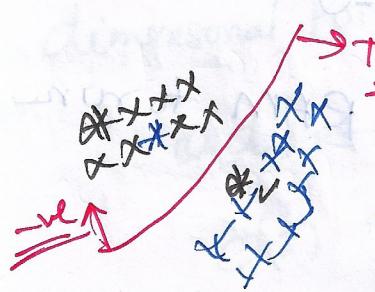


One of the downside of KNN it slows in calculating the test data. We will see some techniques little later.

### Decision Surface for KNN as K changes

K in KNN is a hyper parameter.

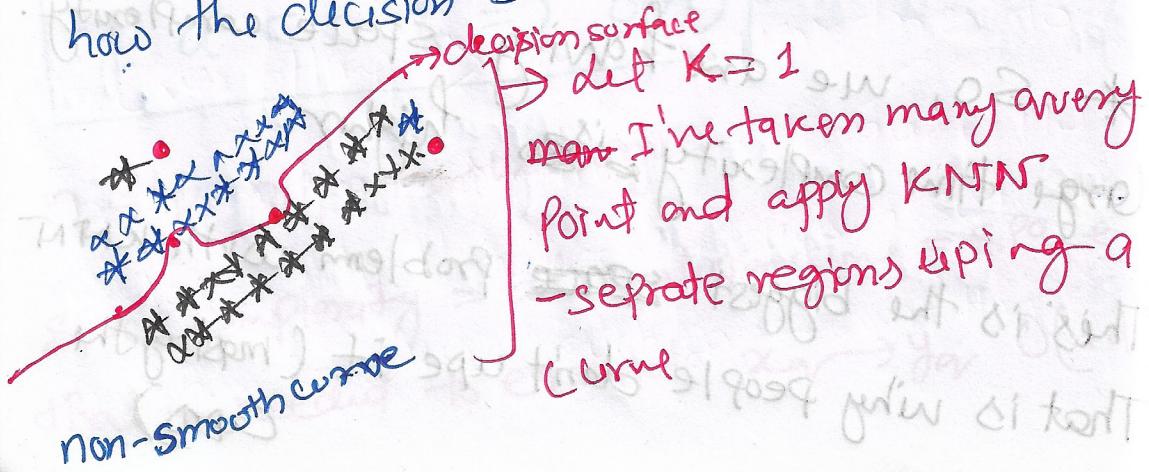
The curves that separates the +ve and -ve points from each other klas Decision Surfaces.

 This is called a decision surfaces,  $\therefore$  these curve decide the +ve/-ve based on direction.

$3D \rightarrow$  Surfaces  $ND \rightarrow$  hypersurfaces

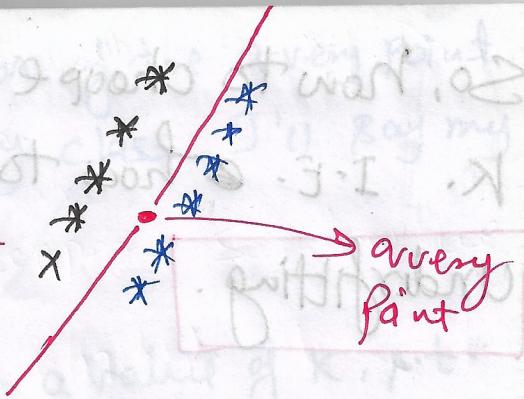
Let's understand what happens as  $K \uparrow$

how the decision surface behave:

  $\rightarrow$  decision surface  
 $\rightarrow$  det K=1  
more I've taken many every point and apply KNN -separate regions using a curve  
non-smooth curve

det  $k=5$

Hence as the  $k \uparrow$  my decision surface is smoother and smoother.



Let's take the extreme case  $k=N$  i.e. number of points in dataset.

Suppose out of  $N$  points  $60\%$  are one and  $40\%$  are the other.

If you think, for any arvery point this result will always remain same.

$$n_1 = 60\% \text{ of } N, n_2 = 40\% \text{ of } N, n_1 + n_2 = N = k$$

i.e. all the arvery points always be one.

i.e. every new arvery is one.

Not good So, if  $k=N$ , whatever be the majority class the result will remain same.

Hence  $k=N$  not a good value of  $k$ .

\* When  $k=N$ , every arvery point become the majority class.

So, how to choose the correct value of K. I.E. how to avoid overfitting and underfitting.

Overfitting and Underfitting are very-very fundamental concepts in machine learning.

Let's understand these concepts in more detail.

$K=1 \rightarrow$  overfitting     $K=N$  underfitting  
our example. And  $K=5$ , well fit / best fit

Say  $K=1$ , the point those makes our surface non-smoother may be outliers. But the decision surface did overfitting to accommodate this.

