

# (Semi-) Distributed Modeling



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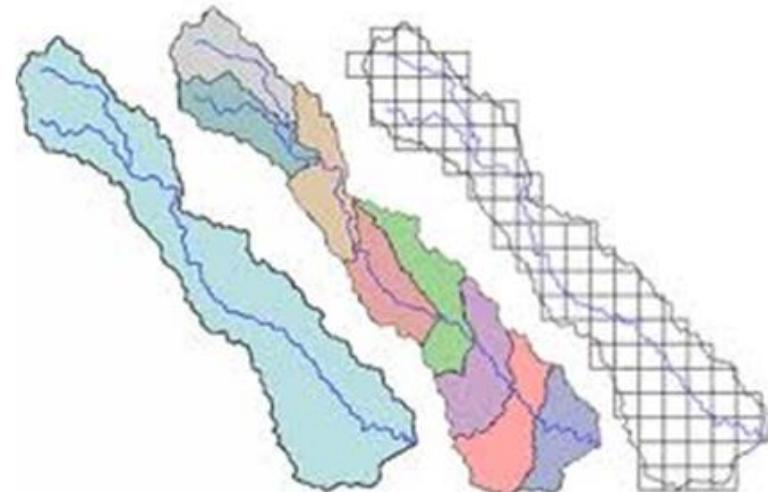
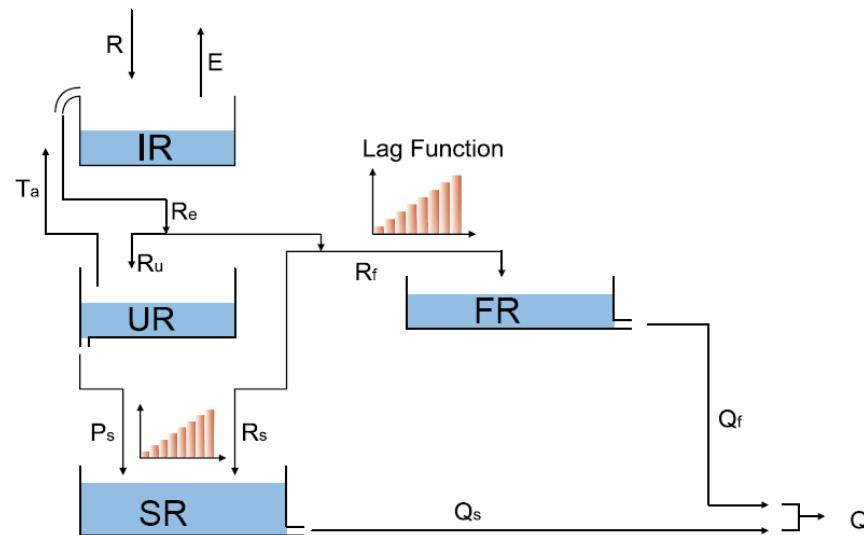
# What is the issue?

One of the fundamental problems in hydrological modeling are the **conflicting priorities** of process representation and model parsimony:

- Lumped conceptual models often too simplistic in process representation
- Distributed

Goal: better process parameters

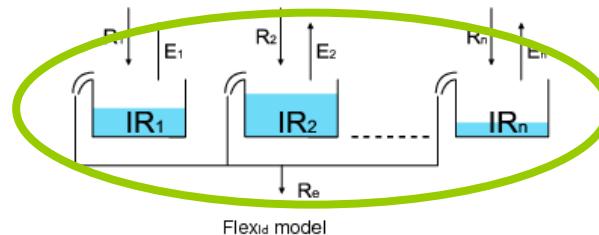
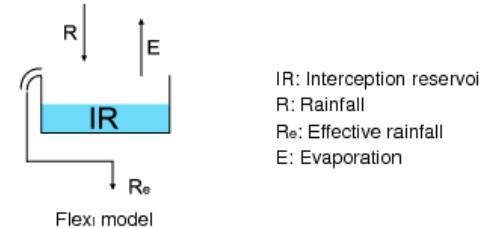
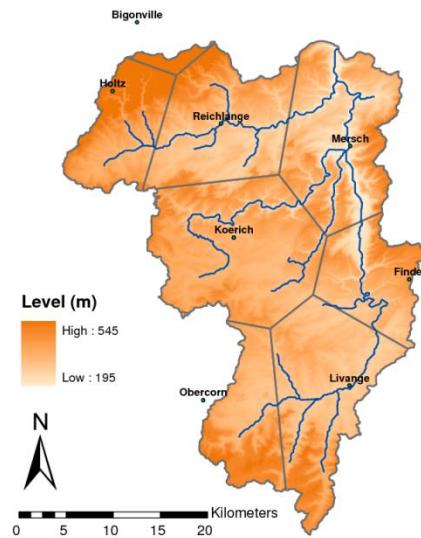
**What does that mean for us?**



# Semi-distributed rainfall accounting

# Semi-distributed rainfall accounting

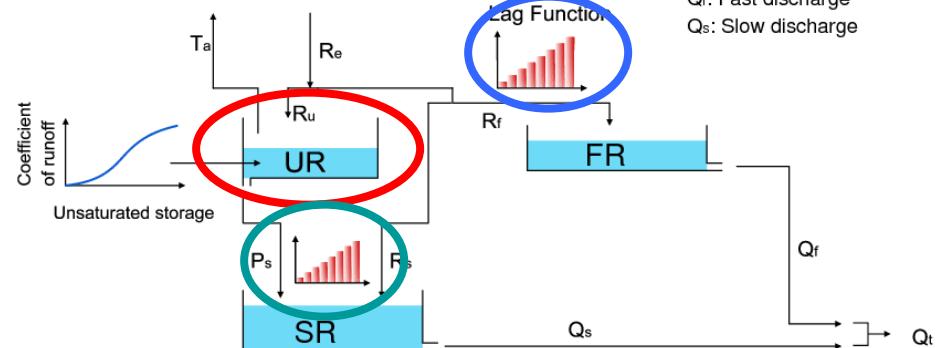
- Distributed **interception**
- Distributed **I+UR**
- Distr **I+UR+LagFR**
- Distr **I+UR+LagFR+ LagSR**



UR: Unsaturated soil reservoir  
FR: Fast reacting reservoir  
SR: Slow reacting reservoir

$R_e$ : Effective rainfall  
 $T_a$ : Actual transpiration  
 $Q_t$ : Total discharge

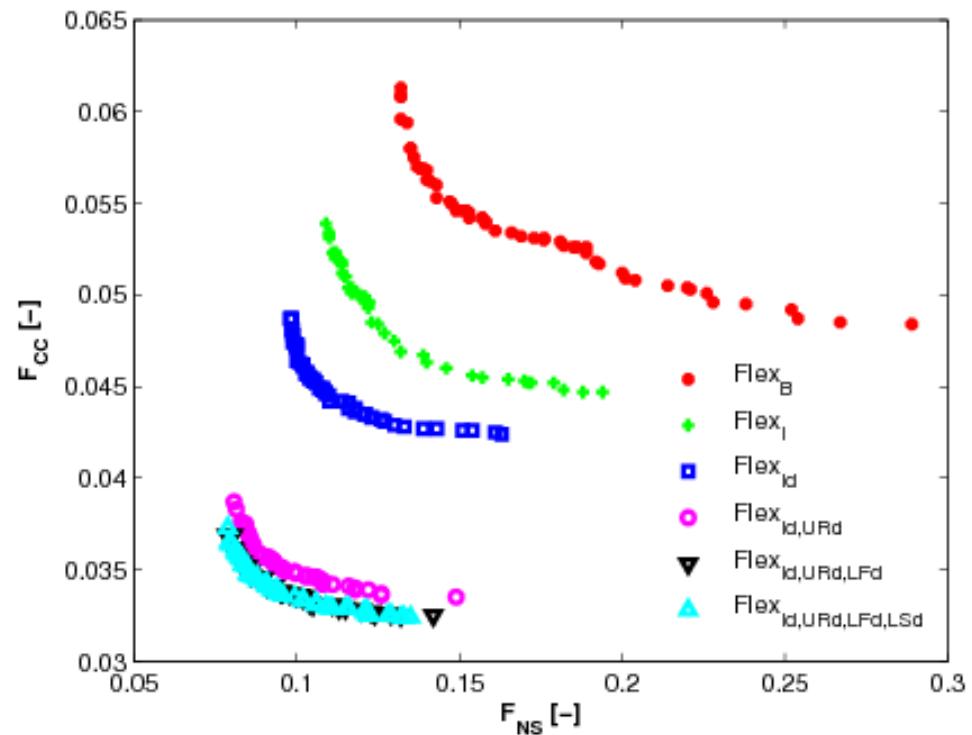
$R_u$ : Recharge to UR  
 $R_f$ : Recharge to FR  
 $P_s$ : Percolation  
 $Q_f$ : Fast discharge  
 $Q_s$ : Slow discharge



# Semi-distributed rainfall accounting

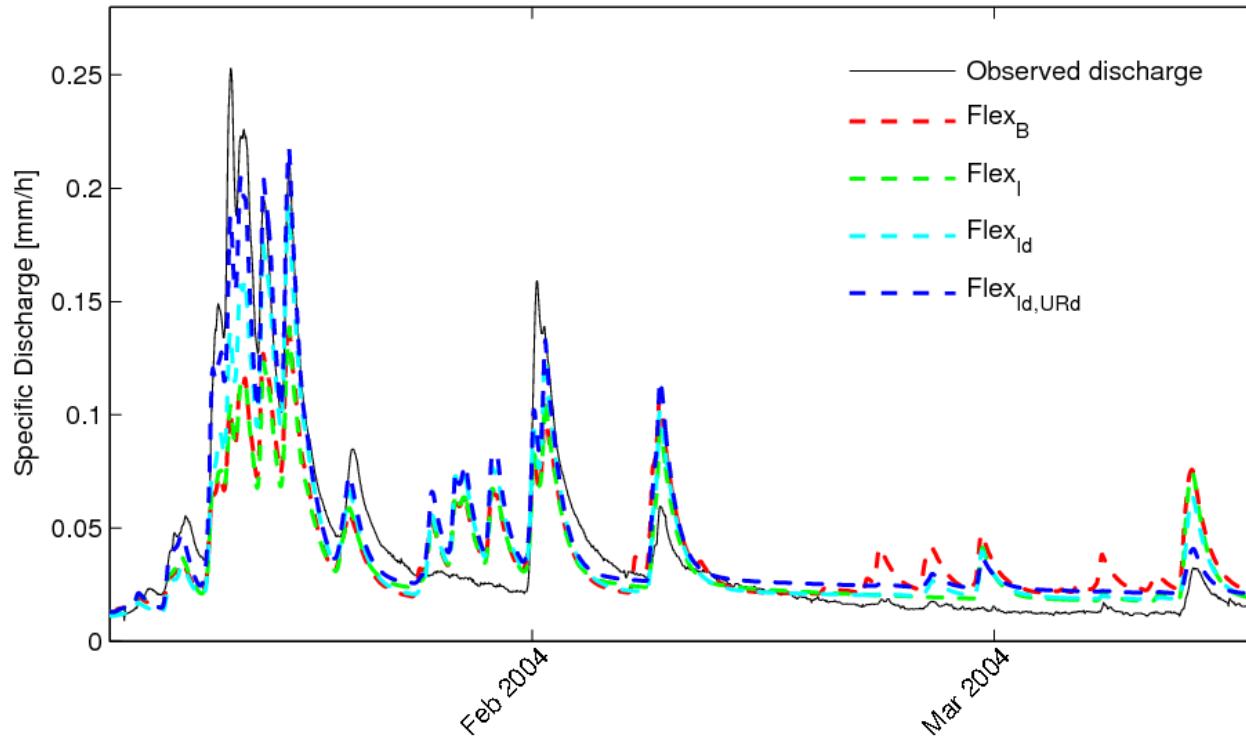
## Effects on model performance:

- Distributed interception and unsaturated soil provide a large improvement
- Distributed lag times associated to fast flow provide a small improvement
- Distributed lag times associated to slow flow provide no improvement



# Semi-distributed rainfall accounting

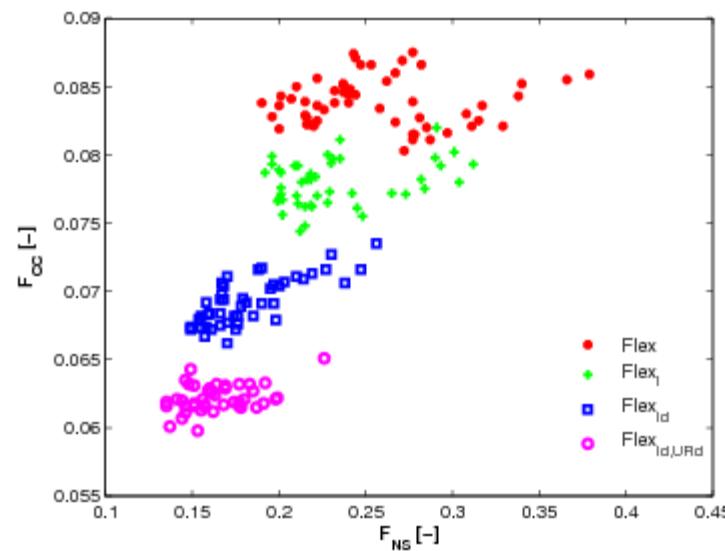
## Effect on hydrograph



# Semi-distributed rainfall accounting

## Model validation:

- Effect of errors
- Hierarchy of performance is maintained: no overfitting



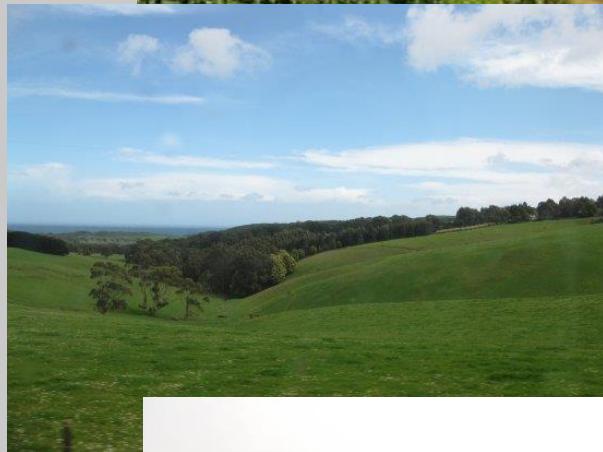
# Topography driven conceptual modeling (FLEX-Topo)



**Let us have a look at  
some landscapes...**



**...can we see some  
recurring patterns?**





### Patterns with similar emergent behaviour:

- agriculturally cultivated **Plateaus**
- forested **Hillslopes**
- **Valley bottoms** used for crop cultivation or grazing

Boundary  
conditions

Self-organizing system

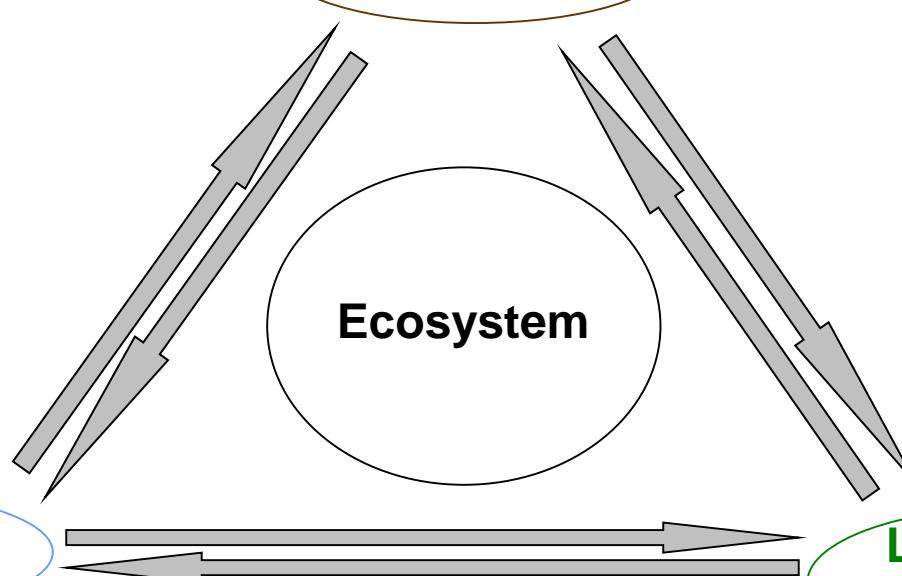
Climate and Geology

Landscape

Ecosystem

Hydrology

Land cover/  
Land use



- Possible way to go is to incorporate available data with knowledge about ecosystem functioning
- A priori definition of landscape units with different function

# Forested hillslopes

Two crucial observations:

- **Floods** predominantly generated on hillslopes
- Hillslopes frequently covered by **forests**

Forest can only survive on hillslope because of

- (a) moisture **retention** to bridge dry spells
- (b) efficient sub-surface **drainage** of excess water to ensure aerated soil and avoid erosion



- **Preferential flow pathways** most dominant and efficient mechanism – “Storage excess subsurface flow”
- **Feedback process:** floods are generated on hillslopes because they are forested and forests are located on hillslopes because there are efficient drainage mechanisms

