 Saturation-based colouring

This is the simplest colour representation scheme. A single colour determined by a hue value is chosen, and in the context of visualising hazards the colour of choice is often red [43] [44]. The saturation of this colour at different points in the visualisation would vary, dependent on the level of risk at that point. As summarised by Cheong *et al.* [44, Ch. 2], there have been conflicting conclusions from researches on the effectiveness of saturation-based risk visualisations, when compared with visualisations using other schemes. Experiments also conducted by Cheong *et al.* showed that the accuracy of user decisions under this scheme is good while multitasking, but otherwise not as good.

2 Literature Review

While the risk mapped by the visualisation of Cheong *et al.* is wildfire hazard, a known visualisation of avalanche hazard under this saturation-based scheme was by Bühler *et al.* [28] as discussed in Section 2.3, however no human-computer interaction (HCI) evaluation was conducted. This scheme is also used by Spachinger *et al.* [45] for flood risks.

2.4.2 Hue-based colouring

This colour representation scheme is similar to the saturation-based scheme, but uses different hues of colours (e.g. yellow and red) for different levels of risk in the visualisation. The European Avalanche Hazard Scale [9, pp. 93-94] – also used by the SAIS in the UK – applies such a hue-based scheme, as shown in Figure 2.3. This scheme is also used in visualisation of avalanche hazards by most studies discussed in Section 2.3, as shown in Figure 2.2.

Low Risk	Moderate Risk	Considerable Risk	High Risk	Very High Risk
----------	---------------	-------------------	-----------	----------------

Figure 2.3: Colouring scheme reconstructed from the European Avalanche Hazard Scale, used by the SAIS [46].

However, some studies have considered the hue-based scheme used in Figure 2.3 to be less effective, most notably by Conger [47], which found that using green to represent low risk deviates from the common perception of green being a safe-indicating colour, which is not always the case in avalanche forecasting. Orange was also found to be inappropriate in association with a risk, and more difficult to print cartographically [47, Ch. 4.2]. Therefore Conger has suggested that the risk scale should be rescaled into four, in order to abolish the use of orange.

HCI evaluations conducted by Cheong *et al.* [44, Ch. 5] concluded that while a hue-based scheme is often most preferred by users, its user decision accuracy is not the best among different colour representation schemes.

Other variations of applying hue-based colouring include an attempt by Gavaldà and Moner [48] to represent mountaineering route hazards with red-yellow-green traffic signals; and a method developed by Saito *et al.* [49], using two tones of hue to represent hazard at each level, which unfortunately is unsuitable for the steep transitions of risk frequently occurring in avalanche hazard maps. Conger [47, Ch. 5.2] also suggested a method of partially filling hazard areas with triangles, which are coloured according to the colouring scheme. This however would be difficult to implement in practice, due to the size variations of neighbouring points with the same risk level.

2.5 Cost-based terrain pathfinding

On completion of per-point risk computations in **Stage 2** of the project, **Stage 3** focuses on implementing the extended functionality of terrain pathfinding, which will involve adapting existing applications of pathfinding algorithms for use under the complicated conditions of backcountry terrain.

As according to Moore *et al.* [50, pp. 4-5], the terrain height-map raster from Ordnance Survey, as discussed in 2.3 is essentially a square-grid network model of the real terrain. The network model was constructed from sampling the real elevation data at a resolution of 5 meters, which minimises the risk of missing abrupt changes in elevation. Pathfinding can then be conducted on the model. The most widely implemented algorithm for this purpose is the A*

2.6 Usability evaluations of a 3D model

Search Algorithm [51], utilising heuristic analysis to guide a graph search based on Dijkstra's Algorithm [52].

A* is most widely implemented in the development of pathfinder artificial intelligences in computer games [8]. Since its introduction, a significant number of studies have been conducted to improve the performance of A* search, including iterative-deepening A* (IDA) [53] which requires less memory at runtime; hierarchical path-finding A* (HPA) [31] which utilises hierarchical abstraction on large data grids to produce a near-optimal solution at very high performance; and navigational mesh (NavMesh) [54] which minimises the structure representation of data to reduce memory use and computation time.

