## **ESE5001 Environmental Engineering Principles**

# Lecture Notes Chemical Principles

#### Introduction

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Concentrations: Quantity of species per volume

#### **Common Units:**

1. Moles per Volume

Eg. 
$$M = \frac{mol}{L}$$
 (in H<sub>2</sub>O, generally not apply in air)

where mole = Avogadro's number of elements:

$$N_{av} = 6.02 \times 10^{23}$$

#### 2. Mass per Volume

- Common concentration units for contaminants in water.
- Eg. mg/L,  $\mu$ g/m<sup>3</sup>
- Milli-: 10<sup>-3</sup>
- Micro-: 10<sup>-6</sup>

#### **Density**

- Mass conc. Summed over all constituents.
  - Fresh water: 1 g cm<sup>-3</sup>
  - Salt water: 1.03 g cm<sup>-3</sup>
    - Pressure has very little influence on density of water
    - Temperature (Yes)
- Air (293K, 1 atm): 1.2 kg m<sup>-3</sup>
   2→3 1.2 mg cm<sup>-3</sup>

Air ~ 1000 x less dense than water



#### 3. Mass or Mole Fraction

- Quantity of species per quantity of base material, both expressed with same measure.
  - ppm  $\equiv 10^{-6} = 1$  part per  $10^6$  parts solution (fluid plus species).
  - ppb  $\equiv 10^{-9} = 1$  part per  $10^9$  parts solution
  - ppt =  $10^{-12}$  = 1 part per  $10^{12}$  parts solution
  - $\% \equiv 10^{-2} = 1$  part per 100 parts solution
- In Air always means \_\_mce\_ Fraction
- In Water always means \_\_\_\_\_ Fraction

### Concentrations and Units of **Measurement Example**

Example 1 (1.C.1 of text): One gram of table salt (NaCl) is dissolved in pure water to make 1 L of solution. Determine mass fraction, mass concentration and molarity of Na<sup>+</sup> in solution.

MW of Nacl = 23 + 35.5 = 58.5 9/mole Soln:

19 of Nau = \frac{1}{58.5} = 0.017 mole of Nat

nutarity of Nat = 0.017 M or IT mM

mass and of  $Na^{-1} = 0.017 \times 23 \frac{9 Na^{+1}}{mate} = 0.39 \frac{9}{L} Na^{+1}$ 

mass fraction:  $\frac{\text{mass of Nat}}{\text{mass of sdr}} = \frac{0.39 \times 10^{-3} (\frac{1}{p})}{(0.00)} = 390 \text{ ppm}$ 

Example 2: A solution contains 8 μg/L Lead (Pb, atomic mass 207). Express this concentration as moles per litre, ppm, and the mole fraction of Pb. Assume the solution has a density of 1 g/ml

solution has a density of 1 g/mL. M= mass and = 8 mg/L Pb = 3.86×10 mode Pb Soln mass frootin: 1 right = 1ppb 8 mg/2 = 8 pph = 0.508 ppm mole fraction = molar come of Pb = 3.8/x10 = 3.8/x10 = (3.8/x10 + 15) = (3.8/x10 + 15) = (3.8/x10 + 15) = (6.95 × 10) = (6.95 × 10) = 18 5/mole = 53-6M

#### **Unit Conversion**

#### Mass and Molar Concentrations Conversion:

$$C_i = MW_i[i]$$

where

[i] = molar concentration of species I

 $MW_i$  = molecular weight of species i

Eg. Convert 50 mg/L of Benzene (C<sub>6</sub>H<sub>6</sub>) into molar concentration?



A natural water had DOC concentration of 3.5 mg/L. The average composition of the organic molecules in the solution is  $C_{30}H_{33}O_{18}N$ . Assuming that all the molecules actually have that composition, compute the molar concentration and mass concentration of the molecules in the sample.

Soln:

n: mw = 3.5 mg C/L mass = 3.5 ms =

 $m = \frac{6.8}{264} = \frac{3.5}{0.20} = \frac{9.7 \times 10^{-6} M}{0.20}$ 

#### **Unit Conversion**

In water, species presents are in dilute levels → density of aqueous solution ≈ density of fresh water = 1000 g/L

#### Therefore:

Mass Conc		Mass Fraction		
1 μg/L	≡	1 ppb		
1 mg/L	=	1 ppm		

Eg. Benzene ( $C_6H_6$ ): WHO standard in drinking water = 10  $\mu$ g/L, as mass fraction?

mad 10.0 se goddol e

Benzene Conc. in air: Singapore outdoor air:  $4 \mu g/m^3$ , convert to mole fraction bic

Consider 1 m³ of air,

Mb fraction = mb y C6HL

mb y sample

mb y Sam  $n = \frac{PV}{RT} = \frac{(1 \text{ atm})(1\text{m}^3)}{82 \times 10^{-6} \text{ md}^{-1}\text{m}^3 \text{k}^{-1} \text{ atm} \times 303 \text{k}} = 41.3 \text{ m/s} \text{ }^{-1}\text{m}^3 \text{k}^{-1} \text{ }$ mole =  $\frac{51 \times 10^{-9}}{(51 \times 10^{-9} + 41.3)} = \frac{1.2 \times 10^{-9}}{1.02 \text{ pob}}$ 

In Air:  $1 \mu g/m^3 \sim 1 ppb$ ;  $1 mg/m^3 \sim 1 ppm$ 

#### **Unit Conversion**

#### Mass Fraction to Mass Concentration:

$$C_i = \rho_s X_i$$

where

 $\rho_{\rm s}$  = solution density (with units of mass per volume).

 $X_i$  = mass fraction

Ci = mass am

## **Impurities**

- Components
- Constituents
- Impurities
- Contaminants
- Pollutants

### **Impurities**

- Inorganic versus Organic (H<sub>2</sub>S vs. Benzene)
- Ionic versus nonionic (HCO<sub>3</sub><sup>-</sup> vs. SiO<sub>2</sub>)
- Elements versus compounds (Pb vs. HCHO)
- Molecular versus particulate (O<sub>2</sub> vs. clay grain)
- Abiotic versus Biotic (soot vs. bacterium)

## **Impurities**

Example of impurity classes — Gases in H<sub>2</sub>O

- Air & water in equlibrium
- O<sub>2</sub> in H<sub>2</sub>O depends on amount in air & originally in H<sub>2</sub>O

## Henry's Law

1st form: 
$$C_w = K_{H,g} \times P_g$$
  
(M) (M atm<sup>-1</sup>) (in atm)  
2nd form:  $P_g = H_g \times C_w$   
(atm) (atm M<sup>-1</sup>) (M)

i.e. Henry's law constants relationship:

$$K_{H,g} = H_g^{-1}$$

### Henry's Law Constant for Water

$$[O_2] = K_{H.O2} \times P_{O2}$$

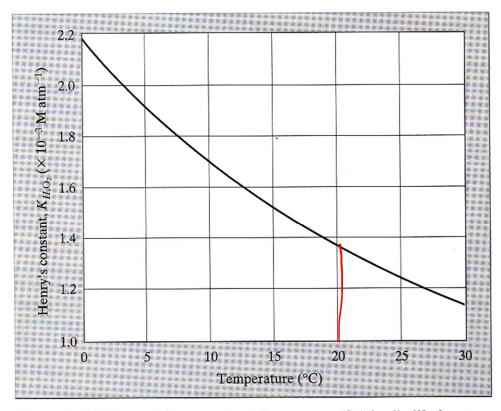
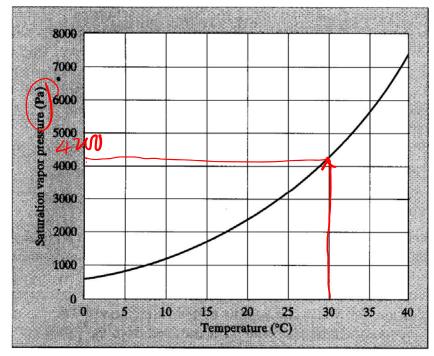


Figure 3.B.2 Henry's law constant for oxygen  $(O_2)$  in distilled water as a function of temperature (Whipple and Whipple, 1911).

## H<sub>2</sub>O Vapor in AIR



$$Y_{H2O} = \frac{P_{H2O}^{o}}{P}$$

Figure 3.B.1 Saturation vapor pressure of water as a function of temperature.

At P = 1 atm =  $1.01 \times 10^5$  Pa & Temp =  $20^{\circ}$ C

$$Y_{H2O} = \frac{4200}{1.01 \times 10^5} = 4\%$$

Relative Humidity = Actual partial pressure/Sat. vapor pressure

## $O_2$ in $H_2O$

At Temp. = 20°C,  

$$K_{H, O2} = /4 \times 10^{-3}$$
 M atm<sup>-1</sup>  
 $[O_2] = K_{H, O2} \times P_{O2} = /4 \times 10^{-3} \times 0.7$  during  $(O_2) = K_{H, O2} \times P_{O2} = 0.2$  dm,  
 $[O_2] = 6.3 \times 10^{-3}$  M  $= \times (16 \times 2) = 0.6$  mg

When bottle opened at Genting Highlands (2 km) above sea level, [O<sub>2</sub>]?

