

# Mass Distributions of Spiral Galaxies

## 1 Introduction

The astronomer Edwin Hubble, in a series of lectures given at Yale in 1935<sup>1</sup>, provided a classification of galaxies, which he referred to as *extragalactic nebulae*, into spiral and elliptic. This classification is used even today by amateur and professional astronomers alike, though the expanded version provided by French astronomer Gérard de Vaucouleurs is preferable. But nowadays, the morphological classification of galaxies — classifying galaxies based on what we perceive their shape to be — is done computationally.

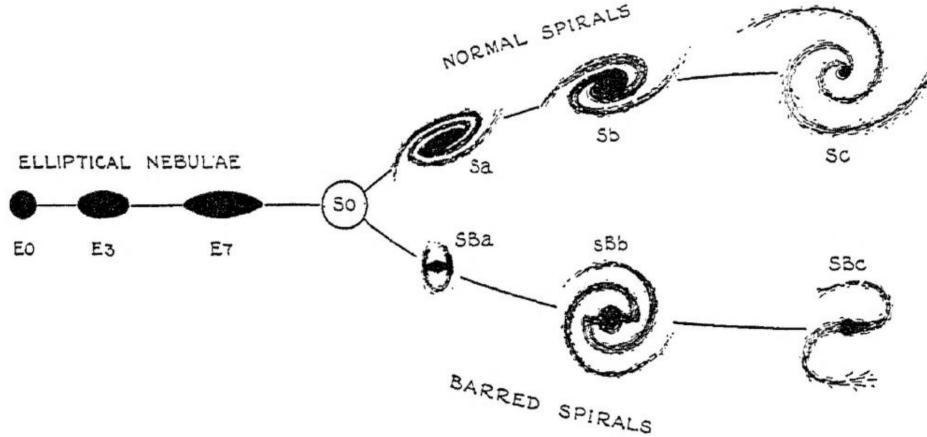


Figure 1: Hubble's "tuning fork" classification scheme, p. 45, [Hub36].

What has enabled such computational work is the significant progress in our ability to make precise astronomical observations over large distances and use them to make physical deductions. One specific instance of this is the use of spectroscopy to understand the motion of galaxies relative to us, in which one measures at two separate occasions the electromagnetic spectrum radiated by a galaxy using a *spectrometer* and uses the shift observed in the emission lines to calculate the speed at which the galaxy is moving relative to us. By making this measurement at different distances from the center of a galaxy, under the assumption that a galaxy is centrally symmetric, and accounting for the inclination possessed by the galaxy when we observe it, we can plot the *rotation curve* of a galaxy; a plot of the rotational velocity against the galactocentric radius.

<sup>1</sup>These lectures were later published under the title *The Realm of the Nebulae* [Hub36].

Since the velocity of a body in circular motion can be related to its mass using Newton's second law, I therefore explore the rotation curves of spiral galaxies under the following research question:

*How is the gravitational mass of a spiral galaxy distributed within its disc, and how is this distribution determined by the rotational velocities?*

## 2 Theory

Consider a spherical gas cloud of radius  $R$  and uniform density  $\rho$  that is rotating about its centre. The rotational speed  $v_{\text{rot}}$  of a particle of mass  $m$  at distance  $r$  from the centre can be found using Newton's law of gravitation and second law of motion, which give us

$$\frac{mv_{\text{rot}}^2}{r} = \frac{GmM}{r^2},$$

or simply

$$v_{\text{rot}} = \sqrt{GM/r}, \quad (1)$$

where  $M$  is the mass of the cloud internal to the particle, naturally called the *cumulative mass of the galaxy*. Substituting

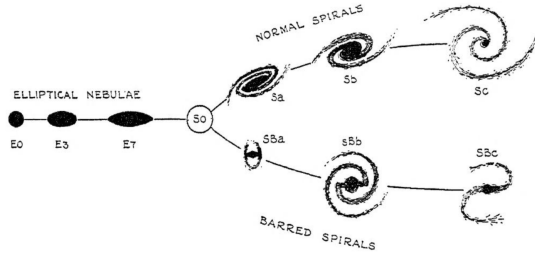
$$M = \begin{cases} \frac{4}{3}\rho\pi r^3 & (r < R) \\ \frac{4}{3}\rho\pi R^3 & (r \geq R) \end{cases} \quad (2)$$

into Equation (1) gives

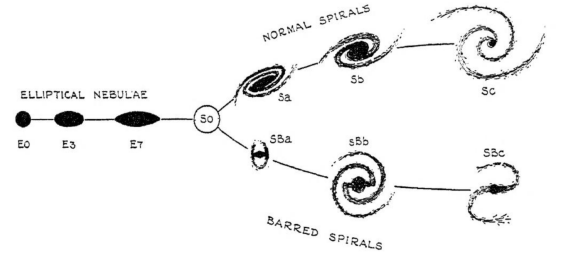
$$v_{\text{rot}} = \begin{cases} \sqrt{\frac{G \cdot \frac{4}{3}\pi\rho r^3}{r}} = \sqrt{\frac{4\rho G\pi}{3}}r & (r < R) \\ \sqrt{\frac{G \cdot \frac{4}{3}\pi\rho R^3}{r}} = \sqrt{\frac{4\rho G\pi R^3}{3}}r^{-1/2} & (r \geq R) \end{cases}. \quad (3)$$

So for a spiral galaxy that can be accurately modelled as a spherical gas cloud of uniform density, we can graph its expected rotation curve and cumulative mass distribution as described by Equations (2) and (3); see Figure 2. Note that in this paper we use astronomical units of measurement to ease our calculations: masses are in *solar masses* ( $M_{\odot}$ ), distances are in *kiloparsecs* (kpc), and velocities and speeds are in *kilometers per second* (km/s).