# Plateaus

Characterized by low gradients and deep groundwater table

## Primary functions:

- (a) moisture retention
- (b) evaporation

Primary processes predominantly vertical

Little contribution to storm runoff generation



# Riparian zone / wetlands

Characterized by modest slopes and located close to open water

- Groundwater table close to ground surface
- Moisture storage potential low

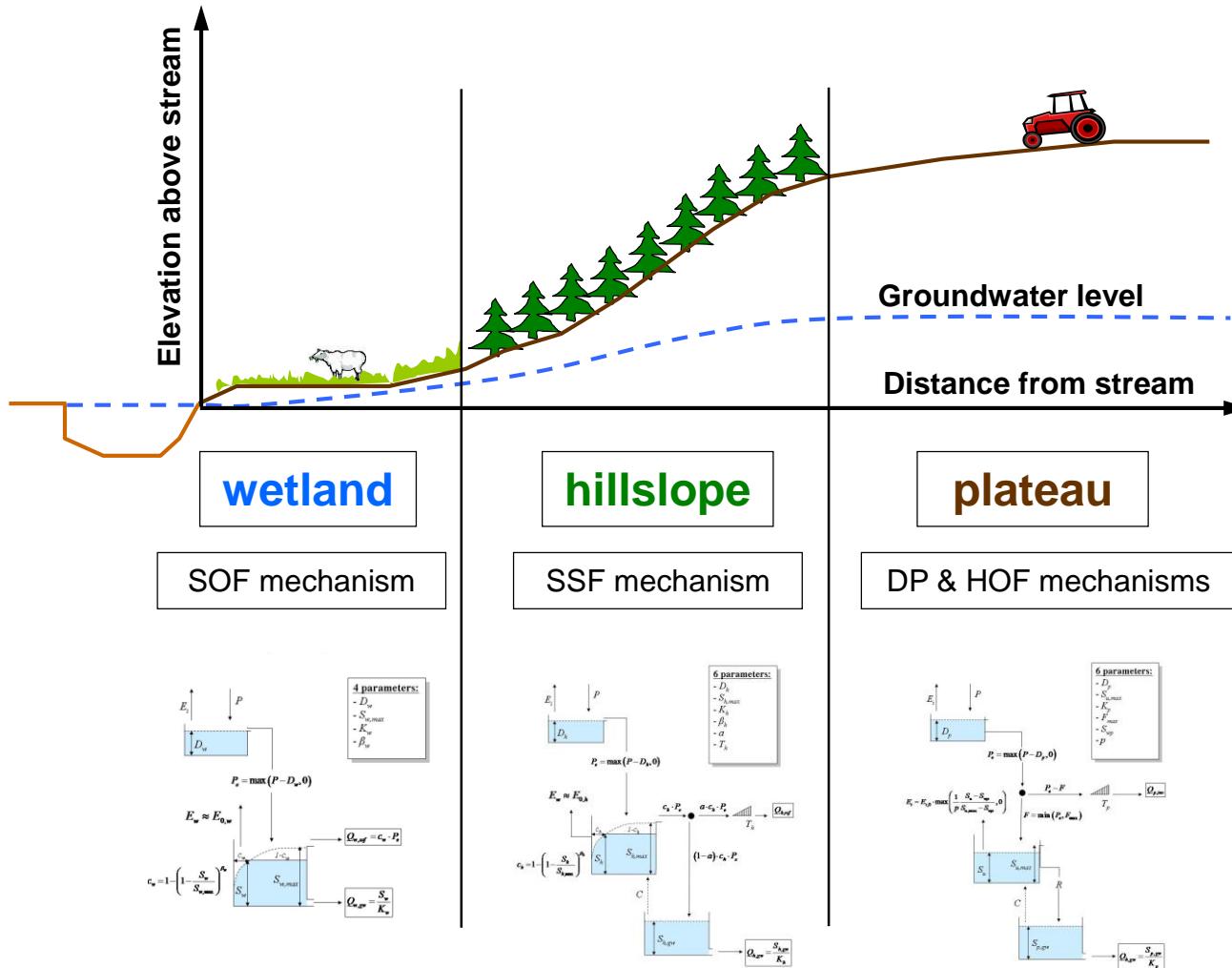
## Primary function:

Contribution to flood generation, but due to small areal extent of riparian areas less important than hillslopes

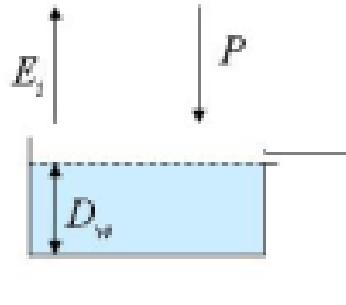


## Primary process saturation overland flow

Different landscape units → different hydrological function → different model structure



# Riparian zone / wetland



**4 parameters:**

- $D_w$
- $S_{w,max}$
- $K_w$
- $\beta_w$

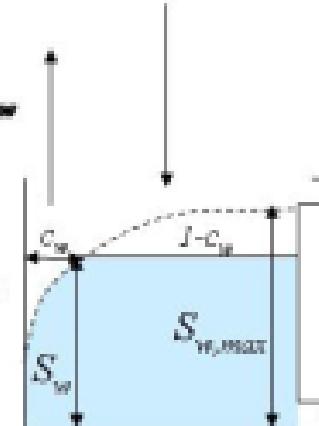
Dominant process:

Saturation overland flow



$$P_s = \max(P - D_w, 0)$$

$$E_w \approx E_{0,w}$$

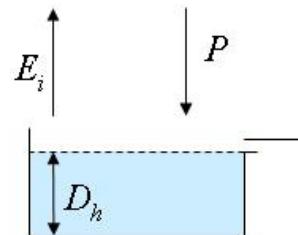


$$Q_{w,sf} = c_w \cdot P_s$$

$$c_w = 1 - \left(1 - \frac{S_w}{S_{w,max}}\right)^{\beta_w}$$

$$Q_{w,sf} = \frac{S_w}{K_w}$$

# Hillslope



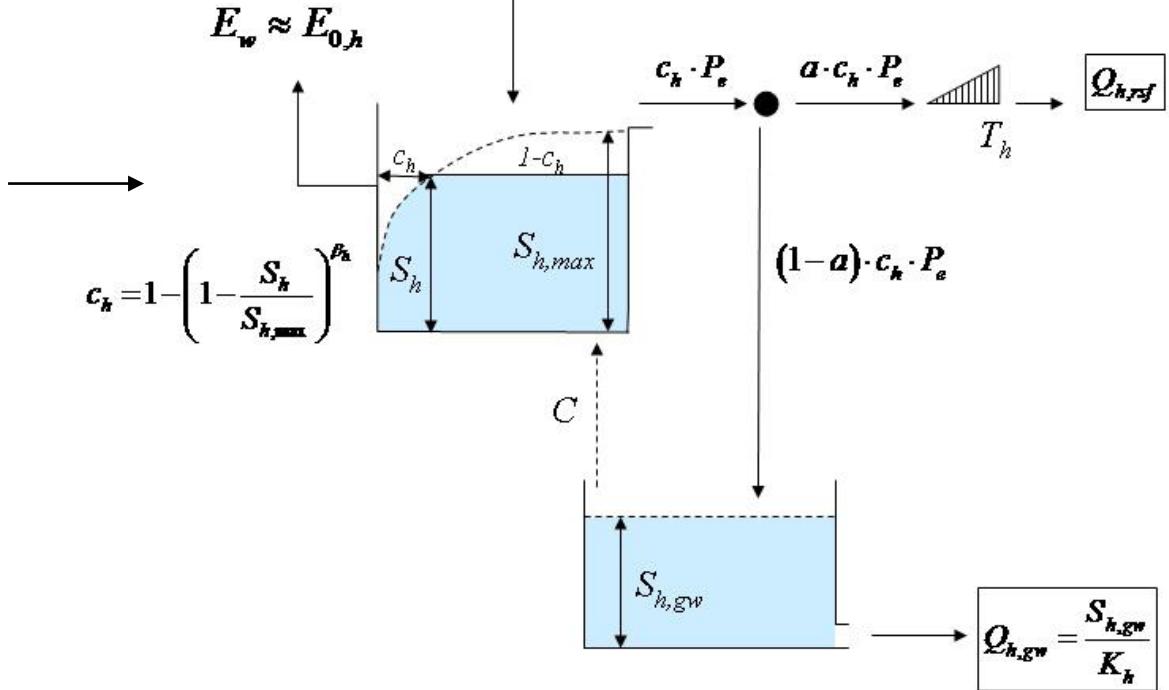
$$P_e = \max(P - D_h, 0)$$

**6 parameters:**

- $D_h$
- $S_{h,max}$
- $K_h$
- $\beta_h$
- $a$
- $T_h$

Dominant process:

Shallow subsurface flow



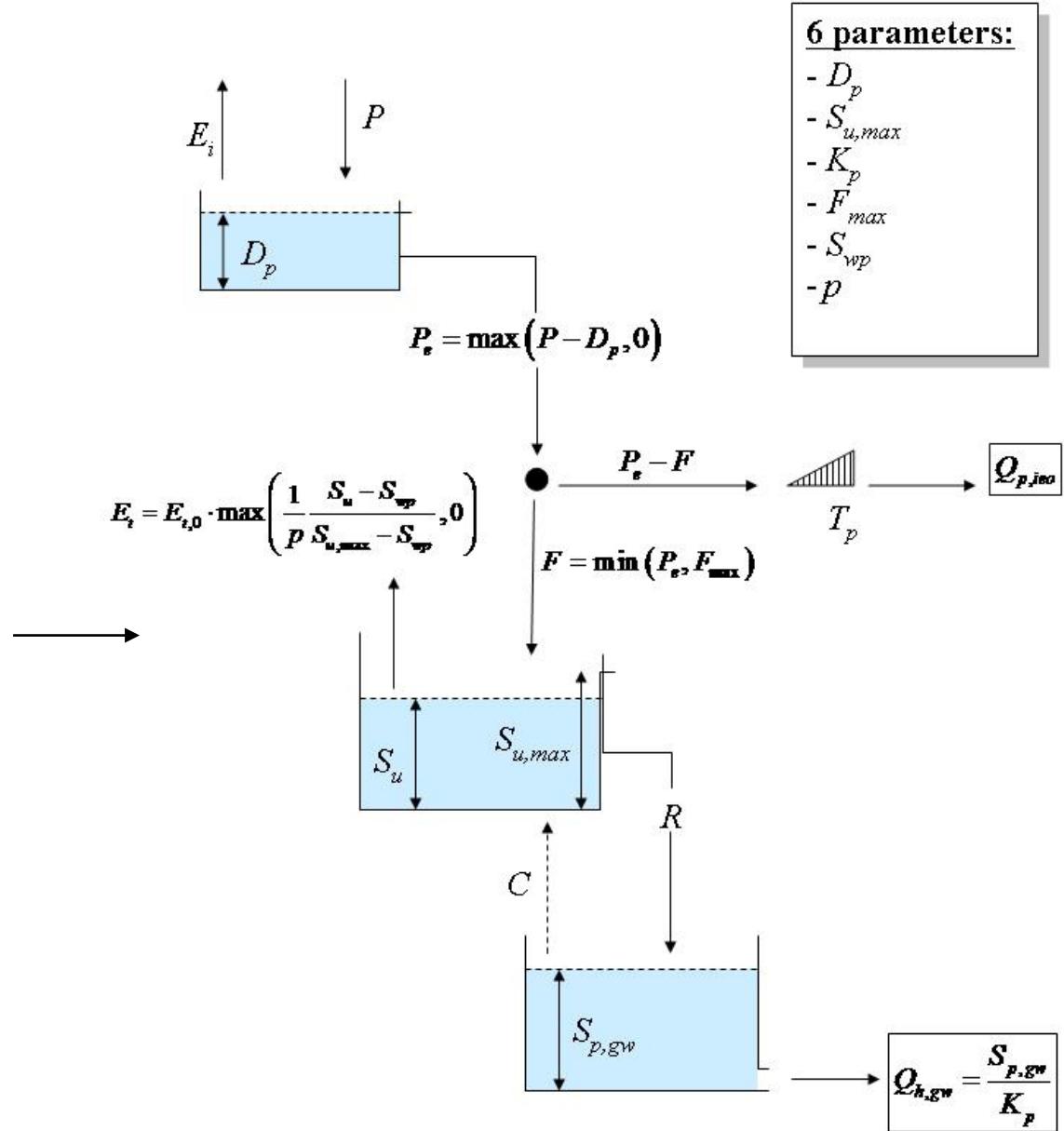
# Plateau



## Dominant processes:

Deep percolation

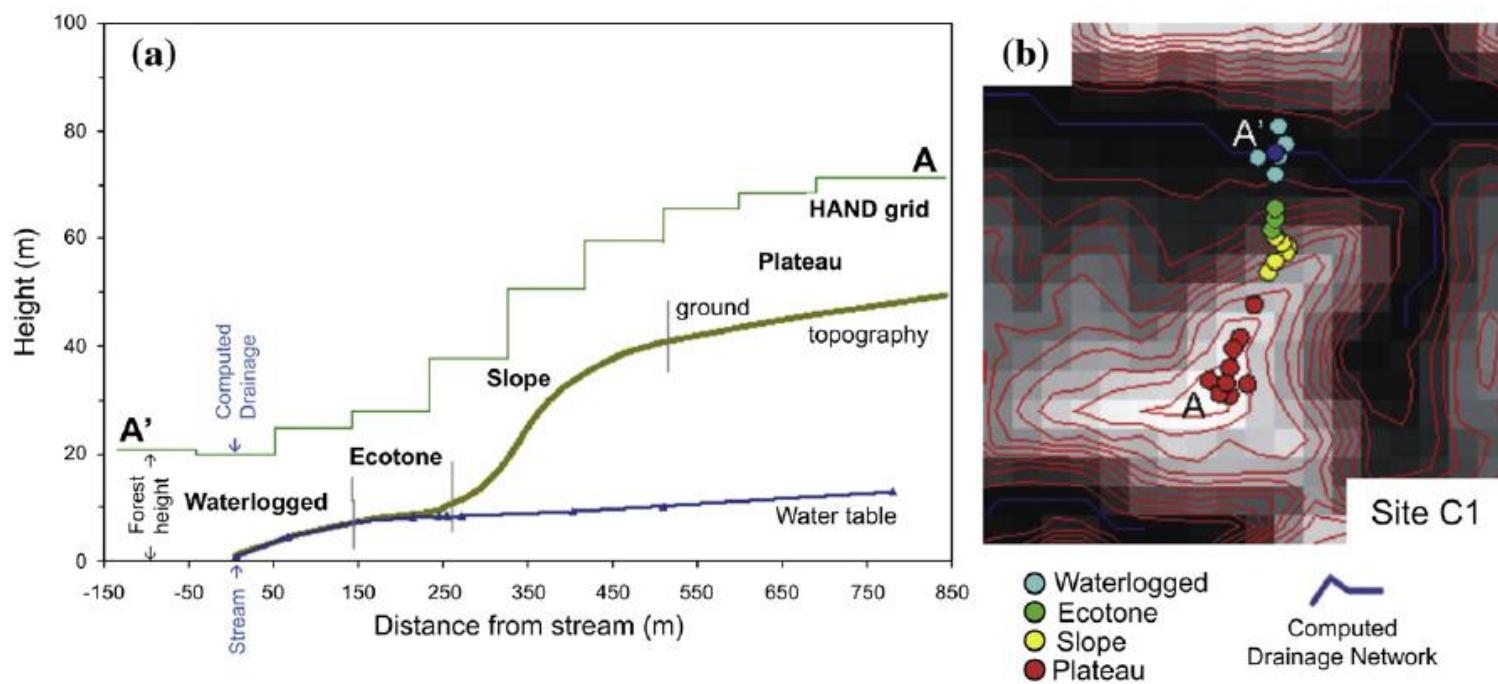
Evaporation



Can we find an **objective measure** to define landscapes which represent different functional units?

