

Evaluating Workload and Machine Heterogeneity in Distributed Computing Systems

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Outline

- Distributed Heterogeneous Computing Systems
- Statistical Measures for Evaluating Heterogeneity
- Simulation Results
- Conclusions



Distributed Heterogeneous Computing System

- ✓ cluster of different types of machines
 - 5 varied computational capabilities among the system machines
- ✓ workload
 - 5 tasks with different computational requirements
- ✓ each task may perform differently on each machine
 - 5 furthermore: machine A can be better than machine B for task 1 but not for task 2
- ✓ resource allocation: assign tasks to machines to optimize some performance measure
 - 5 NP-complete (cannot find optimal in reasonable time)
 - 5 use heuristics to find near-optimal allocation



Estimated Time to Compute (ETC) Matrix

- ✓ ETC obtained from real world systems and benchmark data

		machines	
		m1	m2
tasks	t1	3	5
	t2	7	4
	t3	20	18

*estimated time to compute
task 1 on machine 1*

$ETC(1,1) = 3$

Machine Heterogeneity vs. Task Heterogeneity

- task vs. machine heterogeneity
 - task heterogeneity: variation along a column

	m1	m2
t1	3	5
t2	7	4
t3	20	18

Machine Heterogeneity vs. Task Heterogeneity

- task vs. machine heterogeneity
 - task heterogeneity: variation along a column
 - machine heterogeneity: variation along a row

	m1	m2
t1	3	5
t2	7	4
t3	20	18

Outline

- ✓ Heterogeneous Computing Systems
- ✓ Statistical Measures for Quantifying Heterogeneity
- ✓ Simulation Results
- ✓ Conclusions

Measures of Heterogeneity

- ✓ goal: select heuristic that is best for an environment with a given heterogeneity
 - 5 existing heterogeneity measures not enough
 - 5 more measures correlated with heuristic performance
- ✓ studied measures of task and machine heterogeneities
 1. coefficient of variation
 2. skewness (third central moment)
 3. kurtosis (fourth central moment)

Statistical Measures - COV

- ✓ coefficient of variation (COV):
 - 5 let μ be the mean of a set of values
 - 5 and σ the standard deviation of a set of values
 - 5 the COV, V , is given by

$$V = \sigma/\mu$$

Statistical Measures - Average Task COV

- $V_j^{(m)}$ is the tasks COV for machine j
- $\sigma_j^{(m)}$ task standard deviation for machine j
- $\bar{i}_j^{(m)}$ task mean for machine j

$$V_j^{(m)} = \frac{\sigma_j^{(m)}}{\bar{i}_j^{(m)}}$$

Statistical Measures – Average Task COV

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 - $\sigma_j^{(m)}$ task standard deviation for machine j
 - $\bar{i}_j^{(m)}$ task mean for machine j

$$V_j^{(m)} = \frac{\sigma_j^{(m)}}{\bar{i}_j^{(m)}}$$

- task heterogeneity as measured by the Average Task COV (ATC)
 - M : number of machines

$$ATC = \left[\sum_{j=1}^M V_j^{(m)} \right] / M$$

Statistical Measures – Average Machine COV

- $V_i^{(t)}$ is the machine COV for task i
- $\sigma_i^{(t)}$ machine standard deviation for task i
- $\bar{i}_i^{(t)}$ machine mean for task i

$$V_i^{(t)} = \frac{\sigma_i^{(t)}}{\bar{i}_i^{(t)}}$$

Statistical Measures – Average Machine COV

- $V_i^{(t)}$ is the machine COV for task i
 - $\sigma_i^{(t)}$ machine standard deviation for task i
 - $\bar{i}_i^{(t)}$ machine mean for task i

