

<Equations, parameters and initial values of the β -cell model>

1. General

<Unit>

time in ms

voltage in mV

current in pA

conductance in nS

capacitance in pF

concentration in mM

volume in fl

flux in mM ms⁻¹

J_{SERCA} or J_{rel} in amole ms⁻¹ (= fl mM ms⁻¹)

Thermodynamic constants

R ; 8.3143 (mV C mmol⁻¹ K⁻¹), Gas constant

T ; 273.15 + 37 (K), absolute temperature

F ; 96.4867 (C mmol⁻¹), Faraday const

Extracellular composition

$[\text{Na}^+]_o = 140$ mM, $[\text{K}^+]_o = 5.4$ mM, $[\text{Ca}^{2+}]_o = 2.6$ mM

Cell parameters

C_m ; 6.158 (pF), cell capacitance

vol_i ; 764 (fl), cell volume (cytosol)

vol_{ER} ; 280 (fl), ER volume

f_i ; 0.01, cytosolic Ca^{2+} buffer strength

f_{ER} ; 0.025, ER Ca^{2+} buffer strength

2. Calculation of membrane potential and internal ion concentrations

Membrane potential

$$\frac{dV_m}{dt} = \frac{-(I_{\text{tot}} + I_{\text{inject}})}{C_m} \quad (\text{S1})$$

$$I_{\text{tot}} = I_{\text{CaV}} + I_{\text{TRPM}} + I_{\text{SOC}} + I_{\text{bNSC}} + I_{\text{KDr}} + I_{\text{KCa(BK)}} + I_{\text{KCa(SK)}} + I_{\text{KATP}} + I_{\text{NaK}} + I_{\text{NaCa}} + I_{\text{PMCA}} \quad (\text{S})$$

2)

Internal ion concentrations

$$\frac{d[\text{Na}^+]_i}{dt} = \frac{-I_{\text{CaV,Na}} - I_{\text{TRPM,Na}} - I_{\text{SOC,Na}} - I_{\text{bNSC,Na}} - 3 \cdot I_{\text{NaK}} - 3 \cdot I_{\text{NaCa}} + I_{\text{PMCA}}}{\text{vol}_i \cdot F} \quad (\text{S3})$$

(Assumption; the H^+ flux via PMCA is immediately converted to Na^+ flux through Na/H exchange)

$$\frac{d[\text{K}^+]_i}{dt} = \frac{-I_{\text{KDr}} - I_{\text{KCa(BK)}} - I_{\text{KCa(SK)}} - I_{\text{KATP}} - I_{\text{CaV,K}} - I_{\text{TRPM,K}} - I_{\text{SOC,K}} - I_{\text{bNSC,K}} + 2 \cdot I_{\text{NaK}} - I_{\text{inject}}}{\text{vol}_i \cdot F} \quad (\text{S4})$$

$$\frac{d[\text{Ca}^{2+}]_i}{dt} = \frac{f_i}{\text{vol}_i} \cdot \left(\frac{-I_{\text{CaV,Ca}} - I_{\text{SOC,Ca}} + 2 \cdot I_{\text{NaCa}} - 2 \cdot I_{\text{PMCA}}}{2 \cdot F} - J_{\text{SERCA}} + J_{\text{rel}} \right) \quad (\text{S5})$$

$$\frac{d[\text{Ca}^{2+}]_{\text{ER}}}{dt} = \frac{f_{\text{ER}}}{\text{vol}_{\text{ER}}} \cdot (J_{\text{SERCA}} - J_{\text{rel}}) \quad (\text{S6})$$

Constant field equation and Nernst equation

$$\text{CF}_x = \frac{z_x \cdot F \cdot V_m}{R \cdot T} \cdot \frac{[\text{X}]_i - [\text{X}]_o \exp\left(-\frac{z_x \cdot F \cdot V_m}{R \cdot T}\right)}{1 - \exp\left(-\frac{z_x \cdot F \cdot V_m}{R \cdot T}\right)} \quad (\text{mM}) \quad (\text{S7})$$

$$E_x = \frac{R \cdot T}{z_x \cdot F} \ln \frac{[\text{X}]_o}{[\text{X}]_i} \quad (\text{mV}) \quad (\text{S8})$$

3. Channel currents

I_{CaV} : voltage-dependent Ca^{2+} current

P_{CaV} ; 48.9 (pA mM^{-1}), converting factor of I_{CaV}

po_{CaV} ; open probability of the Ca^{2+} channel

d_{CaV} ; voltage-dependent activation gate of I_{CaV}

α_d, β_d ; (ms^{-1}), rate constants for d_{CaV}

U_{CaV} ; Ca^{2+} -dependent inactivation gate of I_{CaV}

α_U, β_U ; (ms^{-1}), rate constants for u_{CaV}

i_{Ca} ; (pA), amplitude of single channel current of I_{CaV}

f_{us} ; V-dependent ultra-slow inactivation gate of I_{CaV}

$\alpha_{\text{fus}}, \beta_{\text{fus}} ; (\text{ms}^{-1})$, rate constants for f_{us}