One possibility: “Height-above-nearest-drainage” (**HAND**):

- (1) Landscape classified by distance from and elevation above stream
- (2) Inflection points indicate changes in landscape features and functional units



Renno et al., 2008, RSE

## HAND (cont.):

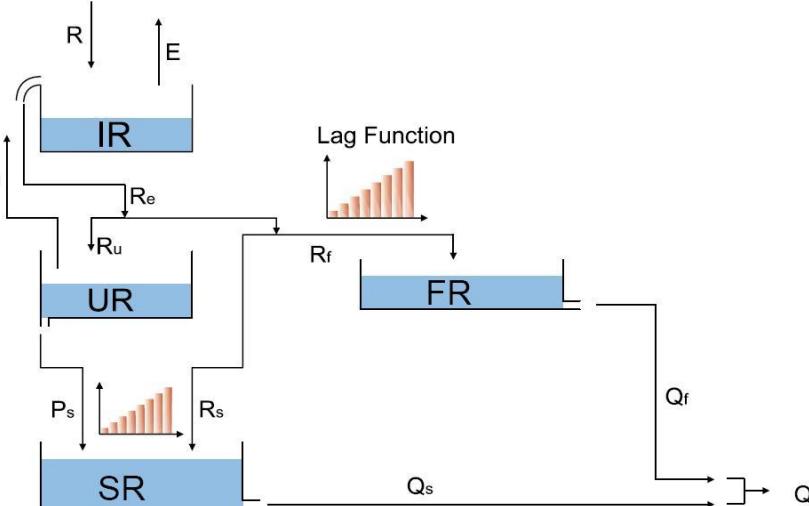
- (3) Suitable model structure assigned to each functional unit
- (4) Modeled runoff is a composite of proportional contributions from each functional unit, i.e. pre-assigned model structure

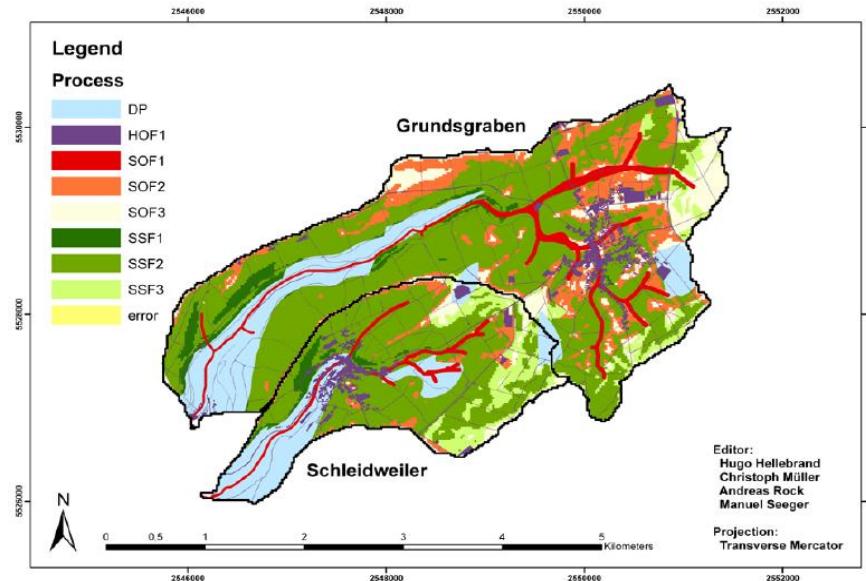
### Advantage:

**Improved process**  
of readily available  
number  
→ Potential for better parameter

model, only on basis  
crease in parameter

ges and ensuring





## Has this not been done before?

To a certain extent yes, **BUT:**

- Incorporated in process based models, resulting in considerable parameter equifinality (e.g. Uhlenbrook et al., 2004) or
- Classification of functional units based on information that is too detailed and therefore mostly not available (e.g. Scherrer et al., 2007; Hellebrand and van den Bos, 2008)

# Flex-TOPO



Land classification



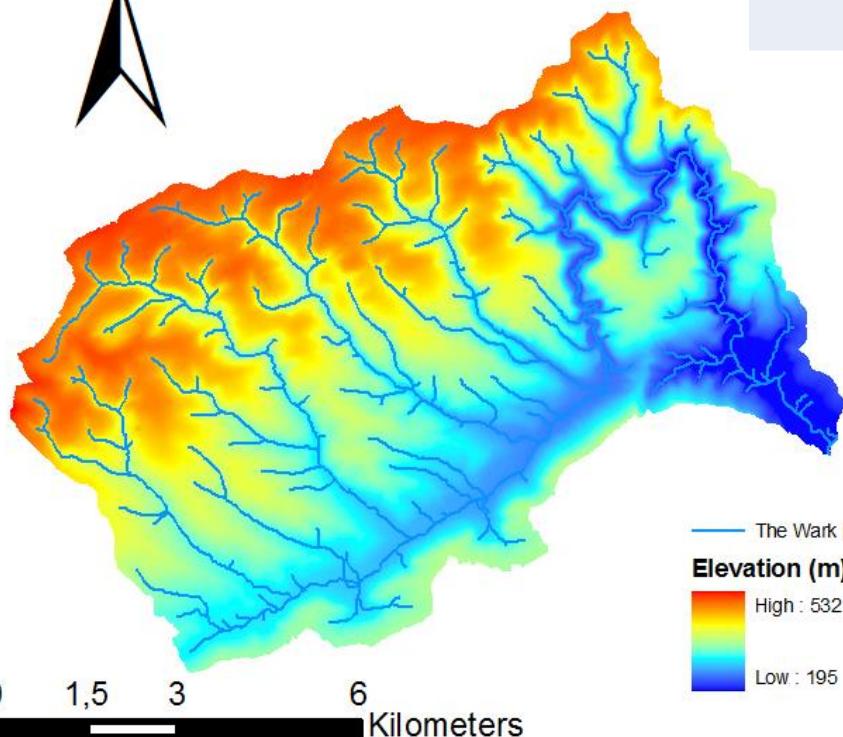
Assigning different hydrological response unit



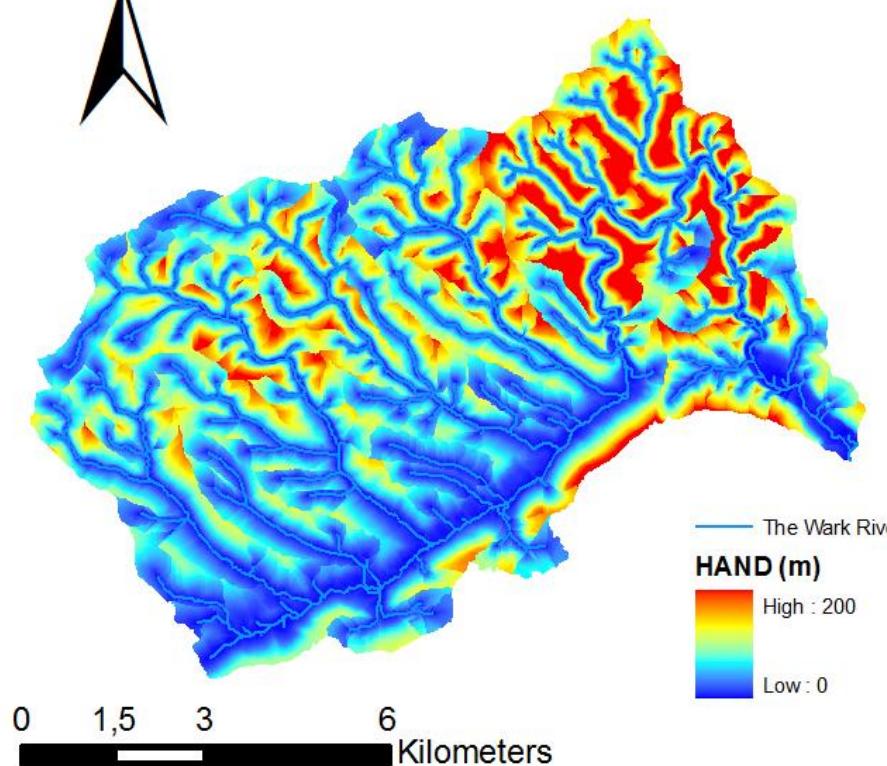
Conceptualization of each response unit

# Flex-TOPO

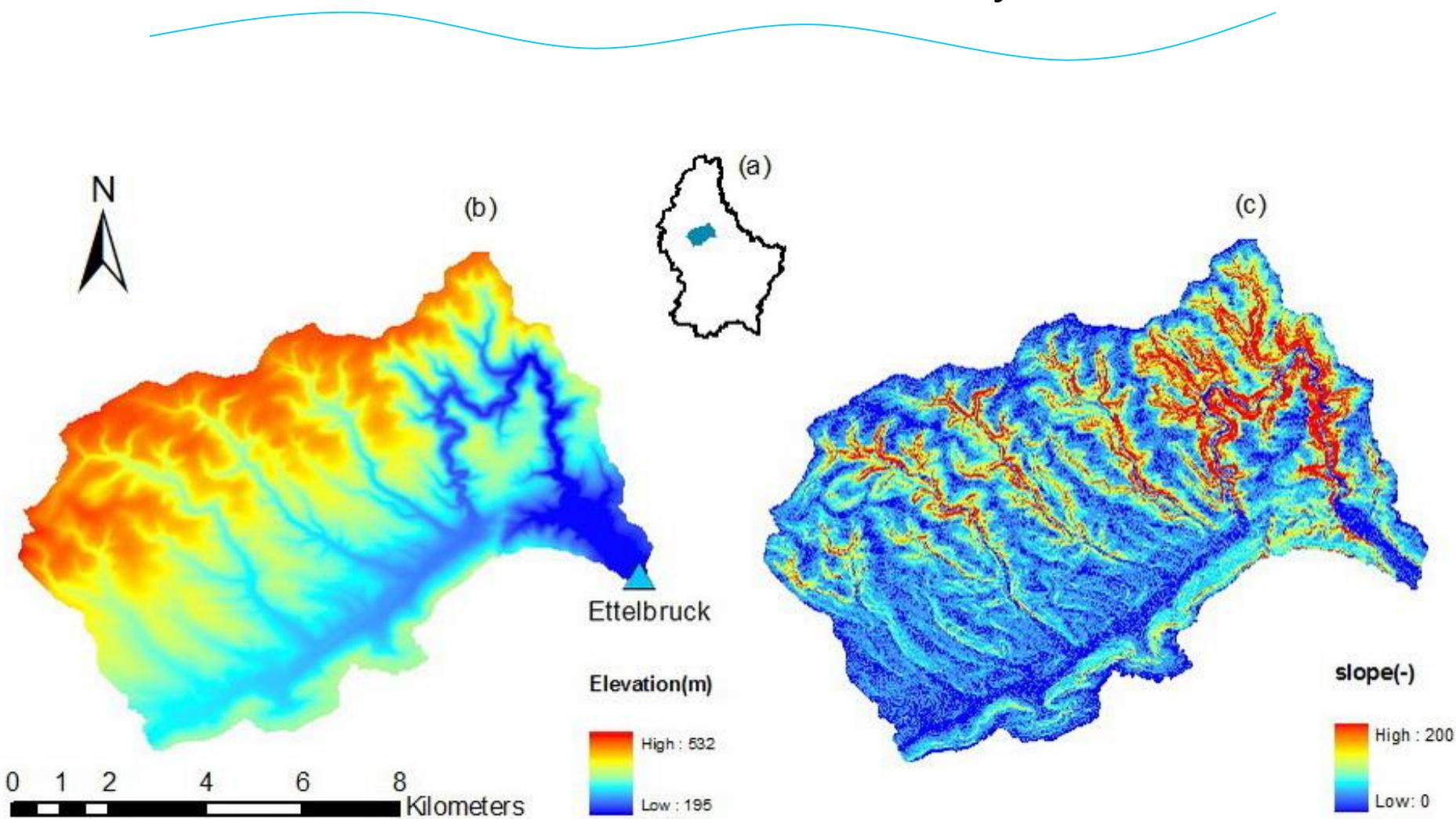
## 1. Landscape classification v



	High Slope	Low Slope
High HAND	Hillslope (B)	Plateau (A)
Low		



# Flex-TOPO: Case study



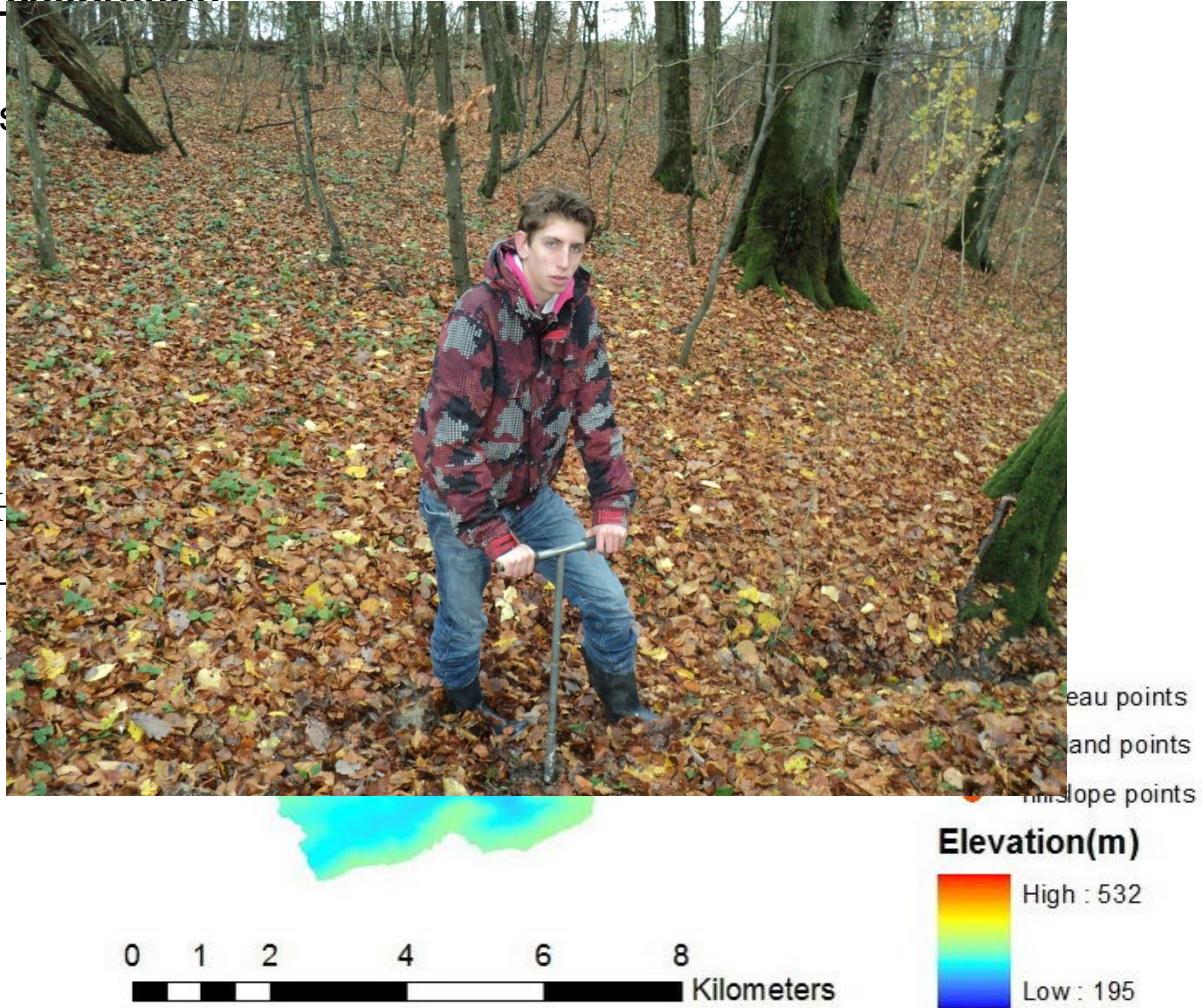
# Flex-TOPO: Case study

## Landscape classification : calibration

A total number of 5611 points:

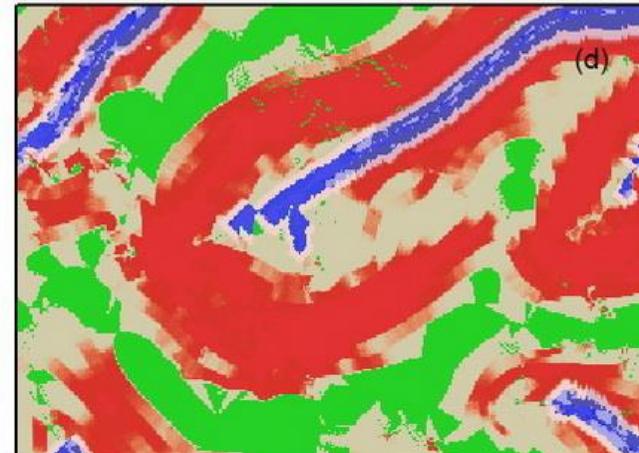
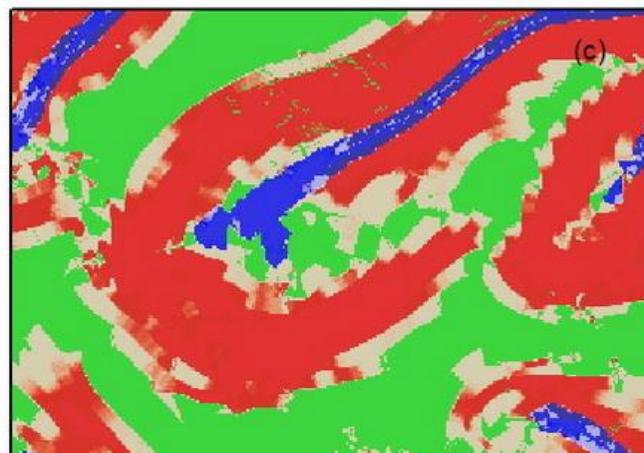
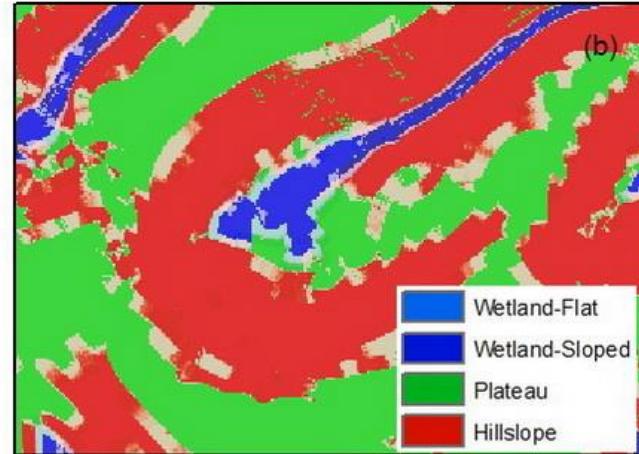
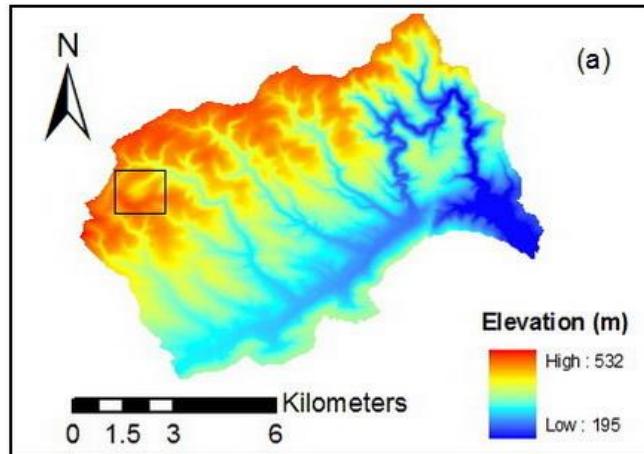
- 1501 (26.8%) Wetland
- 1385 (24.6%) Hillslope
- 2725 (48.6%) plateau

$$\text{ObjFun} = \left[ 1 - \frac{\sum_{i=1}^{N_H} p_H}{N_H} \right]$$

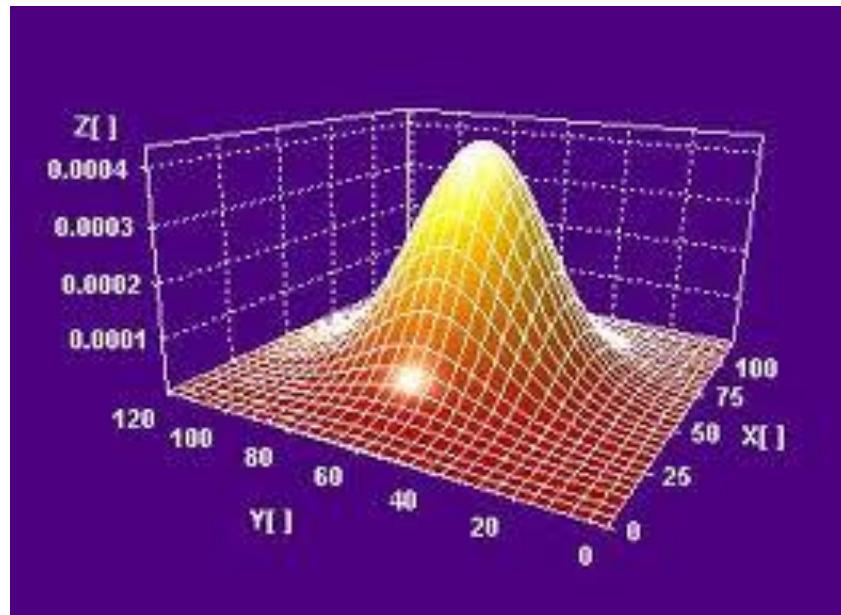


# Flex-TOPO: Case study

HAND landscape classification



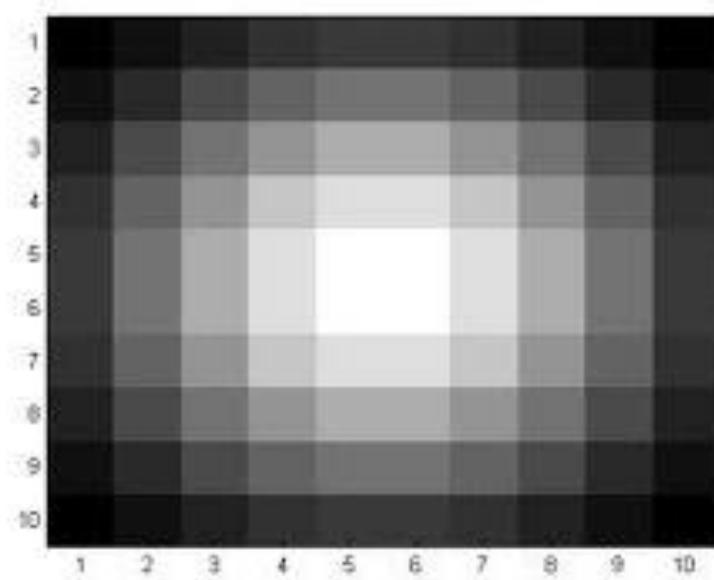
# Flex-TOPO: Case study

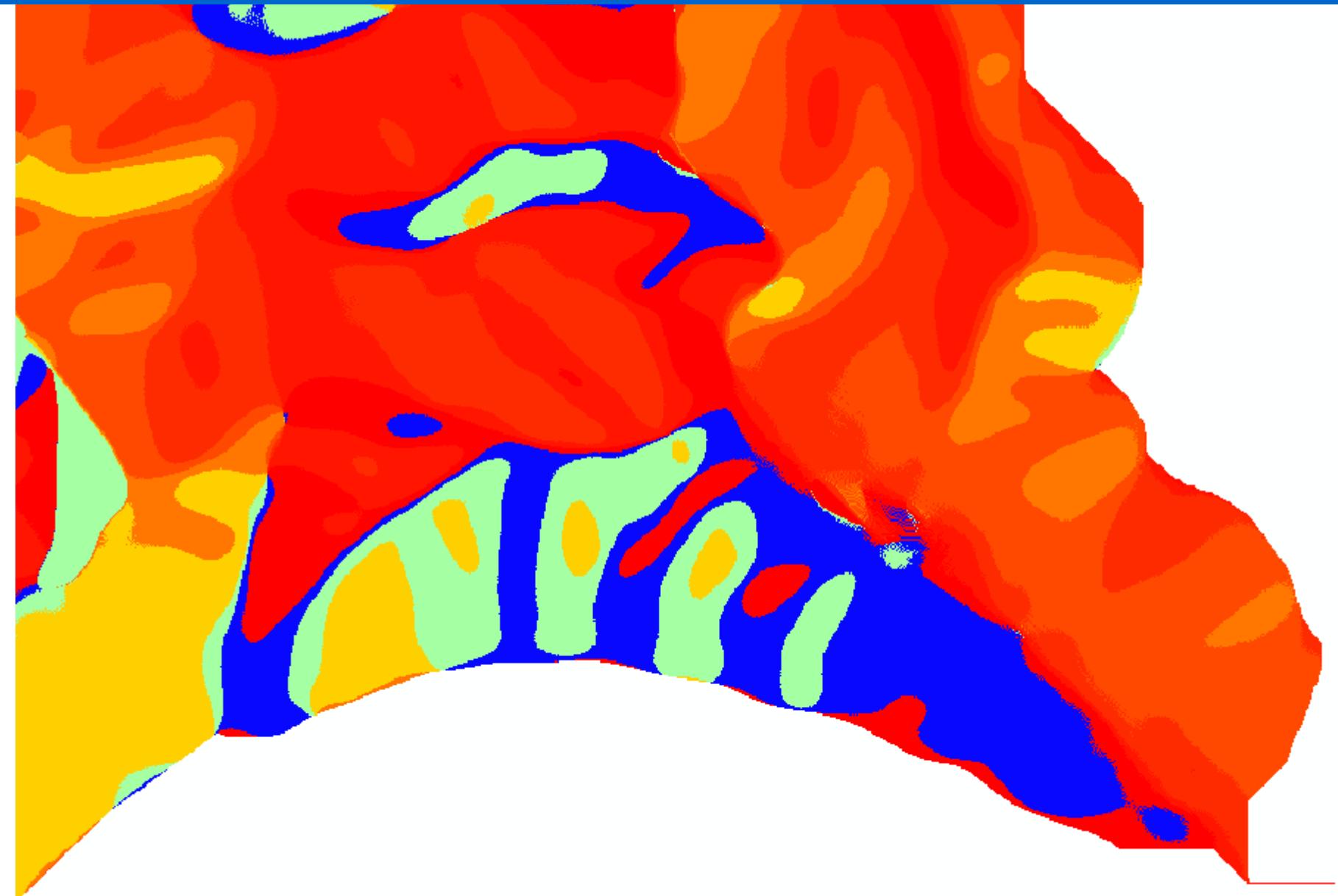


rock outcrop, structures or roads which

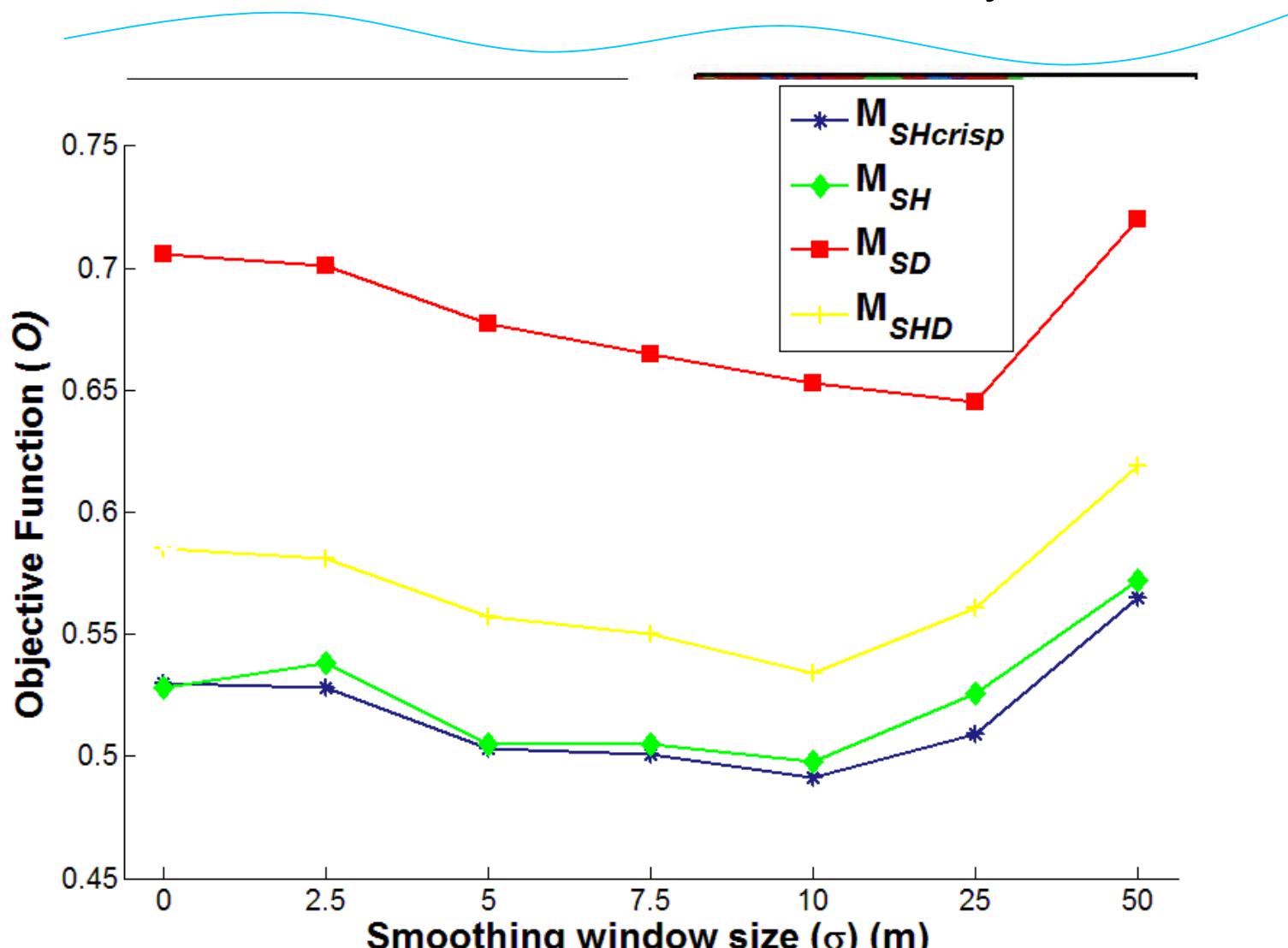
are represented by points in the DEM.

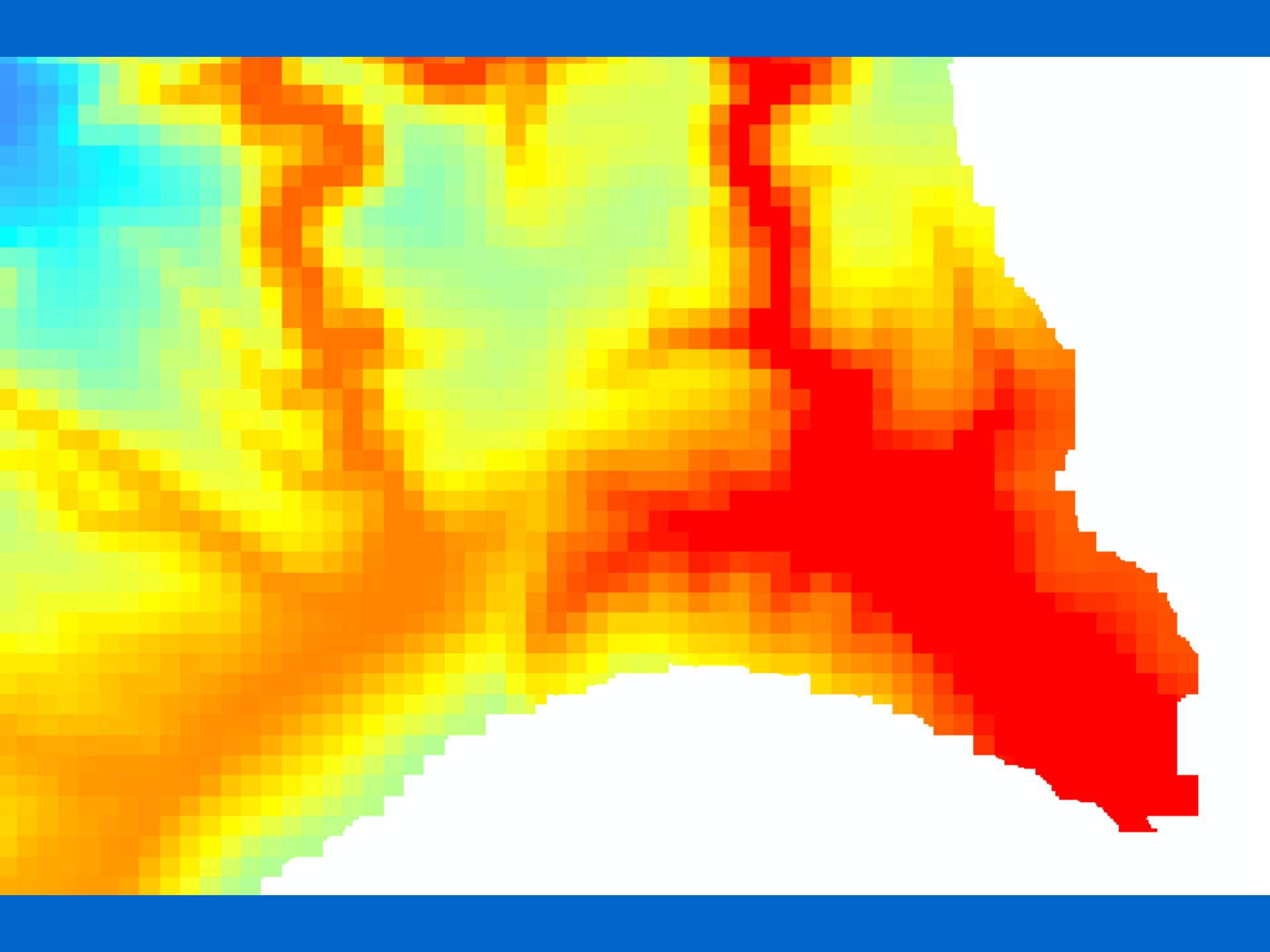
or with different sizes was used.



