

# Coastal Dynamics 1 (CIE4305)

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Section of Hydraulic Engineering

## 8.

### Longshore transport and coastline changes



# Coastal Dynamics 1

## Contents

1. Introduction
2. Large-scale coastal variation
3. Oceanic wind waves and tide
4. Global wave and tidal environments
5. Coastal hydrodynamics
6. Sediment transport
7. Cross-shore transport and profile development
- 8. Longshore transport and coastline changes (Chapter 8)**
9. Coastal inlets and tidal basins
10. Coastal protection

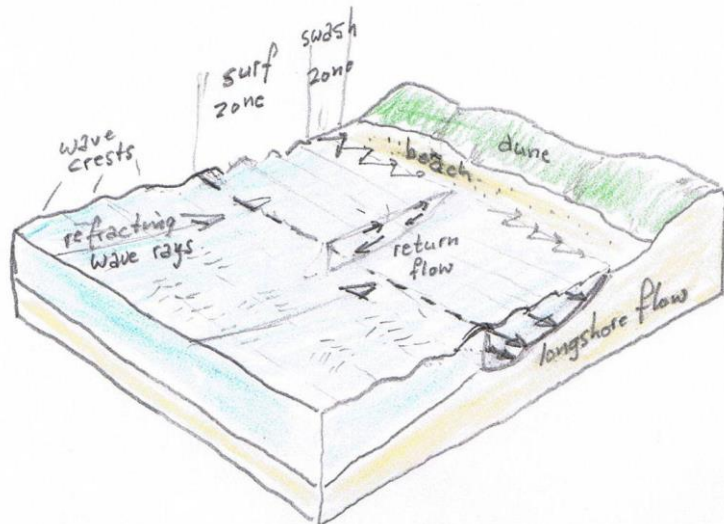
# Longshore transport and coastline changes

## Chapter 8 of lecture notes

- A. Longshore transport**
- B. Calculation of coastline change
- C. Coastline features
- D. Growth of features
- E. Example: Amager beach

## 8-A Longshore transport

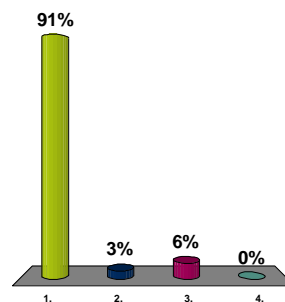
### The beach – a 3D river of sand



## 8-A Longshore transport

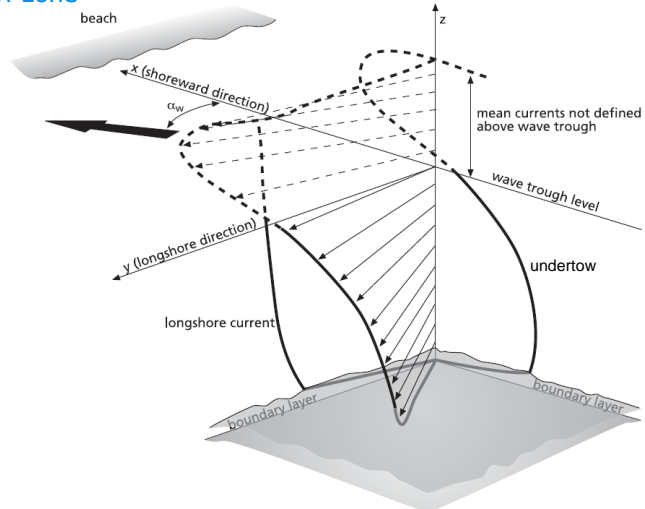
Consider the mean flow velocity in the surf zone.  
Which of the below statements is **wrong**?

- ✓ 1. The mean flow at mean water level is in longshore direction
- 2. The mean flow direction varies with height above the bed
- 3. Near the bottom, the mean current has an offshore directed component
- 4. Abstain



## 8-A Longshore transport

Depth-variation of the combined cross-shore and longshore velocity profiles in the surf zone



## 8-A Longshore transport

Stirring by short waves, transport by longshore current

$$\langle S_y \rangle = \underbrace{\int_a^h VC \, dz}_{\text{current-related part}} + \underbrace{\int_a^h \tilde{v} \tilde{c} \, dz}_{\text{wave-related part}}$$

time-averaged suspended sediment transport rate

$$\langle S_y \rangle = m_1 \langle |\tilde{r}_b|^{(n-1)/2} \rangle V = m_2 \langle |\tilde{u}|^{n-1} \rangle V$$

time-averaged bed / total load transport

$$|\tilde{u}| = \sqrt{u^2 + V^2}$$

$$u = \hat{u} \cos \omega t$$

$$n = 3$$

$$\langle S_y \rangle = \underbrace{m_2 \langle u^2 + V^2 \rangle}_{\text{sediment load stirred by wave-current motion}} V \quad \text{longshore current responsible for transport}$$

$$= \frac{1}{2} m_2 \hat{u}^2 V + m_2 V^3$$

## 8-A Longshore transport

### Cross-shore distribution of longshore transport (1)

- Current  $V$  alone:
  - $S = mV^n$
  - where  $S$  is sediment transport in  $\text{m}^3/\text{s}/\text{m}$  (unit width)
  - $m$  = coefficient
  - $n$  is power between 3 and 5
- Bagnold (>1960), Engelund-Hansen (>1970), Van Rijn (>1980)

## 8-A Longshore transport

### Cross-shore distribution of longshore transport (2)

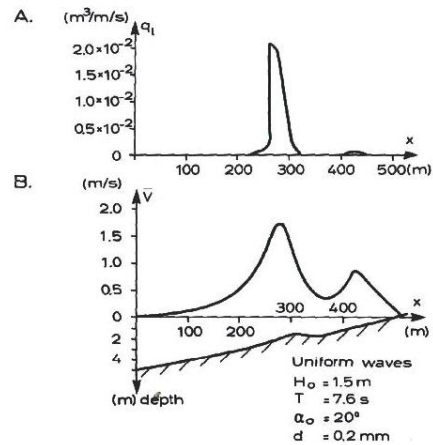
- Waves plus current  $V$ :
  - $S = m_2 \langle |\vec{u}|^{n-1} \rangle V$
  - where  $S$  is sediment transport in  $\text{m}^3/\text{s}/\text{m}$  (unit width)
  - $m_2$  = coefficient
  - $n$  is power between 3 and 5
- For  $n = 3$ :  $S = m_2 \langle u^2 + V^2 \rangle V$
- Bijker (1972), Inman/Bowen/Bailard (> 1980), Van Rijn/Soulsby (> 1990)

## 8-A Longshore transport

### Cross-shore distribution of longshore transport (3)

Littoral sediment transport rates

Littoral current and coastal profile



## 8-A Introduction

### Bulk longshore transport



S per m

$S: m^3/s.m$



S integrated over zone; e.g. surf zone

surf zone

$S: m^3/s; m^3/y$

## 8-A Longshore transport

### Dimensionally correct version

- Based on a large number of field and lab data:
  - $I = K_c P$
  - where  $K_c = 0.77$  is an empirical constant ( $H_{rms}$  !)
  - $I = \rho(s-1)gS$  is the submerged weight of the transported sediment
  - where  $\rho$  is the density of water and  $s$  the relative density, and  $g$  the gravitational acceleration
  - $S$  is the bulk longshore sediment transport rate **measured as a solid volume**

Komar and Inman (1970)

## 8-A Longshore transport

### Dimensional form CERC-formula

- Using non-homogeneous units:
  - $S' = 7500P$
  - $S'$  in cubic yards per year deposited volume (p!)
  - $P$  in US Customary units (slugs, ft) with  $H_s$  as input
- Evaluation by Fredsøe and Deigaard (1992):
  - $\rho g(s-1)S = 0.41P$
- Difference mainly due to use of  $H_s$  instead of  $H_{rms}$

SPM 1984

## 8-A Longshore transport

### Energetics approach to bulk longshore transport (1963-1971)

Dissipated power per unit shoreline

$$(Ec_g)_b \cos \varphi_b$$

Mean frictional force per unit shoreline

$$(Ec_g)_b \cos \varphi_b / \hat{u}_b$$

Frictional resistance of sediment:

$$\mu W = \tan \varphi W$$

$$(Ec_g)_b \cos \varphi_b / \hat{u}_b = \mu W$$

$$I = WV = \varepsilon \times \frac{(Ec_g)_b \cos \varphi_b}{\mu \hat{u}_b} V$$

with  $V \propto \frac{\tan \beta}{c_f} \hat{u}_b \sin \varphi_b \cos \varphi_b$

NB In Chapter 5  $\cos \varphi_b \approx 1$

and neglecting dependencies on slope and sediment properties:

$$I = \text{constant} \times (Enc)_b \cos^2 \varphi_b \sin \varphi_b$$

Compare CERC equation!