$$I_{\text{CaV}} = I_{\text{CaV,Ca}} + I_{\text{CaV,Na}} + I_{\text{CaV,K}} \quad (\text{S9})$$

$$I_{\text{CaV,Ca}} = P_{\text{CaV}} \cdot po_{\text{CaV}} \cdot CF_{\text{Ca}} \quad (\text{S10})$$

$$I_{\text{CaV,Na}} = 0.0000185 \cdot P_{\text{CaV}} \cdot po_{\text{CaV}} \cdot CF_{\text{Na}} \quad (\text{S11})$$

$$I_{\text{CaV,K}} = 0.000367 \cdot P_{\text{CaV}} \cdot po_{\text{CaV}} \cdot CF_{\text{K}} \quad (\text{S12})$$

$$po_{\text{CaV}} = d_{\text{CaV}}^2 \cdot U_{\text{CaV}} \cdot (0.4 + 0.6 \cdot f_{\text{us}}) \cdot \frac{1}{1 + \left(\frac{1.4}{[\text{ATP}]_i}\right)^3} \quad (\text{S13})$$

$$\frac{dd_{\text{CaV}}}{dt} = \alpha_d \cdot (1 - d_{\text{CaV}}) - \beta_d \cdot d_{\text{CaV}} \quad (\text{S14})$$

$$\alpha_d = \frac{1}{0.9344 \cdot \exp\left(-\frac{V_m}{50}\right) + 0.09045 \cdot \exp\left(-\frac{V_m}{600}\right)} \quad (\text{S15})$$

$$\beta_d = \frac{1}{4.2678 \cdot \exp\left(\frac{V_m}{12}\right) + 1.1265 \cdot \exp\left(\frac{V_m}{30}\right)} \quad (\text{S16})$$

$$\frac{dU_{\text{CaV}}}{dt} = \alpha_u \cdot (1 - U_{\text{CaV}}) - \beta_u \cdot U_{\text{CaV}} \quad (\text{S17})$$

$$\alpha_u = 0.0084$$

$$\beta_u = 0.2318 \cdot (-1.15 \cdot i_{\text{Ca}} \cdot d_{\text{CaV}}^2 + [\text{Ca}^{2+}]_i) \quad (\text{S18})$$

$$i_{\text{Ca}} = 0.0676 \cdot CF_{\text{Ca}} \quad (\text{S19})$$

$$\frac{df_{\text{us}}}{dt} = \alpha_{\text{fus}} \cdot (1 - f_{\text{us}}) - \beta_{\text{fus}} \cdot f_{\text{us}} \quad (\text{S20})$$

$$\alpha_{\text{fus}} = \frac{1}{75000 \cdot \exp\left(\frac{V_m}{34}\right)} \quad (\text{S21})$$

$$\beta_{\text{fus}} = \frac{1}{5000 \exp(-\frac{V_m}{19}) + 500 \exp(-\frac{V_m}{100})} \quad (\text{S22})$$

I_{KDr} ; deleyed rectifier K^+ current

P_{KDr} ; 2.1 (pA mM⁻¹), converting factor of I_{KDr}

po_{KDr} ; open probability of I_{KDr} channel

r_{KDr} ; voltage-dependent activation gate of I_{KDr}

q_{KDr} ; voltage-dependent inactivation gate of I_{KDr}

α_r, β_r ; (ms⁻¹), rate constants of r_{KDr}

α_q, β_q ; (ms⁻¹), rate constants of q_{KDr}

$$I_{\text{KDr}} = P_{\text{KDr}} \cdot po_{\text{KDr}} \cdot CF_K \quad (\text{S23})$$

$$po_{\text{KDr}} = r_{\text{KDr}}^2 \cdot (0.6 \cdot q_{\text{KDr}} + 0.4) \quad (\text{S24})$$

$$\frac{dr_{\text{KDr}}}{dt} = \alpha_r \cdot (1 - r_{\text{KDr}}) - \beta_r \cdot r_{\text{KDr}} \quad (\text{S25})$$

$$\alpha_r = \frac{1}{33.07 \cdot \exp(\frac{V_m}{-8}) + 0.937 \cdot \exp(\frac{V_m}{-100})} \quad (\text{S26})$$

$$\beta_r = \frac{1}{22.73 \cdot \exp(\frac{V_m}{100})} \quad (\text{S27})$$

$$\frac{dq_{\text{KDr}}}{dt} = \alpha_q \cdot (1 - q_{\text{KDr}}) - \beta_q \cdot q_{\text{KDr}} \quad (\text{S28})$$

$$\alpha_q = \frac{1}{800} \quad (\text{S29})$$

$$\beta_q = \frac{1}{1000 \cdot \exp(-\frac{V_m}{8}) + 100 \cdot \exp(-\frac{V_m}{100})} \quad (\text{S30})$$

$I_{\text{KCa(BK)}}$; V- and $[\text{Ca}^{2+}]_i$ -dependent transient outward K^+ current

