

**TFL Natural Deduction with Conditionals Exercise**  
PHI 154 (Eliot) Fall 2020

For each argument, construct a proof using the natural deduction system described in Chapter 16. The inference rules we have learned at this point are R,  $\wedge$ I,  $\wedge$ E,  $\rightarrow$ I, and  $\rightarrow$ E. Exercises 1–4 do not require our newest rule,  $\rightarrow$ I. The premises are separated by commas, and the conclusion comes after the “therefore” symbol, which is “ $\therefore$ ” (as introduced on page 2).

1.  $\neg R \rightarrow S, S \rightarrow Q, \neg R \therefore Q$
2.  $(M \vee N) \rightarrow N, C \wedge (M \vee N) \therefore N$
3.  $S \wedge T, T \rightarrow \neg G, S \rightarrow D \therefore D \wedge \neg G$
4.  $[(F \wedge \neg T) \wedge M] \rightarrow A, M \wedge \neg T, \neg T \rightarrow F \therefore A \wedge F$
5.  $C \rightarrow \neg B, \neg B \rightarrow E \therefore C \rightarrow E$
6.  $Z \wedge X, Z \rightarrow H \therefore \neg I \rightarrow (H \wedge X)$
7.  $[B \wedge (L \vee M)] \therefore N \rightarrow [(B \wedge N) \wedge (L \vee M)]$
8.  $\therefore \neg R \rightarrow \neg R$  \*

\* You will have noticed that this proof does not include any premises. That’s intentional. How can you use the rules we have to prove the given sentence anyway?