However, as we shall see, the actual rotation curve of a spiral galaxy as well as the actual cumulative mass distribution does not look as in Figure 2.



(a) Rotation curve



(b) Cumulative mass distribution

Figure 2: Expected rotation curve and cumulative mass distribution for a galaxy.

### 3 Method

This paper attempts to answer the proposed research question by analysing rotation curve data on the following galaxies: NGC0024, NGC0289, NGC1003, NGC2366, NGC2403. The paper relies on two main sources for relevant data. The observed velocities at various distances from the centres of these galaxies and the inclinations of the galaxies are taken from [LMS16], which is a database of 175 spiral and irregular galaxies (including the ones mentioned above) using photometric and spectroscopic measurements from the Spitzer Space Telescope. The chosen galaxies are all of them intentionally spiral galaxies, as the theory developed in Section 2 would not remain accurate for irregulars. In addition to this database, the paper also makes use of the NASA/IPAC Extragalactic Database to ascertain the diameter of the visible disc of each of the chosen galaxies.

The paper proceeds as follows. Section 4 tabulates all of the raw data required from the aforementioned databases; this includes the radii and inclinations of the galaxies, as well as a table for each galaxy tabulating observed velocities at different distances from the centre. Section 5 uses this information to compute and plot the rotation curves and cumulative mass distributions of all of the galaxies. These graphs are analysed in Section 6, and conclusions are presented in Section 7. Finally, Section 8 provides a brief evaluation of the uncertainties involved.

### 4 Raw Data

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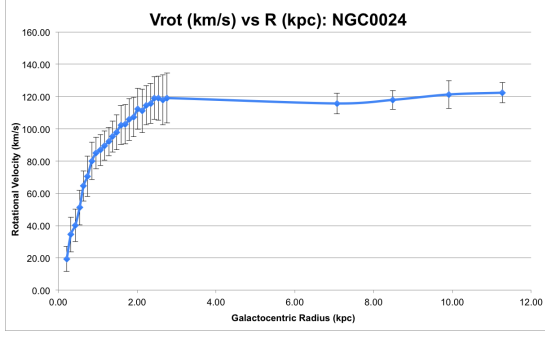
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Galaxy	Diameter (kpc)	Inclination ( $^{\circ}$ )
NGC0024	19.32	$64.0 \pm 3.0$
NGC0289	70.47	$46.0 \pm 5.0$
NGC1003	19.32	$67.0 \pm 5.0$
NGC2366	8.35	$68.0 \pm 5.0$
NGC2403	27.69	$63.0 \pm 3.0$

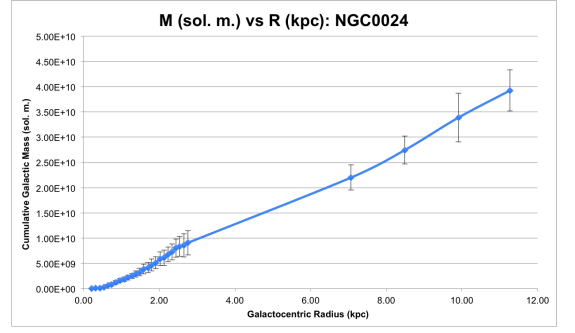
Table 1: Diameters (NASA) and inclinations (SPARC).

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NGC0024	
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{obs}}$ (km/s)
0.21	$17.40 \pm 6.51$
0.32	$31.00 \pm 8.86$
0.43	$36.10 \pm 8.16$
0.54	$46.00 \pm 8.52$
0.64	$58.00 \pm 6.90$
0.74	$63.40 \pm 9.55$
0.85	$71.90 \pm 8.52$
0.96	$76.40 \pm 6.82$
1.07	$78.10 \pm 6.65$
1.17	$80.50 \pm 6.14$
1.28	$82.80 \pm 5.80$
1.38	$85.60 \pm 6.48$
1.48	$88.00 \pm 7.50$
1.59	$92.00 \pm 8.52$
1.70	$92.40 \pm 8.52$
1.80	$95.10 \pm 9.20$
1.91	$96.50 \pm 8.52$
2.02	$101.00 \pm 8.86$
2.13	$99.90 \pm 9.55$
2.23	$103.00 \pm 8.18$
2.34	$104.00 \pm 8.52$
2.44	$107.00 \pm 9.20$
2.54	$107.00 \pm 9.55$
2.65	$106.00 \pm 11.20$
2.76	$107.00 \pm 11.20$
7.07	$104.00 \pm 3.11$
8.49	$106.00 \pm 2.55$
9.91	$109.00 \pm 4.95$
11.27	$110.00 \pm 2.83$

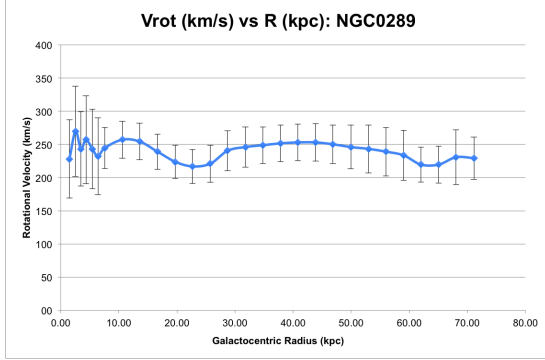


(a) Rotation curve

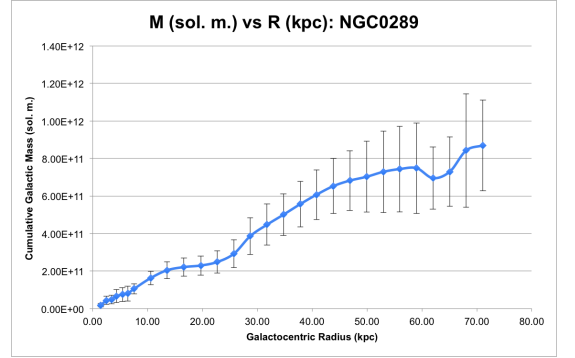


(b) Cumulative mass distribution

Figure 3: Rotation curve and cumulative mass distribution for NGC0024.

