

## R2 数学本試

$$\begin{aligned} \text{① (1)} \quad \frac{1}{\sqrt{3}} \div \left(-\frac{1}{2}\right)^2 - \sqrt{6} \times \frac{\sqrt{2}}{4} &= \frac{1}{\sqrt{3}} \times 4 - \frac{2\sqrt{3}}{4} = \frac{4}{\sqrt{3}} - \frac{\sqrt{3}}{2} \\ &= \frac{4 \times 2 - \sqrt{3} \times \sqrt{3}}{2\sqrt{3}} = \frac{8-3}{2\sqrt{3}} \\ &= \frac{5\sqrt{3}}{6} \end{aligned}$$

$$(2) x^2 + ax - 6 = 0$$

$$(x+3)(x+\beta) = x^2 + (\beta+3)x + 3\beta \Rightarrow x^2 + ax - 6 = x^2 + (\beta+3)x + 3\beta$$

$$\begin{cases} a = \beta + 3 & \text{①} \\ -6 = 3\beta & \text{②} \end{cases}$$

$$a = -2 + 3 = 1$$

$$a = 1$$

$$\beta = -2$$

$$\text{discriminant: } 2$$

(3)

$$\begin{aligned} y &= -\frac{1}{4}x^2 + 2x - 3 \\ x &= -3 \quad y = -\frac{1}{4} \times (-3)^2 = -\frac{9}{4} \\ x &= 7 \quad y = -\frac{1}{4} \times 7^2 = -\frac{49}{4} \end{aligned}$$

$$\text{平均値の定理より } \frac{-\frac{49}{4} - (-\frac{9}{4})}{7 - (-3)} = \frac{-40}{10} = -4$$

$$\begin{aligned} \text{④} \quad & \text{A(2, 4a)} \quad \frac{1}{2} \times (4+2) \times (4a+1) = 11 \quad 4a+1 = \frac{11}{3} \quad 4a = \frac{8}{3} \\ & 3(4a+1) = 11 \quad a = \frac{2}{3} \end{aligned}$$

(5)

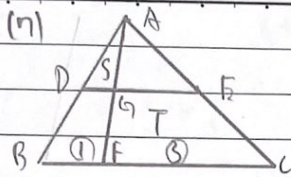
	1	2	3	4	5	6
1	1	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

$$\frac{14}{30} = \frac{7}{15}$$

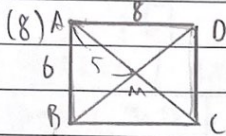
$$(6) \text{ 平均値 } \bar{x} = \frac{1}{40} (2 \times 1 + 3 \times 2 + 4 \times 3 + 5 \times 4 + 6 \times 5 + 7 \times 6 + 8 \times 7 + 9 \times 8 + 10 \times 9) = 7$$

中央値  $\bar{x} = 7.5$ 最頻値  $\bar{x} = 9$ 

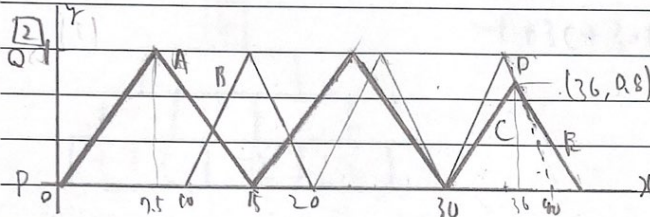
$$\therefore \bar{x} < \bar{y} < \bar{z}$$



$$\begin{aligned} \triangle ADG : \triangle AGE &= 4:3 \\ \triangle AGE : \triangle APC &= 1:4 \Rightarrow \triangle AGE : \triangle EGF : \triangle GFC = 1:3 \\ \therefore \triangle ADG : \triangle EGF : \triangle GFC &= 1:9 \end{aligned}$$



$$\begin{aligned} \frac{1}{3} \times 6 \times 8 \times h &= 192 \quad h = \frac{3 \times 192}{48} = 12 \\ AM &= \frac{1}{2} \sqrt{6^2 + 8^2} = 5 \\ AO &= \sqrt{12^2 + 5^2} = 13 \text{ cm} \end{aligned}$$



$$\begin{aligned} (1) \quad y &= ax + b \quad (12, 1), (15, 0) \text{ を代入} \quad b = 2 \text{ を } \textcircled{1} \text{ に代入} \\ \begin{cases} 1 = 7.5a + b & \textcircled{1} \\ 0 = 15a + b & \textcircled{2} \end{cases} \quad \textcircled{1} \times 2 \quad 2 = 15a + 2b \quad 0 = 15a + 2 \\ \textcircled{2} \quad 0 = 15a + b & \quad \textcircled{1} \times 2 \quad 0 = 15a + b \quad a = -\frac{2}{15} \quad \therefore y = -\frac{2}{15}x + 2 \quad (A) \end{aligned}$$

$$\begin{aligned} (2) \quad B \text{ の } x \text{ と } y \text{ の式を } y &= ax + b \text{ とおき, } (10, 0), (15, 1) \text{ を代入} \\ \begin{cases} 0 = 10a + b & \textcircled{1} \\ 1 = 15a + b & \textcircled{2} \end{cases} \quad \textcircled{1} \times (-1) \quad a = \frac{1}{5} \text{ を } \textcircled{2} \text{ に代入} \\ \textcircled{2} - \textcircled{1} \quad 1 = 5a \quad a = \frac{1}{5} \quad 0 = 10 \times \frac{1}{5} + b \quad b = -2 \quad \therefore y = \frac{1}{5}x - 2 \quad (B) \end{aligned}$$