## lonic Impurities in H<sub>2</sub>O

 $H_2O$ 

$$H_2O \Leftrightarrow H^+ + OH^-$$

- 1.  $K_W = [H^+][OH^-] = 10^{-14} M^2$ in pure  $H_2O$ , eq. conc. of  $H^+$ ,  $OH^-$ ?
- 2. Relationship:  $[H^+] = [OH^-]$

$$\rightarrow$$
 [H<sup>+</sup>] = 10<sup>-7</sup> M = [617]

#### Steps:

- 1. Unknowns
- 2. Relationships
- 3. Solve mathematically

Note:

$$pH \equiv -\log_{10} [H^+]$$

Except when in highly concentrated solution, [H<sup>+</sup>] has to be replaced by activity.

#### lons

Common Drinking Water Ions:

**Cations** 

Ca<sup>2+</sup>

 $Mg^{2+}$ 

Na<sup>+</sup>

K<sup>+</sup>

AS T

**Anions** 

CI-

SO<sub>4</sub><sup>2-</sup>

HCO<sub>3</sub>

NUZ

PO4

## Electroneutrality

 Sum of normalities of cations = sum of normalities of anions

$$\Sigma$$
 cations =  $\Sigma$  anions [=] eq/L

Note: 1 eq = 1 mole of net elect. Charge

Acceptable Limits for charge balance:

$$|\Sigma anions - \Sigma cations| \le (0.1065 + 0.0155\Sigma anions)$$

## Electroneutrality

Eg. Determine the acceptability of the following water analysis submitted by a commercial analytical lab.

Cation	Conc	Anion	Conc
	mg/L		mg/L
Ca <sup>2+</sup>	93.8	HCO <sub>3</sub> -	164.7
Mg <sup>2+</sup>	28.0	SO <sub>4</sub> <sup>2-</sup>	134.0
Na <sup>+</sup>	13.7	CI-	92.5
K+	30.2		

#### Approach:

- Convert all ions concentration into normality
- Check with acceptable limits

### Electroneutrality

#### Solution:

Cation	Conc mg/L	Conc	meq /L	Anion	Conc mg/L	Conc mM	meq/L
Ca <sup>2+</sup>	93.8	2.34	4.68	HCO <sub>3</sub> -	167.4	2.74	2.74
Mg <sup>2+</sup>	28.0	1.15	2.30	SO <sub>4</sub> <sup>2-</sup>	134.0	1.39	2.79
Na <sup>+</sup>	13.7	0.60	0.60	Cl <sup>-</sup>	92.5	2.61	2.61
K <sup>+</sup>	30.2	0.77	0.77				
Total			8.35				8.14

(8.35 - 0.54), (8.35 - 0.54),

#### Check accuracy:

$$|\Sigma anions - \Sigma cations| \leq (0.1065 + 0.0155\Sigma anions)$$
 
$$|8.14 - 8.35| \leq [0.1065 + 0.0155(8.14)]$$
 
$$0.21 \leq (0.2327)$$

Accuracy within allowable limits, water analysis is acceptable.

- Intensity of electric field in a solution

$$\mu = \frac{1}{2} \sum_{i} Z_i^2[i] \qquad \text{[=] M}$$

where  $z_i$  = charge of species I

[i] = molarity of species i

Eg. Compute the ionic strength of a solution containing the following concentration of ions:

$$[Ca^{2+}] = 10^{-4} \text{ M}, [CO_3^{2-}] = 10^{-5} \text{ M}, [HCO_3^{-}] = 10^{-3} \text{ M},$$
  
 $[SO_4^{2-}] = 10^{-4} \text{ M}, [Na^+] = 1.02 \times 10^{-3} \text{ M}$ 

$$M = \frac{1}{2} \left[ (2)^{2} (10^{-4}) + (-2)^{2} (10^{-5}) + (-1)^{2} (10^{-3}) + (-2)^{2} (10^{-4}) + (1)^{2} (1-02 \times 10^{-3}) \right] M$$

$$= \left[ (-2)^{2} (10^{-4}) + (1)^{2} (1-02 \times 10^{-3}) \right] M$$

Find the ionic strength of solution with 50 mg/L of NaCl & 100 mg/L of CaSO<sub>4</sub>.

mg/L of NaCl & 100 mg/L of CaSO<sub>4</sub>.

[Na] [(1]] [(42<sup>1</sup>]] [504<sup>2</sup>]

50 mg/L NaU 
$$\Rightarrow \frac{50}{58.5} = 0.855 \text{ M} = [NaT]$$

[(1)]

[(1)]

[(1)]

50 mg/L NaU  $\Rightarrow \frac{50}{58.5} = 0.855 \text{ M} = [NaT]$ 

[(1)]

[(1)]

[(1)]

[(2)]

[(1)]

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[(2)]

[(2)]

[(2)]

[(2)]

[(3)]

[(42<sup>1</sup>)]

[(5)]

[(42<sup>1</sup>)]

[(5)]

[(42<sup>1</sup>)]

[(42<sup>1</sup>)]

[(5)]

[(42<sup>1</sup>)]

Why need to know ionic strength?

- Used for computation of activity for non-diluted solution.
- As concentration of ions in solution increases, electrostatic interactions between ions also increase and the activity of ions becomes somewhat less than their measured or analytical concentrations

Activity: 
$$\{i\} = \gamma_i[i]$$

Where activity coefficient,  $\gamma_i$  (Debye-Hückey relationship):

$$\log \gamma_i = -0.5 Z_i^2 \frac{\sqrt{\mu}}{1 + \sqrt{\mu}}$$

Eg. Calculate the activity coefficients and activities of each ion solution containing 0.01M MgCl<sub>2</sub> and 0.02 M Na<sub>2</sub>SO<sub>4</sub>.

Soln: When salts are dissolved:

Ion	C (M)	Z	CZ <sup>2</sup>
Mg <sup>2+</sup>	0.01	+2	0.04
Na+	0.04	+1	0.04
Cl-	0.02	-1	0.02
SO <sub>4</sub> <sup>2-</sup>	0.02	-2	0.08
		$\Sigma C_i Z_i^2 =$	0.18

lon	Activity Coefficient (γ)	Activity (γC)
Mg <sup>2+</sup>	0.35	0.0035
Na+	0.77	0.031
CI <sup>-</sup>	0.77	0.015
SO <sub>4</sub> <sup>2-</sup>	0.35	0.007

Ionic strength,  $\mu = 1/2 \Sigma_i C_i Z_i^2 = 0.09$ 

$$\log \gamma_i = -0.5 Z_i^2 \frac{\sqrt{0.09}}{1 + \sqrt{0.09}} = -0.115 Z_i^2$$

#### Hardness

- Hard Waters? Water containing multivalents ions
   ⇒ scales in hot-water pipes, heaters, boilers, teapots & precipitates in soap water.
- Expressed as normality (eq/L or meq/L) or as CaCO<sub>3</sub>
- Each mole of CaCO<sub>3</sub> (MW=100 g/mol) liberates 2 moles of cationic charge → a hardness of 1 meq/L is the same as a hardness of 50 mg/L as CaCO<sub>3</sub>.

Classification	Hardness (meq/L)	Hardness (mg/L as CaCO <sub>3</sub> )
Soft	< 1.5	< 7.5
Moderately hard	1.5 - 3	75 -100
Hard	3 - 6	150 - 300
Very hard	>6	>300

#### Hardness

- Total hardness (TH) = sum of normalities of all multivalet cations.
- Carbonate hardness (CH) associated with CO<sub>3</sub><sup>2-</sup> & HCO<sub>3</sub><sup>-</sup>
- Noncarbonate hardness (NCH): the rest

TH =  $\Sigma$  (normalities of multivalent cations)

 In DW Treatment, hardness removal (also called softening) refers to removal of calcium (Ca<sup>2+</sup>) and magnesium (Mg<sup>2+</sup>).

#### Hardness

- To find CH & NCH:
- Compute TH
- $N_c = [HCO_3^-] + 2[CO_3^2] [=] eq/L or meq/L$
- If  $N_c < TH$ ,  $CH = N_c & NCH = TH CH$
- If  $N_c > TH$ , CH = TH & NCH = 0

## **Alkalinity**

- In natural waters, akalinity is attributable to bases such as CO<sub>3</sub>-, HCO<sub>3</sub>- & OH-, ammonia, phosphates, organic bases, etc.
- Refers to the capacity of water to neutralize acids.

$$A = [OH^{-}] + [HCO_{3}^{-}] + 2[CO_{3}^{2-}] - [H^{+}]$$

- Expressed in equivalent per litre.
- Measured by titration: addition of strong acid to water until pH reaches ~ 4.5. Amount of acid added per liter of water sample is the measured alkalinity.

# **Alkalinity**

Eg. NaHCO<sub>3</sub> dissolved in H<sub>2</sub>O
Adding vinegar → bubbling due to CO<sub>2</sub>

# Organics

 Molecule that has carbon and hydrogen, except carbonate and bicarbonate.

**Table C.1** Number of Bonds Associated with Elements in Organic Molecules

Element	Atomic number	Typical number of bonds		
H	1	1		
C	6	4		
N	7	3		
0	8	2		
F	9	1		
P	15	3		
S	16	2		
Cl	17	1		
Br	35	1		
I	53	. 1		

## Organics: Alkanes

Figure C.1 Structures and names of straight-chain alkanes with carbon numbers 1–5.

# Organics: Alkenes

Figure C.2 Structures of some alkenes.

