

# Gaussian Elimination Solution

## System of Linear Equations - Step-by-Step Solution

### Input Matrix (Augmented Form)

$$\begin{bmatrix} 1 & 2 & 3 & 1 \\ 2 & 1 & 3 & 2 \\ 3 & 2 & 1 & 0 \end{bmatrix}$$

### Unique Solution Found

Solution:

$$x_1 = 1/4$$

$$x_2 = -3/4$$

$$x_3 = 3/4$$

## Step-by-Step Solution

### Step 1: Initial Matrix

$$\begin{bmatrix} 1 & 2 & 3 & 1 \\ 2 & 1 & 3 & 2 \\ 3 & 2 & 1 & 0 \end{bmatrix}$$

### Step 2: $R1 \leftrightarrow R3$

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 2 & 1 & 3 & 2 \\ 1 & 2 & 3 & 1 \end{bmatrix}$$

### Step 3: $R2 = R2 - (0.667)R1$

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 0 & -0.333 & 2.333 & 2 \\ 1 & 2 & 3 & 1 \end{bmatrix}$$

### Step 4: $R3 = R3 - (0.333)R1$

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 0 & -0.333 & 2.333 & 2 \\ 0 & 1.333 & 2.667 & 1 \end{bmatrix}$$

### Step 5: $R2 \leftrightarrow R3$

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 0 & 1.333 & 2.667 & 1 \\ 0 & -0.333 & 2.333 & 2 \end{bmatrix}$$

**Step 6:  $R_3 = R_3 - (-0.250)R_2$** 

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 0 & 1.333 & 2.667 & 1 \\ 0 & 0 & 3 & 2.25 \end{bmatrix}$$

**Final Matrix (Row Echelon Form)**

$$\begin{bmatrix} 3 & 2 & 1 & 0 \\ 0 & 1.333 & 2.667 & 1 \\ 0 & 0 & 3 & 2.25 \end{bmatrix}$$