When adapting A* or its aforementioned variants for computing a path in the terrain, taking into account of the avalanche risk level at each point in the terrain raster, both the distance and the risk levels need to be considered by the heuristic function of A*. Due to the nature of the uneven terrain, the proper walking distances between points can be estimated by Naismith's Rule and its variants [55]. To represent the points as a data structure, Yap [56] has suggested using a tiled hex grid to organise neighbouring points for performance optimisation, which we can then analyse with a hierarchical search algorithm such as HPA [31].

2.6 Usability evaluations of a 3D model

3 Procurement and Processing of Data

4 Description of the Application

5 Evaluation and Testing of the Application

6 Conclusions

Bibliography

- [1] "Scottish Avalanche Information Service.". [Online] <http://www.sais.gov.uk/> [Accessed Sep 27, 2016].
- [2] Ordnance Survey (GB), "OS Terrain 5 (ASC geospatial data), Scale 1:10000." EDINA Digimap Ordnance Survey Service, July 2016. [Online] <http://digimap.edina.ac.uk/> [Accessed Oct 23, 2016].
- [3] B. Barton and B. Wright, *A Chance in a Million?: Scottish Avalanches*. Scottish Mountaining Trust, 2000.
- [4] Scottish Avalanche Information Service, "Avalanche map.". [Online] http://www.sais.gov.uk/avalanche_map/ [Accessed Nov 16, 2016].
- [5] Scottish Avalanche Information Service, "Avalanche Report for Lochaber, Issued 06/01/2016," January 2016. [Online] http://www.sais.gov.uk/lochaber/?report_id=4753 [Accessed Nov 18, 2016].
- [6] Cesium Team, "Cesium API Reference.". [Online] <http://cesiumjs.org/> [Accessed Nov 16, 2016].
- [7] The MathWorks, Inc., *MATLAB Primer*. Natick, MA, US, R2016b ed., September 2016.
- [8] X. Cui and H. Shi, "A*-based pathfinding in modern computer games," *International Journal of Computer Science and Network Security*, vol. 11, no. 1, pp. 125–130, 2011.
- [9] F. Rudolf-Miklau *et al.*, *The Technical Avalanche Protection Handbook*. Ernst & Sohn, 2015.
- [10] D. McClung and P. A. Schaefer, *The Avalanche Handbook*. The Mountaineers Books, 2006.
- [11] J. Schweizer and M. Lütschg, "Characteristics of human-triggered avalanches," *Cold Regions Science and Technology*, vol. 33, no. 2, pp. 147–162, 2001.
- [12] UN Education, Scientific and Cultural Organization, *Avalanche atlas: Illustrated international avalanche classification*. the United Nations, 1981.
- [13] C. E. Page *et al.*, "Avalanche deaths in the United States: a 45-year analysis," *Wilderness & Environmental Medicine*, vol. 10, no. 3, pp. 146 – 151, 1999. doi:[http://dx.doi.org/10.1580/1080-6032\(1999\)010\[0146:ADITUS\]2.3.CO;2](http://dx.doi.org/10.1580/1080-6032(1999)010[0146:ADITUS]2.3.CO;2).
- [14] S. Hudson, *Sport and adventure tourism*. Routledge, 2003.
- [15] D. M. McClung, "The elements of applied avalanche forecasting, part ii: The physical issues and the rules of applied avalanche forecasting," *Natural Hazards*, vol. 26, no. 2, pp. 131–146, 2002. doi:[10.1023/A:1015604600361](https://doi.org/10.1023/A:1015604600361).
- [16] E. R. Lachapelle, "The fundamental processes in conventional avalanche forecasting," *Journal of Glaciology*, vol. 26, pp. 75–84, 1980.
- [17] Scottish Avalanche Information Service, "Scottish avalanche information service report for winter 2014/15," January 2016. [Online] http://www.sais.gov.uk/wp-content/uploads/2016/01/SAIS-Winter-Report-2014_15.pdf [Accessed Nov 16, 2016].
- [18] D. M. McClung, "Computer assisted avalanche forecasting," in *Stochastic and Statistical Methods in Hydrology and Environmental Engineering*, pp. 347–358, Springer, 1994.
- [19] M. Lehning *et al.*, "An objective snow profile comparison method and its application to SNOWPACK," *Cold Regions Science and Technology*, vol. 33, no. 2–3, pp. 253 – 261, 2001.
- [20] H. Hirashima *et al.*, "Avalanche forecasting in a heavy snowfall area using the snow model," *Cold Regions Science and Technology*, vol. 51, no. 2–3, pp. 191 – 203, 2008. International Snow Science Workshop (ISSW) 2006. doi:<http://dx.doi.org/10.1016/j.coldregions.2007.05.013>.
- [21] O. Buser, "Avalanche forecast with the method of nearest neighbours: an interactive approach," *Cold Regions Science and Technology*, vol. 8, no. 2, pp. 155–163, 1983.
- [22] A. Singh and A. Ganju, "A supplement to nearest-neighbour method for avalanche forecasting," *Cold Regions Science and Technology*, vol. 39, no. 2–3, pp. 105 – 113, 2004.