# Organics: Aromatic

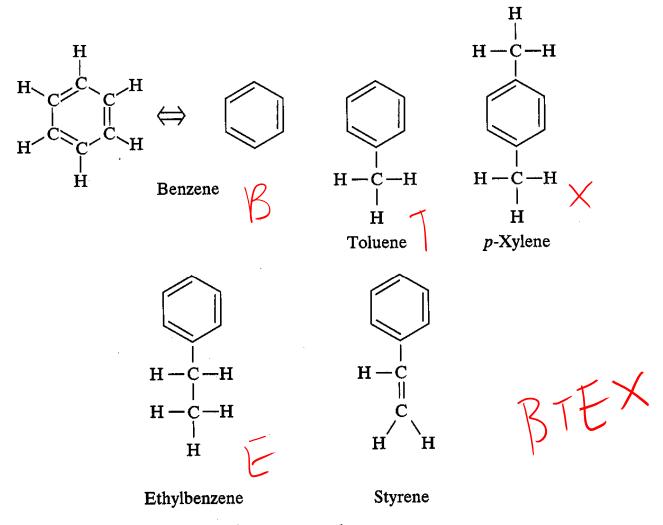


Figure C.3 Some aromatic compounds.

# Organics: Oxygenated

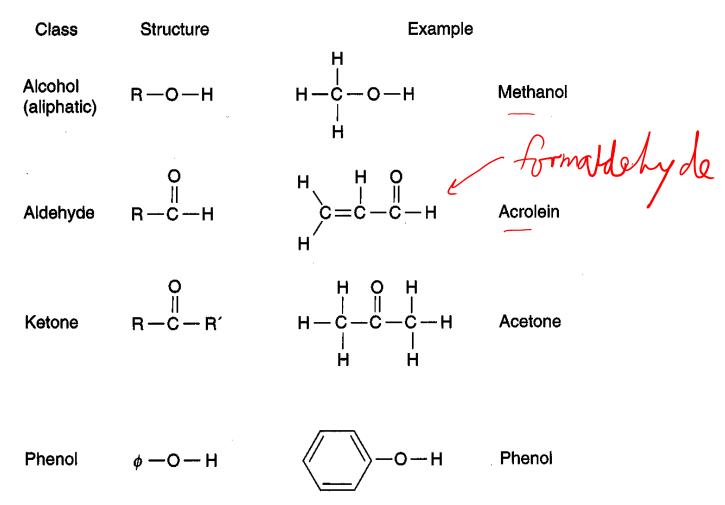


Figure C.4 Representative classes and examples of oxygenated organic compounds of environmental significance.

# Organics: Chlorinated

Dichloromethane 1,1,1-Trichloroethane Trichloroethene Tetrachloroethene (TCA) (TCE) (PCE)

Figure C.5 Chlorinated solvents.

# Organics: Sulfur and Nitrogen Containing

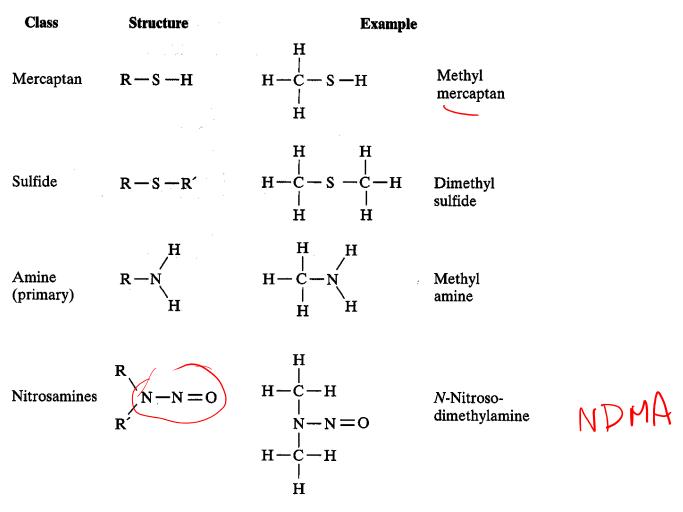


Figure C.7 General structures and specific examples of some organic compounds that contain either sulfur or nitrogen.

#### **Environmental Transformation**

- Partitioning
- Stoichiometry
- Equlibrium
- Kinetics

#### **Partitioning**

# Equilibrium Relationship (or data)

1) Water-gas phase

2) Liquid (NAPL)-water

3) Solid-water

Henry's Law

Solubility

Solubility

regions agreement

# Vapor Pressure of Some Organic Substances at 25°C

Table 3.B.1 Vapor Pressure of Some Organic Substances at 25 °C

Species	Chemical formula	Molecular weight (g/mol)	Vapor pressure (Pa)
Acetone	C <sub>3</sub> H <sub>6</sub> O	58	28,600
Benzene	$C_6H_6$	78	12,800
Benzo(a)pyrene	$C_{20}H_{12}$	252	$7 \times 10^{-7}$
Chloroform	CHCl <sub>3</sub>	119.4	26,000
Dieldrin	$C_{12}H_8Cl_6O$	380	$7 \times 10^{-4}$
Ethylbenzene	$C_8H_{10}$	106	1,280
Ethylene dibromide	$CH_4Br_2$	176	270
n-Octane	$C_8H_{18}$	114	1,890
Naphthalene	$C_{10}H_8$	128	10.6
Phenol	$C_6H_6O$	94	26
2,3,7,8-TCDD	$C_{12}H_4O_2Cl_4$	322	$2 \times 10^{-7}$
Tetrachloroethylene	$C_2Cl_4$	166	2,550
Toluene	$C_7H_8$	92	3,850
1,1,1-Trichloroethane	$C_2H_3Cl_3$	133.4	16,800
Trichloroethylene	$C_2HCl_3$	131.4	9,900

Source: Schwarzenbach et al., 1993.

# Henry's Constant

Table 3.B.2 Henry's Law Constants for Selected Species

Species	Formula	$K_H (M atm^{-1})$	$H_g$ (atm M <sup>-1</sup> )	Temperature (°C)
Ammonia <sup>a</sup>	NH <sub>3</sub>	62	0.016	25
Benzene	$C_6H_6$	0.18	5.6	20
Benzo(a)pyrene	$C_{20}H_{12}$	2040	$4.9 \times 10^{-4}$	20
Carbon dioxide <sup>a</sup>	$CO_2$	0.034	29	25
Carbon monoxide	CO	0.0010	1000	20
Chloroform	CHCl <sub>3</sub>	0.31	3.2	20
Ethylbenzene	$C_8H_{10}$	0.11	9.1	20
Formaldehyde	HCHO	6300	$1.6 \times 10^{-4}$	25
Hydrogen sulfide <sup>a</sup>	$H_2S$	0.115	8.7	20
Methane	$\tilde{\mathrm{CH}_4}$	0.0015	670	20
Naphthalene	$C_{10}H_8$	2.2	0.45	20
Nitric acid <sup>a</sup>	HNO <sub>3</sub>	$2.1 \times 10^{5}$	$4.8 \times 10^{-6}$	25
Nitrogen	$N_2$	0.00067	1500	20
Oxygen	$O_2^-$	0.00138	720	20
Phenol	$C_6H_6O$	2200	$4.5 \times 10^{-4}$	20
Sulfur dioxide <sup>a</sup>	$\tilde{SO}_2$	1.24	0.81	25
Tetrachloroethylene	$C_2Cl_4$	0.083	12	20
Toluene	$C_7H_8$	0.15	6.7	20
1,1,1-Trichloroethane	$C_2H_3Cl_3$	0.055	18	20
Trichloroethylene	$C_2HCl_3$	0.11	9.1	20

<sup>&</sup>lt;sup>a</sup>These species participate in acid-base reactions when dissolved in water. The coefficients listed refer to the solubility of the unreacted species only.

## Solubility of selected organics

 Table 3.B.3
 Water Solubility of Selected Organic Liquids

Species	Solubility (mg/L) <sup>a</sup>
Benzene	1,780
Benzo(a)pyrene	0.0038
Chloroform	8,200
Dieldrin	0.2
Ethylbenzene	152
Ethylene dibromide	4,300
<i>n</i> -Octane <sup>b</sup>	0.72
Naphthalene <sup>b</sup>	31
Phenol	93,000
2,3,7,8-TCDD	0.0002
Tetrachloroethylene	200
Toluene	535
1,1,1-Trichloroethane	4,400
Trichloroethylene	1,100

<sup>&</sup>lt;sup>a</sup>At 20 °C unless otherwise noted.

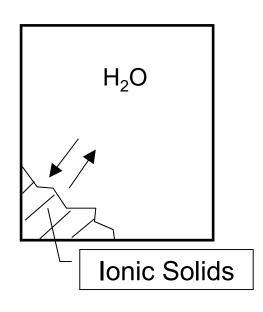
Source: Sawyer et al., 1994; LaGrega et al., 1994; Schwarzenbach et al., 1993.

<sup>&</sup>lt;sup>b</sup>At 25 °C.

# **Water-Gas Partitioning**

• Henry's Law: [i] = 
$$K_{H,I}$$
  $P_i$   
• Eg. 3.11 Given 89 mg/L in gas phase, Find Henry's constant! Add 1 g of CHCl<sub>3</sub> in 2 L vessel  $M_{\text{N}}$  ×  $(i)$  ×  $(i)$  +  $(89 \text{ mHz})(1 \times L)$  =  $19$ 

# **Solid Solubility**



$$A_xB_y$$
 dissolution  $A_xB_y$   $A^{(+)} + yB^{(-)}$  precipitation

$$K_{sp} = [A^{(+)}]^x [B^{(-)}]^y$$

Note: Valid only if solid is present at Equilibrium!