(A) と (B) を連立すると

$$\begin{aligned} -\frac{2}{15}x + 2 &= \frac{1}{5}x - 2 \quad -2x + 30 = 3x - 30 \quad x = 12 \text{ を } (B) \text{ に代入} \\ 5x &= 60 \quad x = 12 \quad y = 0.5 \times 12 - 2 = 2.4 - 2 = 0.4 \text{ km} \end{aligned}$$

$$(3) \quad (C) \quad y = \frac{2}{15}(x - 30) = \frac{2}{15}x - 4 \quad \frac{2}{15}x - 4 = -\frac{1}{5}x + 8 \quad y = -\frac{1}{5}(36 - 40) = \frac{4}{5}$$

$$(D) \quad y = -\frac{1}{5}(x - 40) = -\frac{1}{5}x + 8 \quad 2x - 60 = -3x + 120 \quad (x, y) = (36, 0.8)$$

$$(E) \quad y = \frac{2}{15}(x - C) \quad (36, 0.8) \text{ を代入} \quad \frac{4}{5} = \frac{2}{15}(36 - C) \quad C = 36 + 6 = 42 \text{ 分}$$

$$(4) \quad 1 \times 4 + 0.8 \times 2 = 5.6 \text{ km}$$



(1) 
$$\begin{array}{|c|c|c|} \hline & 12 & \\ \hline b+a & a-4 & \\ \hline 6 & a & 4 \\ \hline \end{array}$$

$$b+a+a-4=12$$

$$2a=10$$

$$a=5$$

$$\begin{array}{|c|c|c|c|} \hline & b & & \\ \hline p+2a+r & a+2r+s & & \\ \hline p+a & a+r & r+s & \\ \hline p & a & r & s \\ \hline \end{array}$$

$$b=p+3a+3r+s$$

$$\begin{array}{|c|c|c|c|} \hline & 4 & & \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline -1 & c & -2 & -3 \\ \hline \end{array}$$

$$-1+3c+3(-2)+3=4$$

$$3c=14$$

$$c=\frac{14}{3}$$

(2) 
$$\begin{array}{|c|c|c|} \hline & b & \\ \hline & & \\ \hline p & d & q \\ \hline 5 & e & f & 1 \\ \hline \end{array}$$

$$5+3e+3f+1=6$$

$$3e+3f=0$$

$$f=-e$$

$$\therefore d=e-e=0$$

$$-6 \leq e \leq 6$$

$$\textcircled{1} 5+e \leq 6 \Rightarrow e \leq 1$$

$$\textcircled{2} -e+1 \leq 6 \Rightarrow e \geq -5$$

$$\therefore -5 \leq e \leq 1 \Rightarrow 7 \text{ 個}$$

(3) 
$$\begin{array}{|c|c|c|c|} \hline & 9 & & \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ \hline -5 & -4 & -3 & -2 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline \end{array}$$

$$-f+3-6=9$$

$$-f+3=12$$

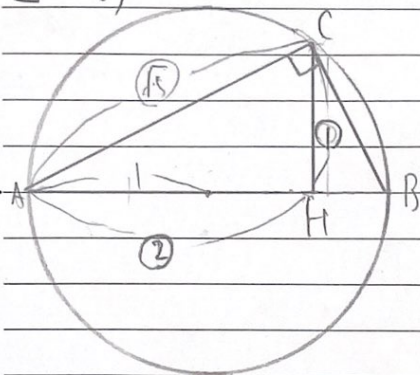
$$f=-9$$

$$6+2f+3=-7f-18$$

$$\begin{cases} f+g=-3 \\ 9f=-27 \end{cases} \rightarrow \begin{cases} f=-3 \\ g=0 \end{cases}$$

$$\therefore (f, g) = (-3, 0)$$

□ (1)



$$(1) \quad (H^2)(U_1 \cap U_2)$$

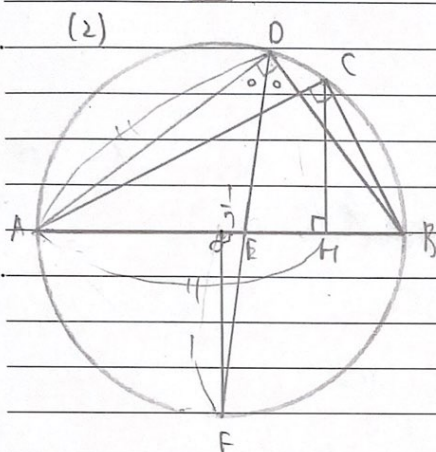
$$AH:AC = AC:AB$$

$$2x : \sqrt{5}x = \sqrt{5}x : 2$$

$$5x^2 = 4x$$

$$x = \frac{4}{5} \therefore AH = 2x = \frac{8}{5}$$

(2)



$$\angle ADB = 90^\circ \text{ Py } \angle ADB = 45^\circ$$

$$DB = \sqrt{AB^2 - AD^2} = \sqrt{AB^2 - AC^2}$$

$$= \sqrt{2^2 - \left(\frac{8}{5}\right)^2} = \sqrt{\frac{100}{25} - \frac{64}{25}} = \sqrt{\frac{36}{25}} = \frac{6}{5}$$

$\triangle DAB$  12f. 47

$$AE:BE = AD:BD = \frac{8}{5} : \frac{6}{5} = 4:3$$

$$\therefore AE = \frac{4}{7} AB = \frac{4}{7} \times 2 = \frac{8}{7}$$

(3)  $OE = AE - AO = \frac{9}{4} - 1 = \frac{5}{4}$ ,  $OF = 1$   $\therefore$

$$EF = \sqrt{\left(\frac{1}{7}\right)^2 + 1^2} = \sqrt{\frac{1}{49} + 1} = \sqrt{\frac{50}{49}} = \frac{5\sqrt{2}}{7}$$