HW7A

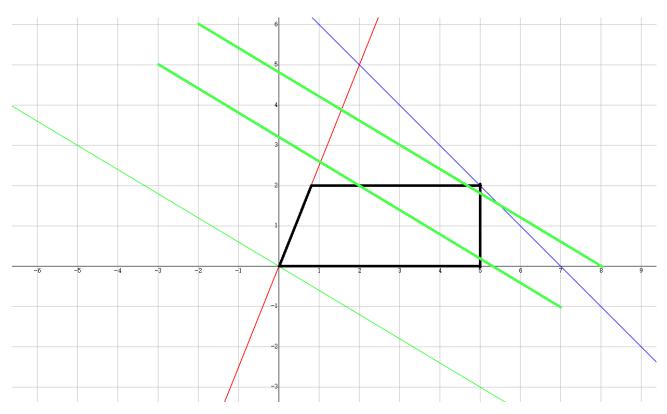
Section II

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7.1

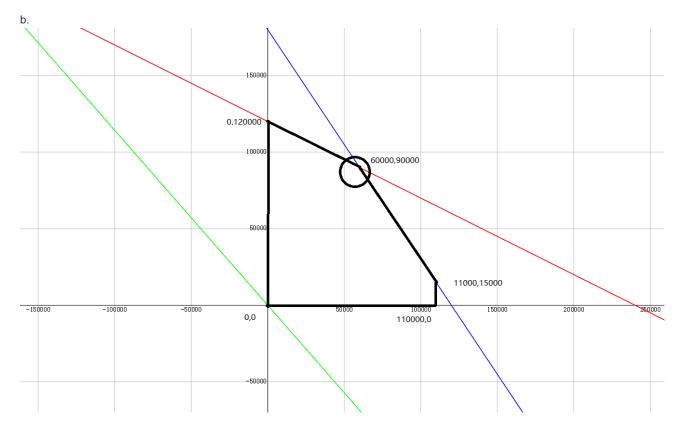


From picture we can see, the maximum value of the linear programming is when x=5,y=2, the result is 31.

7.5

a. x is the number of Frisky Pup, y is the number of Husky Hound.

$$\begin{array}{ll} \textit{maximize} & (7-1*1-2*1.5-1.4)x + (6-2*1-1*2-0.6)y \\ & 1.6x + 1.4y \\ x + 2y & \leq 240000 \\ 1.5x + y & \leq 180000 \\ x & \leq 110000 \\ x & \geq 0 \\ y & \geq 0 \end{array}$$



The max profit is when x = 60000 y = 90000, profit is 222000

7.8

We can introduce a variable ${\bf z}$ to replace the formula. z_m is the minimize

In standard form, the linear program is given by

Minimize \boldsymbol{z}_m for 1 to 7

$$egin{array}{ll} z & \geq a*x_i+b*y_i-c \ z & \geq -(a*x_i+b*y_i-c) \ z_m & > z \end{array}$$

7.10

The maxumun flow is 13, the mathing cur is($\{S,C,F\}$, $\{A,B,D,E,G,T\}$)

7.12

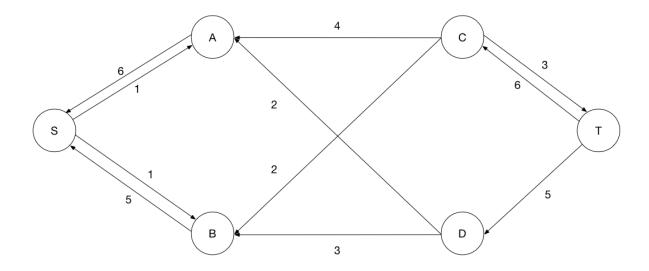
combine (a), (b), we can get:

$$egin{array}{lll} 2x_1-x_3 & \leq 3 \ x_1-x_3/2 & \leq 3/2 \ since \ x_3 \geq 0 \ x_1-2x_3 & \leq x_1-x_3/2 \leq 3/2 \end{array}$$

Thus, the optimal solution for x_1-2x_3 is 3/2, with $x_3=0$ when equality. So $(x_1,x_2,x_3)=(3/2,1/2,0)$ is optimal.

7.17

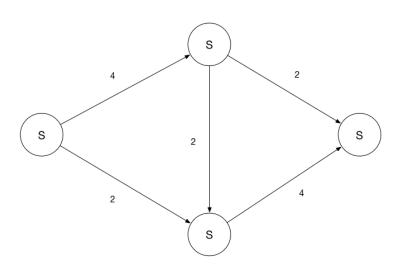
(a). Max Flow = 11, minimum cut = $\{(S, A, B), (C, D, T)\}$.



Nodes reachable from S are $\{A,B\}$, nodes reachable from T are $\{S,A,B,C,D\}$.

(c) Bottleneck edges are: e(A,C) and e(B,C). Inreasing both's capacity will increase the capacity going through node C, and thus increases the maximum flow.

(d)



- 1. Run the network flow algorithm and compute the residual graph R.
- 2. Run DFS on the residual graph R starting from node S. The nodes visited are those reachable by S, remember as set I.
- 3. Reverse the esidual graph R.
- 4. Run DFS from node T. Remember visited nodes as set J.
- 5. Last, go over all the vertices in the graph. If there exist an edge e(u, v), which $u \in J, v \in I$, then that edge is a bottleneck edge.