Eg. 
$$AI(OH)_3$$
  $\rightarrow$   $AI^{3+} + 3 OH^{-}$ 

Al can also be in (+2) or (+4) state, but not common.

$$K_{sp} = [AI^{3+}][OH^{-}]^{3}$$

# **Solubility Product**

**Table 3.B.4** Solubility Products for Some Ionic Solids at T = 25 °C

Compound	Equilibrium relationship	$K_{\mathrm{sp}}^{}a}$	$K_{\mathrm{sp}}^{}\mathrm{b}}$
Aluminum hydroxide	$Al(OH)_3 \Leftrightarrow Al^{3+} + 3 OH^-$	$1 \times 10^{-32} \mathrm{M}^4$	$2 \times 10^{-32} \mathrm{M}^4$
Cadmium hydroxide	$Cd(OH)_2 \Leftrightarrow Cd^{2+} + 2OH^{-}$	$2 \times 10^{-14} \mathrm{M}^3$	$5.9 \times 10^{-15} \mathrm{M}^3$
Calcium carbonate	$CaCO_3 \Leftrightarrow Ca^{2+} + CO_3^{2-}$	$5 \times 10^{-9} \mathrm{M}^2$	$8.7 \times 10^{-9} \mathrm{M}^2$
Calcium fluoride	$CaF_2 \Leftrightarrow Ca^{2+} + 2F^{-}$	$3 \times 10^{-11} \mathrm{M}^3$	$4 \times 10^{-11} \mathrm{M}^3$
Calcium hydroxide	$Ca(OH)_2 \Leftrightarrow Ca^{2+} + 2 OH^{-}$	$8 \times 10^{-6} \mathrm{M}^3$	$5.5 \times 10^{-6} \mathrm{M}^3$
Calcium phosphate	$\operatorname{Ca_3(PO_4)_2} \Leftrightarrow 3 \operatorname{Ca}^{2+} + 2 \operatorname{PO_4}^{3-}$	$1 \times 10^{-27} \mathrm{M}^5$	$2.0 \times 10^{-29} \mathrm{M}^5$
Calcium sulfate	$CaSO_4 \Leftrightarrow Ca^{2+} + SO_4^{2-}$	$2 \times 10^{-5} \mathrm{M}^2$	$1.9 \times 10^{-4} \mathrm{M}^2$
Chromium(III) hydroxide	$Cr(OH)_3 \Leftrightarrow Cr^{3+} + 3OH^{-}$	$6 \times 10^{-31} \mathrm{M}^4$	$6 \times 10^{-31} \mathrm{M}^4$
Iron(II) hydroxide	$Fe(OH)_2 \Leftrightarrow Fe^{2+} + 2OH^{-}$	$5 \times 10^{-15} \mathrm{M}^3$	$8 \times 10^{-16} \mathrm{M}^3$
Iron(III) hydroxide	$Fe(OH)_3 \Leftrightarrow Fe^{3+} + 3 OH^{-}$	$6 \times 10^{-38} \mathrm{M}^4$	$4 \times 10^{-38} \mathrm{M}^4$
Magnesium carbonate	$MgCO_3 \Leftrightarrow Mg^{2+} + CO_3^{2-}$	$4 \times 10^{-5} \mathrm{M}^2$	$1 \times 10^{-5} \mathrm{M}^2$
Magnesium hydroxide	$Mg(OH)_2 \Leftrightarrow Mg^{2+} + 2OH^-$	$9 \times 10^{-12} \mathrm{M}^3$	$1.2 \times 10^{-11} \mathrm{M}^3$
Nickel hydroxide	$Ni(OH)_2 \Leftrightarrow Ni^{2+} + 2 OH^-$	$2\times10^{-16}\mathrm{M}^3$	$6.5 \times 10^{-18} \mathrm{M}^3$

<sup>&</sup>lt;sup>a</sup>Sawyer et al., 1994, p. 38.

<sup>&</sup>lt;sup>b</sup>Benefield and Morgan, 1990.

# **Solid Solubility**

Eg. 3.14:  $CaSO_4 \leftarrow Ca^{2+} + SO_4^{2-}$ 

At Equilibrium,

$$K_{sp} = 2 \times 10^{-5} = [Ca^{2+}][SO_4^{2-}]$$

$$Ca^{2+} = [SO_4^{2-}]$$

$$V_{sp} = [a^{2+}]^2 = [SO_4^{2-}]^2 = 2 \times 10^{-5}$$

$$(4.5 \times 10^{3}) = (504^{2}) = 504^{2} = 4.5 \times 10^{3} \text{ M}$$

$$(4.5 \times 10^{3}) = 50.6129 \text{ M}$$

$$(4.5 \times 10^{3}) = 50.6129 \text{ M}$$

$$(4.5 \times 10^{3}) = 50.6129 \text{ M}$$

# **Stoichiometry**

- A chemical reaction must conserve the number of atoms for each element involved in the reaction and the electrical charge associated with ions.
- Eg.

$$C_3H_6CI_{2(I)} + aO_2 \longrightarrow bCO_2 + cH_2O_{(I)} + dHCI$$

$$C: \frac{LNS}{3} = \frac{RNS}{b}$$

$$H: 6 = 2c + d$$

$$C: 2 = d$$

$$0: 26 = 2b + C$$

# Chemical Equilibrium

#### Equilibrium:

1. Not vary with time.



- 2. Internally uniform.
- 3. NO net flows of mass, heat, or species within system or between system and its surroundings.
- 4. Net rate of chemical reactions is ZERO.

# Chemical Equilibrium

$$_{\alpha}A + _{b}B \Leftrightarrow _{c}C + _{d}D$$

- 1) Rate of reaction in forward direction:  $R_f = k_f [A][B]^b$
- Rate of reaction in reverse direction:

$$R_r = k_r [C][D]^4$$

At equilibrium:  $R_f = R_r$   $\rightarrow k_f [A][B] = k_r [C][D]^f$ 

or 
$$\frac{[C][D]^{4}}{[A][B]} = \frac{k_f}{k_r} = K$$

where K = equilibrium constant of the reaction

#### **Acid-Base Reaction**

$$PH = - \log_{10} [H^+]$$

A generic expression:

$$HA \leftarrow H^+ + A^-$$

$$K_A = \frac{[H^+][A^-]}{[HA]}$$

# Strength of Acid $pK_A = -\log_{10}(K_A)$

Define

$$pK_A = -\log_{10}(K_A)$$

- Strong acid: pK<sub>A</sub> ≤ 1 (fully dissociate)
- Weak acid: pK<sub>A</sub> ≥ 1 (partially dissociate)

$$HCI \longrightarrow H^{+} + CI \qquad k_{H4} = \underbrace{[H^{+}][Ci]}_{[HCI]}$$

$$-|0j,k_{H4}| = -|0j,[H^{+}][Gi]$$

$$pk_{A}$$

#### **Acid Dissociation Constants**

**Table 3.C.1** Acid Dissociation Constants  $(T = 25 \, ^{\circ}\text{C})$ 

Species	Chemical formula	р <i>К<sub>A</sub></i>
Perchloric acid	HClO₄	<u>-7</u>
Hydrochloric acid	HC1	-3
Sulfuric acid	$H_2SO_4$	-3
Nitric acid	HNO <sub>3</sub>	-1.2
Sulfonic acid	$H_2SO_3$	1.89
Bisulfate	HSO <sub>4</sub> -	1.92
Phosphoric acid	$H_3PO_4$	2.12
Acetic acid	CH₃COOH	4.7
Butyric acid	C <sub>3</sub> H <sub>7</sub> COOH	4.8
Propionic acid	C <sub>2</sub> H <sub>5</sub> COOH	4.9
Carbonic acid	$H_2CO_3$	6.35
Hydrogen sulfide	$H_2S$	7.1
Dihydrogen phosphate	$H_2^{2}PO_4^{-}$	7.21
Bisulfite	HSO <sub>3</sub>	7.22
Hypochlorous acid	HOCl	7.6
Hydrogen cyanide	HCN	9.2
Ammonium	$\mathrm{NH_4}^+$	9.23
Bicarbonate	HCO <sub>3</sub>	10.33
Hydrogen phosphate	$HPO_4^{32}$	12.32
Bisulfide	HS <sup>-</sup>	12.9

pka-7.6, 7.6

## **Acid-Base Reaction**



• If pH >> pKA, acid is fully Months

• If pH << pK, aicd is fully mon-discretely

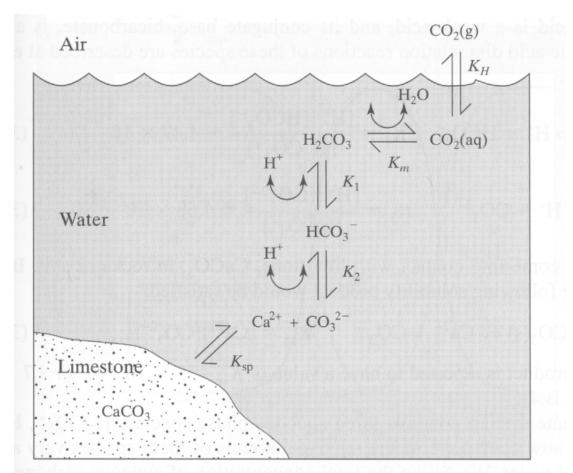
$$-\log_{10}[47] \ll -\log_{10}(K_A)$$

$$[47] \gg K_A$$

$$-\log_{10}[47] ( -\log_{10}[K_A] ) \qquad \underline{(47)(04)} = K_A \Rightarrow \underline{(44)} = \underline{(404)} = K_A \Rightarrow \underline{(44)} = \underline{(404)} = K_A \Rightarrow \underline{(44)} = \underline{(44)} =$$

MOCI !

