

NATIONAL UNIVERSITY OF SINGAPORE

CE5312 – RIVER MECHANICS

(Semester I: AY2015/2016)

Time Allowed: 2.5 Hours

INSTRUCTIONS TO CANDIDATES

1. Please write your student number only. **Do not write your name.**
2. This assessment paper contains **FIVE** questions and comprises **FIVE** printed pages.
3. Answer **ALL** questions. All questions carry equal marks.
4. Please start each question on a new page.
5. This is an “OPEN BOOK” assessment.

Question 1 [25 marks]

A long and straight rectangular channel is controlled by an ideal sharp-crested weir in the downstream. The channel is 10-meter wide and has a constant slope $S_0=2/1000$. The channel bottom gives a Manning's coefficient $n=0.05$. It carries a steady flow with a discharge $Q=50\text{m}^3/\text{s}$. The height of the weir is $W=5\text{m}$.

- (a) Find the normal and critical depth in this channel.

(10 marks)

- (b) Find water depth in front of weir.

(5 marks)

- (c) Assume the channel is infinitely long in the upstream direction, sketch the water surface profile upstream of the weir.

(5 marks)

- (d) Estimate the length of non-uniform region.

(5 marks)

Question 2 [10 marks]

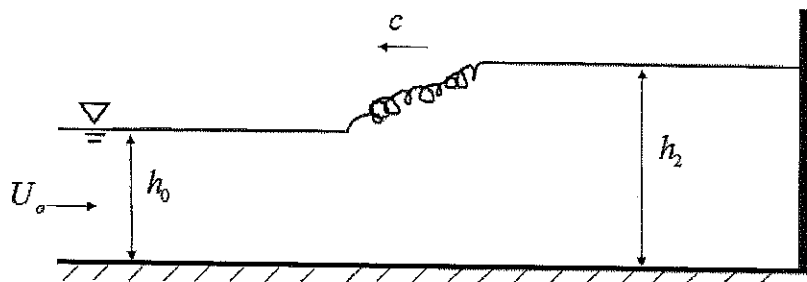
An infinitely long and very wide rectangular channel initially carries a uniform flow at $U_0=2\text{m/s}$ and $h_0=5\text{m}$. For some reason, a sluice gate, which was completely open initially, is suddenly closed, as shown in the following figure. This produces a bore that travels upstream into the channel. The region from the bore to the gate can be considered to have a uniform water depth h_2 .

- (a) Derive two equations that allow you to solve for the celerity of the bore, c , and water depth h_2 (no need to solve them)

(7 marks)

- (b) Determine c and h_2 .

(3 marks)



Question 3 [25 marks]

A long, rectangular canal of width 8 m carries flow of $48 \text{ m}^3/\text{s}$ at uniform depth $h_0=3 \text{ m}$. At the upstream end ($x=0$) a hydraulic structure controls the discharge into the canal ($x>0$). From $t=0$, the discharge begins to reduce at $8 \text{ m}^3/\text{hour}$ for 5 hours and then remains constant. Neglect channel slope and resistance, and use method of characteristics to solve the following questions.

- (a) Obtain an equation for determining h at $x=0$ with given conditions

(5 marks)

- (b) Mathematically prove that the C^+ characteristics initiated on the t -axis from $0 < t < 5$ hours are diverging straight lines, but the C^+ characteristics initiated on the t -axis for $t > 5$ hours are parallel straight lines.

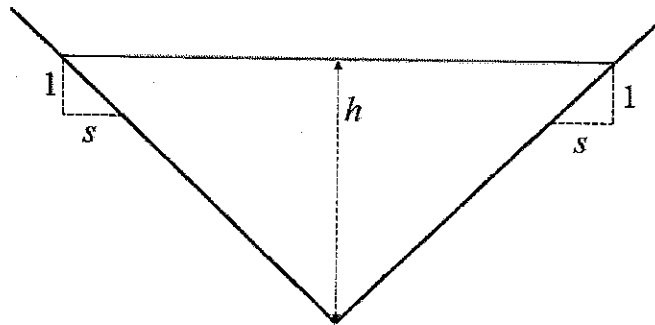
(10 marks)

- (c) Determine when h is 2.6m at $x=10 \text{ km}$.