$G_{\text{KCa(BK)}}$; 2.13 (pA mV⁻¹), conductance of $I_{\text{KCa(BK)}}$

$m_{\text{KCa(BK)}}$; activation gate for $I_{\text{KCa(BK)}}$

$po_{\text{KCa(BK)}}$; open probability of $I_{\text{KCa(BK)}}$ channel

α_m, β_m ; (ms⁻¹), rate constants for $m_{\text{KCa(BK)}}$

$h_{\text{KCa(BK)}} ; \text{inactivation gate for } I_{\text{KCa(BK)}}$

$\alpha_h, \beta_h ; (\text{ms}^{-1})$, rate constants for $h_{\text{KCa(BK)}}$

$$po_{\text{KCa(BK)}} = m_{\text{KCa(BK)}} \cdot h_{\text{KCa(BK)}}$$

$$I_{\text{KCa(BK)}} = G_{\text{KCa(BK)}} \cdot po_{\text{KCa(BK)}} \cdot (V_m - E_K) \quad (\text{S31})$$

$$\frac{dm_{\text{KCa(BK)}}}{dt} = \alpha_m \cdot (1 - m_{\text{KCa(BK)}}) - \beta_m \cdot m_{\text{KCa(BK)}} \quad (\text{S32})$$

$$\alpha_m = \frac{1}{13.65 \cdot \exp(-\frac{V_m}{20})} \quad (\text{S33})$$

$$\beta_m = \frac{1}{6.2 \cdot \exp(\frac{V_m}{60})} \quad (\text{S34})$$

$$\frac{dh_{\text{KCa(BK)}}}{dt} = \alpha_h \cdot (1 - h_{\text{KCa(BK)}}) - \beta_h \cdot h_{\text{KCa(BK)}} \quad (\text{S35})$$

$$\alpha_h = \frac{1}{570 \cdot \exp(\frac{V_m}{500})} \quad (\text{S36})$$

$$\beta_h = \frac{1}{7.765 \cdot \exp(-\frac{V_m}{9}) + 4.076 \cdot \exp(-\frac{V_m}{1000})} \quad (\text{S37})$$

$I_{\text{KCa(SK)}} ; \text{Ca}^{2+}\text{-activated K}^+ \text{ current}$

$P_{\text{KCa(SK)}} ; 0.2 (\text{pA mM}^{-1})$, converting factor of $I_{\text{KCa(SK)}}$

$po_{\text{KCa(SK)}} ; \text{open probability of } I_{\text{KCa(SK)}}$

$$po_{\text{KCa(SK)}} = \frac{1}{1 + (\frac{0.00074}{[\text{Ca}^{2+}]_i})^{2.2}} \quad (\text{S38})$$

$$I_{\text{KCa(SK)}} = P_{\text{KCa(SK)}} \cdot po_{\text{KCa(SK)}} \cdot CF_K \quad (\text{S39})$$

I_{bNSC} ; background non-selective cation current

P_{bNSC} ; 0.00396 (pA mM⁻¹), converting factor of I_{bNSC}

$$I_{bNSC} = I_{bNSC,Na} + I_{bNSC,K} \quad (S40)$$

$$I_{bNSC,Na} = P_{bNSC} \cdot CF_{Na} \quad (S41)$$

$$I_{bNSC,K} = 2.525 \cdot P_{bNSC} \cdot CF_K \quad (S42)$$

I_{SOC} ; store-operated current

P_{SOC} ; 0.00764 (pA mM⁻¹), converting factor of I_{SOC}

po_{SOC} ; open probability of I_{SOC}

K_{0.5,ER} ; 0.003 (mM), half activation concentration of Ca²⁺ in the ER

$$I_{SOC} = I_{SOC,Na} + I_{SOC,K} + I_{SOC,Ca} \quad (S43)$$

$$po_{SOC} = \frac{1}{1 + \exp\left(\frac{[Ca^{2+}]_{ER} - K_{0.5,ER}}{0.003}\right)} \quad (S44)$$

$$I_{SOC,Na} = 0.8 \cdot P_{SOC} \cdot po_{SOC} \cdot CF_{Na} \quad (S45)$$

$$I_{SOC,K} = P_{SOC} \cdot po_{SOC} \cdot CF_K \quad (S46)$$

$$I_{SOC,Ca} = 20 \cdot P_{SOC} \cdot po_{SOC} \cdot CF_{Ca} \quad (S47)$$

I_{TRPM} ; Ca²⁺-activated non-selective cation current (TRPM channel)

P_{TRPM} ; 0.0234 (pA mM⁻¹), converting factor of I_{TRPM}

po_{TRPM} ; open probability of I_{TRPM}

$$po_{TRPM} = \frac{1}{1 + \left(\frac{0.00076}{[Ca^{2+}]_i}\right)^{1.7}} \quad (S48)$$

$$I_{TRPM} = I_{TRPM,Na} + I_{TRPM,K} \quad (S49)$$

$$I_{\text{TRPM,Na}} = 0.8 \cdot P_{\text{TRPM}} \cdot po_{\text{TRPM}} \cdot CF_{\text{Na}} \quad (\text{S50})$$

$$I_{\text{TRPM,K}} = P_{\text{TRPM}} \cdot po_{\text{TRPM}} \cdot CF_{\text{K}} \quad (\text{S51})$$