## 8-A Longshore transport

### Interpretation CERC formula?

$$I = K_c P$$

$$P = (Enc)_b \cos(\varphi_b) \sin(\varphi_b)$$

- In 1972: new concept of radiation stresses

$$P = S_{yx,b} c_b$$

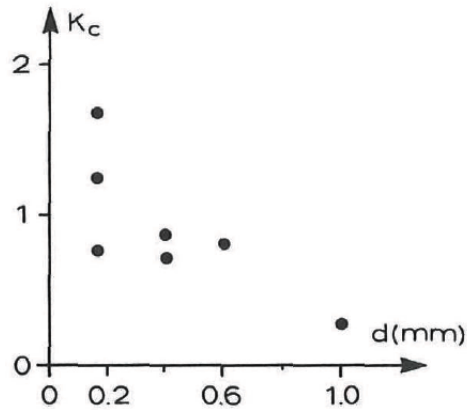
- Energetics approach

$$I = \text{constant} \times (Enc)_b \cos^2 \varphi_b \sin \varphi_b$$



## 8-A Longshore transport

### Grain-size dependency



Variation in  $K_c$  factor with grain size according to Dean et al. (1982)

## 8-A Longshore transport

### Alternative analysis of field and lab data

$$I_m = 2.27 H_{s,b}^2 T_p^{1.5} (\tan \alpha_b)^{0.75} D^{-0.25} (\sin 2\phi_b)^{0.6}$$

where  $I_m = \rho(s-1)(1-p)S$  is in kg/s, H and D in m

- NB1: proportional to the beach slope
- NB2: inversely proportional to grain size

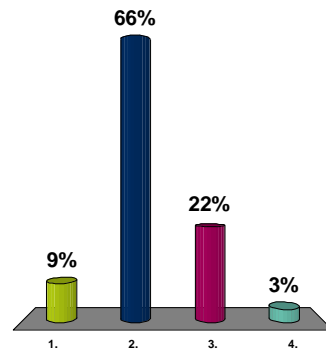
Kamphuis (1991)

## 8-A Longshore transport

Kamphuis' formula is proportional to the beach slope and inversely proportional to the grain size diameter.  
The CERC formula contains neither of these variables.

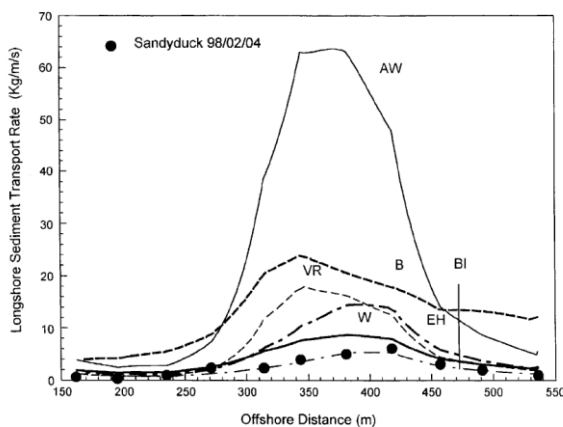
These two findings ...

1. ... contradict each other
- ✓ 2. ... are in agreement with each other
3. ... are completely unrelated
4. Abstain



## 8-A Longshore transport

Comparison measured and calculated cross-shore distribution



B: Bijker,  
BI: Bailard-Inman,  
VR: Van Rijn

Bayram et al. 2001

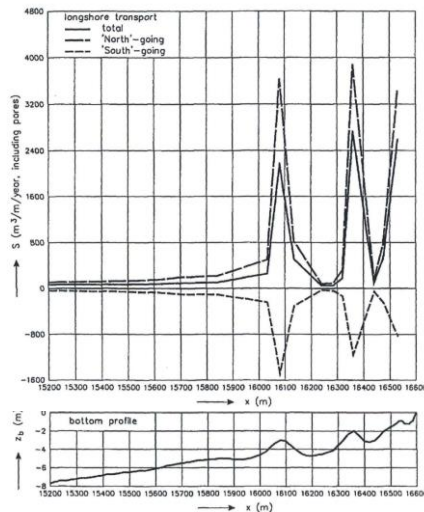
## 8-A Longshore transport

### Cross-shore distribution of longshore transport along Dutch coast

Noordwijk model computations

The effect of tidal currents is also taken into account

Van Rijn et al. 1997

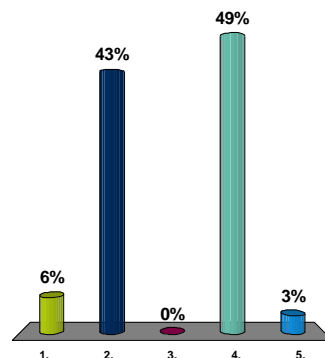


## 8-A Longshore transport

The northward transport is larger on the inner bar than on the outer bar. The southward transport is larger on the outer bar.

Which of the following explanations is **true**?

1. There is a correlation between SW waves and high tide
2. Swell generally arrives from the NW in the shallow North Sea basin
3. The wave-driven and tide-driven flows work in concert
- ✓ 4. Tidal water levels are different for the northward flood and southward ebb current
5. Abstain

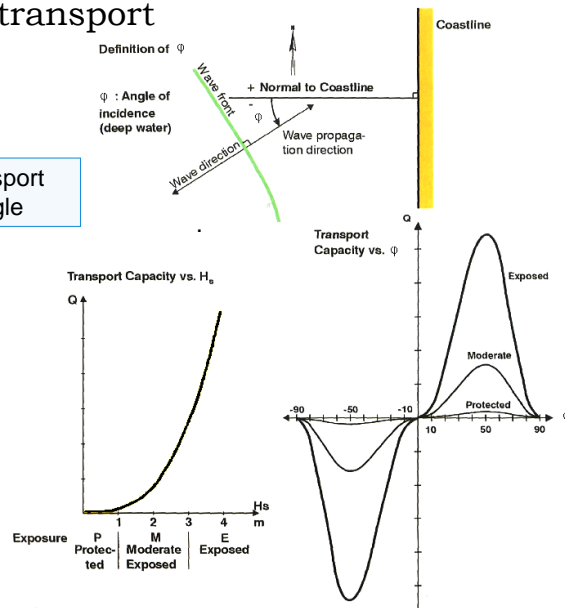


## 8-A Longshore transport

### $S, \phi$ diagram (1)

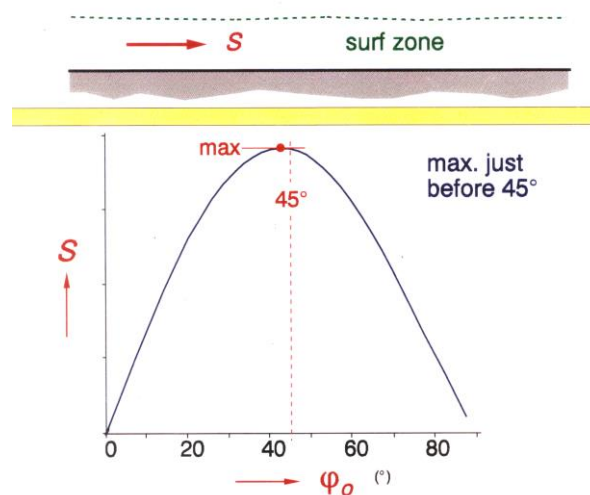
Variations in longshore transport with wave exposure and angle