Overfitting  $\Rightarrow$  The classifier tries to fix a function or purpose, tries to make no mistake, which makes the decision surface more non-smoother such come overfitting.

Underfitting: Don't care of the accuracy point, whatever is the majority class I'll say my data is same.

So, we have to choose a value of  $K$ , s.t. the ML model should not be either a overfitting or underfitting solution.

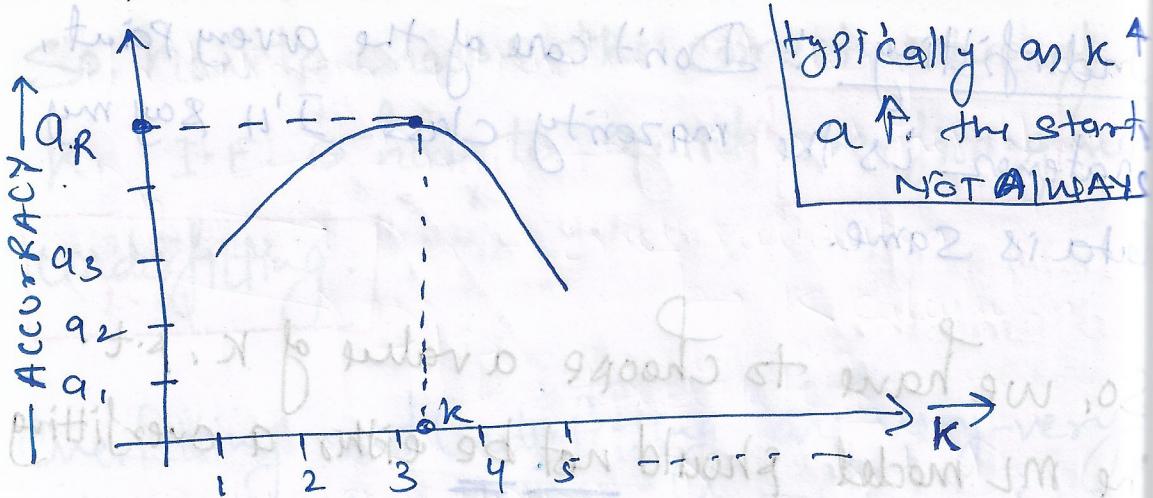
It should be a well balanced system. As in our example  $K=5$ .

Note with How to determine  $K$  [Need of cross Validation]

$D_n \rightarrow D_{train} (70\%) \quad \left. \begin{array}{l} \\ \end{array} \right\}$  we choose this randomly.

Now let's follow the below method to choose the value of  $K$ .

$K=1$	$D_{train}$	Calculate Accuracy $D_{test}$	Accuracy = $\frac{\# \text{ of correctly classified points}}{\text{total \# points}}$
$K=2$	"	$q_1$	
$K=3$	"	$q_2$	
!	"	$q_3$	
		$q_4$	



But at  $k=4$  I'm getting highest accu

∴ we will choose  $k=4$

Let's talk about in terms of Amazon

Food Review Dc. Let's take an hypothetical number for accuracy = 96 %.

Using  $D_{train}$  and 4NN, on amazon review dataset, we get an acc of 96 %

Hmm... But there is a small problem

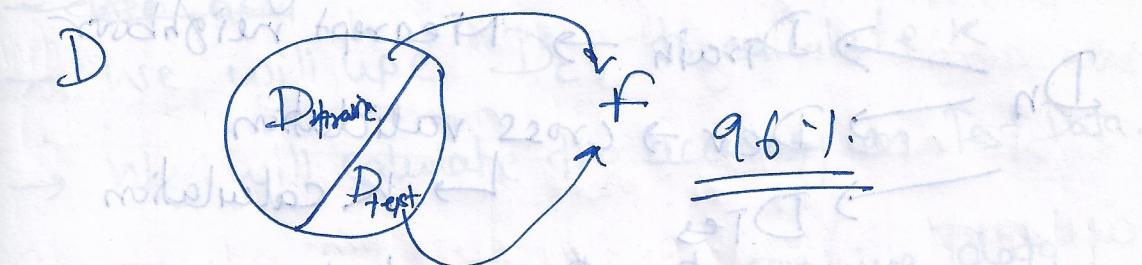
with this statement

let see what

What As we discussed in very begining the objective of ML



But here, we broke the data into 2 parts



If you think, we also up ~~what about~~

D<sub>Test</sub> to calculate the value of  $K_{RT}$ ?

So, we use all the Data  $D_{TR}$  to get the value of  $K$ .

How this ML model behave for a future unseen point? What would be my accuracy.