I_{KATP} ; ATP-sensitive K^+ current

G_{KATP} ; 2.31 (pA mV⁻¹), maximum conductance of I_{KATP}

po_{KATP} ; open probability of I_{KATP}

$$po_{\text{KATP}} = \frac{0.08 \cdot (1 + \frac{2 \cdot [\text{MgADP}]}{0.01}) + 0.89 \cdot (\frac{[\text{MgADP}]}{0.01})^2}{(1 + \frac{[\text{MgADP}]}{0.01})^2 (1 + \frac{0.45 \cdot [\text{MgADP}]}{0.026} + \frac{[\text{ATP}]}{0.05})} \quad (\text{S52})$$

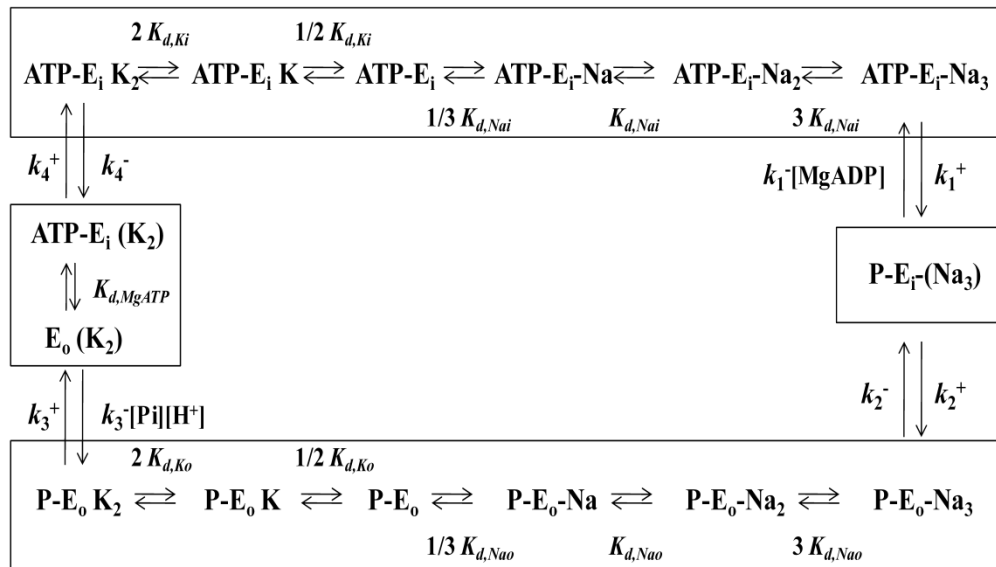
$$I_{\text{KATP}} = G_{\text{KATP}} \cdot po_{\text{KATP}} \cdot (V_m - E_K) \quad (\text{S53})$$

4. Transporters

I_{NaK} : Na^+/K^+ pump current

* The rate constants, k^\pm s in their Table1 were multiplied by 1.74 according Oka et al. (2010).

[Pi] of 1.9 mM and $[\text{H}^+]$ of 0.0001 mM were assumed only for calculating $I_{\text{Na/K}}$.



P_{NaK} ; 350 (pA ms), limiting amplitude of I_{NaK}

v_{cyc} ; turnover rate (ms^{-1})

F_{glc} ; inhibition factor of glucose ([G]) on I_{NaK}

k^{\pm} ; (ms^{-1}), rate constants

$K_{\text{d,X}}$; (mM), dissociation constant of ion X

$$I_{\text{NaK}} = P_{\text{NaK}} \cdot v_{\text{cyc}} \cdot F_{\text{glc}} \quad (\text{S54})$$

$$F_{\text{glc}} = 0.4 + 0.6 \exp\left(-\frac{[\text{G}]}{5.84}\right) \quad (\text{S55})$$

$$v_{\text{cyc}} = \frac{\alpha_1^+ \alpha_2^+ \alpha_3^+ \alpha_4^+ - \alpha_1^- \alpha_2^- \alpha_3^- \alpha_4^-}{\sum} \quad (\text{S56})$$

$$\begin{aligned} \sum = & \alpha_1^- \alpha_2^- \alpha_3^- + \alpha_1^+ \alpha_2^- \alpha_3^- + \alpha_1^+ \alpha_2^+ \alpha_3^- + \alpha_1^+ \alpha_2^+ \alpha_3^+ \\ & + \alpha_2^- \alpha_3^- \alpha_4^- + \alpha_2^+ \alpha_3^- \alpha_4^- + \alpha_2^+ \alpha_3^+ \alpha_4^- + \alpha_2^+ \alpha_3^+ \alpha_4^+ \\ & + \alpha_3^- \alpha_4^- \alpha_1^- + \alpha_3^+ \alpha_4^- \alpha_1^- + \alpha_3^+ \alpha_4^+ \alpha_1^- + \alpha_3^+ \alpha_4^+ \alpha_1^+ \\ & + \alpha_4^- \alpha_1^- \alpha_2^- + \alpha_4^+ \alpha_1^- \alpha_2^- + \alpha_4^+ \alpha_1^+ \alpha_2^- + \alpha_4^+ \alpha_1^+ \alpha_2^+ \end{aligned} \quad (\text{S57})$$

