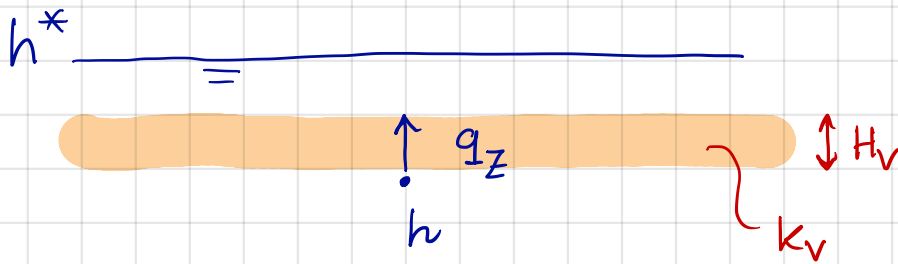
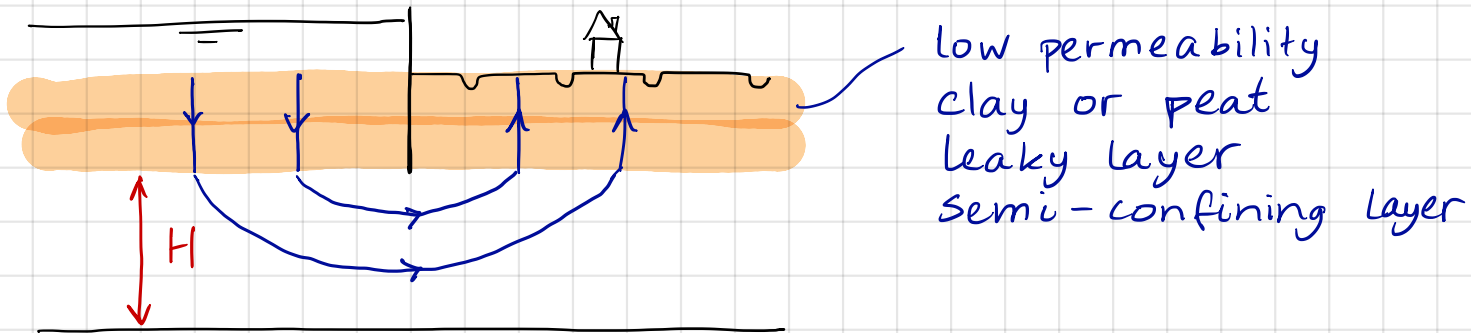


## SEMI-CONFINED FLOW



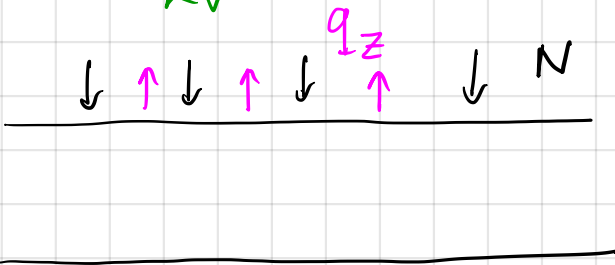
$$q_z = k_v \frac{h - h^*}{H_v}$$

$$q_z = \frac{h - h^*}{c}$$

resistance of leaky layer

$$c = \frac{H_v}{k_v}$$

$$\frac{m d}{m}$$



$$\frac{d^2 h}{dx^2} = -\frac{N}{kH} = \frac{+q_z}{kH}$$

$$\frac{d^2 h}{dx^2} = \frac{h - h^*}{c k H} = \frac{h - h^*}{\lambda^2}$$

$$\lambda = \sqrt{k H c}$$

$$\sqrt{\frac{m}{d} m d} = m$$

$\lambda \rightarrow$  leakage factor

"spreading length"