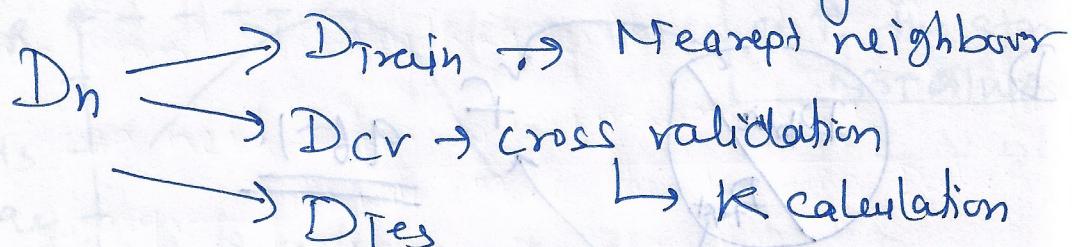
So for [That we don't know]

And for my ML model it has to work very well for future UNSEEN point. Otherwise it is of no importance/useless.

An algorithm which does very well on future unseen point is  $K$ /as Generalization.

So, our ML model should be Generalized

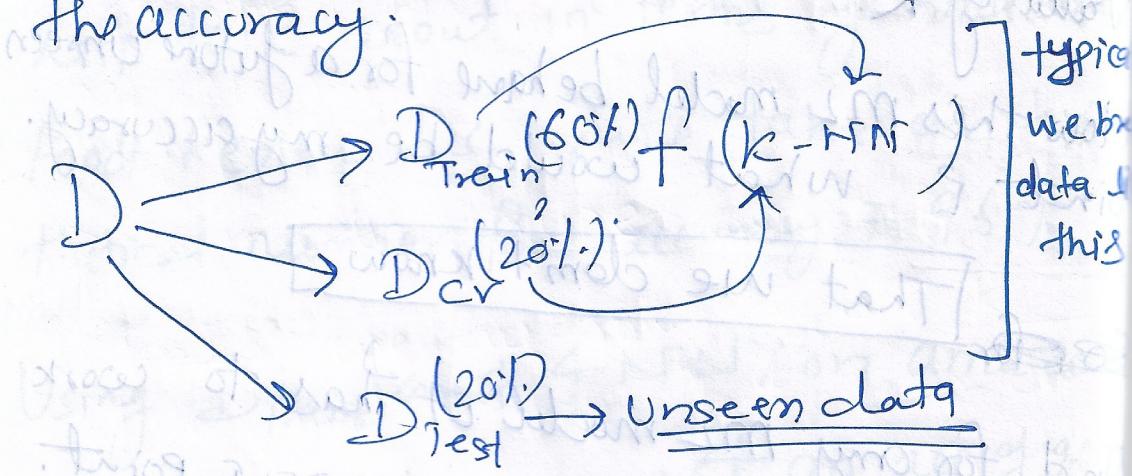
let's take an alternative strategy:



~~for cross validation~~

So, we are using  $D_{\text{train}}$  and  $D_{\text{cv}}$

To compute my function. We will apply this function on  $\underline{\underline{D_{\text{test}}}}$  to calculate the accuracy.



Say if my acc = 93%. Can I say, my algorithm has an accuracy of 93% on Unseen data?

We can't. ~~because it's small~~

This is something known as Cross Validation

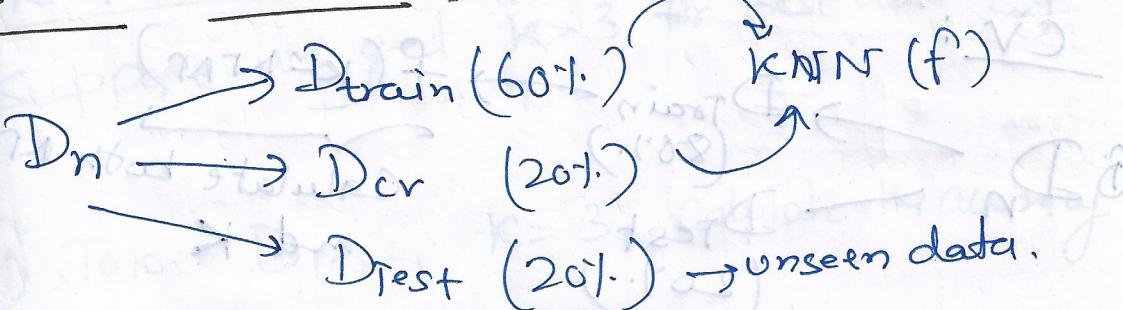
- We will train our model using  $D_{train}$ .
- ~~date with~~  
we will use  $D_{cv}$  to calculate  $K$
- We will calculate the accuracy on Test Data.
- Statement: Using  $D_{train}$  on training data,  
I find 16-NN to have an acc of 93% on  
future/unseen data.

93% → Generalize Accuracy.