$$\alpha_1^+ = \frac{k_1^+ \overline{\text{Na}_i}^3}{(1 + \overline{\text{Na}_i})^3 + (1 + \overline{\text{K}_i})^2 - 1} \quad (\text{S58})$$

$$\alpha_2^+ = k_2^+ \quad (\text{S59})$$

$$\alpha_3^+ = \frac{k_3^+ \overline{\text{K}_o}^2}{(1 + \overline{\text{Na}_o})^3 + (1 + \overline{\text{K}_o})^2 - 1} \quad (\text{S60})$$

$$\alpha_4^+ = \frac{k_4^+ \overline{\text{MgATP}}}{1 + \overline{\text{MgATP}}} \quad (\text{S61})$$

$$\alpha_1^- = k_1^- [\text{MgADP}] \quad (\text{S62})$$

$$\alpha_2^- = \frac{k_2^- \overline{\text{Na}_o}^3}{(1 + \overline{\text{Na}_o})^3 + (1 + \overline{\text{K}_o})^2 - 1} \quad (\text{S63})$$

$$\alpha_3^- = \frac{k_3^- [\text{Pi}] [\text{H}^+]}{1 + \overline{\text{MgATP}}} \quad (\text{S64})$$

$$\alpha_4^- = \frac{k_4^- \overline{\text{K}_i}^2}{(1 + \overline{\text{Na}_i})^3 + (1 + \overline{\text{K}_i})^2 - 1} \quad (\text{S65})$$

$$k_1^- = 0.139 \text{ mM}^{-1} \text{ms}^{-1}, k_2^- = 0.0139 \text{ ms}^{-1}, k_3^- = 13900 \text{ mM}^{-2} \text{ms}^{-1}, k_4^- = 0.348 \text{ ms}^{-1}$$

$$\overline{\text{Na}_i} = \frac{[\text{Na}^+]_i}{\text{K}_{\text{d},\text{Na}_i}}, \quad (\text{S66})$$

$$\overline{\text{K}_i} = \frac{[\text{K}^+]_i}{\text{K}_{\text{d},\text{K}_i}} \quad (\text{S67})$$

$$\overline{\text{Na}_o} = \frac{[\text{Na}^+]_o}{\text{K}_{\text{d},\text{Na}_o}}, \quad (\text{S68})$$

$$\overline{\text{K}_o} = \frac{[\text{K}^+]_o}{\text{K}_{\text{d},\text{K}_o}} \quad (\text{S69})$$

$$\overline{\text{MgATP}} = \frac{[\text{MgATP}]}{\text{K}_{\text{d},\text{MgATP}}} \quad (\text{S70})$$

$$\text{K}_{\text{d},\text{Na}_o} = \text{K}_{\text{d},\text{Na}_o}^0 \cdot \exp \frac{\Delta_{\text{Na}_o} \cdot \text{FV}_m}{RT} \quad (\text{S71})$$

$$\text{K}_{\text{d},\text{Na}_i} = \text{K}_{\text{d},\text{Na}_i}^0 \cdot \exp \frac{\Delta_{\text{Na}_i} \cdot \text{FV}_m}{RT} \quad (\text{S72})$$

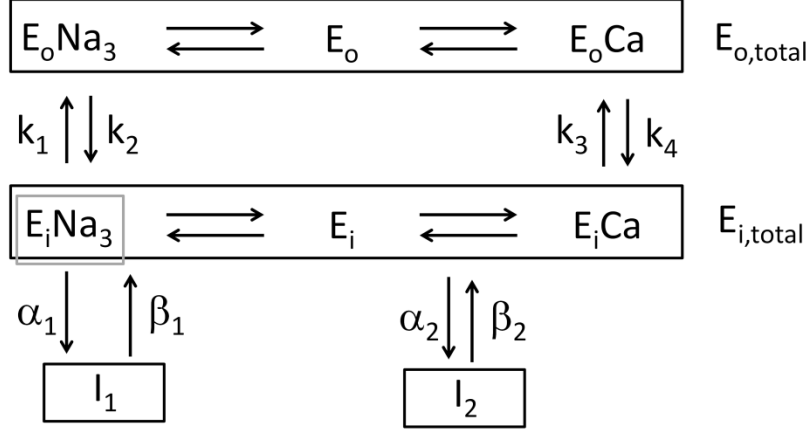
$$\text{K}_{\text{d},\text{K}_o} = \text{K}_{\text{d},\text{K}_o}^0 \cdot \exp \frac{\Delta_{\text{K}_o} \cdot \text{FV}_m}{RT} \quad (\text{S73})$$

$$\text{K}_{\text{d},\text{K}_i} = \text{K}_{\text{d},\text{K}_i}^0 \cdot \exp \frac{\Delta_{\text{K}_i} \cdot \text{FV}_m}{RT} \quad (\text{S74})$$

$$\text{K}_{\text{d},\text{MgATP}} = 0.6 \text{ mM}, \quad \text{K}_{\text{d},\text{Na}_o}^0 = 26.8 \text{ mM}, \quad \text{K}_{\text{d},\text{K}_o}^0 = 0.8 \text{ mM}, \quad \text{K}_{\text{d},\text{Na}_i}^0 = 5.0 \text{ mM}, \quad \text{K}_{\text{d},\text{K}_i}^0 = 18.8 \text{ mM},$$

$$\Delta_{\text{Na}_o} = 0.44, \Delta_{\text{Na}_i} = -0.14, \Delta_{\text{K}_o} = 0.23, \Delta_{\text{K}_i} = -0.14$$

