

UE07: OWL Reasoning

Semantic AI 2023, JKU
Course Instructor: Bernd Neumayr

Your tasks:

- Read and understand the given OWL ontologies.
- Do the OWL reasoning in your head and indicate the entailments in the given tables.
- You may use Protégé to check your reasoning (see 06-Intro-OWL).

Part I: Instance Checking (8 points)

Given are the following OWL ontologies.

For each individual derive

- of which classes it is definitely a member, i.e., that individual is a member of that class in every possible world (mark with "+"),
- of which classes it is definitely not a member, i.e., there is no possible world in which that individual is a member of that class (mark with "-"),
- and of which classes it is possibly a member, i.e., there is at least one possible world in which that individual is a member of that class and at least one possible world in which that individual is not a member of that class (mark with "?" or leave empty).

Task 1

Class: A
Class: B
Class: C
EquivalentTo: A or B
Class: D
EquivalentTo: C and (not (B))
Individual: o1
Types: A
Individual: o2
Types: B
Individual: o3
Types: C
Individual: o4
Types: D



| | A | B | C | D |
|----|---|---|---|---|
| o1 | + | ? | + | ? |
| o2 | ? | + | + | - |
| o3 | ? | ? | + | ? |
| o4 | + | - | + | + |

Kann Sein,
dass sich A&B
überschneiden

Task 2

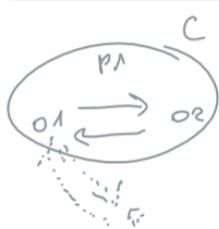
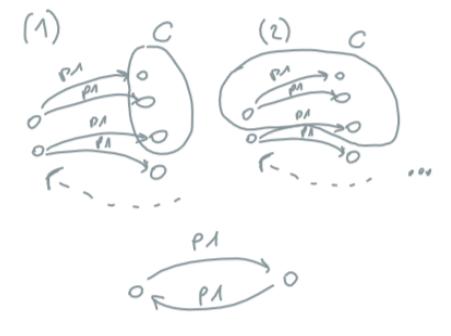
Individual: o1
Facts: p1 o2
Types: C
Individual: o2
Types: C
ObjectProperty: p1
Characteristics: Symmetric
Class: C1
EquivalentTo: p1 some C
Class: C2
SubclassOf: p1 some C
Class: C3
EquivalentTo: p1 only C

edit:

| | C1 | C2 | C3 |
|----|----|----|----|
| o1 | + | ? | ? |
| o2 | + | ? | ? |

OPEN WORLD ASS.

→ KANN sein

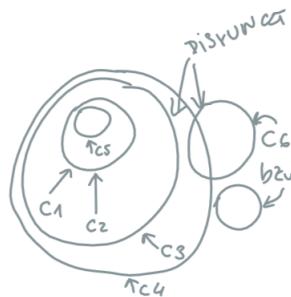


→ es KANN sein, dass o1 p1 some other obj.
→ wir wissen NICHT, dass C1 & C disjunkt
sind → würden wir das wissen, wäre
C3 bei o1 & o2 jeweils " "

Task 3

Individual: o1
 Types: C1
 Class: C1
 Class: C2
 EquivalentTo: C1
 SubclassOf: C3
 Class: C3
 SubclassOf: C4
 Class: C4
 Class: C5
 SubclassOf: C1
 Class: C6
 DisjointWith: C3

| | C1 | C2 | C3 | C4 | C5 | C6 |
|----|----|----|----|----|----|----|
| o1 | + | + | + | + | ? | - |



Task 4

Individual: o1
 Facts: p1 o2, p1 o3

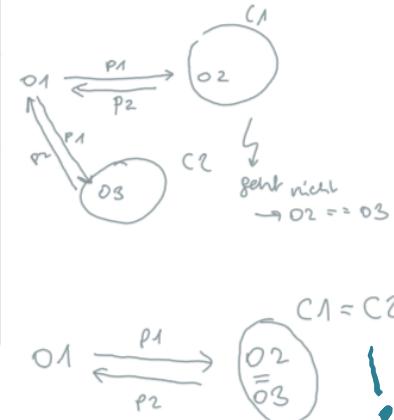
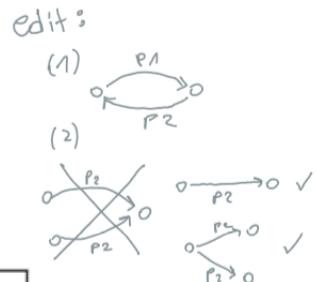
Individual: o2
 Types: C1
 Individual: o3
 Types: C2

ObjectProperty: p1
 InverseOf: p2

ObjectProperty: p2
 Characteristics: InverseFunctional

AXIOM → ALWAYS TRUE!