# Acid-Base Reaction Example: Carbonate System



**Figure 3.C.1** Species and transformations for the carbonate system in natural air-water-limestone environments.

# Acid-Base Reaction Example: Carbonate System

Species involved:  $CO_{2(g)}$ ,  $H_2CO_3^*$ ,  $HCO_3^-$ ,  $CO_3^2$ .

$$[CO_{2}(aq)] = K_{H}P_{CO2}$$

$$CO_{2}(aq) + H_{2}O \Leftrightarrow H_{2}CO_{3} \qquad [H_{2}CO_{3}]/[CO_{2}(aq)] = K_{m} = 1.58 \times 10^{3}$$

$$[H_{2}CO_{3}^{*}] = [CO_{2}(aq)] + [H_{2}CO_{3}] = [CO_{2}(aq)](1 + K_{m})$$

1) 
$$CO_{2(g)} \xrightarrow{H_2O} H_2CO_3^*$$

$$[H_2CO_3^*] = (1+K_m)K_HP_{CO2}$$

2) 
$$H_2CO_3^* + H^+ + HCO_3^-$$

$$K_{C1} = \frac{[H^+][HCO_3^-]}{[H_2CO_3^*]}$$

3) 
$$HCO_3^- + CO_3^2$$

$$K_{C2} = \frac{[H^+][CO_3^{2-}]}{[HCO_3^{-}]}$$

## Eg. Carbonate System

What is the pH of soda "Coca-Cola" (when it is still haven't been opened)?

Assume  $P_{CO2} = 2$  atm

Unknowns (5): [H<sup>+</sup>], [OH<sup>-</sup>], [HCO<sub>3</sub><sup>-</sup>], 
$$[W_1W_3]$$
,  $[W_3]$ 

$$0 \quad [u^*](ou) : K_w = 10^{-14}$$

(2) 
$$K_{ci} = \frac{[H+][H\omega_{i}]}{[U_{i}\omega_{i}]} = 10^{-6.35}$$

Of 
$$[u^*](ou): K_{\omega} = 10^{-14}$$

Of  $[u^*](ou): K_{\omega} = 10^{-14}$ 

Of  $[u^*](ou): K_{\omega} = 10^{-14}$ 

Of  $[u^*](u_{\omega_3}): [u^*](u_{\omega_3}): [u^$ 

$$(4) \quad [U_2 \omega_3^*] = K_u C_{\omega_2}$$

$$(3) \quad [N_1 : [u^+] = (u \omega_3) + [ou] + 2[\omega_3^2]$$

#### Solve using algorithm:

- 1) Use one equation (EN) and pick one variable [H<sup>+</sup>]
- 2) Transform that equation in terms of one unknown. e.g., [H<sup>+</sup>]

# Chemical Equilibrium

#### Coca-cola Example:

• EN + equilibrium:

$$[H^{+}] = \frac{K_{W}}{[H^{+}]} + \frac{K_{c1}K_{H}P_{CO2}}{[H^{+}]} + 2\frac{K_{c1}K_{c2}P_{CO2}}{[H^{+}]^{2}}$$
Where do we get the parameters?

- P<sub>CO2</sub>: 2 atm (given)
- K<sub>H CO2</sub>: Table 3.B.2: K<sub>H CO2</sub>=0.034 M atm<sup>-1</sup> (25°C)

# Chemical Equilibrium

Where do we get the parameters?

$$K_{C1} = \frac{[H^{+}][HCO_{3}^{-}]}{[H_{2}CO_{3}^{*}]}$$
  $(H_{2}CO_{3}^{*} \longleftrightarrow H^{+} + HCO_{3}^{-})$ 

Table 3.C.1: For 
$$H_2CO_3$$
,  $pK_A = 6.35$   
 $pK_A = -log_{10}$  (K)  
 $K_A = 10^{-6.35}$ 

$$K_{C2} = 10^{-10.33}$$

# Henry's Constants

Table 3.B.2 Henry's Law Constants for Selected Species

Species	Formula	$K_H  (\mathrm{M \ atm}^{-1})$	$H_g$ (atm $M^{-1}$ )	Temperature (°C)
Ammonia <sup>a</sup>	NH <sub>3</sub>	62	0.016	25
Benzene	$C_6H_6$	0.18	5.6	20
Benzo(a)pyrene	$C_{20}H_{12}$	2040	$4.9 \times 10^{-4}$	20
Carbon dioxide <sup>a</sup>	$CO_2$	0.034	29	25
Carbon monoxide	CO	0.0010	1000	20
Chloroform	CHCl <sub>3</sub>	0.31	3.2	20
Ethylbenzene	$C_8H_{10}$	0.11	9.1	20
Formaldehyde	HCHO	6300	$1.6 \times 10^{-4}$	25
Hydrogen sulfide <sup>a</sup>	$H_2S$	0.115	8.7	20
Methane	$\overline{\mathrm{CH}_{4}}$	0.0015	670	20
Naphthalene	$C_{10}H_{8}$	2.2	0.45	20
Nitric acid <sup>a</sup>	HNO <sub>3</sub>	$2.1 \times 10^{5}$	$4.8 \times 10^{-6}$	25
Nitrogen	$N_2$	0.00067	1500	20
Oxygen	$O_2^-$	0.00138	720	20
Phenol	$C_6H_6O$	2200	$4.5 \times 10^{-4}$	20
Sulfur dioxide <sup>a</sup>	$SO_2$	1.24	0.81	25
Tetrachloroethylene	$C_2Cl_4$	0.083	12	20
Toluene	$C_7H_8$	0.15	6.7	20
1,1,1-Trichloroethane	$C_2H_3Cl_3$	0.055	18	20
Trichloroethylene	C <sub>2</sub> HCl <sub>3</sub>	0.11	9.1	20

<sup>&</sup>lt;sup>a</sup>These species participate in acid-base reactions when dissolved in water. The coefficients listed refer to the solubility of the unreacted species only.



**Table 3.C.1** Acid Dissociation Constants (T = 25 °C)

Species	Chemical formula	$pK_A$
Perchloric acid	HClO₄	<del>-</del> 7
Hydrochloric acid	HC1	-3
Sulfuric acid	$H_2SO_4$	-3
Nitric acid	HNO <sub>3</sub>	-1.2
Sulfonic acid	$H_2SO_3$	1.89
Bisulfate	HSO <sub>4</sub> <sup>2</sup>	1.92
Phosphoric acid	$H_3PO_4$	2.12
Acetic acid	CH₃COOH	4.7
Butyric acid	C <sub>3</sub> H <sub>7</sub> COOH	4.8
Propionic acid	C <sub>2</sub> H <sub>5</sub> COOH	4.9
Carbonic acid	H <sub>2</sub> CO <sub>3</sub>	6.35
Hydrogen sulfide	$H_2S$	<del>7.</del> 1
Dihydrogen phosphate	$H_2^2PO_4^-$	7.21
Bisulfite	HSO <sub>3</sub>	7.22
Hypochlorous acid	HOCI	7.6
Hydrogen cyanide	HCN	9.2
Ammonium	$\mathrm{NH_4}^+$	9.23
Bicarbonate	HCO <sub>3</sub>	10.33
Hydrogen phosphate	HPO <sub>4</sub> <sup>2</sup> -	12.32
Bisulfide	HS <sup>-</sup>	12.9

# Chemical Equilibrium

How to solve using a spread sheet?

# What is the pH of water in a carbonated beverage? (Using a spread sheet)

KHC	0.034	M/atm			
pCO2	2	atm			
H2CO3*	0.068	М			
Kc1	4.47E-07	М			
Kc2	4.68E-11	М			
Kw	1.00E-14	М			
рН	[H+]	[OH-]	[HCO3-]	[CO32-]	EN
1	1.00E-01	1.00E-13	3.04E-07	1.42E-16	1.00E-01
2	1.00E-02	1.00E-12	3.04E-06	1.42E-14	1.00E-02
3	1.00E-03	1.00E-11	3.04E-05	1.42E-12	9.70E-04
4	1.00E-04	1.00E-10	3.04E-04	1.42E-10	-2.04E-04
5	1.00E-05	1.00E-09	3.04E-03	1.42E-08	-3.03E-03
6	1.00E-06	1.00E-08	3.04E-02	1.42E-06	-3.04E-02
7	1.00E-07	1.00E-07	3.04E-01	1.42E-04	-3.04E-01
8	1.00E-08	1.00E-06	3.04E+00	1.42E-02	-3.07E+00
9	1.00E-09	1.00E-05	3.04E+01	1.42E+00	-3.32E+01
10	1.00E-10	1.00E-04	3.04E+02	1.42E+02	-5.88E+02
11	1.00E-11	1.00E-03	3.04E+03	1.42E+04	-3.15E+04
12	1.00E-12	1.00E-02	3.04E+04	1.42E+06	-2.88E+06
13	1.00E-13	1.00E-01	3.04E+05	1.42E+08	-2.85E+08
14	1.00E-14	1.00E+00	3.04E+06	1.42E+10	-2.85E+10