I_{NaCa} : Na^+/Ca^{2+} exchange current



P_{NaCa} ; 204 (pA), maximum amplitude of I_{NaCa}

$E_{i,total}$, $E_{o,total}$; probability of active states with an internal or external binding site, respectively

I_1 , I_2 ; probabilities of inactive states

k , α and β ; (ms^{-1}), rate constants

$K_{d,X}$; (mM), dissociation constant of ion X

f_{Ca} ; parameter to define the Ca^{2+} -dependency of the inactivation gates, I_1 , I_2

$$I_{NaCa} = P_{NaCa} \cdot (k_1 \cdot p_{EiNa} \cdot E_{i,total} - k_2 \cdot p_{EoNa} \cdot E_{o,total}) \quad (S75)$$

$$\frac{dI_1}{dt} = \alpha_1 \cdot p_{EiNa} \cdot E_{i,total} - \beta_1 \cdot I_1 \quad (S76)$$

$$\frac{dI_2}{dt} = \alpha_2 \cdot E_{i,total} - \beta_2 \cdot I_2 \quad (S77)$$

$$k_f = k_2 \cdot p_{EoNa} + k_4 \cdot p_{EoCa} \quad (S78)$$

$$k_b = k_1 \cdot p_{EiNa} + k_3 \cdot p_{EiCa} \quad (S79)$$

$$\frac{dE_{i,total}}{dt} = k_f \cdot E_{o,total} + \beta_1 \cdot I_1 + \beta_2 \cdot I_2 - (k_b + \alpha_1 \cdot p_{EiNa} + \alpha_2) \cdot E_{i,total} \quad (S80)$$

$$E_{o,total} = 1 - (E_{i,total} + I_1 + I_2) \quad (S81)$$

$$k_1 = \exp\left(\frac{0.32 \cdot V_m \cdot F}{R \cdot T}\right) \quad (\text{S82})$$

$$k_2 = \exp\left(\frac{(0.32 - 1) \cdot V_m \cdot F}{R \cdot T}\right) \quad (\text{S83})$$

$$k_3 = 1 \quad (\text{S84})$$

$$k_4 = 1 \quad (\text{S85})$$

$$\alpha_1 = 0.002 \cdot f_{\text{Ca}} + 0.0015 \cdot (1 - f_{\text{Ca}}) \quad (\text{S86})$$

$$\beta_1 = 0.0012 \cdot f_{\text{Ca}} + 0.0000005 \cdot (1 - f_{\text{Ca}}) \quad (\text{S87})$$

$$\alpha_2 = 0.00003 \cdot f_{\text{Ca}} + 0.01 \cdot (1 - f_{\text{Ca}}) \quad (\text{S88})$$

$$\beta_2 = 0.09 \cdot f_{\text{Ca}} + 0.0001 \cdot (1 - f_{\text{Ca}}) \quad (\text{S89})$$

$$f_{\text{Ca}} = \frac{[\text{Ca}^{2+}]_i}{[\text{Ca}^{2+}]_i + 0.004} \quad (\text{S90})$$

$$p_{\text{EiNa}} = \frac{\left(\frac{[\text{Na}^+]_i}{K_{\text{d, Nai}}}\right)^3}{1 + \left(\frac{[\text{Na}^+]_i}{K_{\text{d, Nai}}}\right)^3 + \frac{[\text{Ca}^{2+}]_i}{K_{\text{d, Cai}}}} \quad (\text{S91})$$

$$p_{\text{EiNa}} = \frac{\frac{[\text{Ca}^{2+}]_i}{K_{\text{d, Cai}}}}{1 + \left(\frac{[\text{Na}^+]_i}{K_{\text{d, Nai}}}\right)^3 + \frac{[\text{Ca}^{2+}]_i}{K_{\text{d, Cai}}}} \quad (\text{S92})$$

$$p_{\text{EoNa}} = \frac{\left(\frac{[\text{Na}^+]_o}{K_{\text{d, Nao}}}\right)^3}{1 + \left(\frac{[\text{Na}^+]_o}{K_{\text{d, Nao}}}\right)^3 + \frac{[\text{Ca}^{2+}]_o}{K_{\text{d, Cao}}}} \quad (\text{S93})$$

$$p_{\text{EoCa}} = \frac{\frac{[\text{Ca}^{2+}]_o}{K_{\text{d, Cao}}}}{1 + \left(\frac{[\text{Na}^+]_o}{K_{\text{d, Nao}}}\right)^3 + \frac{[\text{Ca}^{2+}]_o}{K_{\text{d, Cao}}}} \quad (\text{S94})$$

