## ASSIGNMENT 1

PAGEL

- 1.(a) Figure 0.1.1, page 2 Math model is a way to describe an applied problem using mathematics. It consists of the following stages:
  - \* observation, question or problem
  - \* mathematical formulation, using degracional cyclems or differential equations or other objects from math
  - \* SOLHW
  - \* interpretation in terms of the application
  - \* if needed: improvement of the model, adjustment, refinement, etc.
  - (b) discrete—time: values given at equally spaced intervals (graph is a collection of dots)

    continuous time: values given (n all values of the variable (continuous curve)

hose (c)

(1,4) open (-0,7] dved

[1,4] closed (0,00) open

one order of magnifiede is one power of 10 37 - 4 one vider of magn. is 370 2 viders 37,000

3 orders 37000 [4 orders] 37000

- 2(a) Assume 1 year 2365 days 365.24.60.60 = 31,536,000 seconds if Lyear ~ 365,25 days 365,25.24.60.60 = 31,557,600 &cmds
  - 72.60 · 24 · 365 · 50 = 1,892,160,000 (b) one hour one day one year
- volume  $V = \frac{4\pi}{3} \text{ radius}^3$ (c)

diameter = 15 inches - radius = 7.5 inches = 7.5.2.54= 19.05 CM

 $V = \frac{47}{3}(19.05)^3 \approx 28.958.33 \text{ cm}^3$ 

mass = density. volume = 3.4 2 . 28,958.33 cm3 =98,458.32g = 98.4 kg

650 kg = 650,000 g (d)

 $650 \text{ lng} = 650 \cdot 2.204 \text{ lb} = 1432.6 \text{ lb}$   $95 \frac{\text{km}}{\text{h}} = 95 \cdot \frac{1.609}{1} \frac{\text{nniles}}{\text{h}}$ (e)

= 59,04 mph

3 (a) A parameter is a vanishle which changes from experiment to experiment, but is constant within an experiment exercise L: dependent: wombat dentity independent: altitude pardimeter: verinfall

texto ook

nages Lout7

look at

(b) A relation is a set of all pairs of values of independent and dependent vanishes A finition is a <u>unique</u> assignment of a number y (or fix) to a number x

g... derindent & g(m) disparameter m. independent & J.

- (c) To identify those curves that one the graphs of frations
- (d) Nahral dimain: largest set of values where f is defined. Given dimain: subset of the nahral dimain that has to be explicitly stated
- (e) Set of all points (x, fax), where x is in the domain of f
- 4. (a) f1, f2, f3, f4, f5, f9, f20
  - (b) fo, f7
  - (c) f6, f7
  - (d) for for seep in mind that it says increasing for all real numbers

    (1x is increasing, but only for x70)

    X2 is increasing only for x70)
  - (e) fy, fro
  - (f) linear means fix= mx+6: f2,f2,f3

fro is not linear, but consists of two linear pieces:  $|X| = \begin{cases} -x & \text{if } x > 0 \\ 1 & \text{if } x < 0 \end{cases}$ 

(8) positive means >0 fn all x (so if a finching touches x-axis it is not called positive; it's called non-negative

f3,f7

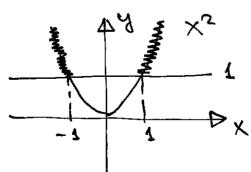
(h) f2, f5, f6, fg

(i) f3, f4, f7, f20

(i) f3

domain: all x range:  $(-\infty, 0]$  and (0, 1/2) combine:  $(-\infty, 1/2)$ 

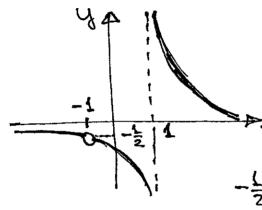
 $6. \qquad x^2 - 1 \geqslant 0 - x^2 \geqslant 1$ 



(identify  $\times$  where  $\times^2$  lies above, or forches (hvirtual line) 1)  $\times \le -1$  or  $\times > 1$ 

- (b)  $\chi^2 1 = 0 0 \times = \pm 1 \dots$  domain: all  $\times \pm \pm 1$
- (c) x2+1=0 has no solutions ... duncuin: all x

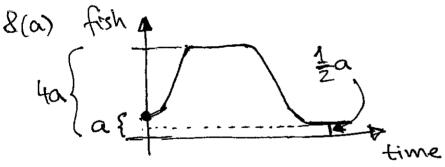
(d) 
$$f_2(x) = \frac{(x+1)(x-1)}{x+1} = \begin{cases} \frac{1}{x-1} & \text{if } x \neq -1 \\ \frac{1}{x-1} & \text{if } x \neq -1 \end{cases}$$

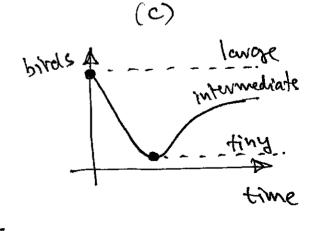


range: all real numbers except

- \frac{1}{2} and 0

- \frac{1}{2} is what we get when we substitute - 1 into \frac{1}{x-1}





- 9. Average height increases with the age of a her until their about 30 years old. Then, the height stants decreasing.
- 10.(a)  $f(\alpha+1) = 3(\alpha+1)^2 (\alpha+1) + 2 = 3\alpha^2 + 5\alpha + 4$ 
  - (b)  $f(\alpha) + f(1) = (3\alpha^2 \alpha + 2) + (4) = 3\alpha^2 \alpha + 6$
  - (c)  $f(1+h)-f(1)=(3(1+h)^2-(1+h)+2)-(4)$ =  $3h^2+5h$
- 11. (a)  $f(\frac{a}{4}) = \frac{2}{\frac{a}{4}} = 2 \cdot \frac{4}{6} = \frac{8}{6}$ 
  - (b)  $f(\frac{22}{0}) = \frac{2}{\frac{22}{0}} = 2 \cdot \frac{2}{21} = \frac{2}{11}$
  - (c)  $\frac{f(3+h)-f(3)}{h} = \frac{\frac{2}{3+h}-\frac{2}{3}}{h}$ 
    - $=\frac{2(3)-2(3+h)}{(3+h)(3)}\cdot\frac{1}{h}=\frac{-2h}{3(3+h)}\cdot\frac{1}{h}$ 
      - $=\frac{-2}{3(3+h)}$