рН	[H+]	[OH-]	[HCO3-]	[CO32-]	EN
3	1.00E-03	1.00E-11	3.04E-05	1.42E-12	9.70E-04
3.1	7.94E-04	1.26E-11	3.83E-05	2.25E-12	7.56E-04
3.2	6.31E-04	1.58E-11	4.82E-05	3.57E-12	5.83E-04
3.3	5.01E-04	2.00E-11	6.06E-05	5.66E-12	4.41E-04
3.4	3.98E-04	2.51E-11	7.64E-05	8.98E-12	3.22E-04
3.5	3.16E-04	3.16E-11	9.61E-05	1.42E-11	2.20E-04
3.6	2.51E-04	3.98E-11	1.21E-04	2.25E-11	1.30E-04
3.7	2.00E-04	5.01E-11	1.52E-04	3.57E-11	4.72E-05
3.8	1.58E-04	6.31E-11	1.92E-04	5.66E-11	-3.33E-05
3.9	1.26E-04	7.94E-11	2.41E-04	8.98E-11	-1.16E-04

3.7	2.00E-04	5.01E-11	1.52E-04	3.57E-11	4.72E-05
3.71	1.95E-04	5.13E-11	1.56E-04	3.74E-11	3.91E-05
3.72	1.91E-04	5.25E-11	1.60E-04	3.92E-11	3.10E-05
3.74	1.82E-04	5.50E-11	1.67E-04	4.30E-11	1.49E-05
3.75	1.78E-04	5.62E-11	1.71E-04	4.50E-11	6.90E-06
3.76	1.74E-04	5.75E-11	1.75E-04	4.71E-11	-1.13E-06
3.78	1.66E-04	6.03E-11	1.83E-04	5.16E-11	-1.72E-05
3.79	1.62E-04	6.17E-11	1.87E-04	5.41E-11	-2.52E-05
	3.71 3.72 3.74 3.75 3.76 3.78	3.71 1.95E-04 3.72 1.91E-04 3.74 1.82E-04 3.75 1.78E-04 3.76 1.74E-04 3.78 1.66E-04	3.71 1.95E-04 5.13E-11 3.72 1.91E-04 5.25E-11 3.74 1.82E-04 5.50E-11 3.75 1.78E-04 5.62E-11 3.76 1.74E-04 5.75E-11 3.78 1.66E-04 6.03E-11	3.71       1.95E-04       5.13E-11       1.56E-04         3.72       1.91E-04       5.25E-11       1.60E-04         3.74       1.82E-04       5.50E-11       1.67E-04         3.75       1.78E-04       5.62E-11       1.71E-04         3.76       1.74E-04       5.75E-11       1.75E-04         3.78       1.66E-04       6.03E-11       1.83E-04	3.71       1.95E-04       5.13E-11       1.56E-04       3.74E-11         3.72       1.91E-04       5.25E-11       1.60E-04       3.92E-11         3.74       1.82E-04       5.50E-11       1.67E-04       4.30E-11         3.75       1.78E-04       5.62E-11       1.71E-04       4.50E-11         3.76       1.74E-04       5.75E-11       1.75E-04       4.71E-11         3.78       1.66E-04       6.03E-11       1.83E-04       5.16E-11

**Answer:** pH = 3.76

#### **Chemical Equilibrium Example**

Hypochlorus acid (HOCI), a weak acid, can be used for disinfecting water. If 1 mg of HOCL is added to pure water to make up 1 L of liquid volume, what is the equilibrium pH?

#### **Chemical Kinetics**

- Time scale for reaction to achieve equilibrium is "large"
   → Kinetics.
- Example: Glucose in oxygenated water

$$C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O$$

- Glucose in sterile (no bugs) distilled H<sub>2</sub>O at pH 7 in contact with air is stable "forever", i.e., a kinetic barrier to its oxidation.
- When pH is > 13, oxidation will occur.
- Methylene Blue (MeB) is a redox indicator which is blue when
   O<sub>2</sub> is present and colourless when O<sub>2</sub> is absent.

$$H_2O$$
 + Glucose +  $O_2$  + MeB @ pH>7  $\rightarrow$  blue  $H_2O$  + Glucose +  $O_2$  + MeB @ pH>13  $\rightarrow$  colourless

#### **Definitions**

- An elementary reaction is one that proceeds as stoichiometrically written.
- Rate law for irreversible elementary reaction:

$$aA + bB \xrightarrow{\gamma} cC + dD$$

$$R_{\gamma} = \frac{1}{a} \left( \frac{d[A]}{dt} \right) = \frac{1}{b} \left( \frac{d[B]}{dt} \right) = \frac{1}{c} \left( \frac{d[C]}{dt} \right) = \frac{1}{d} \left( \frac{d[D]}{dt} \right)$$

$$(A_{1} - A_{1})$$

$$(A_{2} - A_{1})$$

$$(A_{2} - A_{1})$$

$$(A_{3} - A_{1})$$

$$(A_{4} - A_{1})$$

$$(A_{5} - A_{1})$$

$$(A_{7} - A_{1})$$

where a,b,c,d = constants = stoichiometric coefficients  $k_{\gamma}$  = reaction rate constant

Example of Rate Calculations: Reaction of disinfectant HOCL (hypochlorous acid) with NH<sub>3</sub> (ammonia) to form NH<sub>2</sub>Cl (monochloramine):

$$NH_3 + HOCI \rightarrow NH_2CI + H_2O$$
  
k = 5.1 x 10<sup>6</sup> l/mole, sec at 25°C

If initial NH<sub>3</sub> and HOCL concentrations are both 10<sup>-3</sup> M, what is the overall

reaction rate?

Rate Law: 
$$R = -\frac{1}{2} \frac{d(NV_3)}{dt} = -\frac{1}{2} \frac{d(NV_3)}{dt} = k(NV_3)[400]$$

$$|M = -\frac{1}{2} \frac{d(NV_3)}{dt} = -\frac{1}{2} \frac{d(NV_3)}{dt} = k(NV_3)[400]$$

$$|M = -\frac{1}{2} \frac{d(NV_3)}{dt} = -\frac{1}{2} \frac{d(NV_3)}{dt} = k(NV_3)[400]$$

$$= -\frac{1}{2} \frac{d(NV_3)}{dt} = -\frac{1}{$$

#### **Batch Reactor**

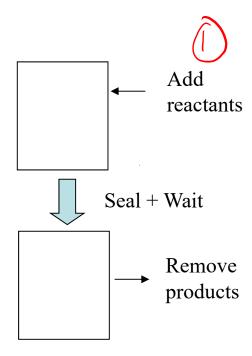
Consider chemical reaction in batch reactor.

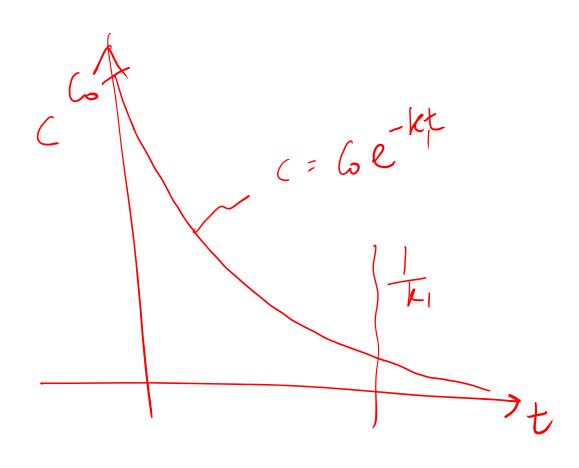
1<sup>st</sup> order decay rxn.: A — → products

Rate Law:  $R_1 = k_1[A]$ 

In a batch reactor with only rxn. 1 occurring:

$$\frac{d[A]}{dt} = -R_1 = -k_1[A]$$





#### 1) 1st Order Decay Reaction

Consider chemical reaction in batch reactor.

1<sup>st</sup> order decay rxn.: A  $\xrightarrow{1}$  products

Rate Law:  $R_1 = k_1[A]$ 

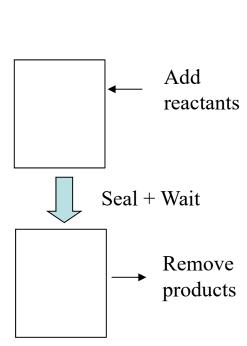
$$\frac{d[A]}{dt} = -R_1 = -k_1[A]$$

$$[A](t) = A_o e^{-k_1 t}$$

Characteristics time,

$$\tau = \frac{\text{Stock}}{\text{Outflow Rate}}$$

$$\tau \sim \frac{A_0}{k_1 A_0} = \frac{1}{k_1}$$



Other variations:

2) Oth Order Decay Reaction:

(provided [B]>>0)

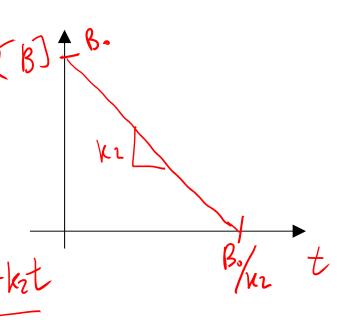
$$B \xrightarrow{2}$$
 products

Rate Law:  $R_2 = k_2$  & [B](t=0) =  $B_0$  In a batch reactor,

$$\frac{d[B]}{dt} = -R_2 = -k_2$$

$$\int_{B_0}^{B} d(B) = \int_{0}^{t} k_1 dt$$

Valid for  $t < B_o/k_2$ ; [B](t) = 0 for  $t \ge B_o/k_2$ 



Characteristics time,

$$\tau = \frac{\text{Stock}}{\text{Outflow-Rate}}$$

$$\tau = \frac{B_0}{k_2}$$

#### 3) <u>i) 2<sup>th</sup> Order Decay Reaction</u>:

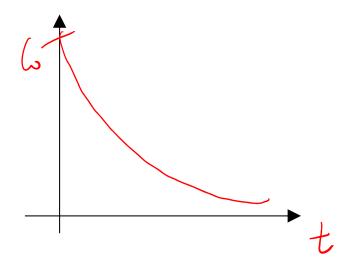
Rate Law:  $R_3 = k_3[C]^2$ 

$$\frac{1}{2} \frac{d[C]}{dt} = -R_3 = -k_3[C]^2$$

$$\frac{dC}{dC} = \int_{0}^{t} -2k_3 dt$$

$$C(t) = \frac{C}{1 + 2k_3t_6}$$

$$C + C \xrightarrow{3}$$
 products



- Characteristics time,

$$\tau = \frac{\text{Stock}}{\text{Outflow Rate}}$$

$$\tau \sim \frac{9}{2 k_3 6} = \frac{1}{2 k_3 6}$$

ii) 2<sup>th</sup> Order Decay Reaction: A+B → products 3.

$$A + B \xrightarrow{4} products$$

Rate Law:  $R_4 = k_4[A][B]$  Note: 1<sup>st</sup> order in [A] &[B]; 2<sup>nd</sup> order over all.