$K_{d,Na_i} = 20.75 \text{ mM}$, $K_{d,Ca_i} = 0.0184 \text{ mM}$, $K_{d,Na_o} = 87.5 \text{ mM}$, $K_{d,Ca_o} = 1.38 \text{ mM}$

I_{PMCA} : plasma membrane Ca^{2+} pump (PMCA) current

P_{PMCA} ; 1.56 (pA), maximum amplitude of I_{PMCA}

$$I_{PMCA} = P_{PMCA} \frac{1}{1 + \left(\frac{0.00014}{[Ca^{2+}]_i}\right)^2} \quad (S95)$$

5.ER calcium dynamics

J_{SERCA} ; Ca^{2+} uptake by SERCA

P_{SERCA} ; 0.096 (amole ms^{-1}), the maximum rate of pumping Ca^{2+} into ER.

$$J_{SERCA} = P_{SERCA} \frac{1}{1 + \left(\frac{0.0005}{[Ca^{2+}]_i}\right)^2} \quad (S96)$$

J_{rel} ; Ca^{2+} release from ER

P_{rel} ; 0.46 (fl ms^{-1}), converting factor for Ca^{2+} release from ER

$$J_{rel} = P_{rel} \cdot ([Ca^{2+}]_{ER} - [Ca^{2+}]_i) \quad (S97)$$

6.Glycolysis and oxidative phospholylation

J_{glc} or $J_{\beta,ox}$; NADH production through glycolysis or β -oxidation

k_{glc} ; 0.000126 (ms^{-1}), rate constant of glycolysis

$k_{\beta,ox}$; 0.0000063 (ms^{-1}), rate constant of β -oxidation

$[Re_{tot}]$; 10 (mM), total amount of pyrimidine nucleotides

$$J_{glc} = k_{glc} \cdot f_{glc} \cdot ([Re_{tot}] - [Re]) \quad (S98)$$

$$J_{\beta,ox} = k_{\beta,ox} ([Re_{tot}] - [Re]) \quad (S99)$$

f_{glc} ; ATP- and glucose- dependency of glycolysis

$[G]$; extracellular glucose concentration

hgl ; 2.5, Hill coefficient for glucose-dependency

K_G ; 13 (mM), half-maximal concentration of glucose

$$f_{\text{glc}} = \frac{1}{1 + \frac{0.5}{[\text{ATP}]_i}} \cdot \frac{1}{1 + \left(\frac{K_G}{[G]}\right)^{\text{hgl}}} \quad (\text{S100})$$

J_{op} ; ATP production through oxidative phosphorylation

* $P_{\text{op}} = 0.0005$; ms^{-1} maximum rate of ATP production

* $N = 2.5$; stoichiometry of conversion from NADH to ATP

* $R_{\text{vol}} = 2.5$; volume ratio between cytosol and mitochondria

$$J_{\text{op}} = P_{\text{op}} \cdot [\text{Re}] \cdot \frac{1}{1 + \left(\frac{0.02}{[\text{MgADP}]}\right)^2} \quad (\text{S101})$$

$$\frac{d[\text{Re}]}{dt} = J_{\text{glc}} + J_{\beta, \text{ox}} - \frac{R_{\text{vol}}}{N} J_{\text{op}} \quad (\text{S102})$$

$J_{\text{c,ATP}}$; flux of Ca^{2+} -dependent/independent ATP consumption

$[\text{ATP}_{\text{tot}}]$; 4 (mM), total amount of ATP species

ADP_b ; bound ADP

ADP_f ; free ADP

k_{ATP} ; $0.000062 (\text{ms}^{-1})$, rate constant of Ca^{2+} -independent ATP consumption

$k_{\text{ATP,Ca}}$; $0.187 (\text{mM}^{-1} \text{ms}^{-1})$, rate constant of Ca^{2+} -dependent ATP consumption

$k_{\text{ADP,f}}$; $0.0002 (\text{ms}^{-1})$, rate constant from ADP_f to ADP_b

$k_{\text{ADP,b}}$; $0.00002 (\text{ms}^{-1})$, rate constant from ADP_b to ADP_f

$$J_{\text{c,ATP}} = (k_{\text{ATP}} + k_{\text{ATP,Ca}} \cdot [\text{Ca}^{2+}]_i) \cdot [\text{ATP}] \quad (\text{S103})$$

$$\frac{d[\text{ATP}]}{dt} = J_{\text{op}} - J_{\text{c,ATP}} - \left(\frac{I_{\text{NaK}} + I_{\text{PMCA}}}{F} + \frac{J_{\text{SERCA}}}{2}\right) / V_i \quad (\text{S104})$$

$$\frac{d[\text{ADP}_b]}{dt} = k_{\text{ADP,f}} \cdot [\text{ADP}_f] - k_{\text{ADP,b}} \cdot [\text{ADP}_b] \quad (\text{S105})$$

$$[\text{ADP}_f] = [\text{ATP}_{\text{total}}] - [\text{ATP}] - [\text{ADP}_b] \quad (\text{S106})$$