$$\frac{d^2 h}{dx^2} = \frac{h-h^*}{\lambda^2}$$

$$\boxed{\frac{d^2(h-h^*)}{dx^2} = \frac{h-h^*}{\lambda^2}}$$

$h^*$  is constant

$$h-h^* = c e^{ax}$$

$$\frac{d(h-h^*)}{dx} = c a e^{ax}$$

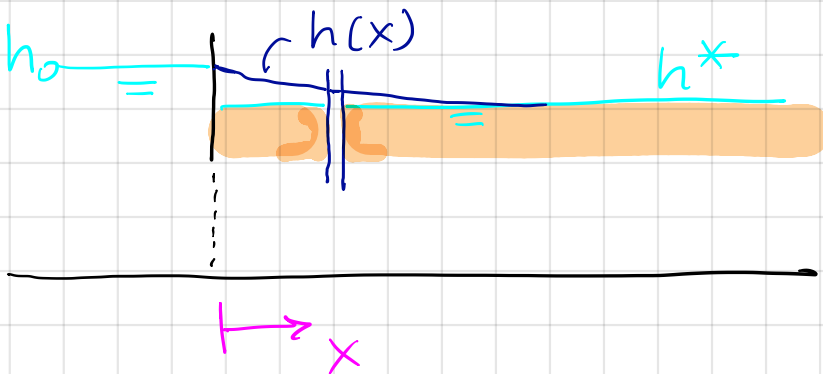
$$\frac{d^2(h-h^*)}{dx^2} = c a^2 e^{ax}$$

$$\cancel{c a^2 e^{ax}} = \frac{\cancel{c} e^{ax}}{\lambda^2}$$

$$a = -\frac{1}{\lambda}$$

$$-\frac{1}{\lambda}$$

$$\boxed{h-h^* = A e^{-x/\lambda} + B e^{+x/\lambda}}$$



$$x=0 \rightarrow h=h_0 \rightarrow h-h^* = h_0-h^*$$

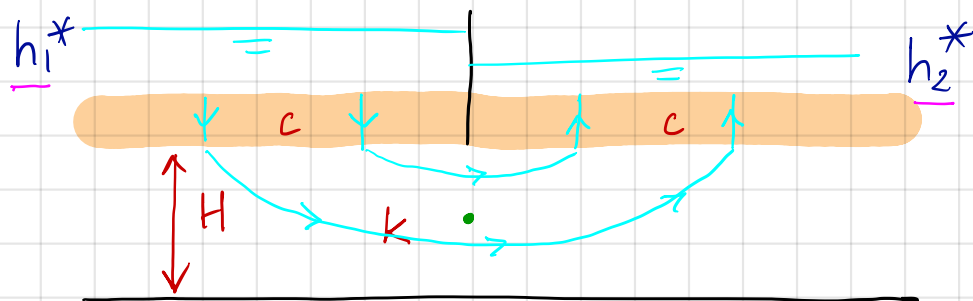
$$x \rightarrow \infty \rightarrow h=h^* \rightarrow \underline{h-h^* = 0}$$

$$B=0$$

$$h(x=0) - h^* = A = h_0 - h^*$$

$$h-h^* = (h_0-h^*) e^{-x/\lambda}$$

$$\boxed{h = h^* + (h_0-h^*) e^{-x/\lambda}}$$



$$x \leq 0 \quad h = h_1^* + A_1 e^{-x/\lambda} + B_1 e^{x/\lambda}$$

$$x \geq 0 \quad h = h_2^* + A_2 e^{-x/\lambda} + B_2 e^{x/\lambda}$$

$$x \rightarrow -\infty \quad h = h_1^* \rightarrow A_1 = 0$$

$$x \rightarrow +\infty \quad h = h_2^* \rightarrow B_2 = 0$$

$$x = 0 \quad h(x=0^-) = h(x=0^+)$$

$$Q_x(x=0^-) = Q_x(x=0^+)$$

$$Q_x = -\frac{kH B_1}{\lambda} e^{x/\lambda}$$

$$Q_x = +\frac{kH A_2}{\lambda} e^{-x/\lambda}$$

$$h(x=0^-) = h(x=0^+)$$

$$h_1^* + B_1 = h_2^* + A_2$$

$$Q_x(x=0^-) = Q_x(x=0^+)$$

$$-\frac{kH B_1}{\lambda} = \frac{kH A_2}{\lambda} \rightarrow A_2 = -B_1$$

$$h_1^* + B_1 = h_2^* - B_1$$

$$B_1 = \frac{h_2^* - h_1^*}{2}$$

$$A_2 = \frac{h_1^* - h_2^*}{2}$$

$$x \leq 0 \quad h = h_1^* + \frac{h_2^* - h_1^*}{2} e^{x/\lambda}$$

$$x \geq 0 \quad h = h_2^* + \frac{h_1^* - h_2^*}{2} e^{-x/\lambda}$$

$$x = 0 \rightarrow h = h_1^* + \frac{h_2^* - h_1^*}{2} = \frac{1}{2} (h_1^* + h_2^*)$$