Mangor, 2004



## 8-A Longshore transport

### $S, \phi$ diagram (2)



## 8-A Longshore transport

### Typical values of longshore transport (1)

#### Typical longshore sediment transport in surfzone Holland coast

Integrated surfzone gross	$O(10^6)$ m <sup>3</sup> /year or per extreme event
Integrated surfzone net	$O(10^5)$ m <sup>3</sup> /year
Natural length scale gradients	10 - 100 km (long term scale)
Human-induced length scale gradients	1 - 10 km (medium term scale)
Net natural gradients	1 - 10 m <sup>3</sup> /m/year
Net human-induced changes	10 - 100 m <sup>3</sup> /m/year
Effective profile height	10 m
Net natural shoreline changes	$O(0.1 - 1)$ m/year
Net human-induced shoreline changes	$O(1 - 10)$ m/year

## 8-A Longshore transport

### Typical values of longshore transport (2)

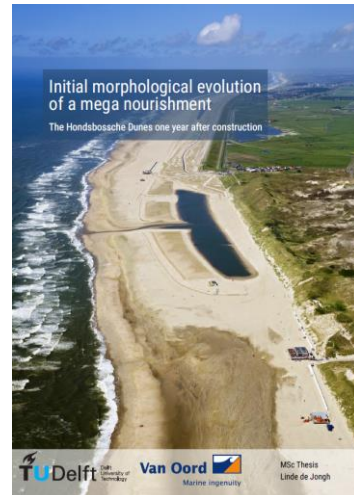
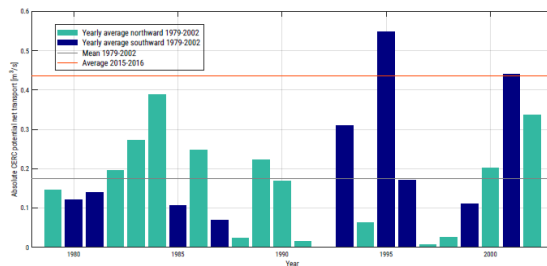
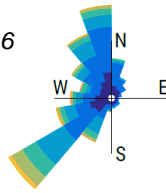
#### Typical longshore sed. transport in surfzone Mediterranean coast

Integrated surfzone gross	$O(10^5)$ m <sup>3</sup> /year or per extreme event
Integrated surfzone net	$O(10^4)$ m <sup>3</sup> /year
Natural length scale gradients	10 km (long term scale)
Human-induced length scale gradients	1 - 10 km (medium term scale)
Net natural gradients	1 m <sup>3</sup> /m/year
Net human-induced changes	1 - 10 m <sup>3</sup> /m/year
Effective profile height	10 m
Net natural shoreline changes	$O(0.1)$ m/year
Net human-induced shoreline changes	$O(0.1 - 1)$ m/year

## 8-A Longshore transport

Engineering use of CERC formula (De Jong, 2017)

Net sediment transport 2015-2016  
factor 2,5 larger than long-term  
average 1979-2002



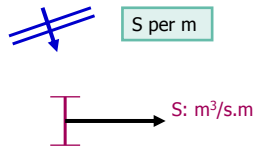
# 8.

## Longshore transport and coastline changes

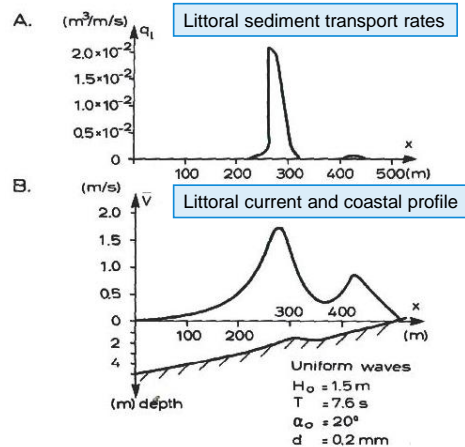
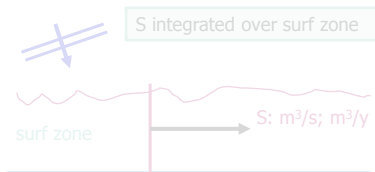


## 8-A Recap: Longshore transport

### Cross-shore distribution of longshore transport



Bulk transport:  $S \sim H^{2.5}, \sin(\dots)$



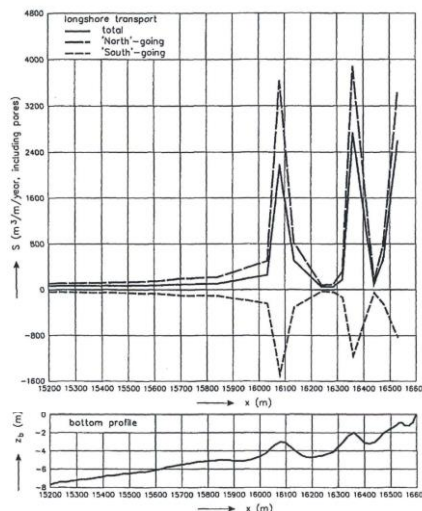
## 8-A Longshore transport

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Noordwijk model computations

The effect of tidal currents is also taken into account

Van Rijn et al. 1997



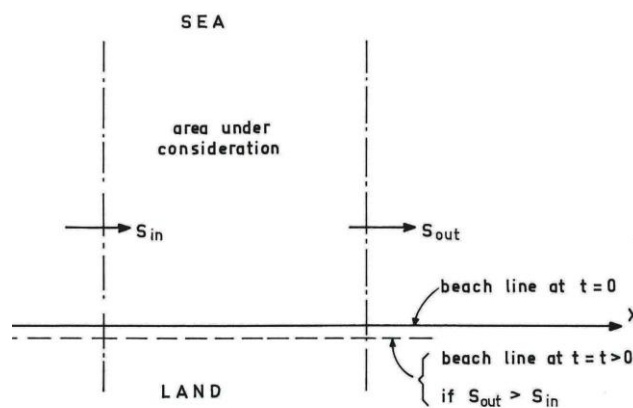
## Longshore transport and coastline changes

### Chapter 8 of lecture notes

- A. Longshore transport
- B. Calculation of coastline change**
- C. Coastline features
- D. Growth of features
- E. Example: Amager beach

## 8-B Calculation of coastline change

### Longshore transport continuity

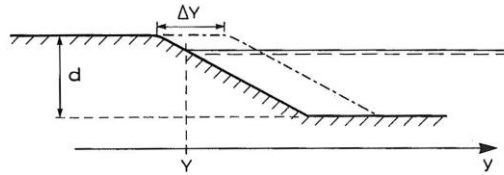




## 8-B Calculation of coastline change

### Longshore transport and coastal change in a coastline model

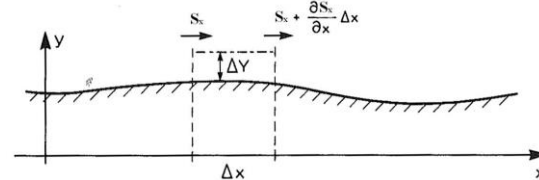
A.



Continuity equation:

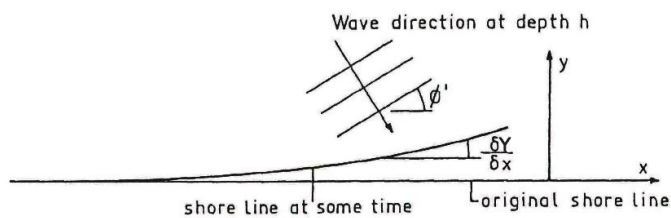
$$\frac{\partial Y}{\partial t} + \frac{1}{d} \frac{\partial S_x}{\partial x} = 0$$

B.