Bibliography

- [23] A. Singh *et al.*, "Calibration of nearest neighbors model for avalanche forecasting," *Cold Regions Science and Technology*, vol. 109, pp. 33 – 42, 2015. doi:<http://dx.doi.org/10.1016/j.coldregions.2014.09.009>.
- [24] A. Pozdnoukhov *et al.*, "Spatio-temporal avalanche forecasting with Support Vector Machines," *Natural Hazards and Earth System Sciences*, vol. 11, no. 2, pp. 367–382, 2011.
- [25] R. Purves *et al.*, "Nearest neighbours for avalanche forecasting in scotland—development, verification and optimisation of a model," *Cold Regions Science and Technology*, vol. 37, no. 3, pp. 343 – 355, 2003. ISSW 2002: International Snow Science Workshop.
- [26] C. Christophe *et al.*, "Spatio-temporal reconstruction of snow avalanche activity using tree rings: Pierres Jeanne avalanche talus, Massif de l'Oisans, France," *CATENA*, vol. 83, no. 2–3, pp. 107 – 118, 2010.
- [27] K. C. Clarke, "Advances in geographic information systems," *Computers, environment and urban systems*, vol. 10, no. 3-4, pp. 175–184, 1986.
- [28] Y. Bühler *et al.*, "Automated identification of potential snow avalanche release areas based on digital elevation models," *Natural Hazards and Earth System Sciences*, vol. 13, no. 5, p. 1321, 2013.
- [29] B. K. P. Horn, "Hill shading and the reflectance map," *Proceedings of the IEEE*, vol. 69, pp. 14–47, Jan 1981. doi:[10.1109/PROC.1981.11918](https://doi.org/10.1109/PROC.1981.11918).
- [30] M. J. De Smith *et al.*, *Geospatial analysis: a comprehensive guide to principles, techniques and software tools*. Troubador Publishing Ltd, 2007.
- [31] M. F. Wilson *et al.*, "Multiscale terrain analysis of multibeam bathymetry data for habitat mapping on the continental slope," *Marine Geodesy*, vol. 30, no. 1-2, pp. 3–35, 2007.
- [32] Ordnance Survey (GB), *OS Terrain 5: User guide and technical specification*, v1.1 ed., 07 2013.
- [33] R. Ward, "Avalanche prediction in scotland: II. development of a predictive model," *Applied Geography*, vol. 4, no. 2, pp. 109 – 133, 1984.
- [34] Y. Durand *et al.*, "A meteorological estimation of relevant parameters for snow models," *Annals of glaciology*, vol. 18, no. 1, pp. 65–71, 1993.
- [35] J. Veitinger *et al.*, "Slab avalanche release area estimation: a new GIS tool," in *Proceedings of International Snow Science Workshop 2014, Banff (Canada)*, 2014.
- [36] Scottish Avalanche Information Service, *Interpreting Snow Profiles*, 2014.
- [37] F. Cappabianca *et al.*, "Snow avalanche risk assessment and mapping: A new method based on a combination of statistical analysis, avalanche dynamics simulation and empirically-based vulnerability relations integrated in a GIS platform," *Cold Regions Science and Technology*, vol. 54, no. 3, pp. 193 – 205, 2008. Snow avalanche formation and dynamics.
- [38] A. Pistocchi and C. Notarnicola, "Data-driven mapping of avalanche release areas: a case study in South Tyrol, Italy," *Natural Hazards*, vol. 65, no. 3, pp. 1313–1330, 2013.
- [39] J. Veitinger *et al.*, "Potential slab avalanche release area identification from estimated winter terrain: a multi-scale, fuzzy logic approach," *Natural Hazards and Earth System Sciences*, vol. 16, no. 10, p. 2211, 2016.
- [40] D. Straub and A. Grêt-Regamey, "A bayesian probabilistic framework for avalanche modelling based on observations," *Cold Regions Science and Technology*, vol. 46, no. 3, pp. 192 – 203, 2006.
- [41] A. Grêt-Regamey and D. Straub, "Spatially explicit avalanche risk assessment linking bayesian networks to a gis," *Natural Hazards and Earth System Science*, vol. 6, no. 6, pp. 911–926, 2006.
- [42] A. Ghinoi and C.-J. Chung, "STARTER: a statistical GIS-based model for the prediction of snow avalanche susceptibility using terrain features—application to Alta Val Badia, Italian Dolomites," *Geomorphology*, vol. 66, no. 1–4, pp. 305 – 325, 2005. Geomorphological hazard and human impact in mountain environmentsRelations between Man and the Mountain Environment in terms of Geomorphological Hazards and Human Impact in Europe.
- [43] J. C. Aerts *et al.*, "Testing popular visualization techniques for representing model uncertainty," *Cartography and Geographic Information Science*, vol. 30, no. 3, pp. 249–261, 2003.
- [44] L. Cheong *et al.*, "Evaluating the impact of visualization of wildfire hazard upon decision-making under uncertainty," *International Journal of Geographical Information Science*, vol. 30, no. 7, pp. 1377–1404, 2016.