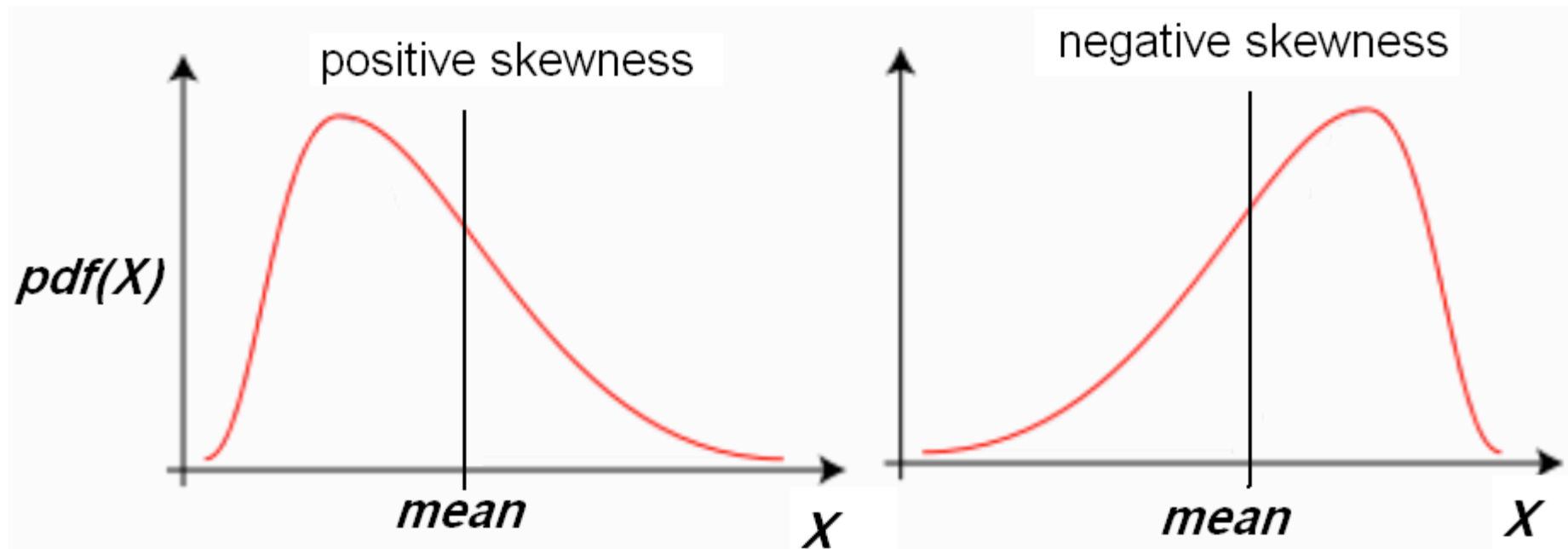
$$V_i^{(t)} = \frac{\sigma_i^{(t)}}{\bar{i}_i^{(t)}}$$

- task heterogeneity as measured by the Average Machine COV (AMC)
 - T : number of tasks

$$AMC = [\sum_{i=1}^T V_i^{(t)}] / T$$

Statistical Measures – Skewness (Third Central Moment)

- ✓ positive skewness
 - 5 more values less than mean
- ✓ negative skewness
 - 5 more values greater than mean



Statistical Measures – Average Task Skewness

✓ $S_j^{(m)}$ tasks skewness for machine j

$$S_j^{(m)} = \left[\frac{1}{T} \sum_{i=1}^T (\text{ETC}(i, j) - \bar{i}_j^{(m)})^3 \right] / (\sigma_j^{(m)})^3$$

Statistical Measures – Average Task Skewness

- ✓ $S_j^{(m)}$ tasks skewness for machine j

$$S_j^{(m)} = \left[\frac{1}{T} \sum_{i=1}^T (\text{ETC}(i, j) - \bar{t}_j^{(m)})^3 \right] / (\sigma_j^{(m)})^3$$

- ✓ task heterogeneity as measured by the Average Task Skewness (ATS)

$$ATS = \left[\sum_{j=1}^M S_j^{(m)} \right] / M$$

Statistical Measures – Average Machine Skewness

✓ $S_i^{(t)}$ machines skewness for task i

$$S_i^{(t)} = \left[\frac{1}{M} \sum_{j=1}^M (\text{ETC}(i, j) - \bar{i}_i^{(t)})^3 \right] / (\sigma_i^{(t)})^3$$