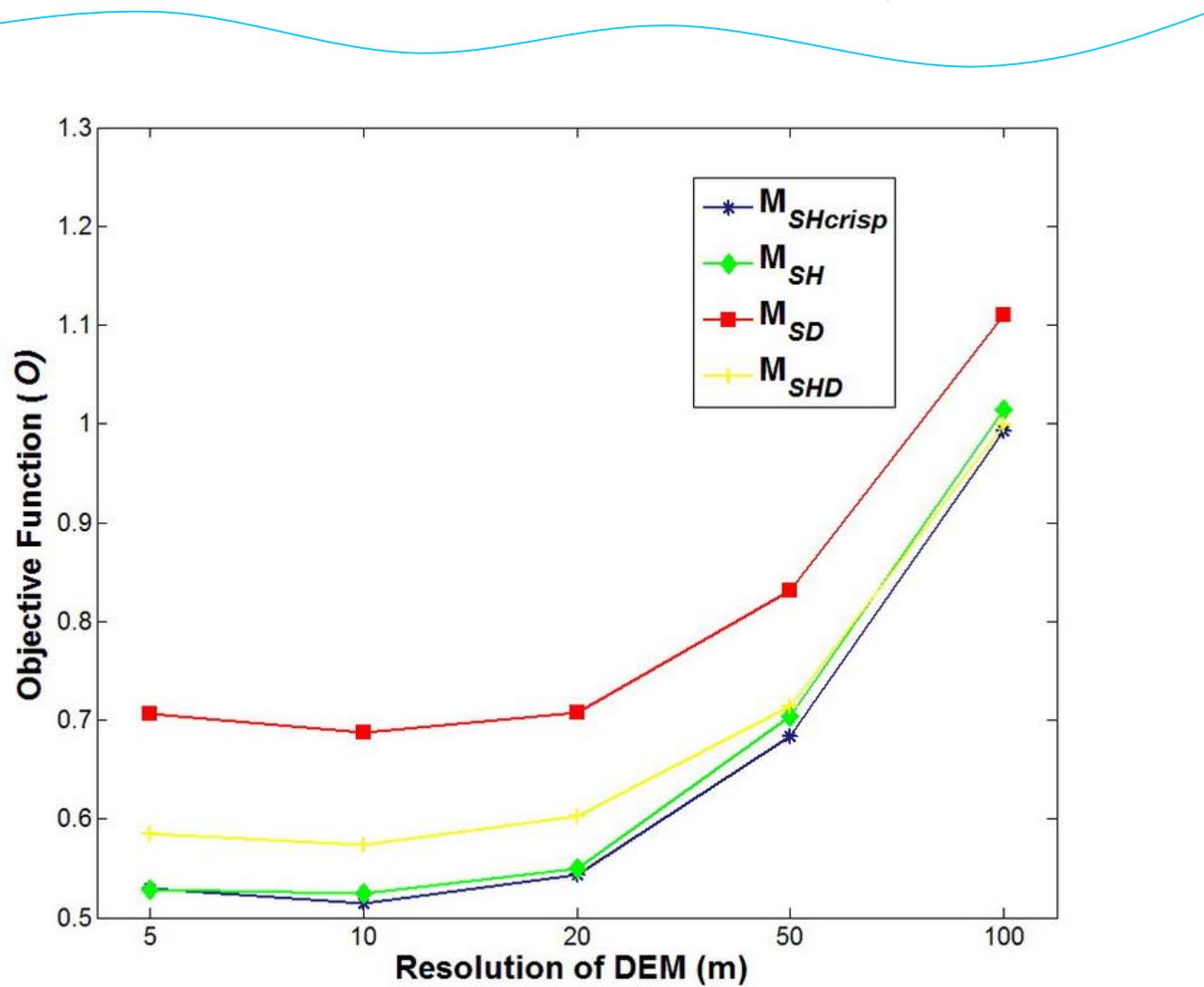


# Flex-TOPO: Case study

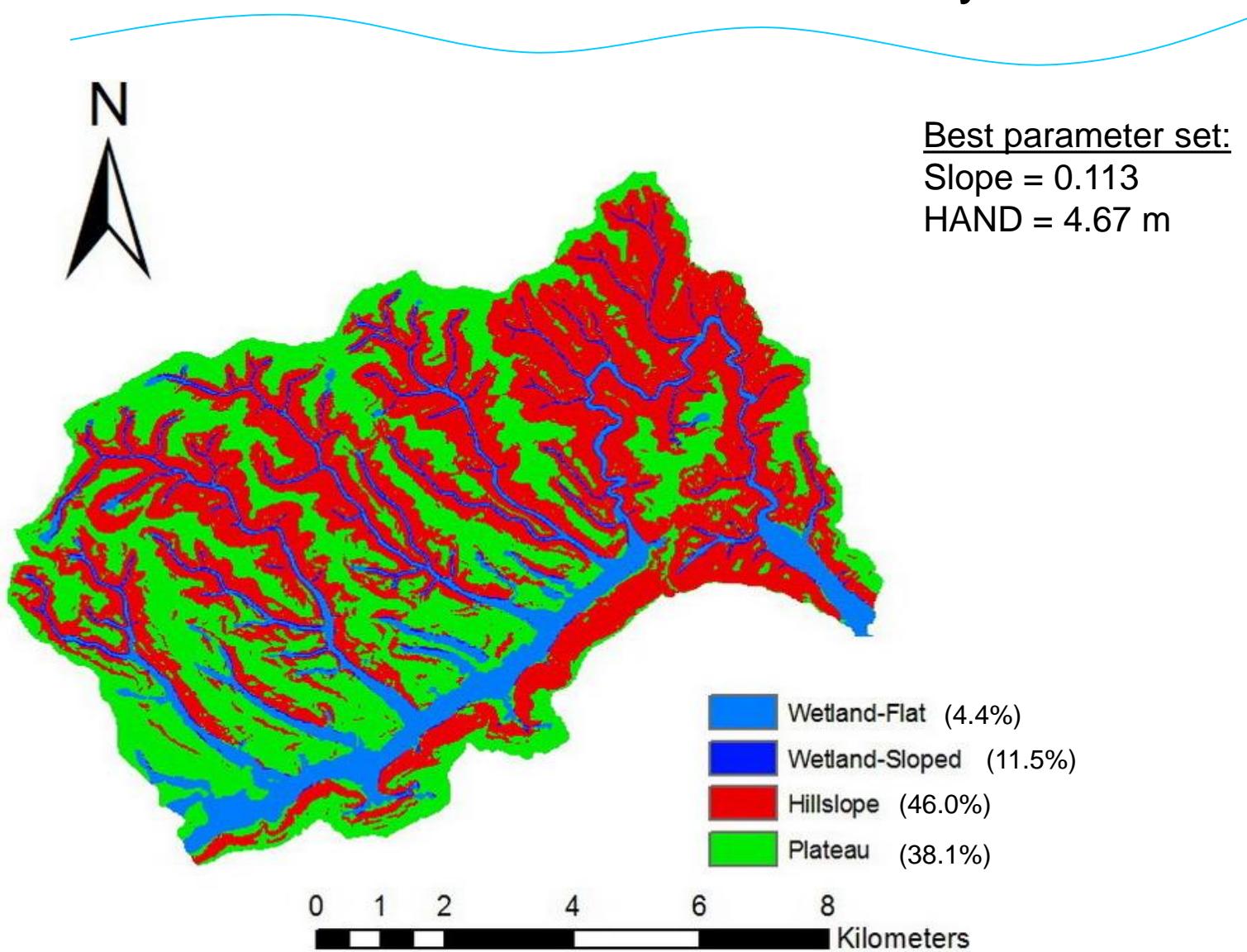




# Flex-TOPO: Case study



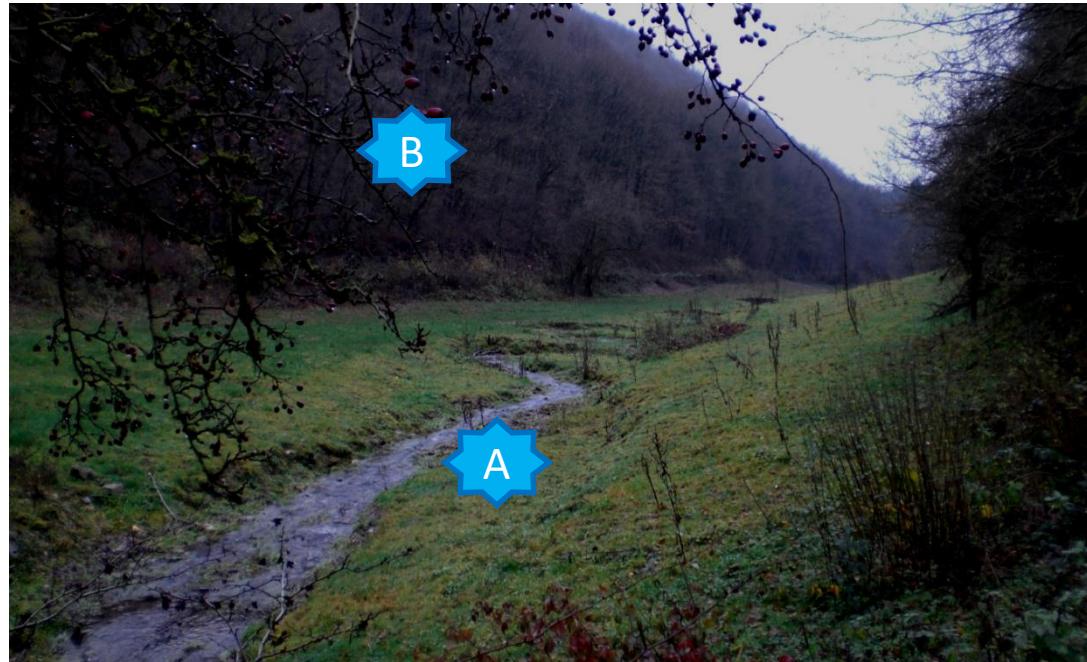
# Flex-TOPO: Case study



# Flex-TOPO: Case study

## Comparison with Topographic Wetness index

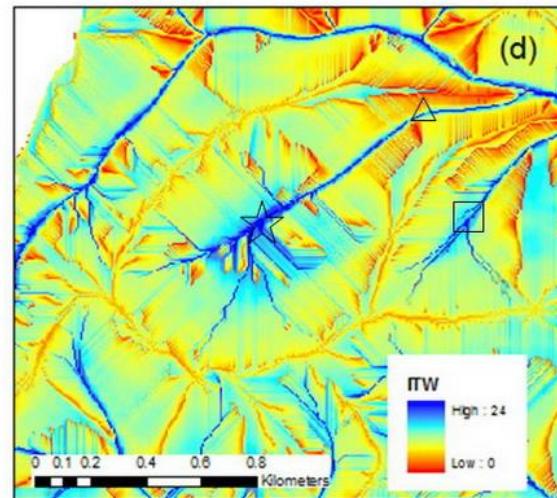
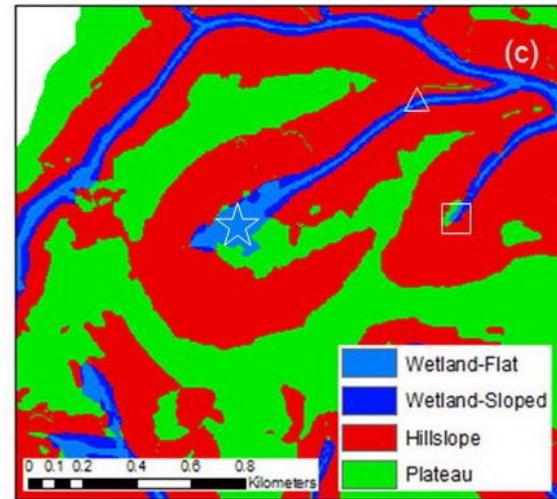
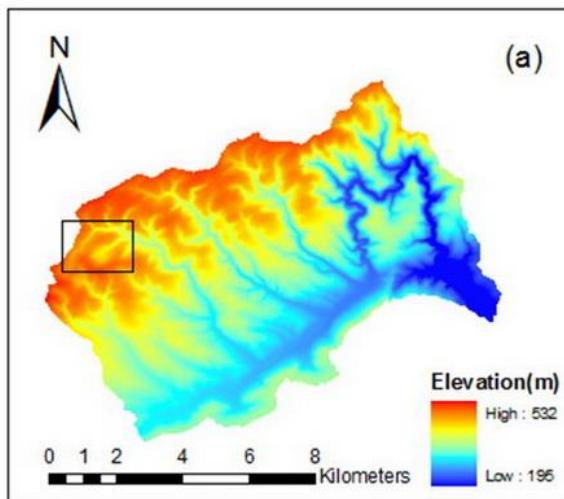
$TWI = \ln(A/s)$ , TOPMODEL(Beven and Kirkby 1979)



For point A:  
 $WI = \ln(A^\uparrow/s^\downarrow)$   
 $WI \uparrow$

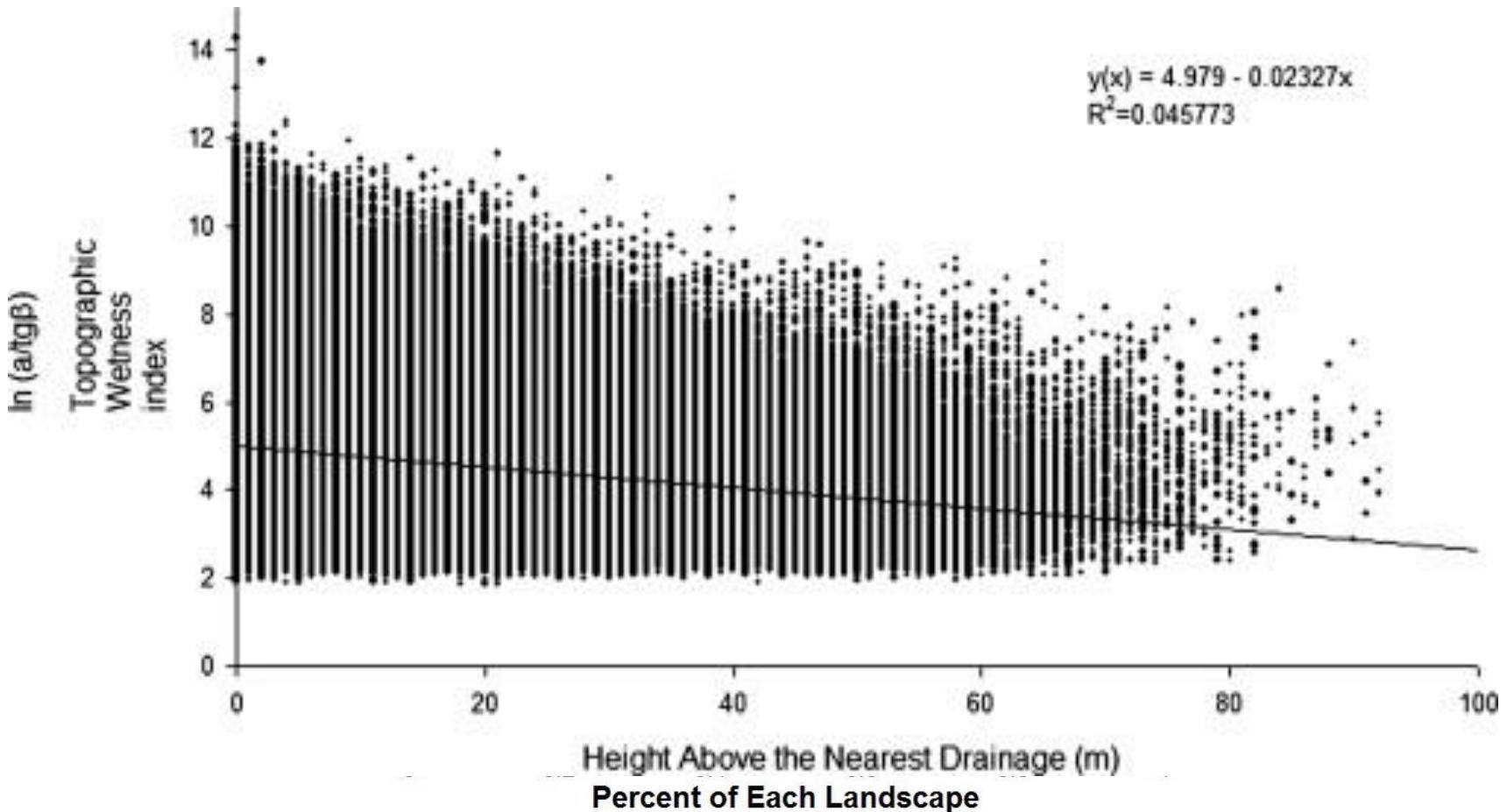
For point B:  
 $WI = \ln(A^\downarrow/s^\uparrow)$   
 $WI \downarrow$