(10 marks)

Question 4 [10 marks]

In this question we investigate the celerity of kinematic wave for kinematic-wave routing method. Assuming Manning's formula, determine the kinematic wave celerity for a long straight channel with the triangular cross section shown in the following figure. The water depth is $h=2 \text{ m}$ and channel slope $s=1$. Manning's coefficient is $n=0.05$ and average velocity is $U=1 \text{ m/s}$.



Question 5 [30 marks]

Assume Manning's formula is always applicable. In a very wide river, the bottom is assumed always flat and covered by uniform sands $d=0.2\text{mm}$ (you can take the bottom roughness $k_s=d$). The flow can be considered steady and uniform, and the discharge per unit width is maintained at $10\text{m}^2/\text{s}$. Neglect the bottom slope here.

- (a) Determine the minimum (or maximum) water depth h_c that can initiate sediment movement, and discuss why this is the minimum (or maximum) water depth.

(14 marks)

Use default value $h_c=14.1\text{m}$ hereafter:

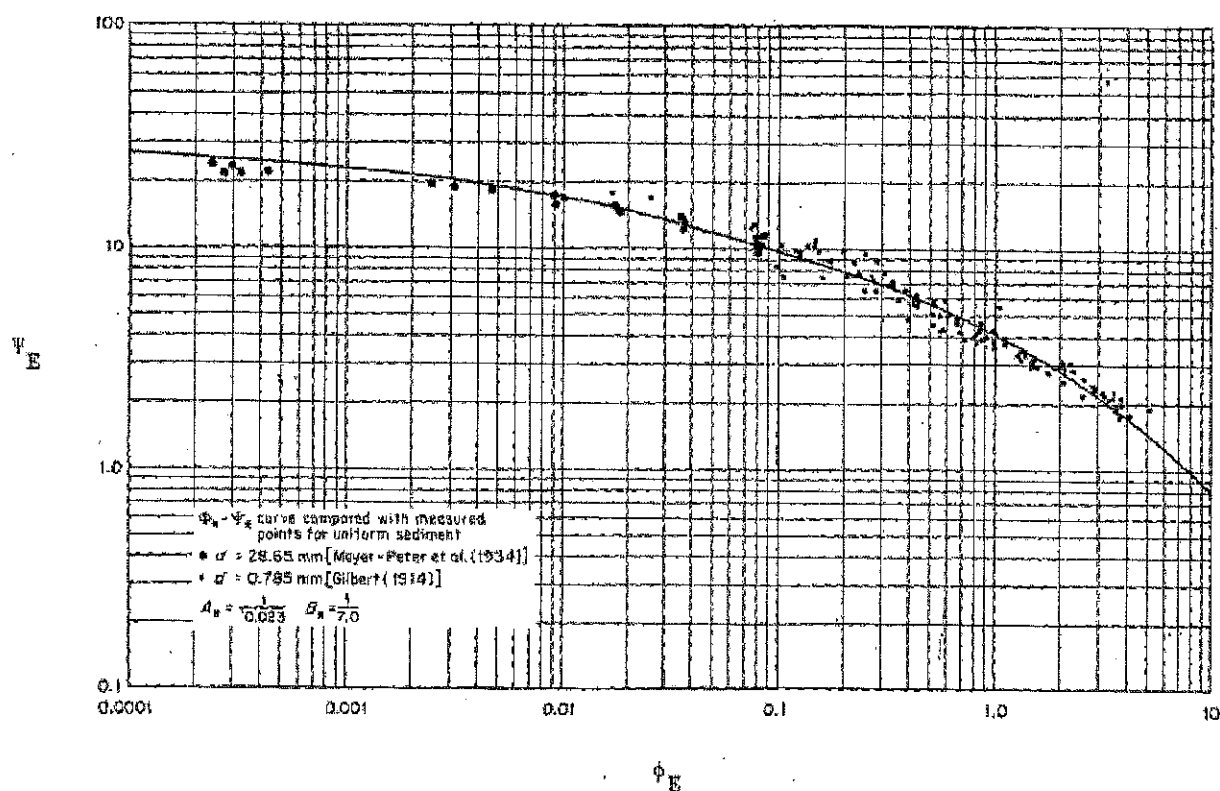
- (b) For $h=0.7h_c$, determine bedload sediment transport rate.

(8 marks)

- (c) For $h=1.1h_c$, determine bedload sediment transport rate.

(8 marks)

Einstein's bedload transport diagram (if you want to use it):



- END OF PAPER -