Statistical Measures – Average Machine Skewness

- $S_i^{(t)}$ machines skewness for task i

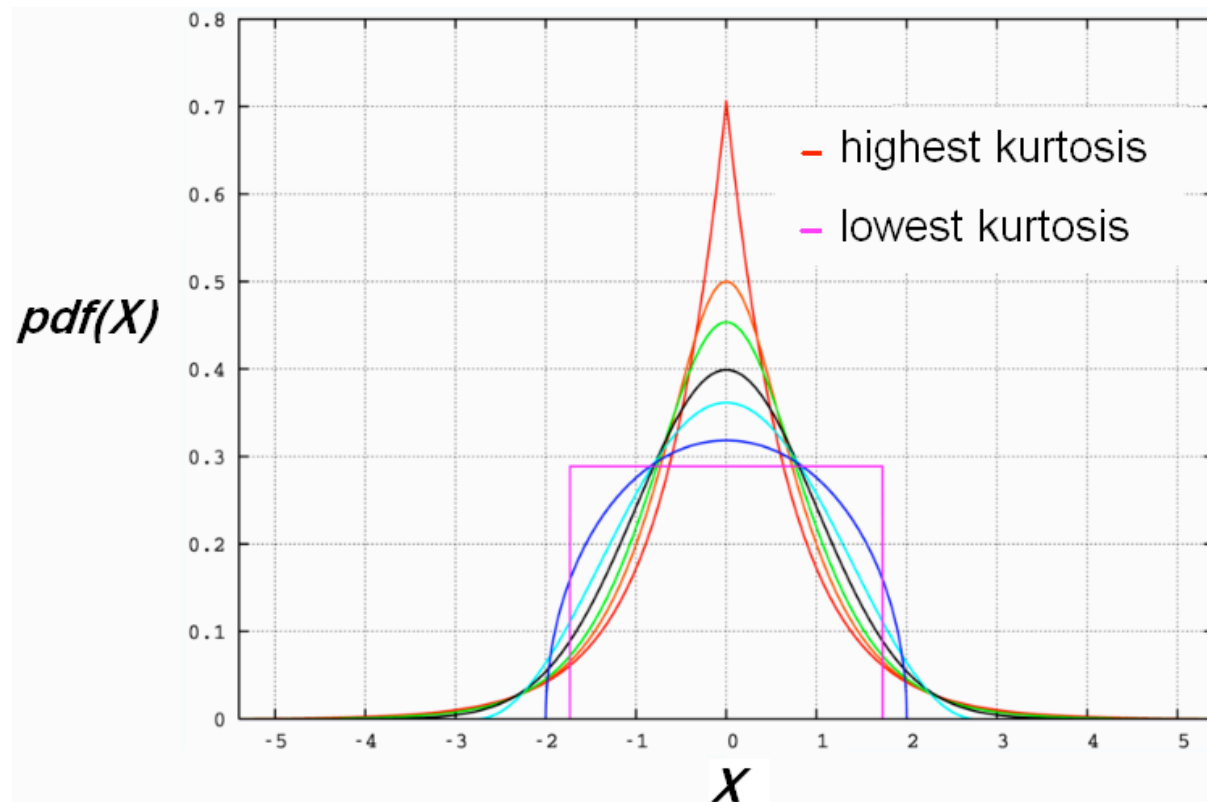
$$S_i^{(t)} = \left[\frac{1}{M} \sum_{j=1}^M (\text{ETC}(i, j) - \bar{i}_i^{(t)})^3 \right] / (\sigma_i^{(t)})^3$$

- machine heterogeneity as measured by the Average Machine Skewness (*AMS*)

$$AMS = \left[\sum_{i=1}^T S_i^{(t)} \right] / T$$

Statistical Measures – Kurtosis (Fourth Central Moment)

- ✓ high kurtosis
 - 5 small number of values having extreme deviations
- ✓ low kurtosis
 - 5 large number of values having modestly-sized deviations



Source: <http://en.wikipedia.org/wiki/Kurtosis>

Statistical Measures – Average Task Kurtosis

✓ $K_j^{(m)}$ tasks kurtosis for machine j

$$K_j^{(m)} = \left[\left(\frac{1}{T} \sum_{i=1}^T (\text{ETC}(i, j) - \bar{i}_j^{(m)})^4 \right) / (\sigma_j^{(m)})^4 \right] - 3$$

Statistical Measures – Average Task Kurtosis

- ✓ $K_j^{(m)}$ tasks kurtosis for machine j

$$K_j^{(m)} = [(\frac{1}{T} \sum_{i=1}^T (\text{ETC}(i, j) - \bar{i}_j^{(m)})^4) / (\sigma_j^{(m)})^4] - 3$$

- ✓ task heterogeneity as measured by the Average Task Kurtosis (ATK)

$$ATK = [\frac{1}{M} \sum_{j=1}^M K_j^{(m)}]$$

Statistical Measures – Average Machine Kurtosis

✓ $K_i^{(t)}$ machines skewness for task i

$$K_i^{(t)} = \left[\left(\frac{1}{M} \sum_{j=1}^M (\text{ETC}(i, j) - \bar{i}_i^{(t)})^4 \right) / (\sigma_i^{(t)})^4 \right] - 3$$

Statistical Measures – Average Machine Kurtosis

- ✓ $K_i^{(t)}$ machines skewness for task i

$$K_i^{(t)} = \left[\left(\frac{1}{M} \sum_{j=1}^M (\text{ETC}(i, j) - \bar{i}_i^{(t)})^4 \right) / (\sigma_i^{(t)})^4 \right] - 3$$