## 8-B Calculation of coastline change

### Governing equations

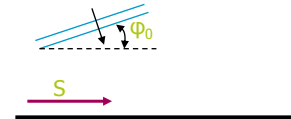
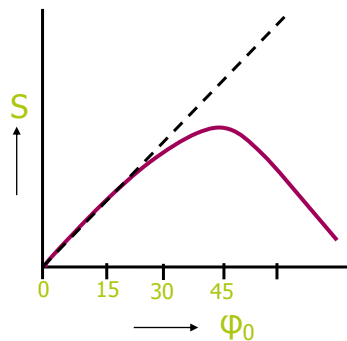


$$\frac{\partial Y}{\partial t} + \frac{1}{d} \frac{\partial S_x}{\partial x} \frac{\partial \phi}{\partial x} = 0 \quad \xrightarrow{\partial \phi = -\partial Y / \partial x} \quad \frac{\partial Y}{\partial t} - \frac{1}{d} \frac{\partial S_x}{\partial x} \frac{\partial^2 Y}{\partial x^2} = 0$$

## 8-B Calculation of coastline change

Simplify governing equations

$S$ : linear function of  $\varphi$  ?



$$\left. \begin{aligned} \frac{\partial Y}{\partial t} - \frac{1}{d} \frac{\partial S_x}{\partial \varphi} \frac{\partial^2 Y}{\partial x^2} &= 0 \\ \frac{\partial S_x}{\partial \varphi} &= s = \frac{S}{\varphi'} \end{aligned} \right\}$$

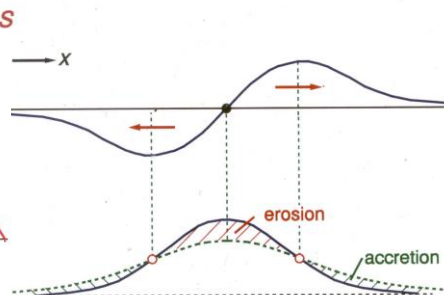
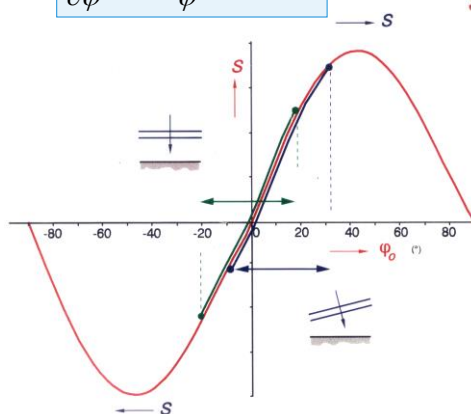
$$\frac{\partial Y}{\partial t} - \frac{s}{d} \frac{\partial^2 Y}{\partial x^2} = 0$$

Heat or diffusion equation

## 8-B Calculation of coastline change

Perturbations (nourishment, delta after cut-off of sediment supply) smooth out if:

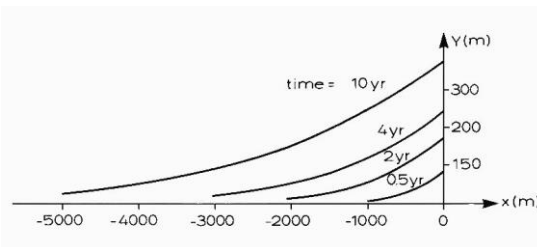
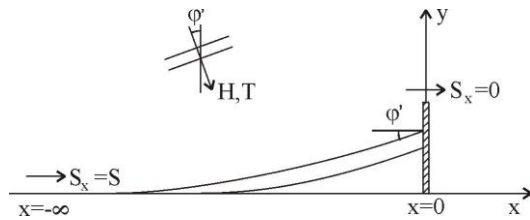
$$\frac{\partial S_x}{\partial \varphi} = s = \frac{S}{\varphi'} \quad \text{positive}$$



What if (deep water) angle  $> 45^\circ$ ?  
See later (growth of features)

## 8-B Calculation of coastline change

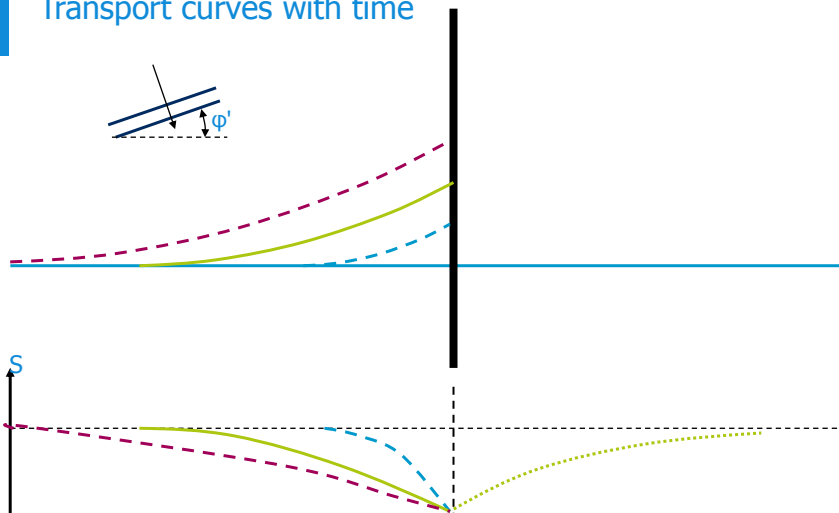
### Analytical solutions for accretion near breakwater



$$L(t) = 2\sqrt{\frac{\phi' S t}{\pi d}}$$

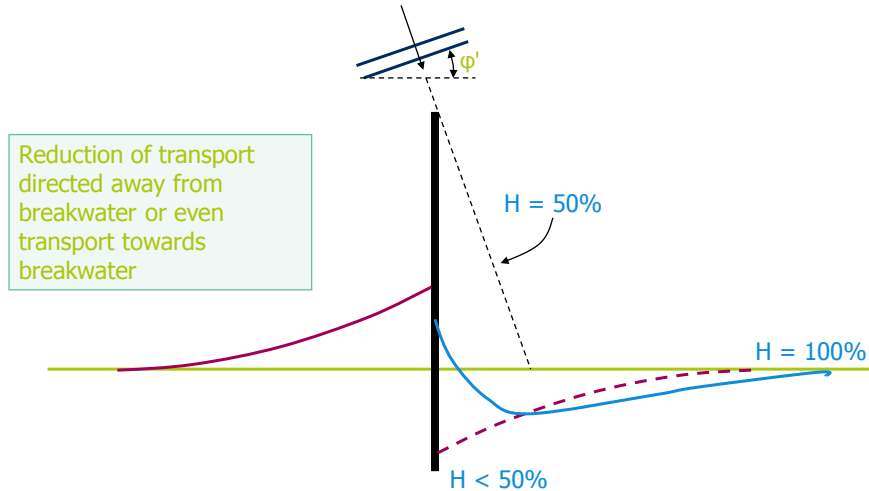
## 8-B Calculation of coastline change

### Transport curves with time



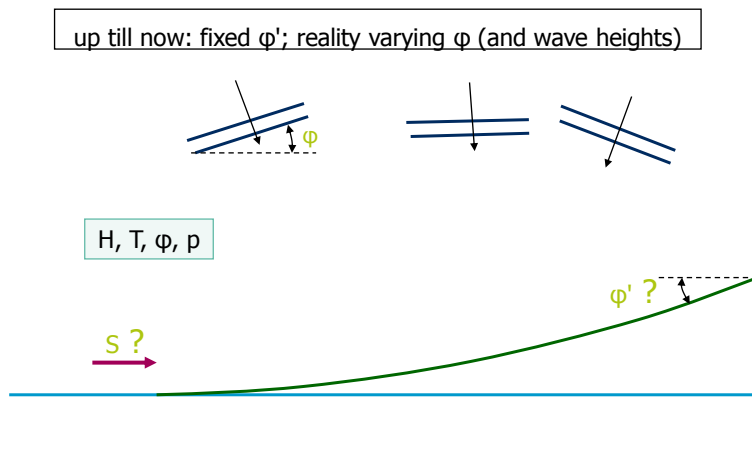
## 8-B Calculation of coastline change

Sheltering and diffraction at lee-side affects wave angles,  
wave heights and set-up