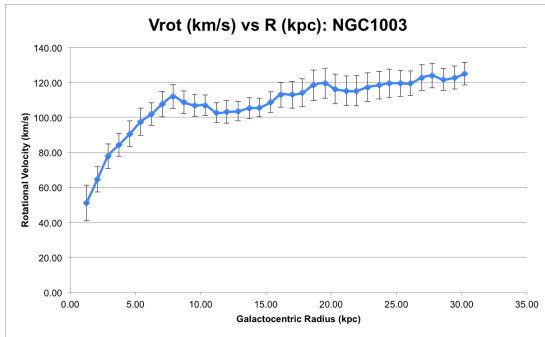


(a) Rotation curve

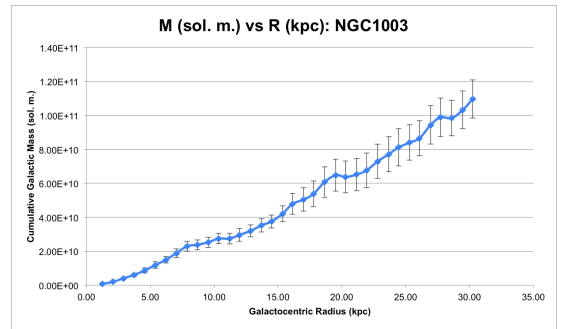


(b) Cumulative mass distribution

Figure 4: Rotation curve and cumulative mass distribution for NGC0289.

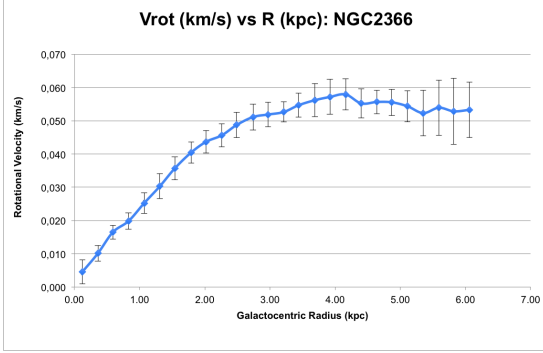


(a) Rotation curve

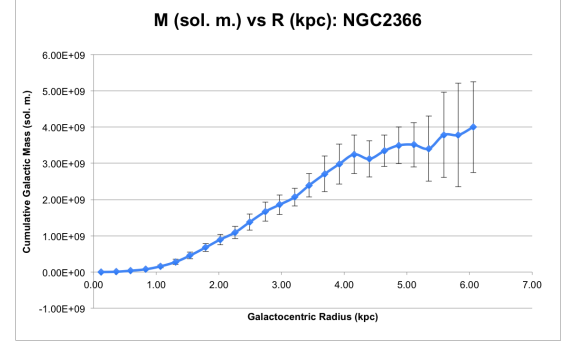


(b) Cumulative mass distribution

Figure 5: Rotation curve and cumulative mass distribution for NGC1003.

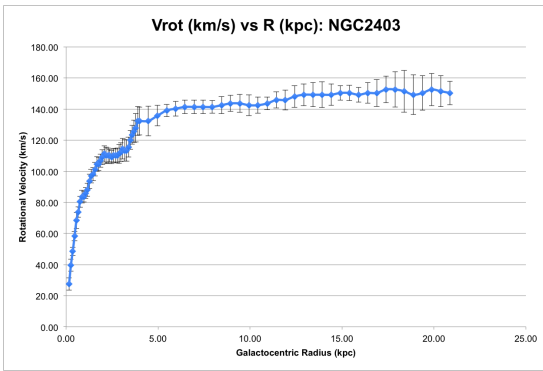


(a) Rotation curve

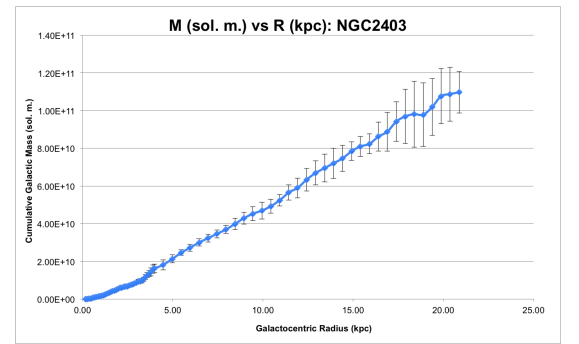


(b) Cumulative mass distribution

Figure 6: Rotation curve and cumulative mass distribution for NGC2366.



(a) Rotation curve



(b) Cumulative mass distribution

Figure 7: Rotation curve and cumulative mass distribution for NGC2403.

