

## CSE221 Assignment 06 Fall 2025

### A. Advising

1 second🕒, 1024 megabytes

In this problem, there are **N** courses in the curriculum and **M** requirements of the form "Course **A** has to be completed before course **B**".

Your task is to find an order in which you can complete the courses. If there are multiple valid order, you may print any of them. If no such sequence exists, then print  $-1$ .

#### Input

The first line contains two integers  $N, M$  ( $1 \leq N \leq 2 \times 10^5, 1 \leq M \leq 3 \times 10^5$ ) — the number of courses and total requirements.

The next  $M$  lines will contain two integers  $A_i, B_i$  ( $1 \leq A_i, B_i \leq N$ ) — Course A has to be completed before course B.

#### Output

Print an order in which you can complete the courses. Please note, that there could be multiple correct sequences. You can print any valid order that includes all the courses.

If there is no valid sequence, print  $-1$ .

input
5 4 2 4 2 5 4 3 1 5
output
2 4 3 1 5

input
8 8 6 4 6 2 4 2 2 1 1 7 7 5 5 8 8 3
output
6 4 2 1 7 5 8 3

input
2 1 1 2
output
1 2

input
4 6 1 2 1 3 4 1 2 3 2 4 4 3

#### output

-1

### B. A Football Match

2 seconds🕒, 1024 megabytes

There is an intense football match going on between Robots and Humans. However, things aren't as simple as they seem — the Robots have disguised themselves to look exactly like Humans! From the outside, it's impossible to tell who is a Robot and who is a Human.

The audience know only one important information — the Robots tackles only the Humans, and the Humans tackles only the Robots.

Now, you are given a list of tackles, each involving two players. Based on this information, find the maximum possible number of Robots or Humans.

#### Input

The first line contains two integers  $N$  and  $M$  ( $1 \leq N \leq 2 \times 10^5, 1 \leq M \leq 3 \times 10^5$ ) — the number of players in the match and the number of tackles occurred during the match respectively.

The next  $M$  lines will contain two integers  $u_i, v_i$  ( $1 \leq u_i, v_i \leq N$ ) — player  $u_i$  tackled player  $v_i$ . Each tackle between two players will be reported at most once.

#### Output

Print the maximum possible number of Robots or Humans.

input
5 6 3 4 3 2 5 4 5 2 4 1 1 2
output
3

input
5 4 4 3 1 3 3 2 3 5
output
4

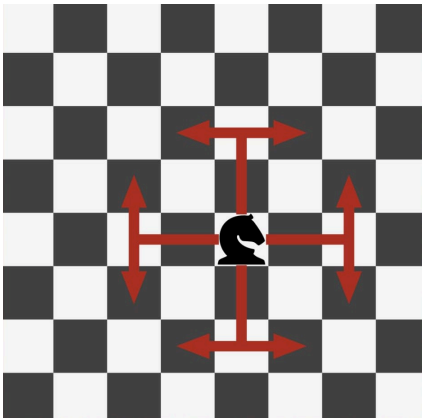
input
4 1 1 3
output
3

input
6 6
1 3
1 4
3 6
4 6
4 5
6 2
output
3

### C. The Knight of Königsberg

1 second🕒, 256 megabytes

You are given an  $N \times N$  chessboard and the initial position  $(x_1, y_1)$  of a Knight piece. You need to find the minimum number of moves the Knight needs to reach the target position  $(x_2, y_2)$ . If it is not possible to reach the target, print  $-1$ .



Moves of a Knight in Chess

The Knight can move one step in any of the 8 possible directions as shown in the picture.

#### Input

The first line contains an integer  $(1 \leq N \leq 2 \times 10^3)$  — the size of the chessboard.

The second line contains four integers  $(1 \leq x_1, y_1, x_2, y_2 \leq N)$  — the initial position  $(x_1, y_1)$  and the target position  $(x_2, y_2)$  of the Knight on the chessboard.

#### Output

Print the minimum number of moves the Knight needs to reach the target position. If it's not possible, print  $-1$ .

input
3
1 2 1 3
output
3

input
3
1 1 2 2
output
-1

input
10
8 4 3 1
output
4

### D. What's the Diameter?

1 second🕒, 1024 megabytes

You are given an **undirected connected** graph with  $N$  nodes and  $N - 1$  edges. Your task is to find two nodes such that the path between those two nodes is the longest possible in the graph.

#### Input

The first line contains one integer  $N$   $(2 \leq N \leq 200000)$  — the number of nodes.

The next  $N - 1$  lines will contain two integers  $u_i, v_i$   $(1 \leq u_i, v_i \leq N)$  — denoting there is a bidirectional road between  $u_i$  and  $v_i$ .