- ✓ machine heterogeneity as measured by the Average Machine Kurtosis (AMK)

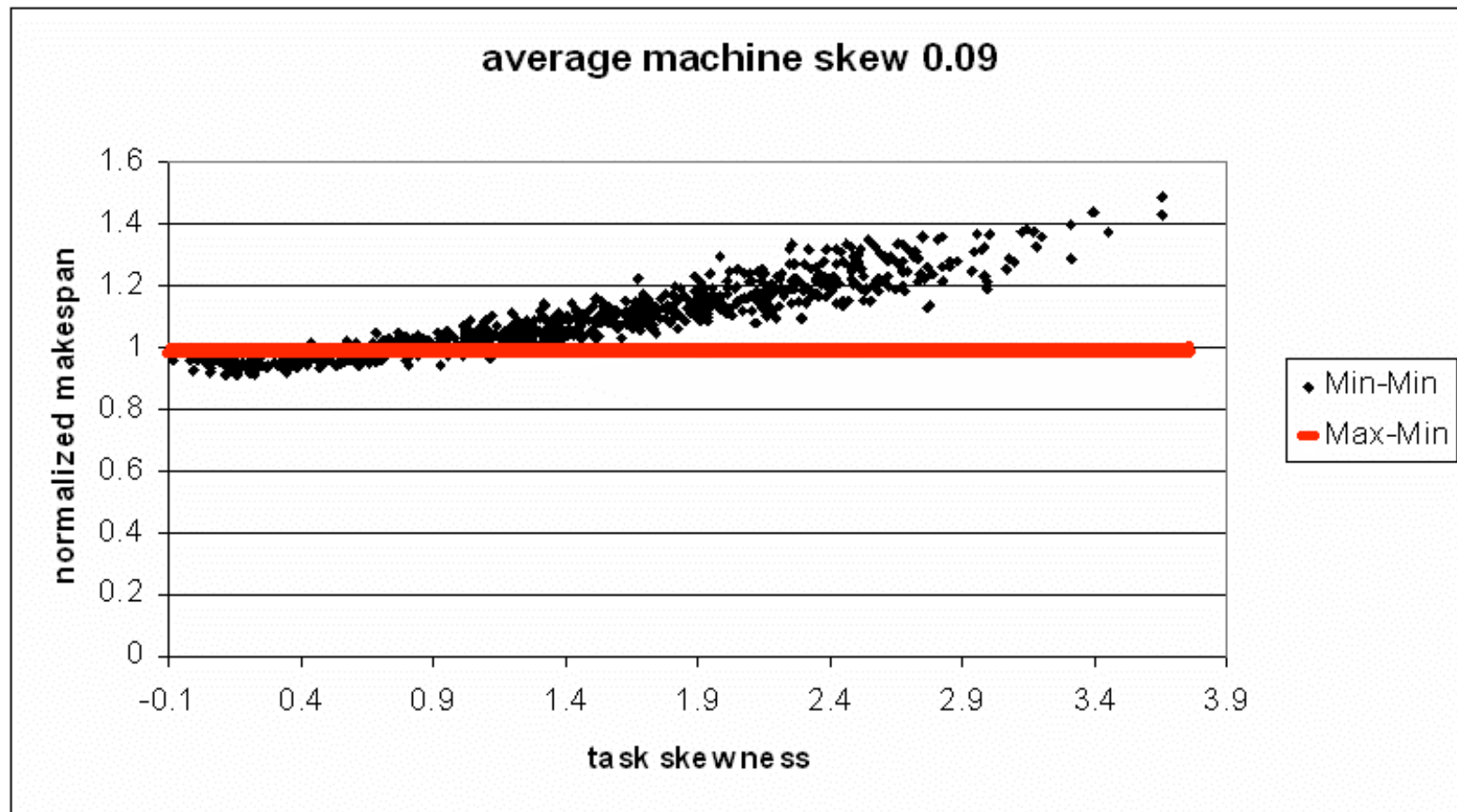
$$AMK = \left[\frac{1}{T} \sum_{i=1}^T K_i^{(t)} \right]$$

Simulation Results

- √ ETC size
 - 5 8 machines
 - 5 128 tasks
- √ static mapping
 - 5 all tasks available for execution
 - 5 mapping done offline
- √ studied heuristics
 - 5 Max-Min and Min-Min
- √ makespan
 - 5 time when all tasks finish
 - 5 lower is better
- √ normalized makespan
 - 5 makespan of Min-Min divided by Max-Min