There ~~was~~ or  $100 - 93 = 7\%$ . Generalized Error

This is small introduction of CROSS VALIDATION

### K-fold Cross-validation



→ There is a problem with this model.  
Problem: We are using only 60% of data  
to get our Nearest Neighbours (NN).

$20\% \rightarrow CV$  and  $20\% \rightarrow Test$

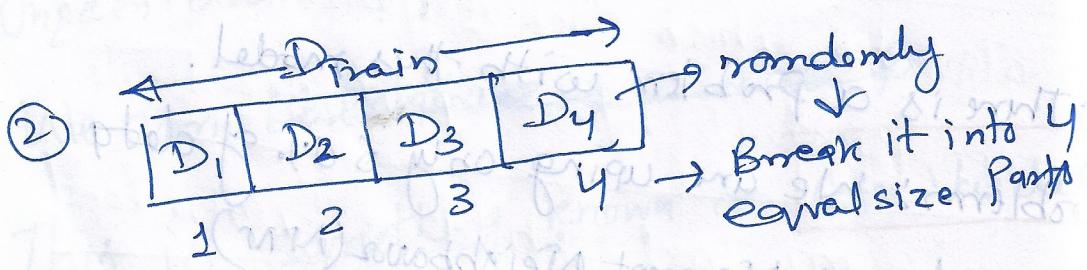
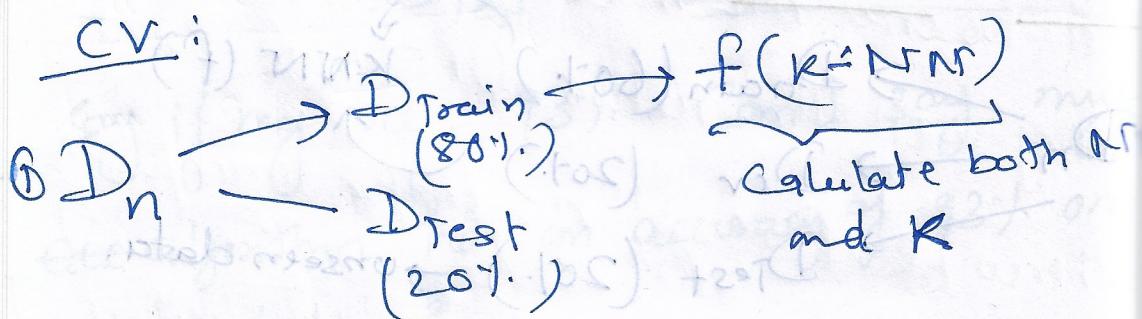
We can't do anything with  $20\% Test$   
We need  $\frac{1}{k}$  unseen data to calculate accuracy.

**ML Rule:** More the training Data better is the algorithm.

So can we do one thing combine this  
 $60\% NN + 20\% CV \rightarrow$  to compute NN

→ More the training data, better is your algorithm, this is always true for any ML Algorithm.

→ So in order to use  $60\% + 20\%$  data is known we are going to use k-fold



	train	cv
$k=1$	$D_1 D_2 D_3$	$D_4 = a_4$
$k=1$	$D_1 D_2 D_4$	$D_3 = a_3$
$k=1$	$D_1 D_3 D_4$	$D_2 = a_2$
$k=1$	$D_2 D_3 D_4$	$D_1 = a_1$
$k=2$		

Remember all  $D_1$ ,  $D_2$ ,  $D_3$  and  $D_4$  20% of the Data

Same 20% CV

→ Perform the Opt for  $k=1, k=2, k=3$

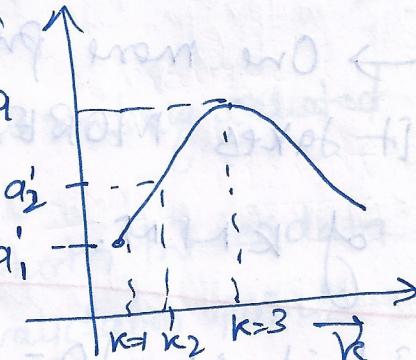
$$k=1 \text{ accuracy} = \frac{a_1 + a_2 + a_3 + a_4}{4} = a'$$

→ So, I use every point of my data for training and cross validation.

This is called as 4 fold cross validation.

k-fold validation

Suppose we get  $k=3$  for best accuracy.



④ Take  $D_{test}$ ,  $k=3$ , calculate the accuracy

e.g. 90%.

90% is the accuracy of the above model

having  $k=3$

Now the question again remain is what is the right value of  $K$  for  $k$ -fold.

Here we have  $K=4$  or  $K=10$ ,  $K=100$  is the right #

→ typically for many m/c learning model we use 10-fold CV.

→ One more problem with  $k$ -fold cross validation it takes MORE time to calculate the  $K$  of KNFMs.

If it is 10-fold, the time ↑ by 10 times

But the good thing is that It is one time effort.