# Flex-TOPO: Case study



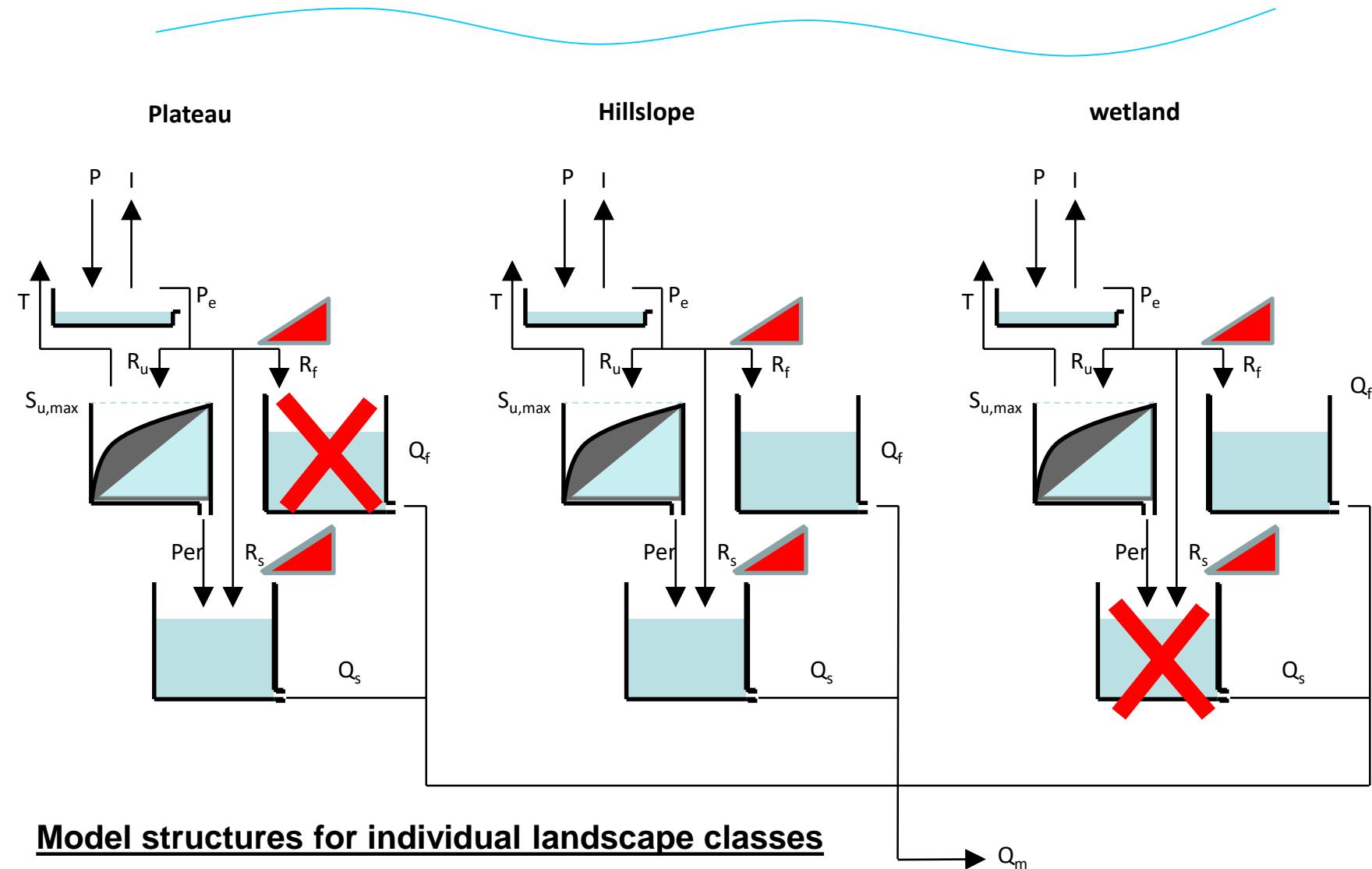
# Flex-TOPO: Case study

## Comparison with Topographic Wetness index



(Nobre et al., 2011)

# Flex-TOPO: Case study



# Flex-TOPO: Case study

**Example:**

## What do we know??

1 - Wetlands response faster to rainfall than hillslope and plateau:

- The fast reaction of wetland should be triggered earlier than other entities.
- Wetlands are active during dry period.

2 - Hillslope of the Wark catchment are mostly forested:

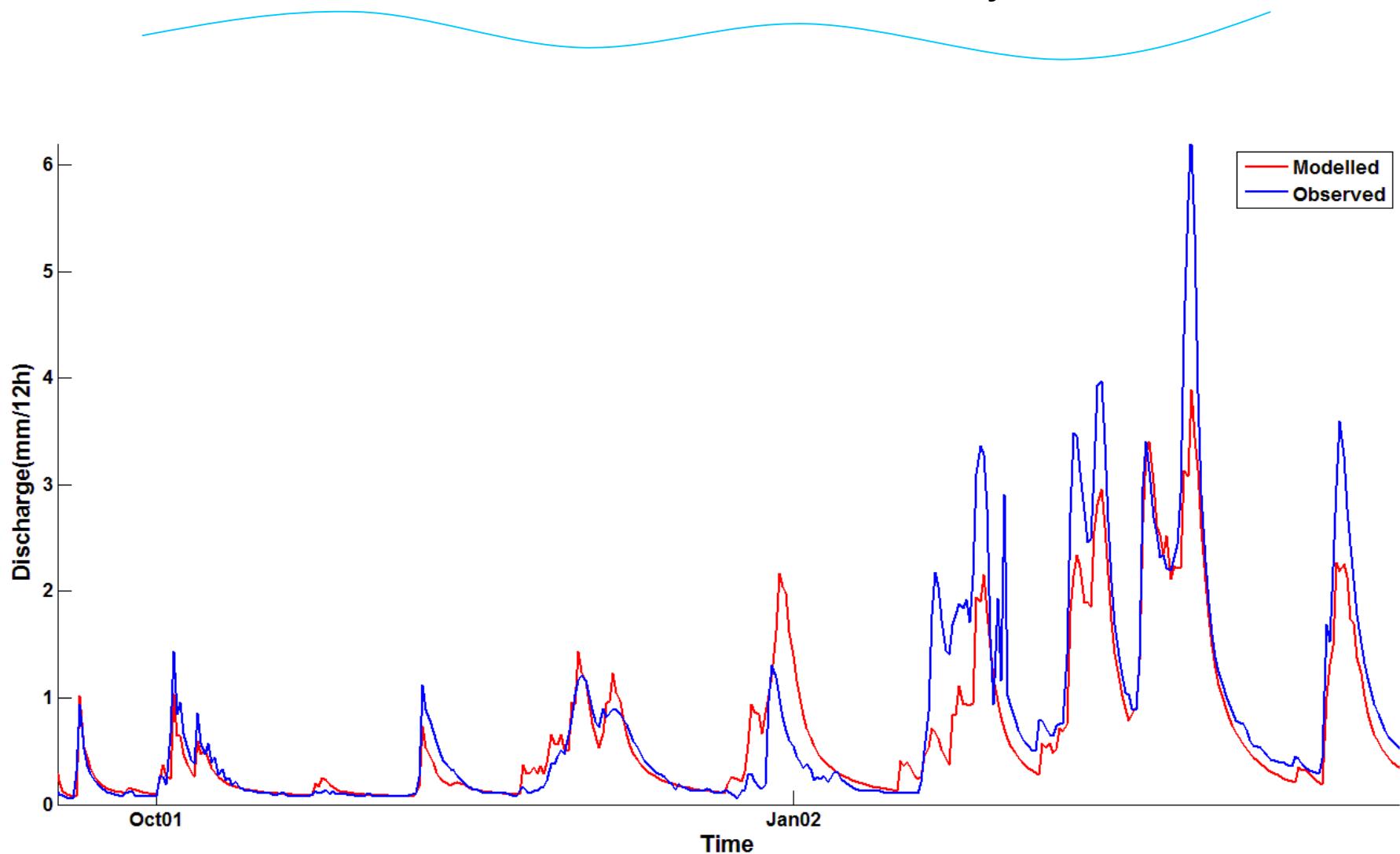
- Interception threshold of hillslope should be higher than the other landscape entities.

# Flex-TOPO: Case study

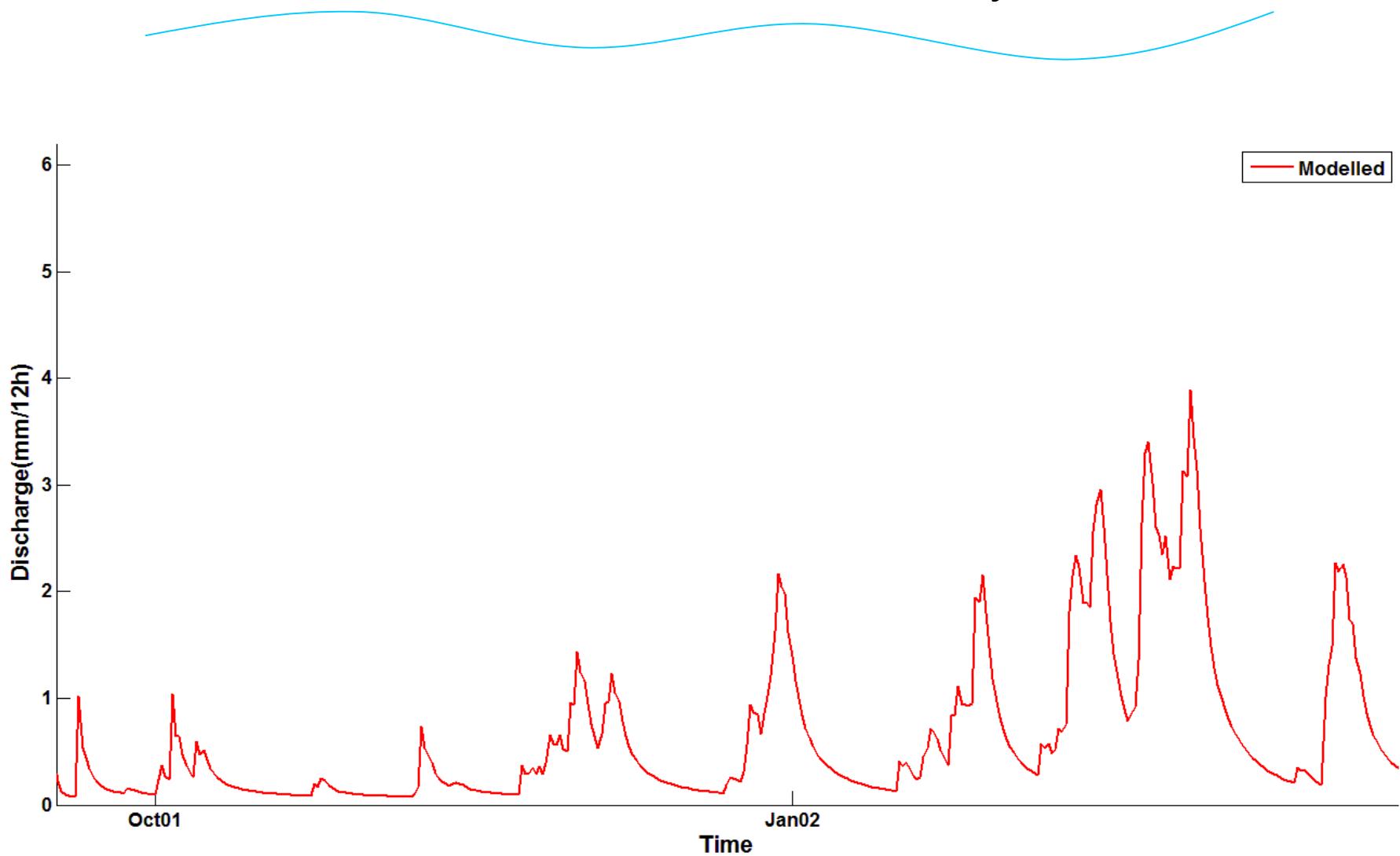
## Calibration

- Possible soft criteria were formulated, e.g.  $I_{max\ hillslope} > I_{max\ Plateau}$
- In a stepwise approach with help of MOSCEM\_UA (Vrugt et al., 2003) more and more criteria were satisfied.
- The optimum solution was found in the area of the parameter space which satisfied all soft criteria.