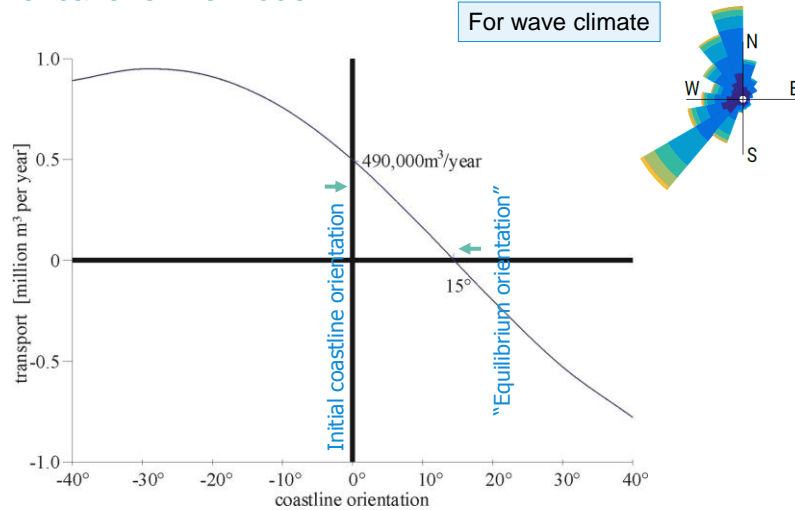
## 8-B Calculation of coastline change

Wave climate instead of waves from one direction



## 8-B Calculation of coastline change

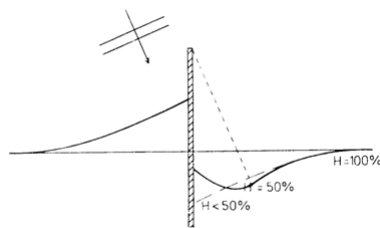
### Numerical one-line model



## 8-B Calculation of coastline change

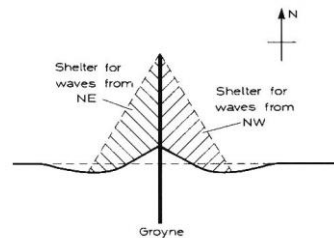
### Leeside

#### One wave condition



Effect diffraction + set-up gradient

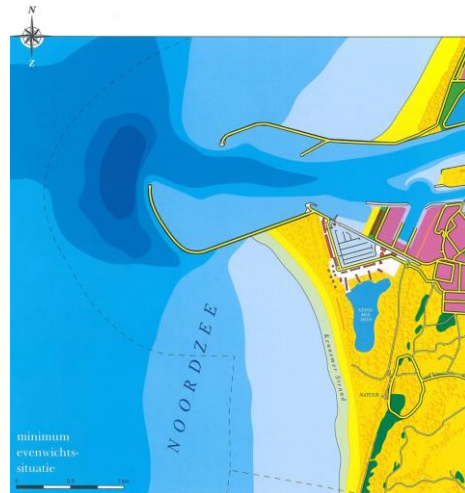
#### Mirrored wave climate



Sheltering effect around a groyne immediately after construction

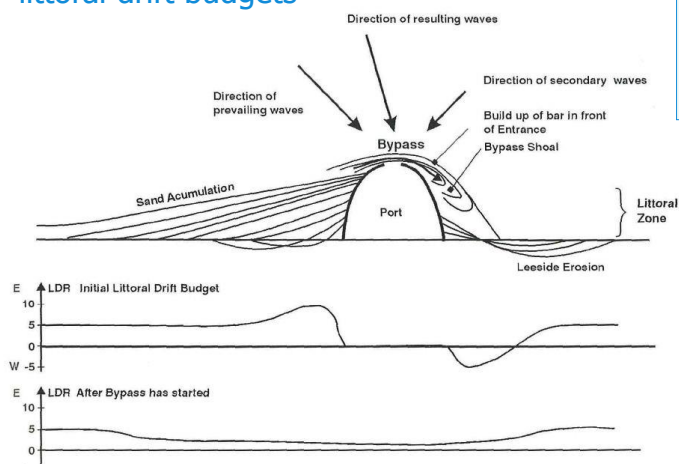
## 8-B Calculation of coastline change

### Accretion next to jetties in IJmuiden



## 8-B Calculation of coastline change

### Schematic shoreline, morphological development and littoral drift budgets



Note:  
Erosion volume  
must be equal to  
accretion volume

Mangor, 2004

# 8.

## Longshore transport and coastline changes



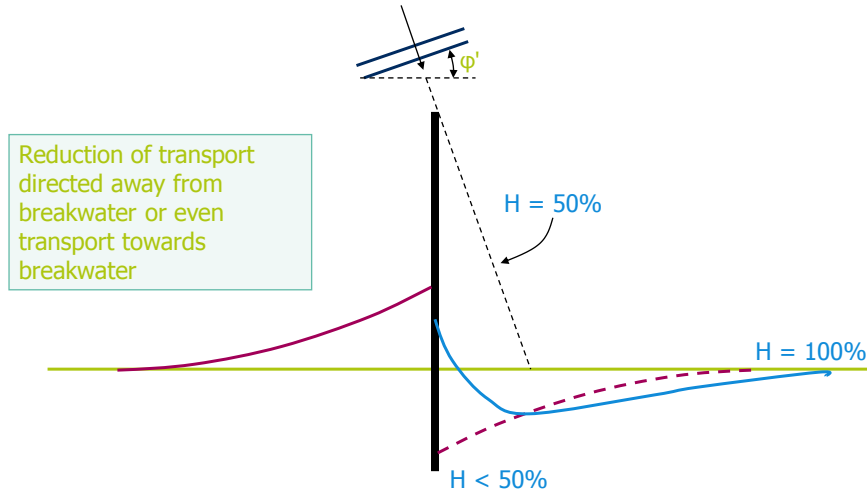
# 8.

## Household announcements

- Extra class on Thu 22 March
  - 13:45-15:30 hr: Tidal inlets by Marcel Stive
  - 15:45-17:30 hr: Extra class by students CD-1
- Maple-TA questions Ch.8 -> Start on time!
  - Sun. 25 March: Deadline submission
  - Tue. 27 March: Special course by TA's

## 8-B Recap: Calculation of coastline change

Shoreline changes around breakwater (first / second order effects due to wave sheltering & diffraction)



## Longshore transport and coastline changes

Chapter 8 of lecture notes

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- B. Calculation of coastline change
- C. Coastline features**
- D. Deltaic coastlines
- E. Growth of features
- F. Example: Amager beach



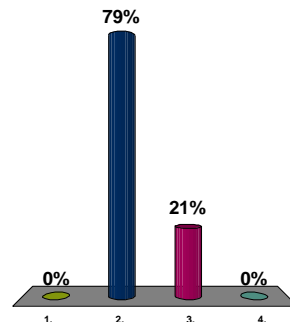


## 8-C Coastline features

Deposition in the shadow zone occurs for normally incident waves also.

Which of the below explanations is **invalid**?

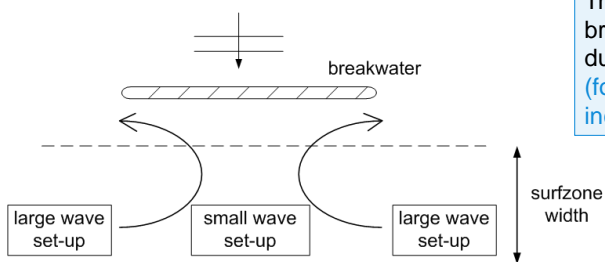
1. Set-up gradients drive a net current from both ends of the breakwater into the shadow zone
- ✓ 2. Refracting waves cause this transport into the shadow zone
3. Diffracting waves induce a longshore transport towards the shadow zone
4. Abstain



Also for oblique wave incidence!