| | C1 | C2 |
|----|----|----|
| o1 | ? | ? |
| o2 | + | + |
| o3 | ≠ | + |



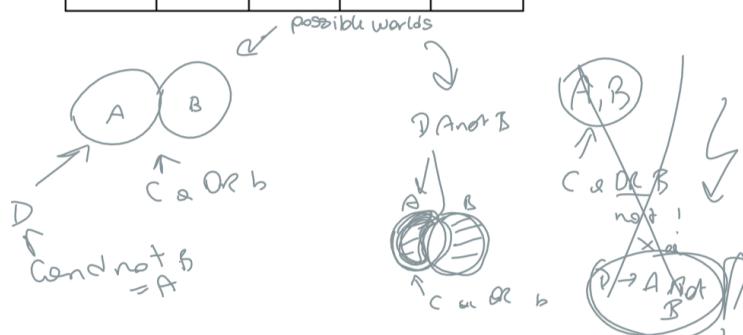
Task 5

(selbes bsp wie task 1)

Class: A
 Class: B
 Class: C
 EquivalentTo: A or B
 Class: D
 EquivalentTo: C and (not (B))
 Individual: o1
 Types: A
 Individual: o2
 Types: B
 Individual: o3
 Types: C
 Individual: o4
 Types: D

| | A | B | C | D |
|----|---|---|---|---|
| o1 | + | ? | + | ? |
| o2 | ? | + | + | - |
| o3 | ? | ? | + | ? |
| o4 | + | - | + | + |

kann sein,
dass sich A & B
überschneiden



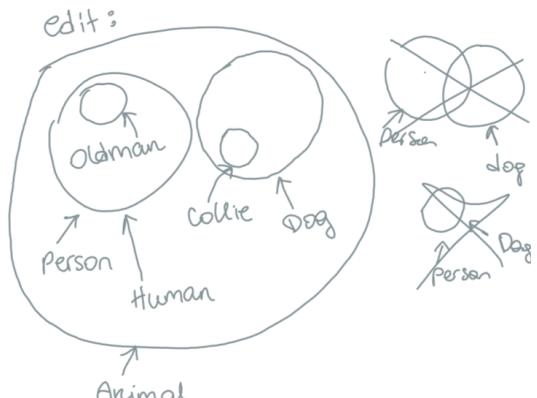
Task 6

```

Class: PERSON
  EquivalentTo: HUMAN
Class: ANIMAL
Class: DOG
  SubClassOf: ANIMAL
  DisjointWith: OLDMAN
Class: HUMAN
  EquivalentTo: PERSON
  SubClassOf: ANIMAL
Class: OLDMAN
  SubClassOf: PERSON
  DisjointWith: DOG
Class: COLLIE
  SubClassOf: DOG
Individual: flipper
  Types: ANIMAL
Individual: rex
  Types: DOG
Individual: mary
  Types: HUMAN
Individual: john
  Types: PERSON
Individual: jim
  Types: OLDMAN
Individual: lassie
  Types: COLLIE

```

| | PERSON | ANIMAL | DOG | HUMAN | OLD-MAN | COL-LIE |
|---------|--------|--------|-----|-------|---------|---------|
| FLIPPER | ? | + | ? | ? | ? | ? |
| REX | - | + | + | - | - | ? |
| MARY | + | + | - | + | ? | - |
| JOHN | + | + | - | + | ? | - |
| JIM | + | + | - | + | + | - |
| lassie | - | + | + | - | - | + |



Task 7

```

Individual: o1
  Types: C
Individual: o2
  Facts: p o1
  Types: C
Individual: o3
  Types: C1
Individual: o4
  Facts: p o1, p o5
Individual: o5
  Types: not C, p exactly 0
Class: C
Class: C1
  SubclassOf: p some C
Class: C2
  EquivalentTo: p some C
Class: C3
  EquivalentTo: p only C

```

| | C | C1 | C2 | C3 |
|----|---|----|----|----|
| o1 | + | ? | ? | ? |
| o2 | + | ? | + | ? |
| o3 | ? | + | + | ? |
| o4 | ? | ? | + | - |
| o5 | - | - | - | + |

p some C p only C

weil leere Menge gilt ✓

Task 8

Class: Woman
 Class: Teacher
 Class: Artist
 Class: JohnsFriends
 EquivalentTo: MarysFriends, {Bob , Mary}
 Class: MarysFriends
 EquivalentTo: JohnsFriends, {MsKeller , Mueller}

Individual: Bob
 Types: Teacher, not (Woman)
 Individual: Mary
 Types: Artist, Woman
 Individual: MsKeller
 Types: Woman
 Individual: Mueller