In a batch reactor with A<sub>o</sub>, B<sub>o</sub> at t=0

$$\frac{d[A]}{dt} = \frac{d[B]}{dt} = -R_4 = -k_4[A][B]$$

Characteristics Time: 
$$\tau \sim \frac{\min (A_o, B_o)}{k_4 A_o B_o}$$

If  $A_0 = B_0$ , all  $A_0$  and  $B_0$  will be consumed.

If  $A_0 > B_0$ , all  $B_0$  will be consumed

Case 2: (Function of A but not B)

$$\frac{d[A]}{dt} = \frac{d[B]}{dt} = -R_4 = -k_4[A]$$
sendo.

4) 2 Reaction in series: 
$$A \xrightarrow{1} B \xrightarrow{2} C$$
 $R_1 = k_1[A];$   $R_2 = k_2[B]$ 

i) Seek [A](t) 
$$\frac{d[A]}{dt} = -R_1 = -k_1[A] \Rightarrow A_0 \in A_0$$

ii) Seek [B](t) 
$$\frac{d[B]}{dt} = R_1 - R_2 = k_1[A] - k_2[B]$$

$$\Rightarrow \frac{d(B)}{dt} = k_1 A_0 e^{-k_1 t} k_2[B]$$

$$Grees (B)(t) = (A_1 e^{-k_1 t} A_2 e^{-k_2 t})$$

$$Grees (B)(t) = (A_1 e^{-k_1 t} A_2 e^{-k_2 t})$$

$$Grees (B)(t) = (A_1 e^{-k_1 t} A_2 e^{-k_2 t})$$

$$r_{1}q_{1}e^{r_{1}t} + r_{2}q_{1}e^{r_{2}t} = k_{1}A_{0}e^{-k_{1}t} - k_{2}G_{1}e^{r_{2}t}$$

$$r_{1}q_{1}e^{r_{1}t} + r_{2}G_{1}e^{r_{2}t} = k_{1}A_{0}e^{-k_{1}t} - k_{2}G_{1}e^{r_{2}t}$$

$$ld \quad r_{1} = -k_{1} \\ -k_{1}G_{1}e^{kt} = k_{1}A_{0}e^{-k_{1}t} + k_{2}G_{1}e^{-k_{1}t}$$

$$-k_{1}G_{1} = k_{1}A_{0}e^{-k_{1}t} - k_{2}G_{1}e^{-k_{1}t}$$

$$r_{2}G_{1}e^{kt} = -k_{2}G_{2}e^{kt} \Rightarrow r_{2} = -k_{2}$$

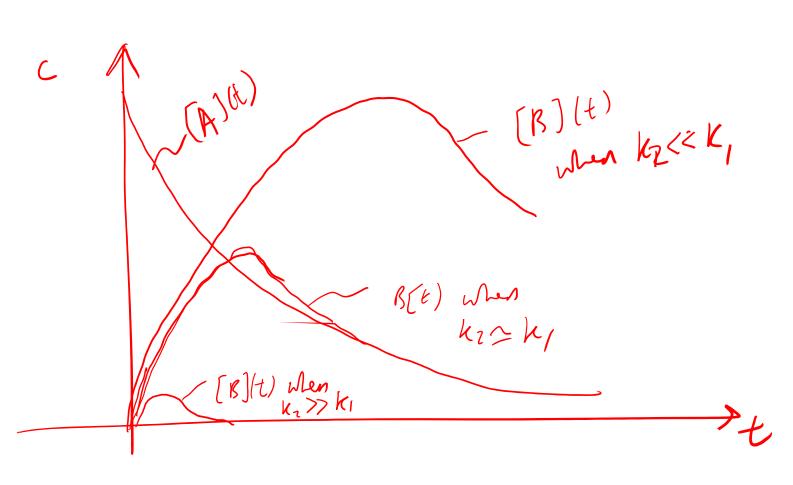
$$r_{2}G_{1}e^{kt} = -k_{2}G_{2}e^{kt} \Rightarrow r_{2} = -k_{2}$$

$$() \Rightarrow [B](t) = G_{1}e^{r_{1}t} + G_{2}e^{-r_{2}t} + G_{2}e^{-k_{1}t} + G_{2}e^{-k_{1}t}$$

$$et=0, (B]: \Rightarrow 0 = \frac{k_{1}A_{0}}{k_{2}-k_{1}} + G_{2} \Rightarrow G_{2}^{-k_{1}} - \frac{k_{1}A_{0}}{k_{2}-k_{1}}$$

$$(B)(t) = \frac{k_1 A_0}{k_2 - k_1} e^{-k_1 t} - \frac{k_1 A_0}{k_2 - k_1} e^{-k_2 t}$$

$$(A)(t) = A_0 e^{-k_1 t}$$



4) <u>2 Reaction in parallel</u>:  $A \xrightarrow{1} B$   $R_1 = k_1[A]$   $A \xrightarrow{2} C$   $R_2 = k_2[A]$  $\frac{d[A]}{dt} = -R_1 - R_2 = -(k_1 + k_2)[A]$ Given [A](t=0) = A<sub>o</sub>, [A](t) = A<sub>o</sub>  $\frac{d[B]}{dt} = R_1 = k_1[A]$  $\frac{d[B]}{dt} = k_1 A_0 \ell - (k_1 + k_2) \ell - (k_1 + k_2) \ell \ell$   $\frac{A(c)}{A(c)} = R_2 = k_2 (A) = k_1 A_0 \ell$ 

$$\frac{d[A]}{dt} = -k_0 \qquad \tau \sim \frac{A_0}{k_0}$$

$$au \sim rac{A_0}{k_0}$$

$$\frac{d[A]}{dt} = -k_1[A] \qquad \tau \sim \frac{A_0}{k_0 A_0} = \frac{1}{k_0}$$

$$\tau \sim \frac{A_0}{k_0 A_0} = \frac{1}{k_0}$$

#### • 2<sup>nd</sup> Order:

$$\frac{d[A]}{dt} = -2k_{2a}[A]^2 \qquad \tau_{2a} \sim \frac{A_0}{2k_{2a}A_0^2} = \frac{1}{2k_{2a}A_0}$$

$$\frac{d[\mathsf{A}]}{d\mathsf{t}} = \frac{d[\mathsf{B}]}{d\mathsf{t}} = -\mathsf{k}_{2\mathsf{b}}[\mathsf{A}][\mathsf{B}] \quad \tau_{2b} \sim \frac{\min(A_0, B_0)}{k_{2b}A_0B_0}$$

#### Redox Reactions

• Chemical species can be characterized by their oxidation state which describes whether they have lost or gained electrons (e<sup>-</sup>) with respect to a reference state (the element; oxidation state = 0).

E.g. Mg<sup>2+</sup> (magnesium ion) has lost 2e<sup>-</sup> compared to Mg<sup>0</sup> (magnesium metal) Cl<sup>-</sup> (chloride ion) has gained 1e<sup>-</sup> compared to 1/2Cl<sub>2</sub><sup>0</sup> (chlorine gas)

- A loss of e<sup>-</sup> is an oxidation
- A gain of e<sup>-</sup> is a reduction

## Rules for determining oxidation state

- Uncombined elements = 0
   e.g. C, O<sub>2</sub> and H<sub>2</sub>
- 2. Sum of oxidation state for compound = ionic charge (element or molecule)
- 3. O in compound is –II
- 4. H in compound is +I

### **Oxidation State**

Example: Determine the oxidation number of C in

- i) CO<sub>2</sub>, ii) CO<sub>3</sub><sup>2</sup>-, iii) HCO<sub>3</sub>- and iv) C<sub>2</sub>H<sub>4</sub>O<sub>2</sub>
- i)  $\omega_2$ :  $1(x) + 2(-2) = 0 \Rightarrow x = +4$

11) 
$$\omega_3^{2-}$$
:  $1(x)+3(-2)=-2 \Rightarrow x=+4$ 

(ii) 
$$U(0)$$
:  $1 + 1(x) + 3(-2) = -1 \Rightarrow x = +4$ 

$$V_{i}) \quad C_{2} H_{4} o_{2}: \quad 2(x) + 4(1) + 2(-2) = 0$$

$$\Rightarrow x = 0$$

#### Oxidation/Reduction

Involve a change in oxidation state of reactants

e.g. 
$$2H_2 + O_2 \rightarrow 2H_2O$$

$$C + O_2 \rightarrow 4CO_2$$

$$2Fe^{2+} + CI_2 \rightarrow 2Fe^{3+} + 2CI^{-1}$$

Note: sum of oxidation states on both sides of equations are equal – a requirement for a balanced redox reaction.