NGC0289	
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{obs}}$ (km/s)
1.50	$164.00 \pm 28.20$
2.52	$194.00 \pm 32.00$
3.46	$175.00 \pm 25.20$
4.32	$185.00 \pm 31.50$
5.43	$175.00 \pm 27.90$
6.38	$167.00 \pm 27.20$
7.57	$176.00 \pm 7.18$
10.60	$185.00 \pm 4.29$
13.57	$183.00 \pm 4.22$
16.64	$172.00 \pm 4.33$
19.71	$161.00 \pm 4.24$
22.68	$156.00 \pm 5.08$
25.75	$159.00 \pm 6.49$
28.72	$173.00 \pm 6.97$
31.79	$177.00 \pm 6.57$
34.77	$179.00 \pm 4.47$
37.84	$181.00 \pm 4.26$
40.81	$182.00 \pm 4.26$
43.88	$182.00 \pm 4.83$
46.85	$180.00 \pm 5.50$
49.92	$177.00 \pm 8.50$
52.99	$175.00 \pm 11.00$
55.96	$172.00 \pm 11.60$
59.03	$168.00 \pm 12.60$
62.00	$158.00 \pm 5.38$
65.07	$158.00 \pm 6.50$
68.05	$166.00 \pm 15.50$
71.12	$165.00 \pm 8.75$

## 5 Processed Data

## 6 Analysis

## 7 Conclusion

- Analysis provides basis for dark matter.
- Mention possible forms of dark matter (WIMPs, etc.)
- Mention alternatives to dark matter (MOND).

## 8 Evaluation

- Where does uncertainty come from?
- How does this uncertainty affect the conclusion?

## References

- [Hub36] Edwin Hubble. *The Realm of the Nebulae*. New Haven, CT: Yale University Press, 1936.
- [LMS16] Federico Lelli, Stacy S. McGaugh, and James M. Schombert. “SPARC: Mass Models for 175 Disk Galaxies with Spitzer Photometry and Accurate Rotation Curves”. In: (2016). DOI: 10.3847/0004-6256/152/6/157.



NGC1003
$r$ (kpc $\pm$ 0.01 kpc)
$v_{\text{obs}}$ (km/s)

1.25
47.00 $\pm$ 7.60
2.08
59.50 $\pm$ 4.50
2.90
71.60 $\pm$ 3.70
3.73
77.60 $\pm$ 3.10
4.56
83.40 $\pm$ 3.60
5.39
89.70 $\pm$ 3.80
6.22
93.80 $\pm$ 2.40
7.04
99.00 $\pm$ 3.00
7.87
103.00 $\pm$ 2.50
8.70
100.00 $\pm$ 2.30
9.54
98.30 $\pm$ 2.00
10.34
98.40 $\pm$ 1.70
11.21
94.50 $\pm$ 1.80
11.98
94.90 $\pm$ 2.40
12.85
95.30 $\pm$ 1.60
13.72
96.90 $\pm$ 1.80
14.49
97.20 $\pm$ 1.30
15.36
100.00 $\pm$ 1.80
16.13
104.00 $\pm$ 2.70
17.00
104.00 $\pm$ 3.20
17.78
105.00 $\pm$ 3.40
18.65
109.00 $\pm$ 3.90
19.52
110.00 $\pm$ 3.80
20.29
107.00 $\pm$ 3.80
21.16
106.00 $\pm$ 3.80
21.93
106.00 $\pm$ 4.00
22.80
108.00 $\pm$ 3.40
23.67
109.00 $\pm$ 3.20
24.44
110.00 $\pm$ 3.30
25.31

NGC2366
$r$ (kpc $\pm$ 0.01 kpc)
$v_{\text{obs}}$ (km/s)
0.12
4.20 $\pm$ 3.15
0.36
9.41 $\pm$ 1.83
0.59
15.30 $\pm$ 1.37
0.83
18.40 $\pm$ 1.64
1.07
23.40 $\pm$ 2.08
1.31
28.10 $\pm$ 2.46
1.54
33.10 $\pm$ 2.01
1.79
37.50 $\pm$ 1.62
2.02
40.50 $\pm$ 1.68
2.26
42.30 $\pm$ 1.69
2.49
45.20 $\pm$ 1.91
2.74
47.40 $\pm$ 1.95
2.97
48.10 $\pm$ 1.74
3.21
48.80 $\pm$ 1.08
3.44
50.70 $\pm$ 1.55
3.69
52.10 $\pm$ 2.78
3.92
53.00 $\pm$ 2.98
4.16
53.70 $\pm$ 2.39
4.40
51.20 $\pm$ 2.21
4.64
51.60 $\pm$ 1.45
4.87
51.50 $\pm$ 1.84
5.11
50.40 $\pm$ 2.53
5.35
48.50 $\pm$ 4.60
5.59
50.00 $\pm$ 5.91
5.82
49.00 $\pm$ 7.42
6.06
49.40 $\pm$ 5.92

NGC2403
$r$ (kpc $\pm$ 0.01 kpc)
$v_{\text{obs}}$ (km/s)

0.16
24.50 $\pm$ 2.83
0.26
35.30 $\pm$ 2.46
0.36
43.20 $\pm$ 1.12
0.46
52.00 $\pm$ 1.25
0.56
60.90 $\pm$ 2.93
0.66
65.80 $\pm$ 1.25
0.76
71.70 $\pm$ 1.25
0.86
74.60 $\pm$ 1.60
0.96
74.60 $\pm$ 1.03
1.06
76.60 $\pm$ 1.12
1.16
78.50 $\pm$ 1.60
1.27
83.40 $\pm$ 1.80
1.36
86.40 $\pm$ 1.60
1.47
87.40 $\pm$ 1.41
1.57
90.30 $\pm$ 1.41
1.67
93.30 $\pm$ 1.60
1.77
93.30 $\pm$ 1.41
1.87
95.20 $\pm$ 1.25
1.97
97.20 $\pm$ 1.60
2.08
99.10 $\pm$ 2.02
2.18
98.20 $\pm$ 2.02
2.28
98.20 $\pm$ 1.60
2.37
98.20 $\pm$ 1.00
2.47
97.20 $\pm$ 1.12
2.57
98.20 $\pm$ 1.41
2.68
98.20 $\pm$ 1.12
2.78
98.20 $\pm$ 1.60
2.88
99.10 $\pm$ 2.69
2.98
100.00 $\pm$ 2.69
3.08