$$[\text{MgADP}] = 0.55 \cdot [\text{ADP}_f] \quad (\text{S107})$$

7. Definition of the lead potential (V_L) for calculation in Figs. 5 and 6

$$\begin{aligned}
& (G_{\text{KCa(BK)}} \cdot \text{po}_{\text{KCa(BK)}} + G_{\text{KATP}} \cdot \text{po}_{\text{KATP}}) \cdot E_K \\
& + \left(\frac{P_{\text{bNSC}} + 0.8 \cdot P_{\text{TRPM}} \cdot \text{po}_{\text{TRPM}} + 0.0000185 \cdot P_{\text{CaV}} \cdot \text{po}_{\text{CaV}}}{+ 0.8 \cdot P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}} \right) \cdot \frac{\partial(\text{CF}_{\text{Na}})}{\partial V_m} \cdot E_{\text{CFNa}} \\
& + \left(\frac{2.525 \cdot P_{\text{bNSC}} + P_{\text{KDr}} \cdot \text{po}_{\text{KDr}} + P_{\text{TRPM}} \cdot \text{po}_{\text{TRPM}}}{+ 0.000367 \cdot P_{\text{CaV}} \cdot \text{po}_{\text{CaV}} + P_{\text{KCa(SK)}} \cdot \text{po}_{\text{KCa(SK)}} + P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}} \right) \cdot \frac{\partial(\text{CF}_K)}{\partial V_m} \cdot E_{\text{CFK}} \\
& + (P_{\text{CaV}} \cdot \text{po}_{\text{CaV}} + 20 \cdot P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}) \cdot \frac{\partial(\text{CF}_{\text{Ca}})}{\partial V_m} \cdot E_{\text{CFCa}} \\
V_L = & \frac{+ G_{\text{NaK}} \cdot E_{x_{\text{NaK}}} + G_{\text{NaCa}} \cdot E_{x_{\text{NaCa}}} - I_{\text{PMCA}} - I_{\text{inject}}}{(G_{\text{KCa(BK)}} \cdot \text{po}_{\text{KCa(BK)}} + G_{\text{KATP}} \cdot \text{po}_{\text{KATP}})} \\
& + \left(\frac{P_{\text{bNSC}} + 0.8 \cdot P_{\text{TRPM}} \cdot \text{po}_{\text{TRPM}} + 0.0000185 \cdot P_{\text{CaV}} \cdot \text{po}_{\text{CaV}}}{+ 0.8 \cdot P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}} \right) \cdot \frac{\partial(\text{CF}_{\text{Na}})}{\partial V_m} \\
& + \left(\frac{2.525 \cdot P_{\text{bNSC}} + P_{\text{KDr}} \cdot \text{po}_{\text{KDr}} + P_{\text{TRPM}} \cdot \text{po}_{\text{TRPM}}}{+ 0.000367 \cdot P_{\text{CaV}} \cdot \text{po}_{\text{CaV}} + P_{\text{KCa(SK)}} \cdot \text{po}_{\text{KCa(SK)}} + P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}} \right) \cdot \frac{\partial(\text{CF}_K)}{\partial V_m} \\
& + (P_{\text{CaV}} \cdot \text{po}_{\text{CaV}} + 20 \cdot P_{\text{SOC}} \cdot \text{po}_{\text{SOC}}) \cdot \frac{\partial(\text{CF}_{\text{Ca}})}{\partial V_m} + G_{\text{NaK}} + G_{\text{NaCa}}
\end{aligned} \tag{S108}$$

where constant field equations for Na^+ , K^+ and Ca^{2+} (CF_{Na} , CF_K and CF_{Ca} , respectively (Eq. S7)) were linearized with respect to V_m , as below:

$$\text{CF}_{\text{Na}} = \frac{\partial(\text{CF}_{\text{Na}})}{\partial V_m} \cdot (V_m - E_{\text{CFNa}}) \tag{S109}$$

$$\text{CF}_K = \frac{\partial(\text{CF}_K)}{\partial V_m} \cdot (V_m - E_{\text{CFK}}) \tag{S110}$$

$$\text{CF}_{\text{Ca}} = \frac{\partial(\text{CF}_{\text{Ca}})}{\partial V_m} \cdot (V_m - E_{\text{CFCa}}) \tag{S111}$$

Table S1. Initial values of independent variables ($X(0)$)

Independent variables	Initial values
V_m	-48.9045
$[Na^+]_i$	5.80400
$[K^+]_i$	126.776
$[Ca^{2+}]_i$	0.000306139
$[Ca^{2+}]_{ER}$	0.0234849
[ATP]	2.64667
[MgADP]	0.127093
[Re]	0.641950
d_{CaL}	0.101898
U_{CaL}	0.635696
f_{us}	0.827114
r_{KDr}	0.00105694
q_{KDr}	0.970421
m_{Kto}	0.0170783
h_{Kto}	0.301612
$E_{i,tot}$	0.354892
I_1	0.151253
I_2	0.489584

* The set of values was obtained when the model shows a steady bursting rhythm at 8 mM [G]. The initial values were used for obtaining all the figures in this paper and Figs. 1, 4 & 5 in the accompanying paper. These initial values define the present model according to the charge conservation law described in the accompanying paper.