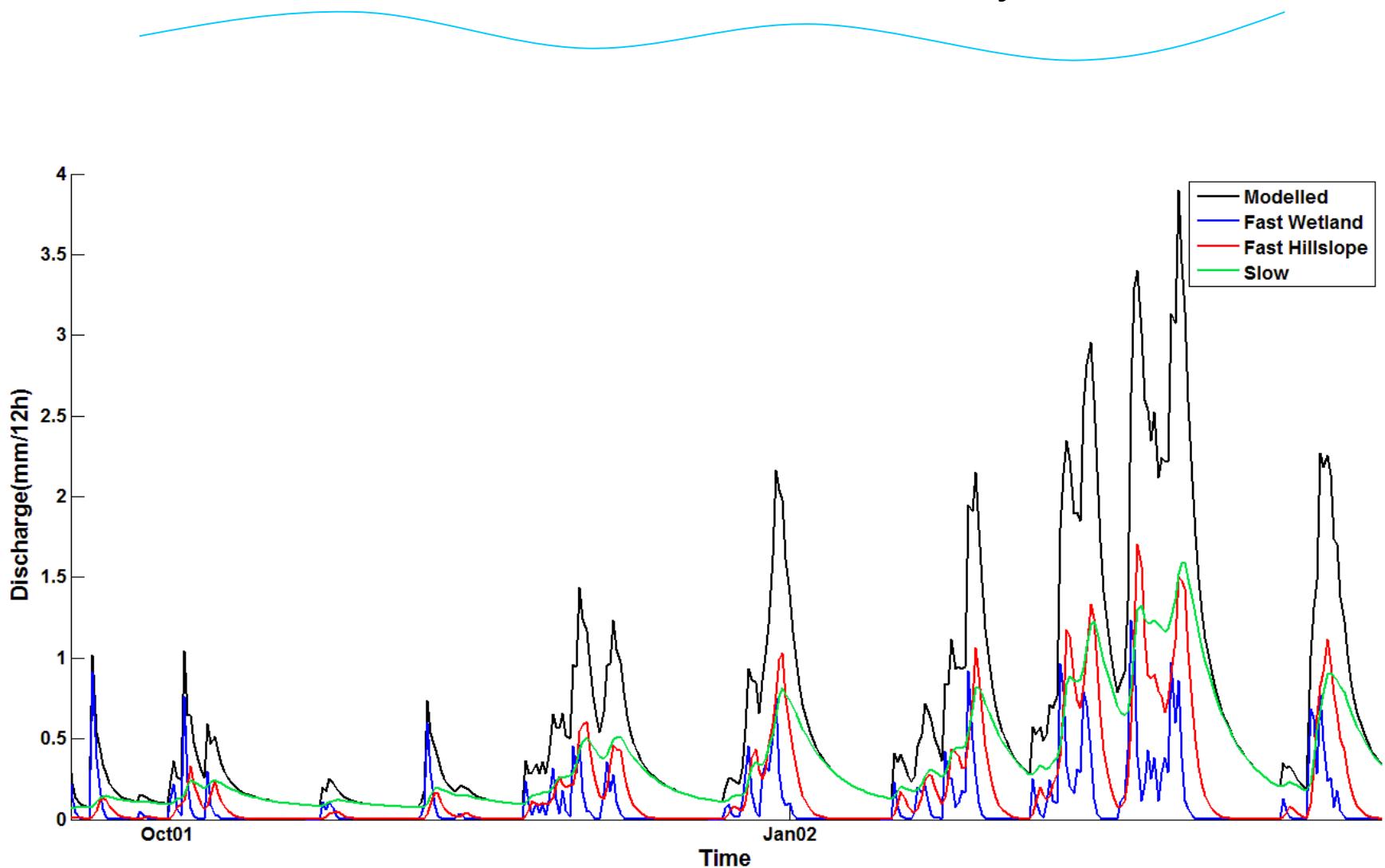
# Flex-TOPO: Case study



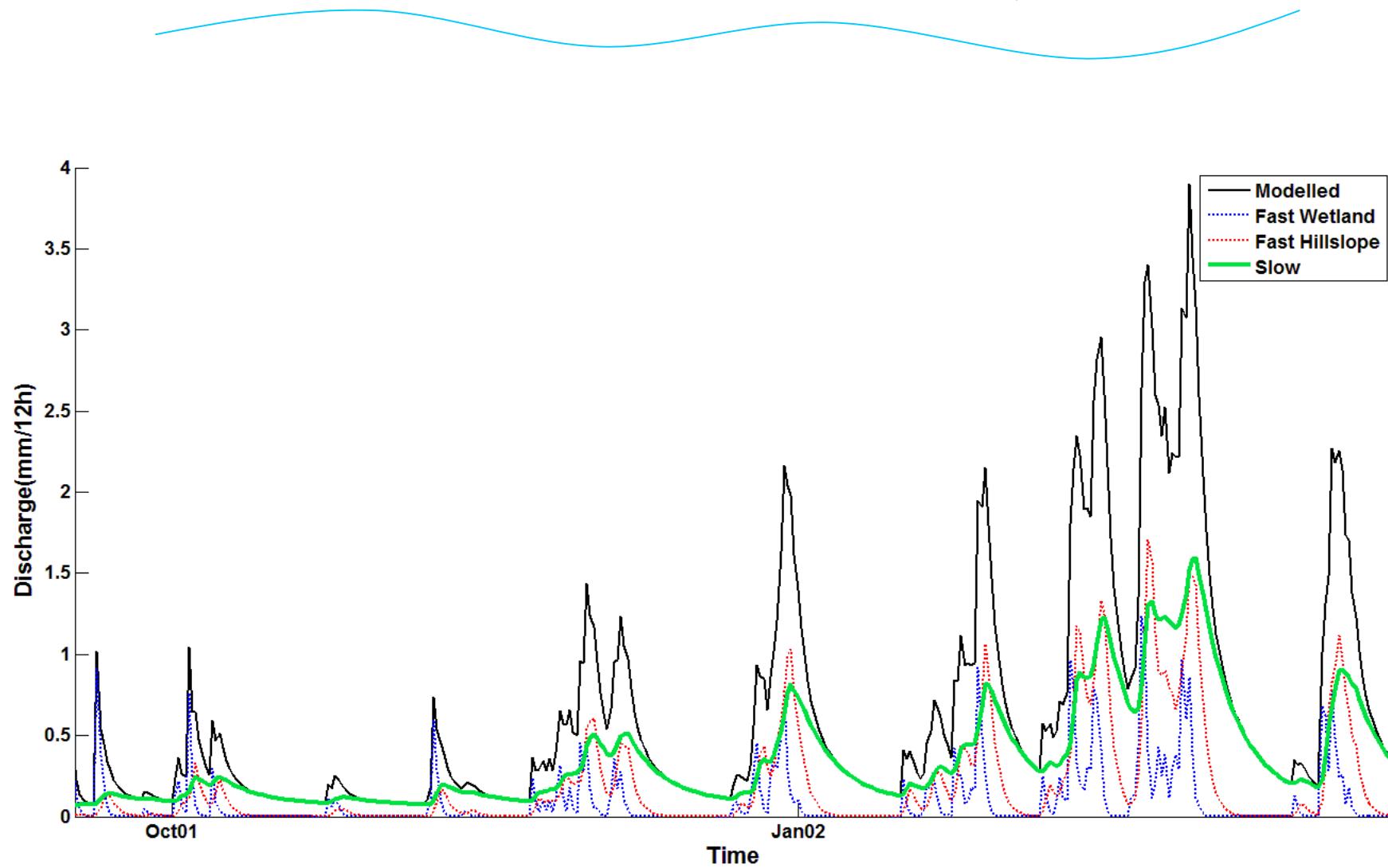
# Flex-TOPO: Case study



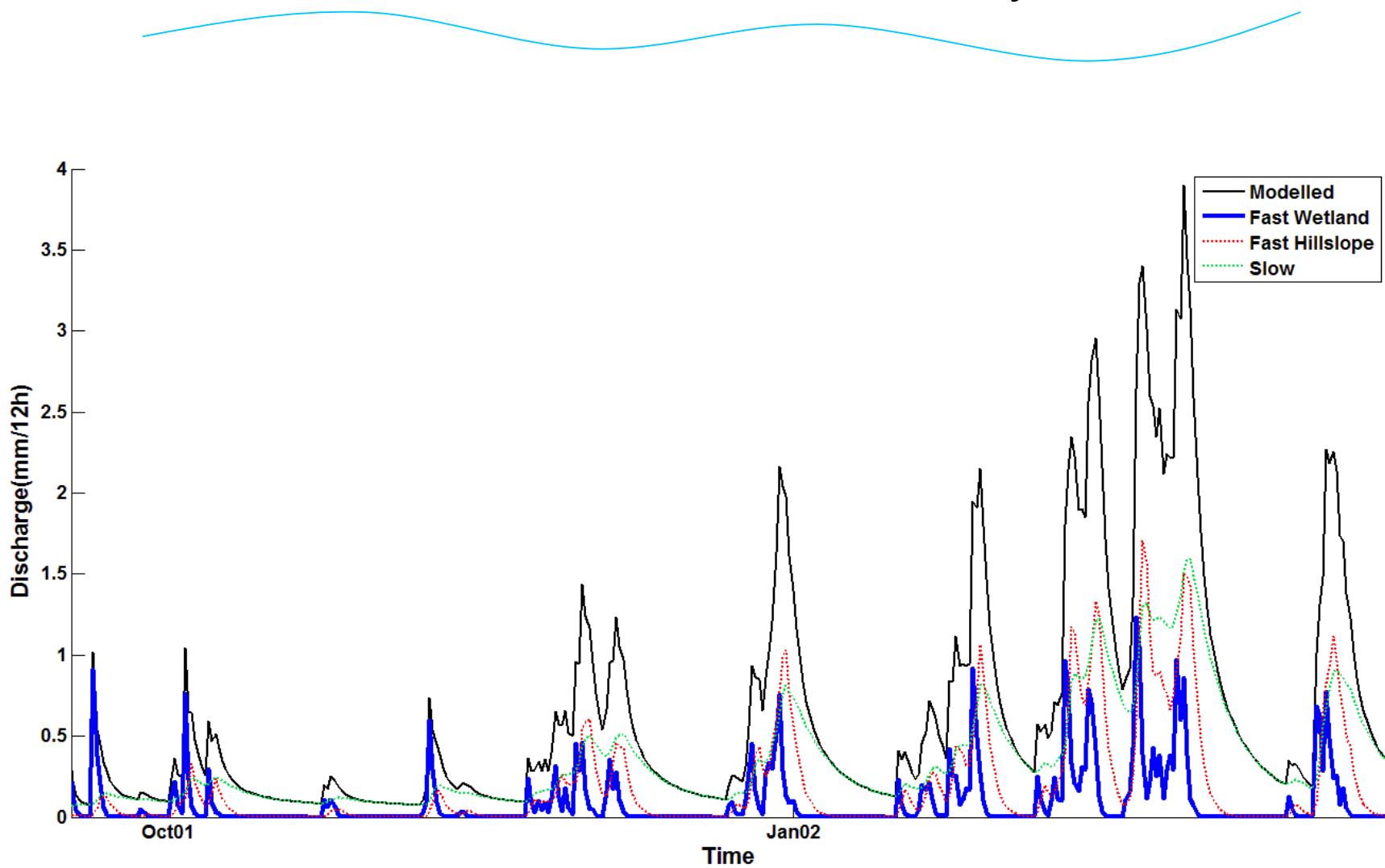
# Flex-TOPO: Case study



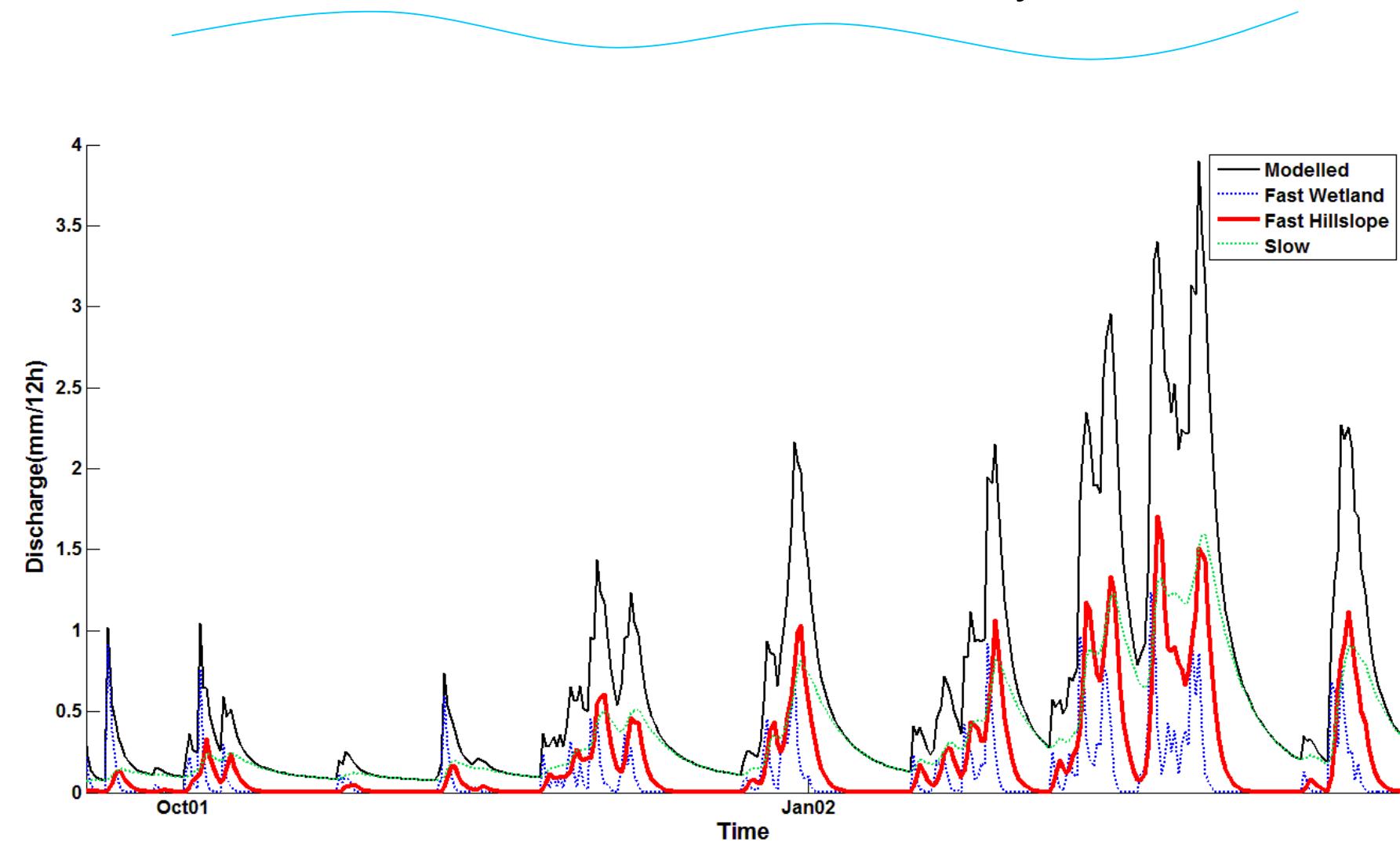
# Flex-TOPO: Case study



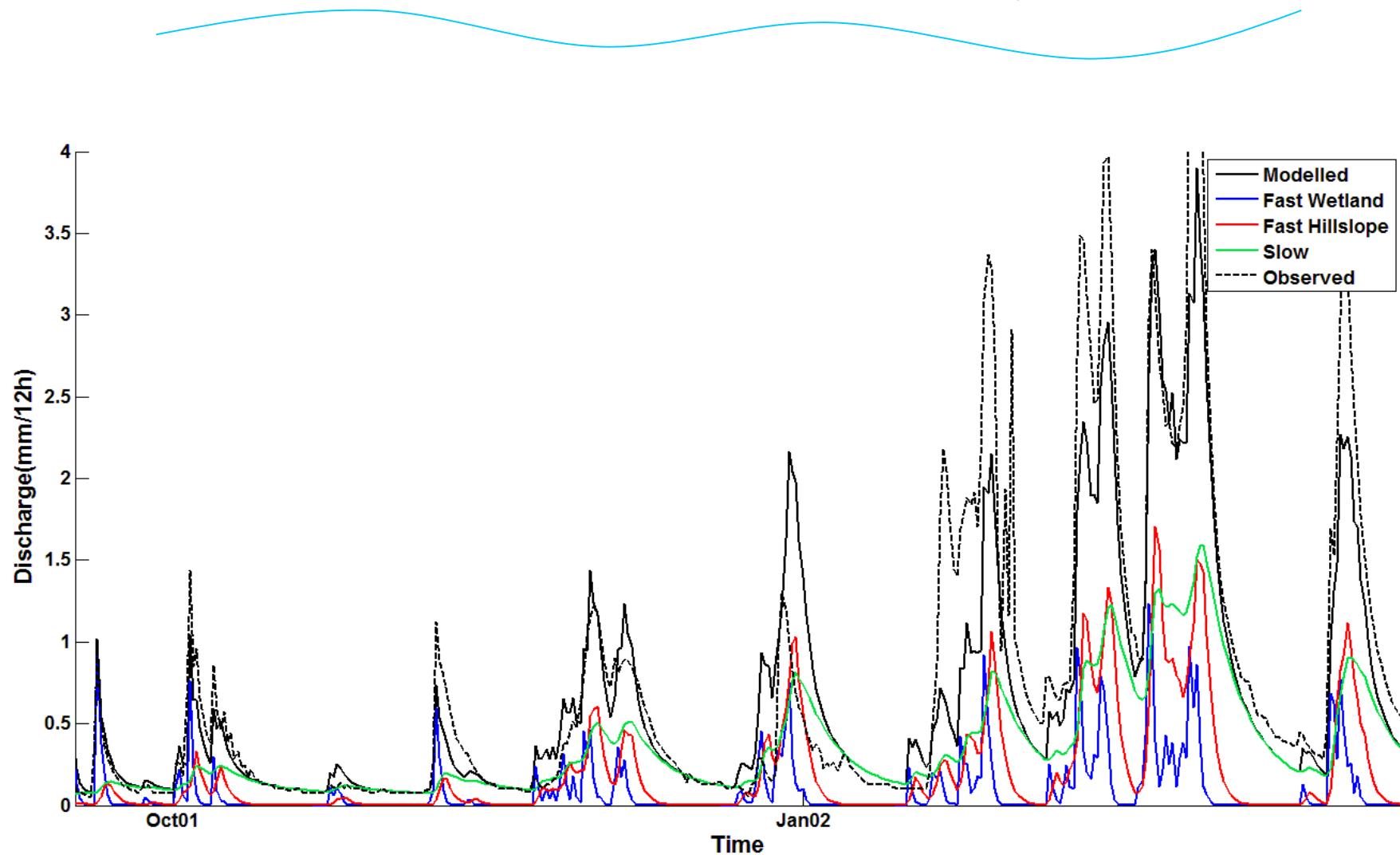
# Flex-TOPO: Case study



# Flex-TOPO: Case study



# Flex-TOPO: Case study



# Getting the right answers for the right reasons



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# Getting the right answers for the right reasons



Or: Why does my model produce weird results ???

After this lecture you will

- know which problems can be introduced by data
- know why data pre-processing is important
- be able to interpret model performance
- know how to diagnose sources of model error
- be able to improve model performance

# Model performance vs. realism

Models should reflect real world processes as exactly as possible to ensure high predictive power of a chosen model.

Conceptual models rely on spatially and temporally averaged inputs, effective parameters and calibration.

Frequently the model performance is wrongly inferred from the ability of the model to mimic the observed variable during calibration.

→ Reduces selection of best parameter set to curve fitting.

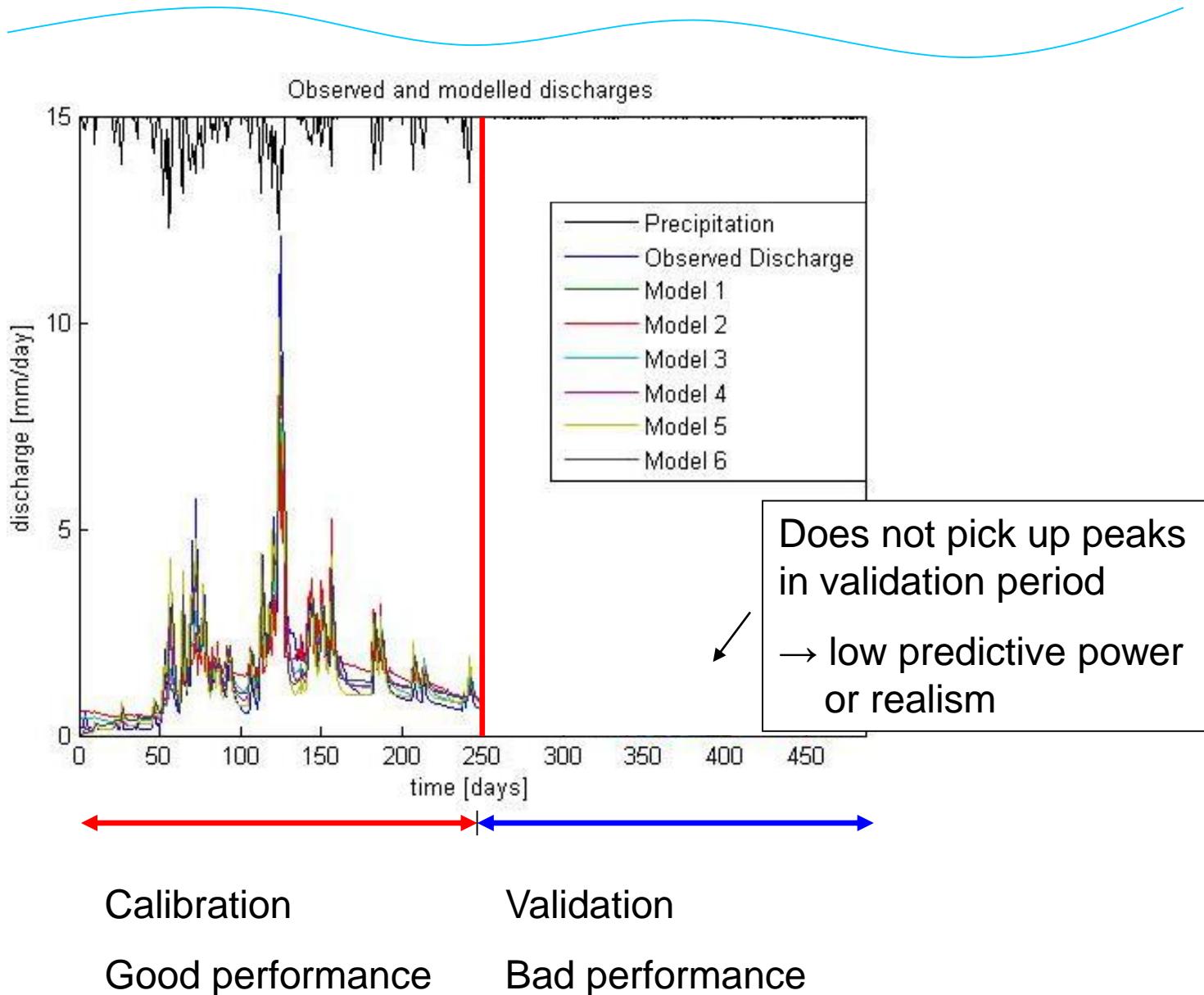
This can result in considerably reduced performance in independent test periods (i.e. validation periods): the high degrees of freedom of a typical conceptual model can produce excellent fits with unsuitable parameter sets: “Crap in, crap out models”

→ Parameters sets with reduced performance can result in higher predictive power!