## 8-C Coastline features

### Salient and tombolo development (2)

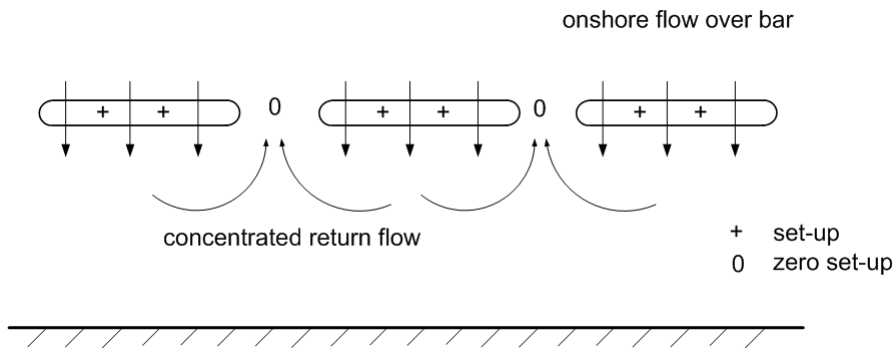


**Effect 2:**  
Transport towards breakwater by current due to set-up variations (for normal and oblique incidence)

**Question:**  
Now consider a submerged breakwater. Which **counteracting erosional effect** can play a role?

## 8-C Coastline features

### Possible erosional effect in case of submerged breakwater



## 8-C Coastline features

### Salient and tombolo development in case of emerged breakwater

Salients



**Question:**  
Salient or tombolo?  
Dependent on.....

## 8-B Coastline features Sitges (Spain)



## 8-B Coastline features Sitges (Spain)



## 8-C Coastline features

Saw tooth pattern of groyned coast



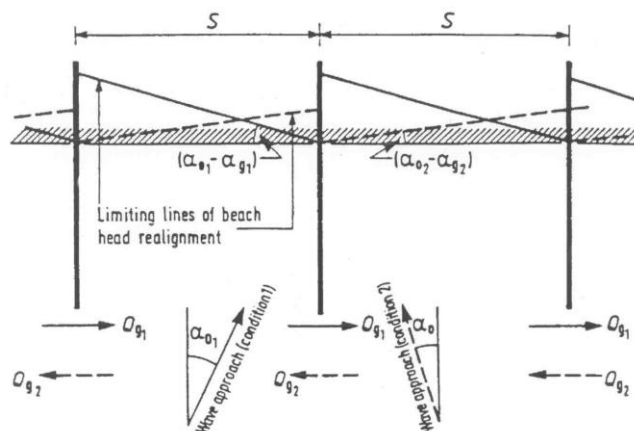
Walcheren, NL



Lake Michigan, Chicago (Oct 2009)

## 8-C Coastline features

Variation of beach on a groyne shore



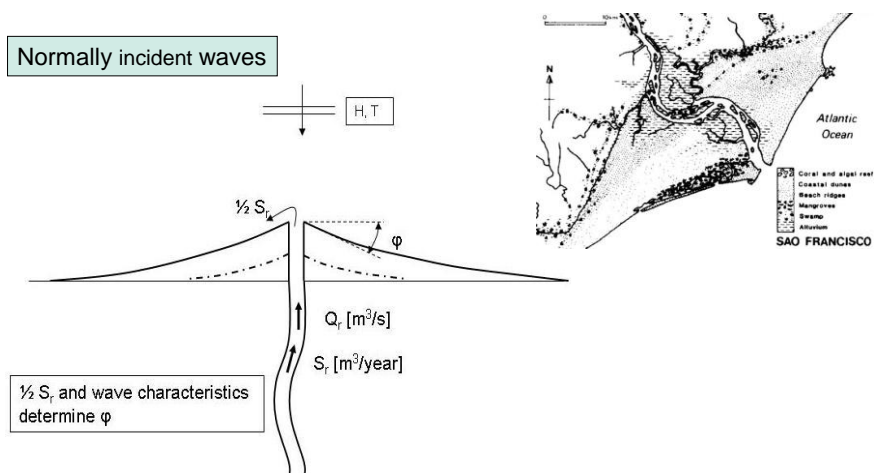
## 8-C Coastline features

Spit (formed with alongshore transported sediment)



## 8-C Coastline features

Development of wave-dominated delta

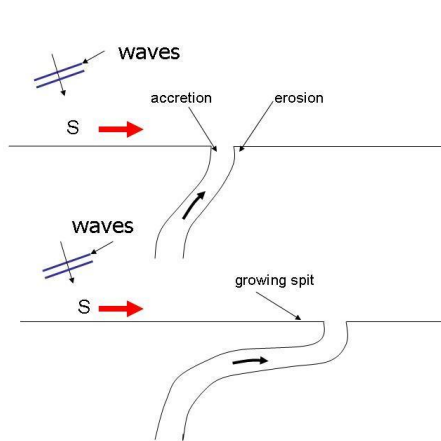




## 8-C Coastline features

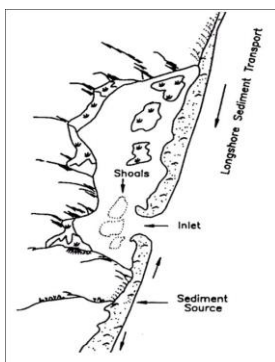
### Spit at river mouth

Kiawah Island, SC



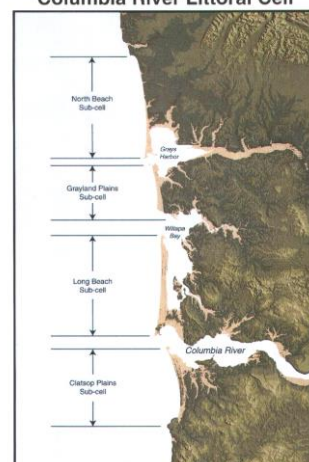
## 8-C Coastline features

### Spit (partially) closing off tidal basin



Dorset, UK

Columbia River Littoral Cell



# Longshore transport and coastline changes

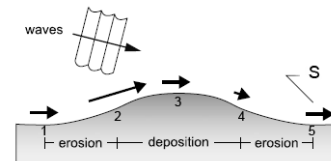
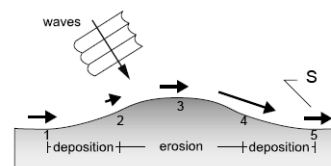
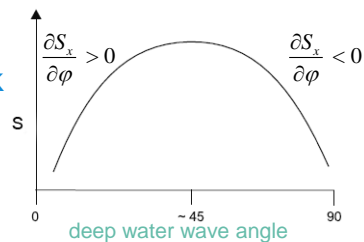
## Chapter 8 of lecture notes

- A. Longshore transport
- B. Calculation of coastline change
- C. Coastline features
- D. Growth of features**
- E. Example: Amager beach

## 8-E Growth of features Negative versus positive feedback

- Low-angle waves ( $< \sim 45^\circ$ ):
  - Sediment transport increases **along the crest** from 2 to 4 (positive gradient) => **erosion**
  - Sediment transport decreases **along flanks** from 1 to 2 and from 4 to 5 (negative gradient) => **accretion**
  - Shape (nourishment, delta, ...) flattens: negative feedback

- High-angle waves ( $> \sim 45^\circ$ ):
  - **Opposite response**
  - Erosion along flanks (increasing S)
  - Accretion along the crest (decreasing S)
  - Features grow: positive feedback

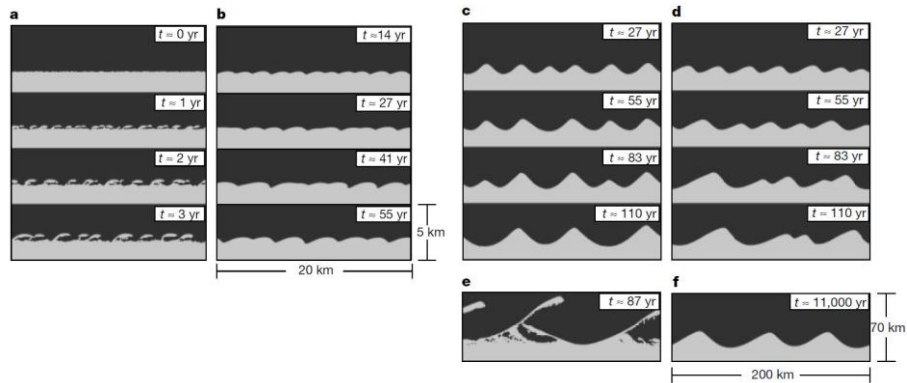




## 8-E Growth of features

Model results Ashton et al. (2001)