NGC0024		
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{rot}}$ (km/s)	$M$ ( $M_{\odot}$ )
0.21	$19.36 \pm 7.8$	$1.83 \times 10^{07} \pm 1.55 \times 10^{07}$
0.32	$34.49 \pm 10.8$	$8.85 \times 10^{07} \pm 5.80 \times 10^{07}$
0.43	$40.16 \pm 10.1$	$1.61 \times 10^{08} \pm 8.51 \times 10^{07}$
0.54	$51.18 \pm 10.8$	$3.29 \times 10^{08} \pm 1.45 \times 10^{08}$
0.64	$64.53 \pm 9.3$	$6.20 \times 10^{08} \pm 1.89 \times 10^{08}$
0.74	$70.54 \pm 12.5$	$8.56 \times 10^{08} \pm 3.14 \times 10^{08}$
0.85	$80.00 \pm 11.5$	$1.26 \times 10^{09} \pm 3.80 \times 10^{08}$
0.96	$85.00 \pm 9.8$	$1.61 \times 10^{09} \pm 3.88 \times 10^{08}$
1.07	$86.89 \pm 9.6$	$1.88 \times 10^{09} \pm 4.34 \times 10^{08}$
1.17	$89.56 \pm 9.1$	$2.18 \times 10^{09} \pm 4.64 \times 10^{08}$
1.28	$92.12 \pm 8.8$	$2.53 \times 10^{09} \pm 5.04 \times 10^{08}$
1.38	$95.24 \pm 9.7$	$2.91 \times 10^{09} \pm 6.12 \times 10^{08}$
1.48	$97.91 \pm 10.9$	$3.30 \times 10^{09} \pm 7.55 \times 10^{08}$
1.59	$102.4 \pm 12.1$	$3.87 \times 10^{09} \pm 9.42 \times 10^{08}$
1.70	$102.8 \pm 12.1$	$4.18 \times 10^{09} \pm 1.01 \times 10^{09}$
1.80	$105.8 \pm 13.0$	$4.69 \times 10^{09} \pm 1.17 \times 10^{09}$
1.91	$107.4 \pm 12.2$	$5.12 \times 10^{09} \pm 1.19 \times 10^{09}$
2.02	$112.4 \pm 12.8$	$5.93 \times 10^{09} \pm 1.38 \times 10^{09}$
2.13	$111.1 \pm 13.5$	$6.12 \times 10^{09} \pm 1.51 \times 10^{09}$
2.23	$114.6 \pm 12.1$	$6.81 \times 10^{09} \pm 1.46 \times 10^{09}$
2.34	$115.7 \pm 12.5$	$7.28 \times 10^{09} \pm 1.60 \times 10^{09}$
2.44	$119.0 \pm 13.3$	$8.04 \times 10^{09} \pm 1.83 \times 10^{09}$
2.54	$119.0 \pm 13.7$	$8.37 \times 10^{09} \pm 1.96 \times 10^{09}$
2.65	$117.9 \pm 15.5$	$8.57 \times 10^{09} \pm 2.29 \times 10^{09}$
2.76	$119.0 \pm 15.5$	$9.09 \times 10^{09} \pm 2.41 \times 10^{09}$
7.07	$115.7 \pm 6.4$	$2.20 \times 10^{10} \pm 2.48 \times 10^{09}$
8.49	$117.9 \pm 5.9$	$2.75 \times 10^{10} \pm 2.76 \times 10^{09}$
9.91	$121.3 \pm 8.6$	$3.39 \times 10^{10} \pm 4.85 \times 10^{09}$
11.27	$122.4 \pm 6.3$	$3.92 \times 10^{10} \pm 4.07 \times 10^{09}$