#### Output

On the first line, print a single integer — the length of the longest path.  
 On the second line, print two integers A and B — the nodes that form this longest path. If multiple pairs exist, you may print any one.

input
5
5 1
1 4
4 2
3 2
output
4
3 5

input
5
1 2
5 3
3 2
2 4
output
3
5 1

input
8
1 7
7 3
3 6
6 5
5 2
2 8
8 4
output
7
4 1

input
7
7 5
5 6
6 1
1 3
3 4
4 2
output
6
7 2

### E. Nearest Tour Destination

1 second🕒, 256 megabytes

**Forbidden Keywords for the Quiz:** open, file, creat(, fstream, thread, process, system(, exec(

You are given an **undirected unweighted** graph with  $N$  nodes and  $M$  edges. The nodes are numbered from 1 to  $N$ . The graph contains no self-loops and no multiple edges.

There are  $S$  sources and  $Q$  destinations. For each destination node, find the length of the shortest path from any source node to that destination. If a destination is unreachable from all sources, output  $-1$ .

#### Input

The first line contains four integers  $N, M, S, Q$   
 $1 \leq N \leq 2 \times 10^5, 0 \leq M \leq 3 \times 10^5, 1 \leq S \leq N, 1 \leq Q \leq N$  — the number of nodes, the number of edges, the number of source nodes, and the number of destination nodes.

The next  $M$  lines will contain two integers  $u_i, v_i (1 \leq u_i, v_i \leq N)$  — denoting there is an edge from node  $u_i$  to node  $v_i$ .

The next line contains  $S$  ( $1 \leq S_i \leq N$ ) integers representing the source nodes, and the final line contains  $Q$  ( $1 \leq Q_i \leq N$ ) integers representing the destination nodes. A node may appear both as a source and as a destination.

#### Output

The output should consist of  $Q$  integers separated by spaces. The  $j$ -th integer denotes the length of the shortest path from any source node to the  $j$ -th destination node. If no such path exists for a destination node, print  $-1$  for that destination. A node may be both a source and a destination, in which case the answer for that destination is 0.

input
8 6 2 4
1 2
2 3
4 5
6 7
7 8
2 6
1 6
3 5 6 8
output
2 -1 0 2

input
18 17 4 10
1 2
2 3
3 4
4 1
3 5
5 6
6 7
8 9
9 10
10 8
10 11
11 12
9 13
13 14
15 16
16 17
17 15
15 1 6 8
14 3 10 7 1 12 11 5 18 16
output
3 2 1 1 0 3 2 1 -1 1

### F. Number Transformation

1 second🕒, 256 megabytes

In this problem, you are given an integer number  $s$ . You can transform any integer number  $A$  to another integer number  $B$  by adding  $x$  to  $A$ . This  $x$  is an integer number which is a prime factor of  $A$  (please note that 1 and  $A$  are not being considered as a factor of  $A$ ). Now, your task is to find the minimum number of transformations required to transform  $s$  to another integer number  $t$ .

#### Input

Input starts with an integer  $T$  ( $1 \leq T \leq 500$ ), denoting the number of test cases.

Each case contains two integers:  $s$  ( $1 \leq s \leq 100$ ) and  $t$  ( $1 \leq t \leq 5000$ ).

#### Output

For each case, print the minimum number of transformations needed. If it's impossible, then print  $-1$ .

input
2
6 12
6 13
output
2
-1

### G. An Ancient Ordering

1 second🕒, 256 megabytes

You have found an old dictionary containing **N** words. The words are stored in an order that is different from the regular Latin lexicographic order.

Your task is to determine the order of the alphabet that satisfies the lexicographic order of this dictionary. If there are multiple valid orders, print the **lexicographically smallest** one. For example, the sequence  $S_1 = \text{"d x i k"}$  is lexicographically smaller than the sequence  $S_2 = \text{"d x p a k"}$ .

If no such valid sequence exists, print  $-1$ . A valid ordering is not possible if the characters create cyclic dependencies or if a longer word appears before a shorter word that is a prefix of it.

Input

The first line contains an integer  $N$  ( $1 \leq N \leq 1000$ ) — the number of words in the dictionary.

The next  $N$  line contains a string  $S$  ( $1 \leq |S| \leq 100$ ). Each word consists of only lowercase Latin letters  $a - z$ .

Output

Find out the order of the alphabets that satisfy the sorting order of the words in the given dictionary. If there are multiple valid orders, print the **lexicographically smallest** one. If no such valid sequence exists, print  $-1$ .

input
3 eat tea ate
output
eta

input
9 error tooth tot teeth their there thi tie hit
output
oethir

input
6 gef gie hf hd hc ha
output
efdcaghi

input
5 cmwaqe yent jtdgx wlp xufjpf
output
acdefglmpqtuyjwx

input
6 abc ab p pq pqr pqrs
output
-1

input
2 pigeon pigeons
output
eginops

input
4 ab bc ca ac
output
-1