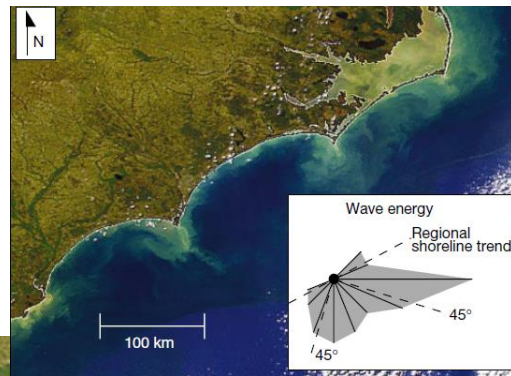
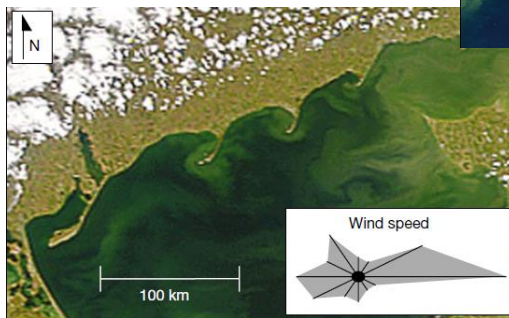
Variations in magnitude and asymmetry of wave angles



## 8-E Growth of features

Examples of large angle incidence

Sea of Azov, Ukraine



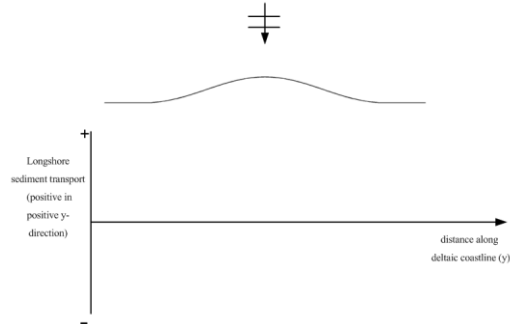
Carolina coast, USA

## Exam question june 2010

75 points  
in total

Assume normally incident waves and ignore all effects of refraction.

- [4] Draw the alongshore sediment transport rate as a function of the distance along the deltaic shoreline just after the damming of the river. *Use the figure on the answer sheet.*
- [2] Indicate in the same figure with + and – in which zones erosion and in which zones accretion can be expected. Explain your reasoning.
- [1] What do you conclude about the long-term fate of the delta?



## Exam question june 2010 (continued)

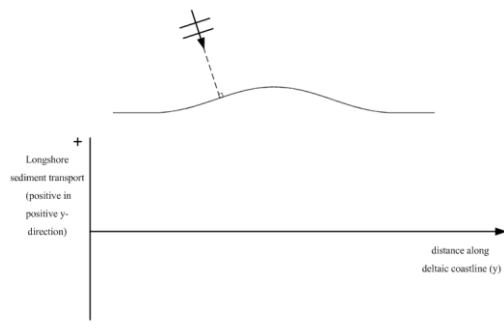
Now assume that instead of normally incident, the waves were obliquely incident under a small angle. The wave angle is indicated in the figure on the answer sheet.

- [4] Draw the alongshore sediment transport rate along the delta just after the damming of the river. Use the same vertical scale as in your answer to a). *Use the figure on the answer sheet.*
- [2] Now draw in the same figure the alongshore sediment transport rate after a new equilibrium has been reached. Explain your reasoning.

Compare Exercise 8-2 in your lecture notes!

### Possible variations:

- Detached breakwater
- Harbour
- Groyne field
- ....

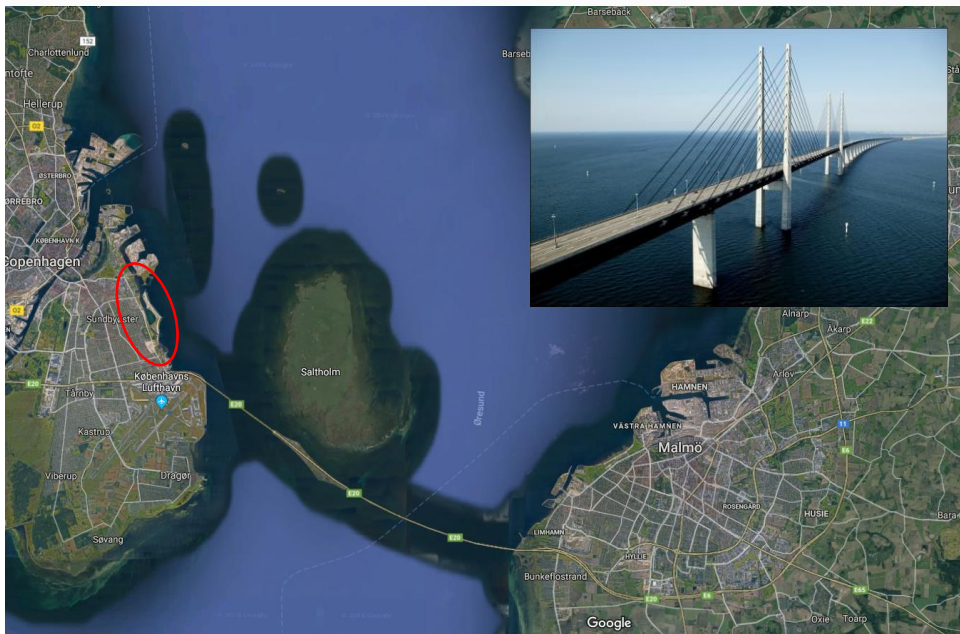


# Longshore transport and coastline changes

## Chapter 8 of lecture notes

- A. Longshore transport
- B. Calculation of coastline change
- C. Coastline features
- D. Growth of features
- E. **Example: Amager beach**

## Amager beach park



## Conditions in 2004

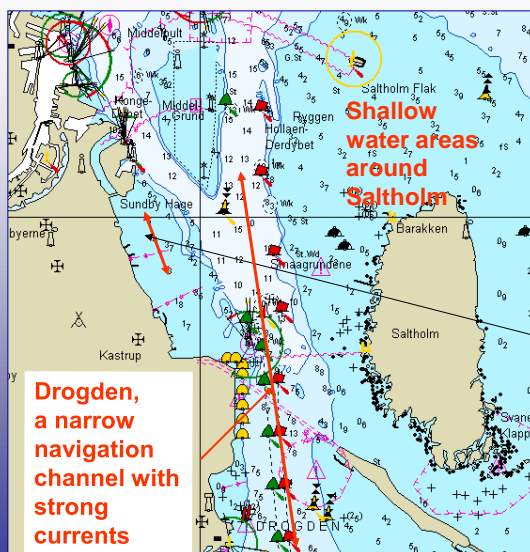


Flat profile approx. 1:200 on the inner 200 m



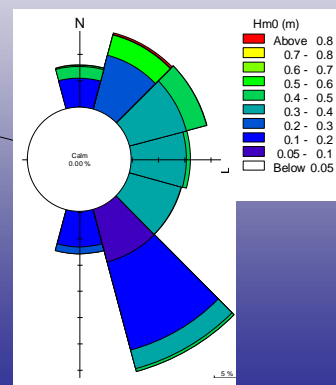
"beach" sand  
behind a wooded  
seawall, soft  
muddy bottom in  
front of wall

## Conditions on the site



Extreme high water level:  
1.25 m

Waves off the beach park





## Requirements to the new beach park

- The beaches shall be exposed to waves to obtain good quality
- Plan form shall be “stable”
- Profiles shall be “stable”
- Loss of sand shall be avoided
- No corners and deep bays to avoid sea weed
- Beach sand shall be coarse enough to avoid problems with wind blown sand
- Not too coarse because the profile will be too steep
- Not too fine as the profile will be too flat and swampy
- Good water quality



Concept:

Move beach seaward to obtain wave exposure

Utilise natural gradient to flush lagoon



Head land

Terminal structures

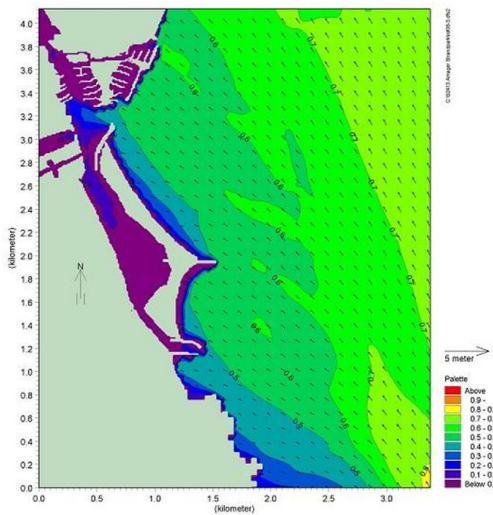
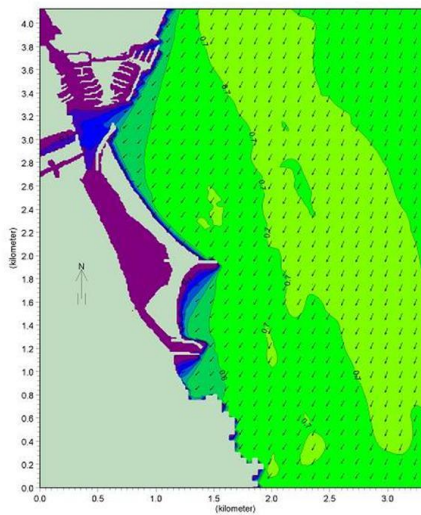


# Wave modelling



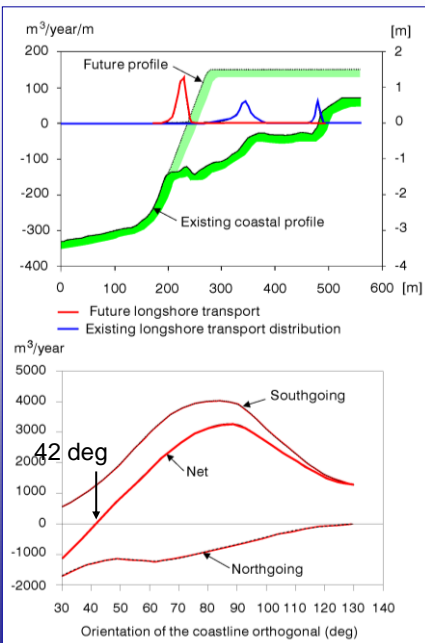
Wind from NNE

Wind from SSE

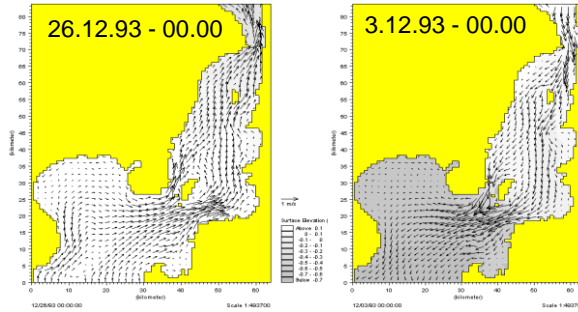


Obtain maximum mobility of the beach sand – steeper profile in deeper water

Align beaches to equilibrium

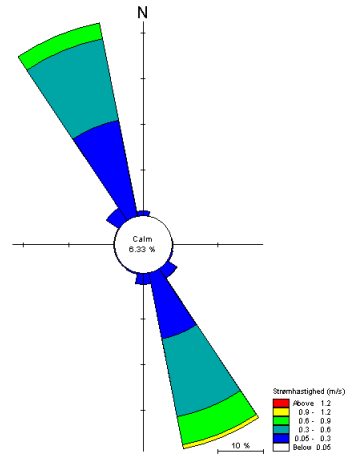
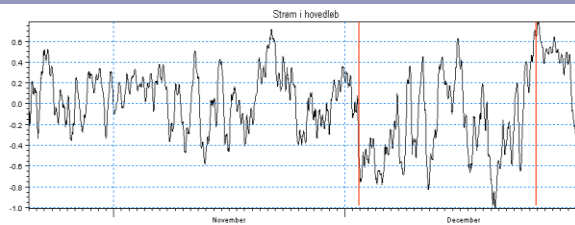


## Regional currents

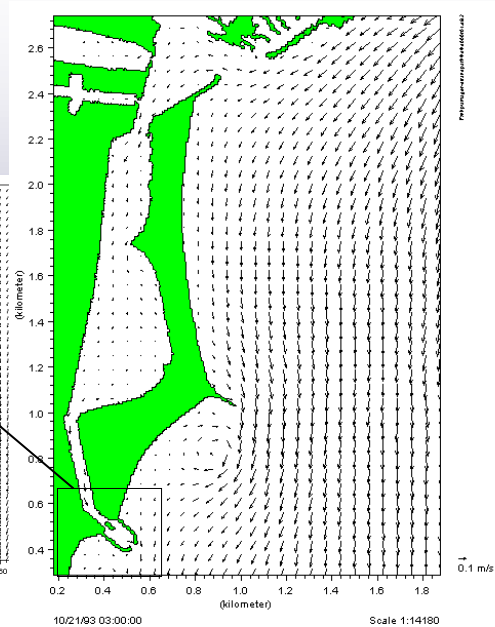
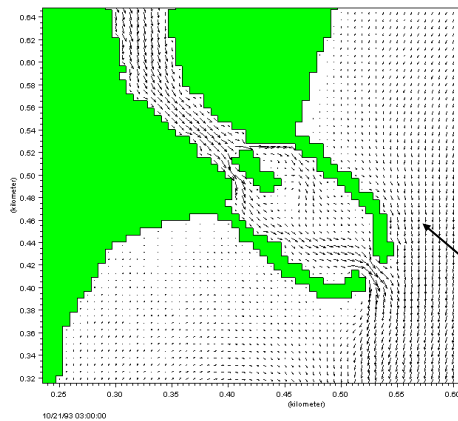


- Good flushing
- Swimmers safety to be checked

## Currents in the navigation channel off the beach park

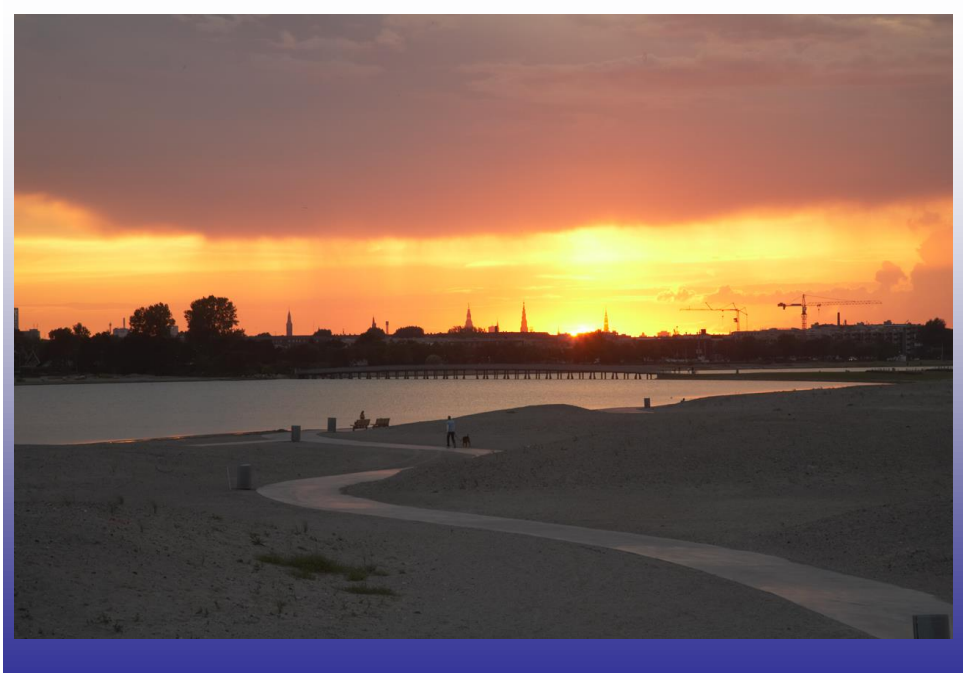


The average time for exchange of water in the lagoon is 24 hours (acceptable)  
Currents along beaches acceptable











August 2005 – just after construction