NGC0289		
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{rot}}$ (km/s)	$M$ ( $M_{\odot}$ )
1.50	$228.0 \pm 59.1$	$1.81 \times 10^{10} \pm 1 \times 10^{10}$
2.52	$269.7 \pm 68.0$	$4.26 \times 10^{10} \pm 2 \times 10^{10}$
3.46	$243.3 \pm 56.2$	$4.76 \times 10^{10} \pm 2 \times 10^{10}$
4.32	$257.2 \pm 66.2$	$6.64 \times 10^{10} \pm 3 \times 10^{10}$
5.43	$243.3 \pm 60.0$	$7.47 \times 10^{10} \pm 4 \times 10^{10}$
6.38	$232.2 \pm 58.1$	$8.00 \times 10^{10} \pm 4 \times 10^{10}$
7.57	$244.7 \pm 31.0$	$1.05 \times 10^{11} \pm 3 \times 10^{10}$
10.60	$257.2 \pm 28.0$	$1.63 \times 10^{11} \pm 4 \times 10^{10}$
13.57	$254.4 \pm 27.7$	$2.04 \times 10^{11} \pm 4 \times 10^{10}$
16.64	$239.1 \pm 26.5$	$2.21 \times 10^{11} \pm 5 \times 10^{10}$
19.71	$223.8 \pm 25.1$	$2.30 \times 10^{11} \pm 5 \times 10^{10}$
22.68	$216.9 \pm 25.7$	$2.48 \times 10^{11} \pm 6 \times 10^{10}$
25.75	$221.0 \pm 28.0$	$2.93 \times 10^{11} \pm 7 \times 10^{10}$
28.72	$240.5 \pm 30.3$	$3.86 \times 10^{11} \pm 1 \times 10^{11}$
31.79	$246.1 \pm 30.3$	$4.48 \times 10^{11} \pm 1 \times 10^{11}$
34.77	$248.8 \pm 27.5$	$5.01 \times 10^{11} \pm 1 \times 10^{11}$
37.84	$251.6 \pm 27.5$	$5.57 \times 10^{11} \pm 1 \times 10^{11}$
40.81	$253.0 \pm 27.6$	$6.07 \times 10^{11} \pm 1 \times 10^{11}$
43.88	$253.0 \pm 28.4$	$6.53 \times 10^{11} \pm 1 \times 10^{11}$
46.85	$250.2 \pm 29.1$	$6.82 \times 10^{11} \pm 2 \times 10^{11}$
49.92	$246.1 \pm 33.0$	$7.03 \times 10^{11} \pm 2 \times 10^{11}$
52.99	$243.3 \pm 36.2$	$7.29 \times 10^{11} \pm 2 \times 10^{11}$
55.96	$239.1 \pm 36.7$	$7.44 \times 10^{11} \pm 2 \times 10^{11}$
59.03	$233.5 \pm 37.7$	$7.49 \times 10^{11} \pm 2 \times 10^{11}$
62.00	$219.6 \pm 26.3$	$6.95 \times 10^{11} \pm 2 \times 10^{11}$
65.07	$219.6 \pm 27.9$	$7.30 \times 10^{11} \pm 2 \times 10^{11}$
68.05	$230.8 \pm 41.5$	$8.43 \times 10^{11} \pm 3 \times 10^{11}$
71.12	$229.4 \pm 31.9$	$8.70 \times 10^{11} \pm 2 \times 10^{11}$

NGC1003		
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{rot}}$ (km/s)	$M$ ( $M_{\odot}$ )
1.25	$51.06 \pm 10.2$	$7.58 \times 10^{08} \pm 3 \times 10^{08}$
2.08	$64.64 \pm 7.3$	$2.02 \times 10^{09} \pm 5 \times 10^{08}$
2.90	$77.78 \pm 6.9$	$4.08 \times 10^{09} \pm 7 \times 10^{08}$
3.73	$84.30 \pm 6.5$	$6.16 \times 10^{09} \pm 1 \times 10^{09}$
4.56	$90.60 \pm 7.3$	$8.70 \times 10^{09} \pm 1 \times 10^{09}$
5.39	$97.45 \pm 7.8$	$1.19 \times 10^{10} \pm 2 \times 10^{09}$
6.22	$101.9 \pm 6.4$	$1.50 \times 10^{10} \pm 2 \times 10^{09}$
7.04	$107.5 \pm 7.3$	$1.89 \times 10^{10} \pm 3 \times 10^{09}$
7.87	$111.9 \pm 6.9$	$2.29 \times 10^{10} \pm 3 \times 10^{09}$
8.70	$108.6 \pm 6.6$	$2.39 \times 10^{10} \pm 3 \times 10^{09}$
9.54	$106.8 \pm 6.2$	$2.53 \times 10^{10} \pm 3 \times 10^{09}$
10.34	$106.9 \pm 5.8$	$2.75 \times 10^{10} \pm 3 \times 10^{09}$
11.21	$102.7 \pm 5.8$	$2.75 \times 10^{10} \pm 3 \times 10^{09}$
11.98	$103.1 \pm 6.5$	$2.96 \times 10^{10} \pm 4 \times 10^{09}$
12.85	$103.5 \pm 5.6$	$3.20 \times 10^{10} \pm 3 \times 10^{09}$
13.72	$105.3 \pm 5.9$	$3.53 \times 10^{10} \pm 4 \times 10^{09}$
14.49	$105.6 \pm 5.4$	$3.76 \times 10^{10} \pm 4 \times 10^{09}$
15.36	$108.6 \pm 6.0$	$4.21 \times 10^{10} \pm 5 \times 10^{09}$
16.13	$113.0 \pm 7.2$	$4.79 \times 10^{10} \pm 6 \times 10^{09}$
17.00	$113.0 \pm 7.7$	$5.05 \times 10^{10} \pm 7 \times 10^{09}$
17.78	$114.1 \pm 8.0$	$5.38 \times 10^{10} \pm 8 \times 10^{09}$
18.65	$118.4 \pm 8.7$	$6.08 \times 10^{10} \pm 9 \times 10^{09}$
19.52	$119.5 \pm 8.6$	$6.48 \times 10^{10} \pm 9 \times 10^{09}$
20.29	$116.2 \pm 8.5$	$6.37 \times 10^{10} \pm 9 \times 10^{09}$
21.16	$115.2 \pm 8.4$	$6.52 \times 10^{10} \pm 1 \times 10^{10}$
21.93	$115.2 \pm 8.7$	$6.76 \times 10^{10} \pm 1 \times 10^{10}$
22.80	$117.3 \pm 8.1$	$7.30 \times 10^{10} \pm 1 \times 10^{10}$
23.67	$118.4 \pm 7.9$	$7.72 \times 10^{10} \pm 1 \times 10^{10}$
24.44	$119.5 \pm 8.1$	$8.11 \times 10^{10} \pm 1 \times 10^{10}$
25.31	$119.5 \pm 7.4$	$8.40 \times 10^{10} \pm 1 \times 10^{10}$
26.08	$119.5 \pm 7.1$	$8.66 \times 10^{10} \pm 1 \times 10^{10}$
26.95	$122.8 \pm 7.3$	$9.44 \times 10^{10} \pm 1 \times 10^{10}$
27.73	$123.8 \pm 7.0$	$9.89 \times 10^{10} \pm 1 \times 10^{10}$
28.60	$121.7 \pm 6.4$	$9.84 \times 10^{10} \pm 1 \times 10^{10}$
29.47	$122.8 \pm 6.5$	$1.03 \times 10^{11} \pm 1 \times 10^{10}$
30.24	$124.9 \pm 6.4$	$1.10 \times 10^{11} \pm 1 \times 10^{10}$