Bibliography

- [45] K. Spachinger *et al.*, "Flood risk and flood hazard maps—visualisation of hydrological risks," in *IOP Conference Series: Earth and Environmental Science*, vol. 4, p. 012043, IOP Publishing, 2008.
- [46] Scottish Avalanche Information Service, *Interpreting Avalanche Reports*, Nov. 2014.
- [47] S. Conger, "A review of colour cartography in avalanche danger visualization," in *Proceedings of the International Snow Science Workshop, Jackson Hole, Wyoming, USA*, vol. 477482, 2004.
- [48] J. Gavaldà and I. Moner, "Mountaineeroriented local avalanche forecasting system in a graphical format in the aran valley (eastern pyrenees)," in *International Snow Science Workshop, Whistler, Canada*, 2008.
- [49] T. Saito *et al.*, "Two-tone pseudo coloring: Compact visualization for one-dimensional data," in *IEEE Symposium on Information Visualization, 2005*, pp. 173–180, IEEE, 2005.
- [50] I. D. Moore *et al.*, "Digital terrain modelling: a review of hydrological, geomorphological, and biological applications," *Hydrological processes*, vol. 5, no. 1, pp. 3–30, 1991.
- [51] P. E. Hart *et al.*, "A formal basis for the heuristic determination of minimum cost paths," *IEEE Transactions on Systems Science and Cybernetics*, vol. 4, pp. 100–107, July 1968.
- [52] E. W. Dijkstra, "A note on two problems in connexion with graphs," *Numer. Math.*, vol. 1, pp. 269–271, Dec. 1959.
- [53] R. E. Korf, "Depth-first iterative-deepening: An optimal admissible tree search," *Artificial intelligence*, vol. 27, no. 1, pp. 97–109, 1985.
- [54] P. Tozour and I. Austin, "Building a near-optimal navigation mesh," *AI game programming wisdom*, vol. 1, pp. 298–304, 2002.
- [55] Z. Magyari-Sáska and Š. Dombay, "Determining minimum hiking time using DEM," *Geographica Napocensis Anul*, vol. 82, no. 4, pp. 124–129, 2012.
- [56] M. Hemetsberger *et al.*, "Risk assessment of avalanches—a fuzzy GIS application," in *Proceedings of 5th International FLINS Conference, Republic of Singapore*, pp. 395–402, 2002.