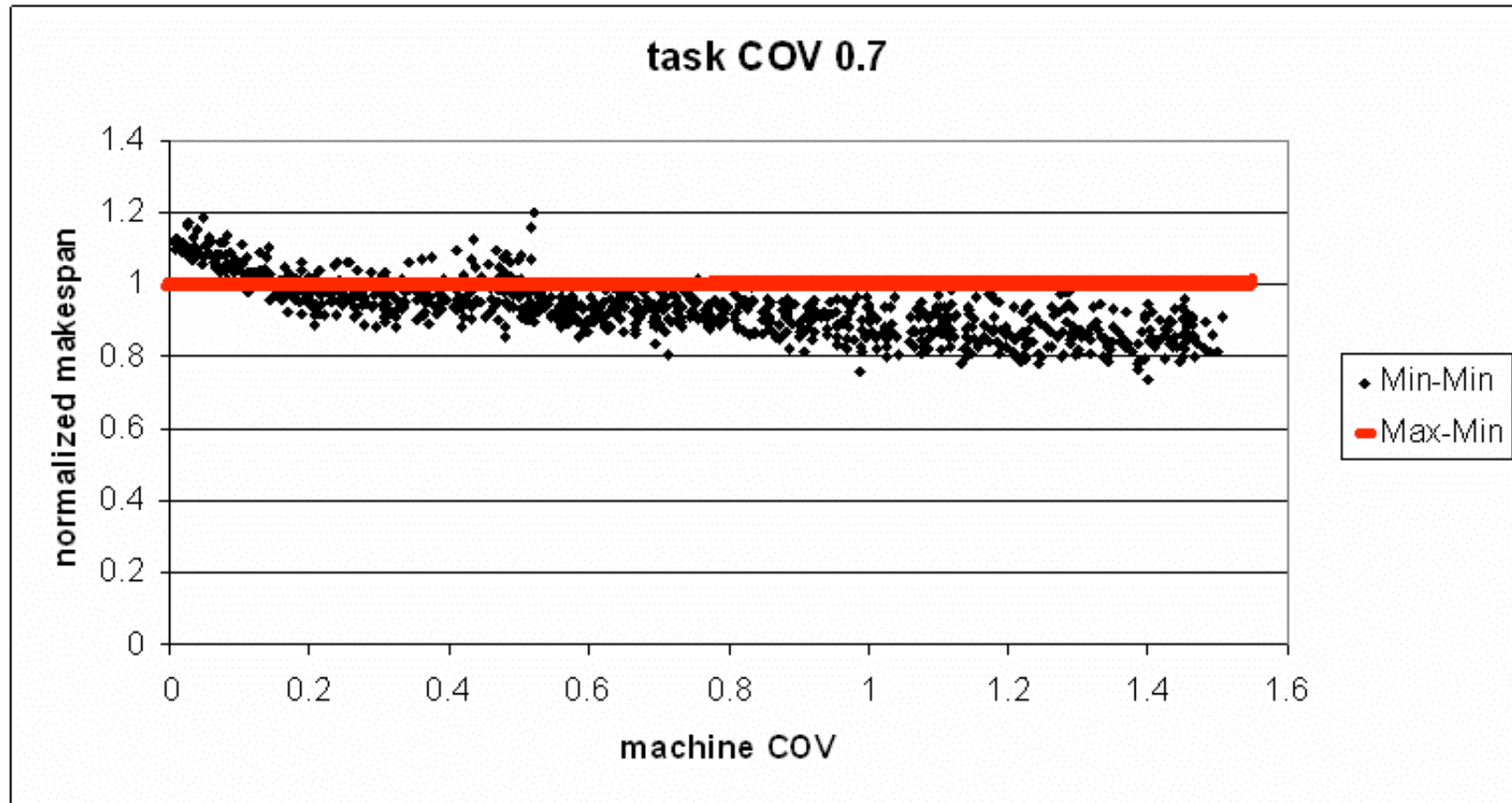
Simulation Results – Effect of ATS

Max-Min outperforms Min-Min for ATS of 1.4 and higher



Simulation Results – Effect of AMC

Min-Min outperforms Max-Min for AMC of 0.5 and higher



Conclusions

- ✓ currently used statistical measures (COV) not sufficient
- ✓ need to use additional measures
 - 5 skewness (third central moment)
 - 5 kurtosis (fourth central moment)
- ✓ skewness and kurtosis impact the performance of heuristics
- ✓ ignoring skewness and kurtosis may lead to wrong use of a heuristic