NGC2366		
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{rot}}$ (km/s)	$M$ ( $M_{\odot}$ )
0.12	$4.530 \pm 3.6$	$5.73 \times 10^{05} \pm 1 \times 10^{06}$
0.36	$10.15 \pm 2.3$	$8.62 \times 10^{06} \pm 4 \times 10^{06}$
0.59	$16.50 \pm 2.1$	$3.74 \times 10^{07} \pm 1 \times 10^{07}$
0.83	$19.85 \pm 2.5$	$7.60 \times 10^{07} \pm 2 \times 10^{07}$
1.07	$25.24 \pm 3.2$	$1.58 \times 10^{08} \pm 4 \times 10^{07}$
1.31	$30.31 \pm 3.7$	$2.80 \times 10^{08} \pm 7 \times 10^{07}$
1.54	$35.70 \pm 3.4$	$4.56 \times 10^{08} \pm 9 \times 10^{07}$
1.79	$40.45 \pm 3.2$	$6.81 \times 10^{08} \pm 1 \times 10^{08}$
2.02	$43.68 \pm 3.4$	$8.96 \times 10^{08} \pm 1 \times 10^{08}$
2.26	$45.62 \pm 3.5$	$1.09 \times 10^{09} \pm 2 \times 10^{08}$
2.49	$48.75 \pm 3.8$	$1.38 \times 10^{09} \pm 2 \times 10^{08}$
2.74	$51.12 \pm 3.9$	$1.67 \times 10^{09} \pm 3 \times 10^{08}$
2.97	$51.88 \pm 3.7$	$1.86 \times 10^{09} \pm 3 \times 10^{08}$
3.21	$52.63 \pm 3.0$	$2.07 \times 10^{09} \pm 2 \times 10^{08}$
3.44	$54.68 \pm 3.6$	$2.39 \times 10^{09} \pm 3 \times 10^{08}$
3.69	$56.19 \pm 5.0$	$2.71 \times 10^{09} \pm 5 \times 10^{08}$
3.92	$57.16 \pm 5.3$	$2.98 \times 10^{09} \pm 6 \times 10^{08}$
4.16	$57.92 \pm 4.6$	$3.24 \times 10^{09} \pm 5 \times 10^{08}$
4.40	$55.22 \pm 4.4$	$3.12 \times 10^{09} \pm 5 \times 10^{08}$
4.64	$55.65 \pm 3.5$	$3.34 \times 10^{09} \pm 4 \times 10^{08}$
4.87	$55.54 \pm 4.0$	$3.49 \times 10^{09} \pm 5 \times 10^{08}$
5.11	$54.36 \pm 4.7$	$3.51 \times 10^{09} \pm 6 \times 10^{08}$
5.35	$52.31 \pm 6.8$	$3.40 \times 10^{09} \pm 9 \times 10^{08}$
5.59	$53.93 \pm 8.3$	$3.78 \times 10^{09} \pm 1 \times 10^{09}$
5.82	$52.85 \pm 9.9$	$3.78 \times 10^{09} \pm 1 \times 10^{09}$
6.06	$53.28 \pm 8.3$	$4.00 \times 10^{09} \pm 1 \times 10^{09}$