#### In last equation,

Fe<sup>2+</sup> is a **reducing agent**; it loses e<sup>-</sup>; it becomes oxidized. Cl<sub>2</sub> is an **oxidizing agent**; it gains e<sup>-</sup>; it becomes reduced.

#### Considering C in:

$$(4)$$
 $CO_{2}(g) < ----> H_{2}CO_{3}^{*} < ----> HCO_{3}^{-} + H^{+}$ 
 $HCO_{3}^{-} < ----> CO_{3}^{2-} + H^{+}$ 

# Balancing Redox Reaction – Electron Balancing Method

- Consist of two half reactions an oxidation half-reaction and a reduction half reaction
- Steps:
  - For each ½ rxn, balance major species (anything but O &H)
  - 2. For each ½ rxn, balance any O with H<sub>2</sub>O
  - 3. For each ½ rxn, balance any H with H<sup>+</sup>
  - 4. For each ½ rxn, balance charge with e
  - 5. Balance both ½ rxns by eliminating e
  - 6. If solution is alkaline (high pH), cancel out any H+ by adding OH- to both side of rxn; sum up H<sub>2</sub>O

## Previous Example

1. Balance major species:

Fe<sup>2+</sup> 
$$\Leftrightarrow$$
 Fe(OH)<sub>3</sub>  
Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>  $\Leftrightarrow$  2Cr(OH)<sub>2</sub><sup>+</sup>

2. Balance any O with H<sub>2</sub>O

Fe<sup>2+</sup> + 
$$3H_20 \Leftrightarrow Fe(OH)_3$$
  
Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>  $\Leftrightarrow$  2Cr(OH)<sub>2</sub><sup>+</sup>+  $3H_20$ 

3. Balance any H with H<sup>+</sup>

Fe<sup>2+</sup> + 
$$3H_20 \Leftrightarrow Fe(OH)_3 + 3H^+$$
  
Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup> +  $10H^+ \Leftrightarrow 2Cr(OH)_2^+ + 3H_2^0$ 

4. Balance charge with e

Fe<sup>2+</sup> + 
$$3H_20 \Leftrightarrow Fe(OH)_3 + 3H^+ + e^-$$
  
Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup> +  $10H^+ + 6e^- \Leftrightarrow 2Cr(OH)_2^+ + 3H_2^0$ 

5. Balance both ½ rxns by eliminating e

$$(Fe^{2+} + 3H_2O \Leftrightarrow Fe(OH)_3 + 3H^{++} e^{-}) \times 6$$
 $Cr_2O_7^{2-} + 10H^{++} 6e^{-} \Leftrightarrow 2Cr(OH)_2^{++} 3H_2O$ 
 $6 Fe^{2+} + Cr_2O_7^{2-} + 15H_2O \Leftrightarrow 6Fe(OH)_3 + 2Cr(OH)_2^{++} 8H^{++}$ 

## Another Example

Balance the reaction in which ferrous iron (Fe<sup>2+</sup>) is converted to ferric iron (Fe<sup>3+</sup>) by permanganate (MnO<sub>4</sub>-), which itself is reduced to manganese dioxide (MnO<sub>2(s)</sub>). The reaction takes place in alkaline solution.

1. Balance major species:

$$Fe^{2+} \Leftrightarrow Fe^{3+}$$
  
 $MnO_4^- \Leftrightarrow MnO_{2(s)}$ 

2. Balance any O with H<sub>2</sub>O

$$Fe^{2+} \Leftrightarrow Fe^{3+}$$
  
 $MnO_4^- \Leftrightarrow MnO_{2(s)} + 2H_20$ 

3. Balance any H with H<sup>+</sup>

$$Fe^{2+} \Leftrightarrow Fe^{3+}$$
  
 $4H^{+} + MnO_{4}^{-} \Leftrightarrow MnO_{2(s)} + 2H_{2}0$ 

4. Balance charge with e

$$Fe^{2+} \Leftrightarrow Fe^{3+} + e^{-}$$
  
 $3e^{-} + 4H^{+} + MnO_{4}^{-} \Leftrightarrow MnO_{2(s)} + 2H_{2}0$ 

5. Balance both ½ rxns by eliminating e

$$(Fe^{2+} \Leftrightarrow Fe^{3+} + e^{-}) \times 3$$
  
 $3e^{-} + 4H^{+} + MnO_{4^{-}} \Leftrightarrow MnO_{2(s)} + 2H_{2}0$   
 $4H^{+} + 3Fe^{2+} + MnO_{4^{-}} \Leftrightarrow 3Fe^{3+} + MnO_{2(s)} + 2H_{2}0$ 

6. Rxn takes place in alkaline soln, add water dissociation equation to eliminate H+ as a reactant:

$$4H^{+} + 3Fe^{2+} + MnO_{4}^{-} \Leftrightarrow 3Fe^{3+} + MnO_{2(s)} + 2H_{2}0$$
  
 $4H_{2}0 \Leftrightarrow 4H^{+} + 4OH^{-}$   
 $2H_{2}0 + 3Fe^{2+} + MnO_{4}^{-} \Leftrightarrow 3Fe^{3+} + MnO_{2(s)} + 4OH^{-}$ 

7. In alkaline soln, Fe<sup>3+</sup> will combine with OH<sup>-</sup> to form Fe(OH)<sub>3/s)</sub>:

$$2H_2O + 3Fe^{2+} + MnO_4^- \Leftrightarrow 3Fe^{3+} + MnO_{2(s)} + 4OH^-$$
  
 $3 \times (Fe^{3+} + 3OH^-) \Leftrightarrow Fe(OH)_{3(s)}$ 

$$2H_20 + 3Fe^{2+} + MnO_4^- + 5OH^- \Leftrightarrow 3 Fe(OH)_{3(s)} + MnO_{2(s)}$$

Last step would not have been necessary if in step (1) we had taken  $Fe(OH)_{3(s)}$  as the product rather than  $Fe^{3+}$ 

## Corrosion









#### Corrosion

Typical corrosion reaction of metal in oxygen containing H<sub>2</sub>O:

$$Fe^0 + 2H^+ + \frac{1}{2}O_2 \rightarrow Fe^{2+} + H_2O$$

Fe oxidized from 0 to +II

Oxygen reduced from 0 to -II

# **Another Corrosion Example**

Q3.35 Write a balanced chemical reaction for the corrosion of pure zinc metal by dissolved oxygen in water to produced zinc rust, Zn(OH)<sub>2</sub>.

$$\frac{2n}{0r} = \frac{2n}{40r} (00)^{2}$$

$$\frac{2n}{40r} = \frac{2n}{40r} (00)^{2}$$

# Theorectical Oxygen Demand

Consider 
$$C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O$$

SW myle of Clumbs, what is the theredred sygen demand?

SWO (1/21) + (1/21) MM × 6 × 32 mg/2

(1/212) + (1/21) MM × 6 × 32 mg/2

= 5-33.44 mg/2

# Biochemical Oxygen Demand (BOD)

- Microbiologically-mediated degradation of organic material (redox reaction) in water using dissolved oxygen.
- BOD + DO → products
- Consider a batch reactor,

$$\frac{d[BOD]}{dt} = -R = -k[BOD]$$

$$\frac{d[DO]}{dt} = -R = -k[BOD]$$

where  $[BOD](t=0) = BOD_0$ ;  $[DO](t=0) = DO_0$ 

# Biochemical Oxygen Demand (BOD)

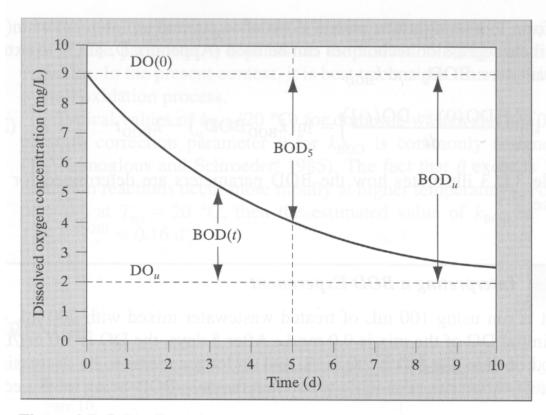
- Microbiologically-mediated degradation of organic material (redox reaction) in water using dissolved oxygen.
- BOD + DO → products
- Consider a batch reactor,

$$\frac{d[BOD]}{dt} = -R = -k[BOD]$$

$$\frac{d[DO]}{dt} = -R = -k[BOD]$$

#### BOD

BOD(t) = BOD<sub>u</sub> exp(
$$-k_{BOD}t$$
)  
DO(t) = DO(0) - BOD<sub>u</sub>[1-exp( $-k_{BOD}t$ )]



**Figure 3.D.5** Idealized decrease in dissolved oxygen concentration in a batch reactor during measurement of BOD.

#### BOD

How to determine  $k_{BOD}$  and  $BOD_u$ ?

- Conduct experiment to determine DO(0) & DO (t).
- Fit data by plotting natural logarithm of time derivative of (DO(t) – DO(0)) against time:

$$\ln\left(\frac{d[DO(0) - DO(t))]}{dt}\right) = \ln(k_{BOD}BOD_{u}) - k_{BOD}t$$

- Slope =  $-k_{BOD}$
- Y Intercept =  $ln(k_{BOD} x BOD_{II})$

# **END**