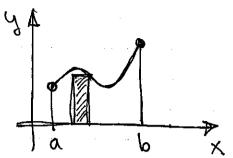
1(a) Take a continuous finction fix) on [a,b]



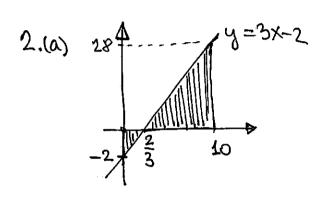
which satisfies fox 70 on [a,b]
Divide [a,b] into equal subintervals
and build a retungle over each
subinferral, whose height is
given by some rule (say, the value

of fix at right end). The sum of areas of these region under fix in [a, b].

- (b) Riemann sum is a common name for any of the sums we obtain when we use approximating sectangles for the area under a curve.
- (c) The area under a curve defined by $f(x) \ge 0$ on an interval is obtained by making the approximating rectangles thinner and funner (ie, by idividing the interval into more and more subintervals). More precitely, we take the limit of the approximating suns as the bases of rectangles approach two.
- (d) It fox>>0 then Infax dx = area under fax)
 un [a,b]

In general, Safardx is the difference of awas Careas of regions above the x-axis minus areas of regions below the x-axis)

(e) As approximating rectingles get thinner, then approximate better the vegton under the curve.

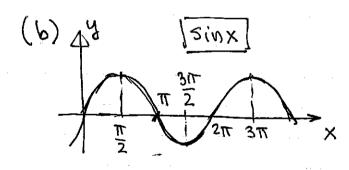


$$\int_{0}^{10} (3x-2)dx = \frac{1}{2}(2\cdot\frac{2}{3})$$

$$+\frac{1}{2}(10-\frac{2}{3})28$$

$$= -\frac{2}{3} + \frac{1}{2}\cdot\frac{28}{3}\cdot28 = -\frac{2}{3} + \frac{392}{3}$$

$$= 130$$

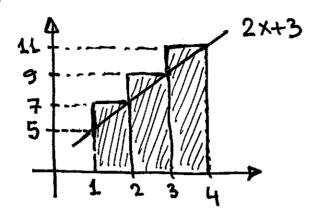


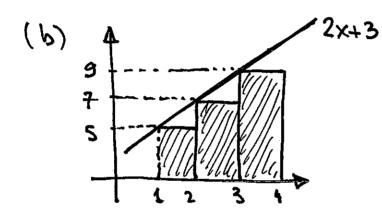
3 TT TT TT X

y = sin 2x

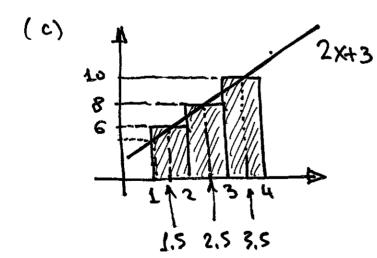
or
$$\int \sin 2x dx = 0$$
,
or $\int \sin 2x dx = 0$,
or $\int \sin 2x dx = 0$,
or $\int \sin 2x dx = 0$,
or $\int \cos 2x dx = 0$,
or $\int \cos 2x dx = 0$,

3. (a)

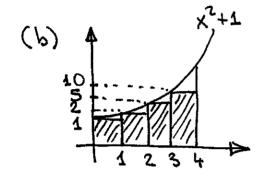




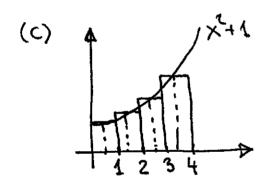
aven ≈ 1.5+1.7+1.9 = 21



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heights of the four rectungles are: 1,2,5,10



5.

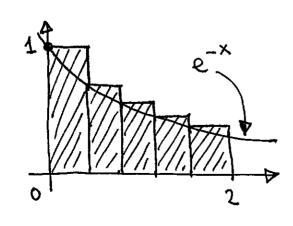
the heights are:

$$(0.5)^{2}+1 = 1.25$$

$$(1.5)^{2}+1 = 3.25$$

$$(2.5)^{2}+1 = 7.25$$

$$(3.5)^{2}+1 = 13.25$$



left sum > area under e-x

since ex is decreasing

$$y = \sqrt{4-x^2} - 4 \quad y^2 = 4-x^2, \quad x^2 + y^2 = 4$$

$$y + 4 \quad \text{opper semi-circle, radius 2}$$

$$\frac{2}{-2} \times \sqrt{4-x^2} \, dx = \frac{1}{2} ax$$

2
$$\int \sqrt{14-x^2} dx = \frac{1}{2} \text{ area of the civele}$$

$$-2 \qquad \text{of vadius 2}$$

$$= \frac{1}{2} \pi \cdot 2^2 = 2\pi$$

$$f(x) = 1 - |x|$$

$$-1$$

$$-2$$

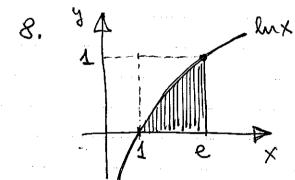
$$-2$$

$$-2$$

$$\int_{-2}^{3} (1-|x|) dx = -\frac{1}{2} \cdot 1 \cdot 1 + \frac{1}{2} \cdot 2 \cdot 1$$

$$-\frac{1}{2} \cdot 2 \cdot 2$$

$$= -\frac{1}{2} + 1 - 2 = -\frac{3}{2}$$



I have dx = area of the shootedregion \angle area of the rectangle

on [1,e] of height 1 $= (e-1)\cdot 1 = e-1$

OK:

e
$$ln \times \leq 1$$
 on $[s,e]$
e $ln \times dx \leq [1.dx]$

$$1$$

(although lux \le 1, in the final answer we use < e-1, since the shaded region is Smaller than the rectnigle)

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9. Given was the vale of change of the amount of chemical p, ie

de de

was given. dp/dt tells us how p changes at timet.

To find the total change in p on some time interval, we add up the changes over small subintervals.