- 1.(a) f'(t) = h.f(t) -> f(t) = f(0) eht = a eht
 - (b) An initial value problem consists of a differential equation (or equations) and initial andition(s). A solution is any fination which satisfies both the diff. equation(s) and initial andition(s).
 - (c) A cont. Function has infinitely many antiderivatives which differ from each other by a constant.

 antiderivatives of x^{-10} are $\frac{x^{-9}}{-2} + C = -\frac{1}{9x^9} + C$
 - (a) $\int Odx = C$
 - (e) $\int c \cdot f \alpha x dx = c \cdot \int f \alpha x dx$ where $c \cdot is a constant$ as well, $\int_{a}^{b} c f(x) dx = c \int_{a}^{b} f(x) dx$
 - 2.(a) No. Take, for vistance f(x) = x and g(x) = 1then $\int f(x)g(x) dx = \int x dx = \frac{x^2}{2} + C$ $(\int f(x)dx)(\int g(x)dx) = (\int x dx)(\int 1 dx)$ $=(\frac{x^2}{2} + C)(x + C)$ so when C = 0, we get $\frac{x^2}{2}$ and $\frac{x^3}{2} \rightarrow not$ equal

- (b) Since e-x>0 on [-3,7] the integral must be positive as well
- (c) to compute a definite integral of a function which is positive (n zero), we can argue using cureas (if the regions involved are simple enough so that we can calculate their areas)
 - (d) the definite integral is equal to the net area. The net area is the area of the region(s) above the x-axis minus the area of the region(s) below the x-axis.

 (see page 444)
- 3.(a) the definite integral of a constant times a fination is equal to the constant times the definite integral.
 - (b) the growth in the first 10 years is given by $\int_0^{10} 6.48 e^{-0.09t} dt$

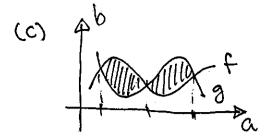
Using the formula for L(t) derived in the example, we get 72 (1-2-0.00+)

$$L(t)|_{0}^{10} = L(10) - L(0)$$

$$= 72(1 - e^{-0.09.10}) - 72(1 - e^{-0.09.0})$$

$$= 72(1 - e^{-0.9})$$

$$\approx 42.73 \text{ cm}$$



identify all bounded regions defined by the two fractions

the ana of each bonded region is introsection (top fuction - bottom function) dx introsection point

- 4. (a) total change in pressure between times a and b
 - (b) distance covered between times a and b
 - (c) total length change between times a and b total change in (d) Victority between times a and b
 - (e) total number of people in fected with a flu between times a and b

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