NGC2403		
$r$ (kpc $\pm$ 0.01 kpc)	$v_{\text{rot}}$ (km/s)	$M$ ( $M_{\odot}$ )
0.16	$27.50 \pm 3.9$	$2.81 \times 10^{07} \pm 1 \times 10^{07}$
0.26	$39.62 \pm 3.8$	$9.49 \times 10^{07} \pm 2 \times 10^{07}$
0.36	$48.48 \pm 2.6$	$1.97 \times 10^{08} \pm 3 \times 10^{07}$
0.46	$58.36 \pm 3.0$	$3.64 \times 10^{08} \pm 4 \times 10^{07}$
0.56	$68.35 \pm 5.1$	$6.08 \times 10^{08} \pm 1 \times 10^{08}$
0.66	$73.85 \pm 3.4$	$8.37 \times 10^{08} \pm 9 \times 10^{07}$
0.76	$80.47 \pm 3.6$	$1.14 \times 10^{09} \pm 1 \times 10^{08}$
0.86	$83.73 \pm 4.0$	$1.40 \times 10^{09} \pm 2 \times 10^{08}$
0.96	$83.73 \pm 3.4$	$1.56 \times 10^{09} \pm 1 \times 10^{08}$
1.06	$85.97 \pm 3.6$	$1.82 \times 10^{09} \pm 2 \times 10^{08}$
1.16	$88.10 \pm 4.2$	$2.09 \times 10^{09} \pm 2 \times 10^{08}$
1.27	$93.60 \pm 4.5$	$2.59 \times 10^{09} \pm 3 \times 10^{08}$
1.36	$96.97 \pm 4.4$	$2.97 \times 10^{09} \pm 3 \times 10^{08}$
1.47	$98.09 \pm 4.2$	$3.29 \times 10^{09} \pm 3 \times 10^{08}$
1.57	$101.3 \pm 4.3$	$3.75 \times 10^{09} \pm 3 \times 10^{08}$
1.67	$104.7 \pm 4.6$	$4.26 \times 10^{09} \pm 4 \times 10^{08}$
1.77	$104.7 \pm 4.4$	$4.51 \times 10^{09} \pm 4 \times 10^{08}$
1.87	$106.8 \pm 4.3$	$4.96 \times 10^{09} \pm 4 \times 10^{08}$
1.97	$109.1 \pm 4.7$	$5.45 \times 10^{09} \pm 5 \times 10^{08}$
2.08	$111.2 \pm 5.2$	$5.98 \times 10^{09} \pm 6 \times 10^{08}$
2.18	$110.2 \pm 5.2$	$6.16 \times 10^{09} \pm 6 \times 10^{08}$
2.28	$110.2 \pm 4.7$	$6.44 \times 10^{09} \pm 6 \times 10^{08}$
2.37	$110.2 \pm 4.1$	$6.69 \times 10^{09} \pm 5 \times 10^{08}$
2.47	$109.1 \pm 4.2$	$6.83 \times 10^{09} \pm 6 \times 10^{08}$
2.57	$110.2 \pm 4.5$	$7.26 \times 10^{09} \pm 6 \times 10^{08}$
2.68	$110.2 \pm 4.2$	$7.57 \times 10^{09} \pm 6 \times 10^{08}$
2.78	$110.2 \pm 4.7$	$7.85 \times 10^{09} \pm 7 \times 10^{08}$
2.88	$111.2 \pm 6.0$	$8.28 \times 10^{09} \pm 9 \times 10^{08}$
2.98	$112.2 \pm 6.0$	$8.73 \times 10^{09} \pm 1 \times 10^{09}$
3.08	$114.5 \pm 6.6$	$9.38 \times 10^{09} \pm 1 \times 10^{09}$
3.19	$113.4 \pm 6.9$	$9.53 \times 10^{09} \pm 1 \times 10^{09}$
3.29	$113.4 \pm 6.9$	$9.83 \times 10^{09} \pm 1 \times 10^{09}$
3.39	$115.6 \pm 6.4$	$1.05 \times 10^{10} \pm 1 \times 10^{09}$
3.49	$120.1 \pm 6.0$	$1.17 \times 10^{10} \pm 1 \times 10^{09}$
3.59	$123.5 \pm 6.1$	$1.27 \times 10^{10} \pm 1 \times 10^{09}$
3.69	$125.7 \pm 7.2$	$1.36 \times 10^{10} \pm 2 \times 10^{09}$
3.79	$127.9 \pm 9.2$	$1.44 \times 10^{10} \pm 2 \times 10^{09}$
3.90	$132.4 \pm 9.3$	$1.59 \times 10^{10} \pm 2 \times 10^{09}$
3.99	$132.4 \pm 9.0$	$1.63 \times 10^{10} \pm 2 \times 10^{09}$
4.47	$132.4 \pm 9.6$	$1.82 \times 10^{10} \pm 3 \times 10^{09}$
4.97	$135.8 \pm 6.5$	$2.13 \times 10^{10} \pm 2 \times 10^{09}$
5.47	$139.2 \pm 4.0$	$2.46 \times 10^{10} \pm 1 \times 10^{09}$
5.96	$140.3 \pm 4.7$	$2.73 \times 10^{10} \pm 2 \times 10^{09}$
6.46	$141.4 \pm 4.3$	$3.00 \times 10^{10} \pm 2 \times 10^{09}$
6.96	$141.4 \pm 4.4$	$3.24 \times 10^{10} \pm 2 \times 10^{09}$
7.45	$141.4 \pm 4.3$	$3.46 \times 10^{10} \pm 2 \times 10^{09}$
7.95	$141.4 \pm 4.1$	$3.70 \times 10^{10} \pm 2 \times 10^{09}$
8.45	$142.5 \pm 5.4$	$3.99 \times 10^{10} \pm 3 \times 10^{09}$
8.94	$143.7 \pm 5.1$	$4.29 \times 10^{10} \pm 3 \times 10^{09}$
9.44	$143.7 \pm 5.7$	$4.53 \times 10^{10} \pm 4 \times 10^{09}$
9.94	$142.5 \pm 6.7$	$4.70 \times 10^{10} \pm 4 \times 10^{09}$
10.43	$142.5 \pm 5.2$	$4.93 \times 10^{10} \pm 4 \times 10^{09}$
10.93	$143.7 \pm 4.1$	$5.24 \times 10^{10} \pm 3 \times 10^{09}$
11.43	$145.9 \pm 5.2$	$5.66 \times 10^{10} \pm 4 \times 10^{09}$
11.92	$145.9 \pm 6.4$	$5.90 \times 10^{10} \pm 5 \times 10^{09}$
12.42	$148.1 \pm 7.0$	$6.34 \times 10^{10} \pm 6 \times 10^{09}$
12.92	$149.3 \pm 7.0$	$6.69 \times 10^{10} \pm 6 \times 10^{09}$
13.42	$149.3 \pm 7.8$	$6.95 \times 10^{10} \pm 7 \times 10^{09}$
13.91	$149.3 \pm 8.3$	$7.21 \times 10^{10} \pm 8 \times 10^{09}$
14.41	$149.3 \pm 6.9$	$7.47 \times 10^{10} \pm 7 \times 10^{09}$