$\{ \text{Bob} , \text{Mary} \}$ $\Rightarrow 2 \text{ Personen}$
 $= \{ \text{MsK.} , \text{Mueller} \}$
 $\begin{cases} \text{Mary} \rightarrow \text{Woman (not man)} \\ \text{MsK.} \rightarrow \text{Woman (not man)} \end{cases} \} 1 \text{ Pers.}$
 $\begin{cases} \text{Bob} \rightarrow \text{not Woman} \\ \text{Mueller} \rightarrow ? \end{cases} \} 1 \text{ Pers.}$

| | JohnsFriends | MarysFriends | Teacher | Artist | Woman |
|----------|--------------|--------------|---------|--------|-------|
| Bob | + | + | + | ? | - |
| Mary | + | + | ? | + | + |
| MsKeller | + | + | ? | ? | + |
| Mueller | + | + | ? | ? | ? |

Part II: Subsumption Checking (2 points)

Task 9

Given is an OWL ontology in Manchester Syntax.

```

ObjectProperty: eats
Class: Cereals
Class: Egg
Class: Fish
Class: Fruits
Class: Meat
Class: Milk
Class: Vegetables
DisjointClasses:
    Cereals,Egg,Fish,Fruits,Meat,Milk,Vegetables
Class: Person
    SubClassOf: eats some Food
    DisjointWith: Food
Class: Food
    EquivalentTo: Cereals or Egg or Fish or Fruits or Meat or Milk or Vegetables
    DisjointWith: Person
Class: Carnivore
    EquivalentTo: Person and (eats only (Fish or Meat))
Class: Frutarier
    EquivalentTo: Person and (eats only Fruits)
Class: Vegan
    EquivalentTo: Person and (eats only (Cereals or Fruits or Vegetables))
Class: Vegetarian
    EquivalentTo: Person and (eats only (not (Fish or Meat)))
Class: xPerson
    SubClassOf: Person and (eats some Fruits)
Class: yPerson
    EquivalentTo: Person and (eats some Fruits)
Class: zPerson
    EquivalentTo: (eats some Cereals) and (eats some Fruits) and (eats some Vegetables)
SubClassOf: Person

```

Your task is to find the pairwise semantic relationships of classes `Carnivore`, `Frutarier`, `Vegan`, `Vegetarian`, `zPerson`, `xPerson`, `yPerson`. Indicate the relationships in the cells in the table below using the following symbols:

- subclass of \sqsubseteq
- equivalent to \equiv
- superclass of \sqsupseteq
- disjoint with $\sqsubseteq \neg$
- none of the above leave empty

As an example, the semantic relationship `xPerson` is subclass of `yPerson` is already indicated in the table.

| | yPerson | xPerson | zPerson | Vegetarian | Vegan | Frutarier | Carnivore |
|------------|----------------------------------|----------------------------------|--------------------------------|---|----------------------------------|--------------------|-----------|
| Carnivore | $\sqsubseteq \neg$ | $\sqsubseteq \neg$ | $\sqsubseteq \neg$ | $\sqsubseteq \neg$ | $\sqsubseteq \neg$ | $\sqsubseteq \neg$ | \equiv |
| Frutarier | $\sqsubseteq f \text{ sub } y$ | \sqsubseteq | $\sqsubseteq f \text{ sub } z$ | $\sqsubseteq (f \text{ sub } v)$ | $\sqsubseteq (f \text{ sub } v)$ | \equiv | |
| Vegan | $\sqsupseteq v \text{ super } y$ | \sqsubseteq | $\sqsubseteq v \text{ sub } z$ | $\sqsupseteq \text{vegan } s \text{ v}$ | \equiv | | |
| Vegetarian | $\sqsupseteq v \text{ super } y$ | \sqsubseteq | $\sqsubseteq v \text{ sub } z$ | \equiv | | | |
| zPerson | $\sqsupseteq z \text{ super } y$ | $\sqsupseteq z \text{ super } x$ | \equiv | | | | |
| xPerson | $\sqsubseteq x \text{ sub } y$ | \equiv | | | | | |
| yPerson | \equiv | | | | | | |

Edit:

| | yPerson | xPerson | zPerson | Vegetarian | Vegan | Frutarier | Carnivor |
|------------|------------------|------------------|----------------------------------|------------------|------------------|------------------|----------|
| Carnivor | $\subseteq \cap$ | $\subseteq \cap$ | $\subseteq \cap$ | $\subseteq \cap$ | $\subseteq \cap$ | $\subseteq \cap$ | \equiv |
| Frutarier | \subseteq | | \subseteq | \subseteq | \subseteq | $\subseteq \cap$ | |
| Vegan | \supseteq | \supseteq | \supseteq (very sub of person) | \supseteq | \equiv | | |
| Vegetarian | \supseteq | \supseteq | \supseteq | \equiv | | | |
| zPerson | | | \equiv | | | | |
| xPerson | \subseteq | \equiv | | | | | |
| yPerson | \equiv | | | | | | |