→ Model performance should be evaluated according to reality checks and assessment of performance during validation periods

→ **“model realism”**

# Model performance vs. realism example



# Steps towards a useful model

- 
- (1) Screening and cleaning of data
  - (2) Choice of appropriate interpolation methods for input data
  - (3) Choice of appropriate time-stepping of model (dictated by data and objective)
  - (4) Plausibility check of observed runoff data (rating curve!)
  - (5) Choice of an appropriate model spin-up period
  - (6) Choice of a plausible model structure based on perception of the system
  - (7) Choice of an appropriate numerical method to solve the water balance
  - (8) Choice of an appropriate model calibration method
  - (9) Choice of appropriate objective functions
  - (10) Testing (validation) of the model to infer most adequate parameterization

# Data screening

This is a bit of a no-brainer:

Check the available data for plausibility and obvious errors (e.g. temperature sensor shows -32°C in southern Spain during summer). Important when data come from different sources.

Where possible and appropriate close gaps in the input data series using an adequate method, e.g.:

- Long term averages
- (Non-)Linear interpolation between previous and following available data points
- Spatial interpolation (with or without the use of spatial correlation features) if data from nearby climate stations are available.

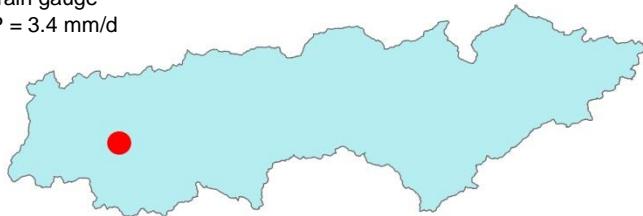
Gaps in stream flow observation do not have to be closed (only used for calibration!)

# Uncertainty in observed precipitation

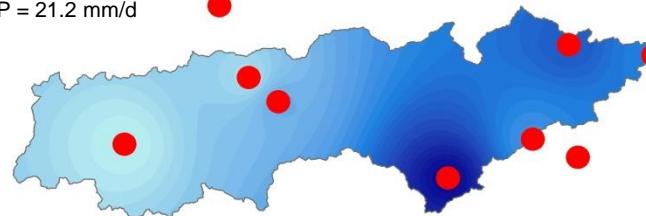
## One individual storm event



1 rain gauge  
 $P = 3.4 \text{ mm/d}$



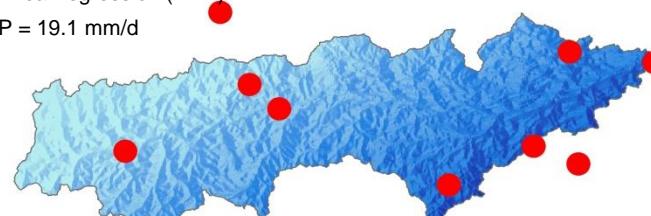
Inverse distance weight (IDW)  
 $P = 21.2 \text{ mm/d}$



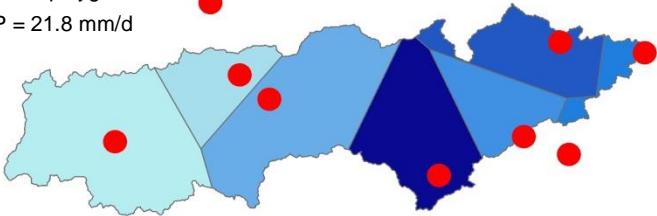
1 alternative rain gauge  
 $P = 29.2 \text{ mm/d}$



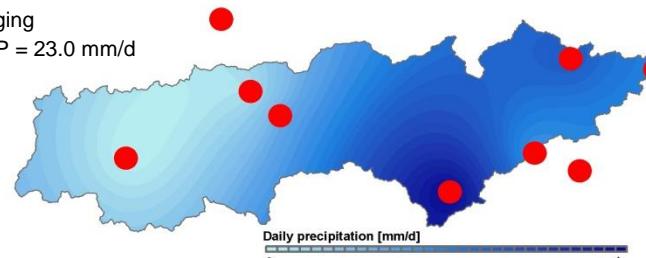
Multiple linear regression (MLR)  
 $P = 19.1 \text{ mm/d}$



Thiessen polygons  
 $P = 21.8 \text{ mm/d}$



Kriging  
 $P = 23.0 \text{ mm/d}$



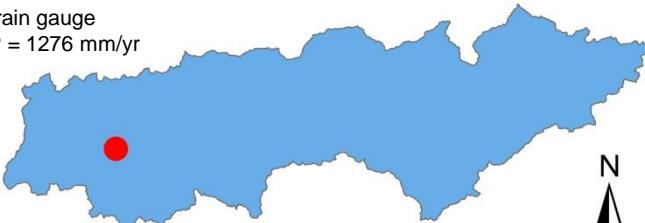
0 25 50 km

Daily precipitation [mm/d]

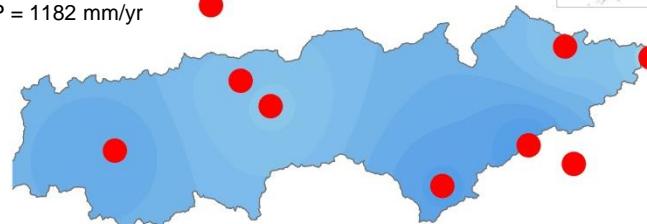
# Uncertainty in observed precipitation

## Long annual average precipitation

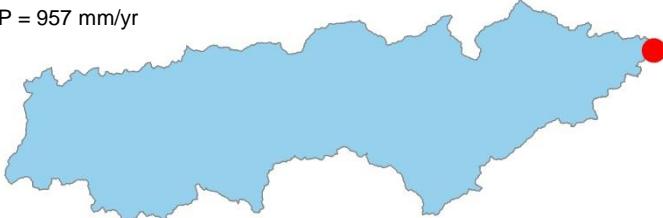
1 rain gauge  
 $P = 1276 \text{ mm/yr}$



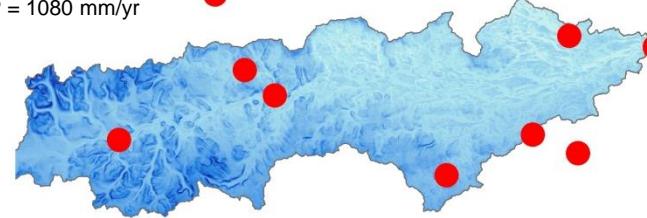
Inverse distance weight (IDW)  
 $P = 1182 \text{ mm/yr}$



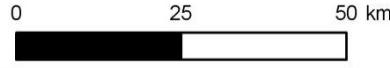
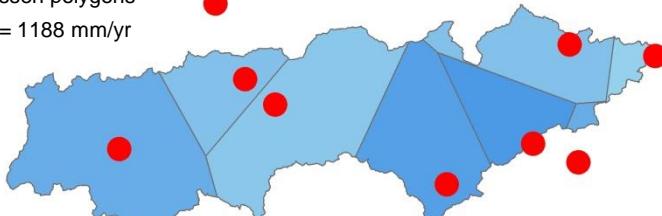
1 alternative rain gauge  
 $P = 957 \text{ mm/yr}$



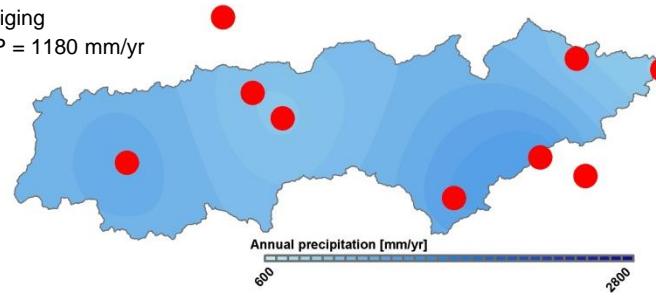
Multiple linear regression (MLR)  
 $P = 1080 \text{ mm/yr}$



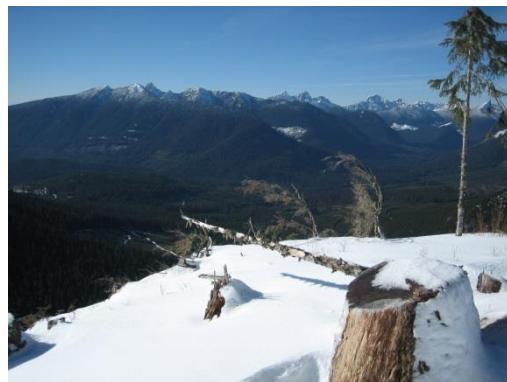
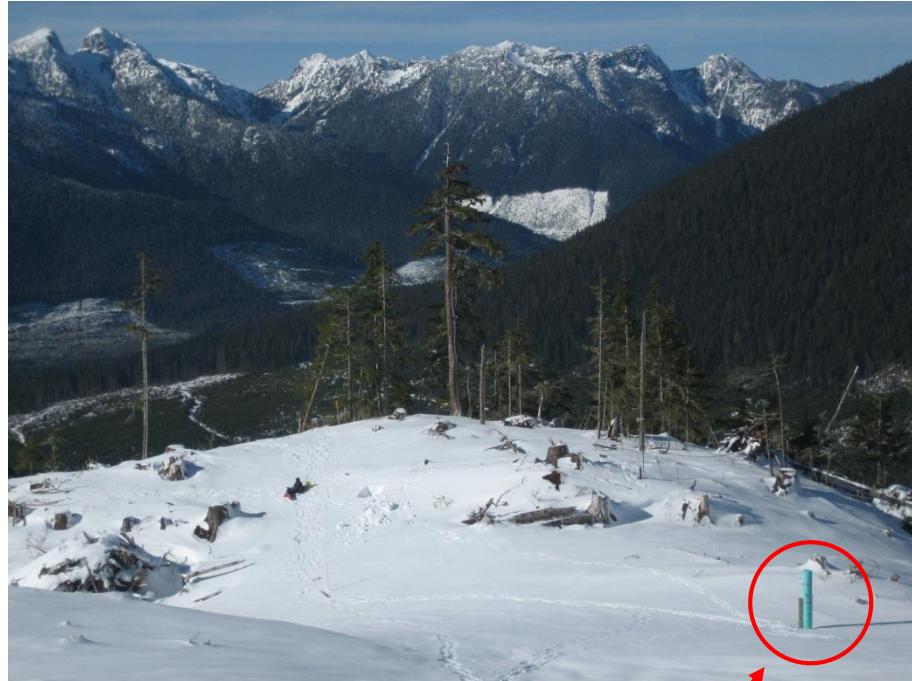
Thiessen polygons  
 $P = 1188 \text{ mm/yr}$



Kriging  
 $P = 1180 \text{ mm/yr}$



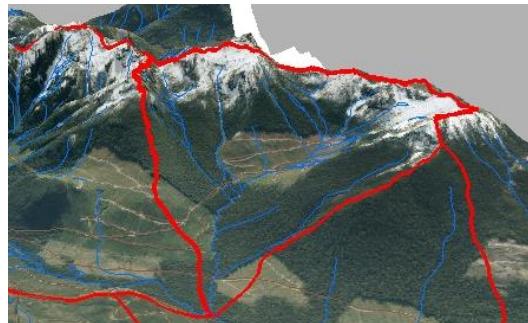
# Precipitation uncertainty



BAD location!  
No snow measured,  
but.....



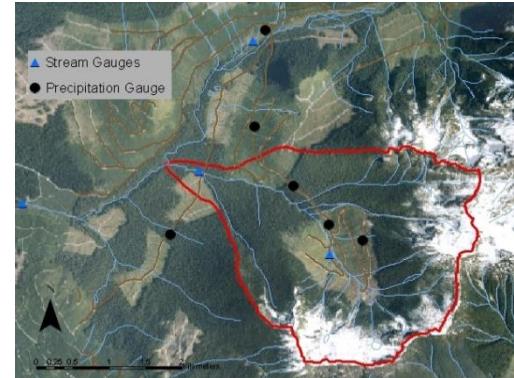
# Precipitation uncertainty – case study



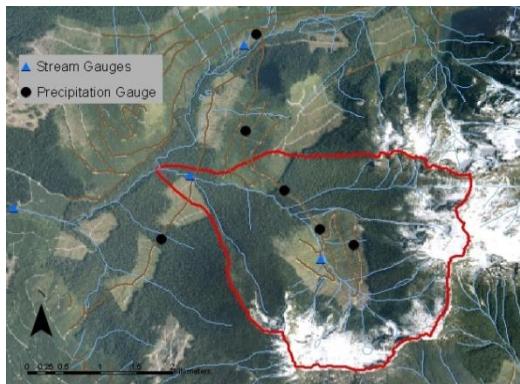
## Stephanie Creek experimental catchment

Coastal British Columbia ( $8 \text{ km}^2$ ), highly dynamic meteorological conditions, pronounced relief, 2000mm/yr

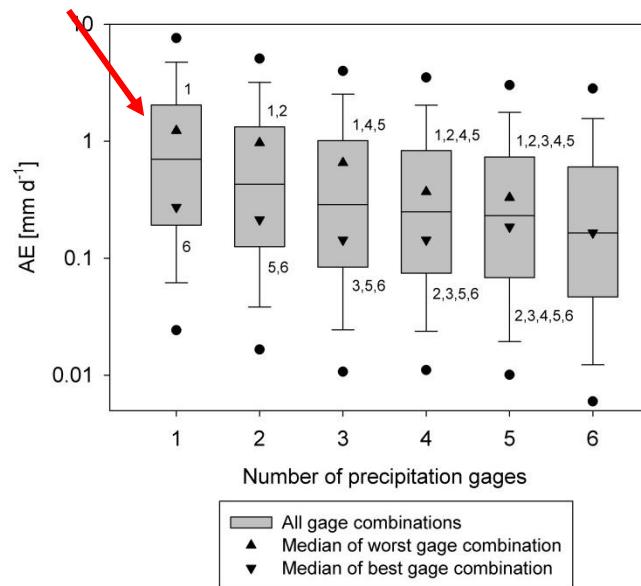
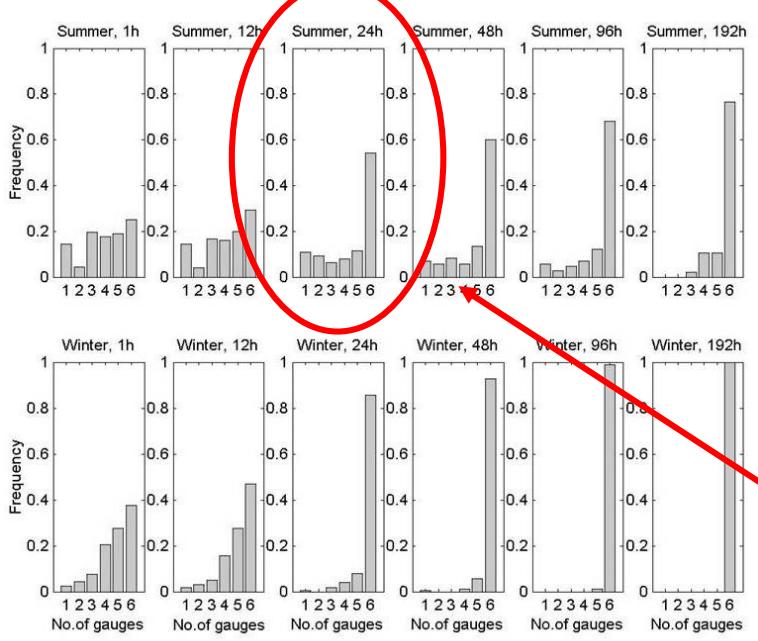
Study on the effect of climate station network design on average catchment precipitation estimates



# Precipitation uncertainty – case study



Deviation from best estimates increases with lower number of gauges. Mean deviation for single gauges ~700 mm/yr or 40%!!



In more than 40% of the rain events (summer), not all gauges recorded rain within 24h.

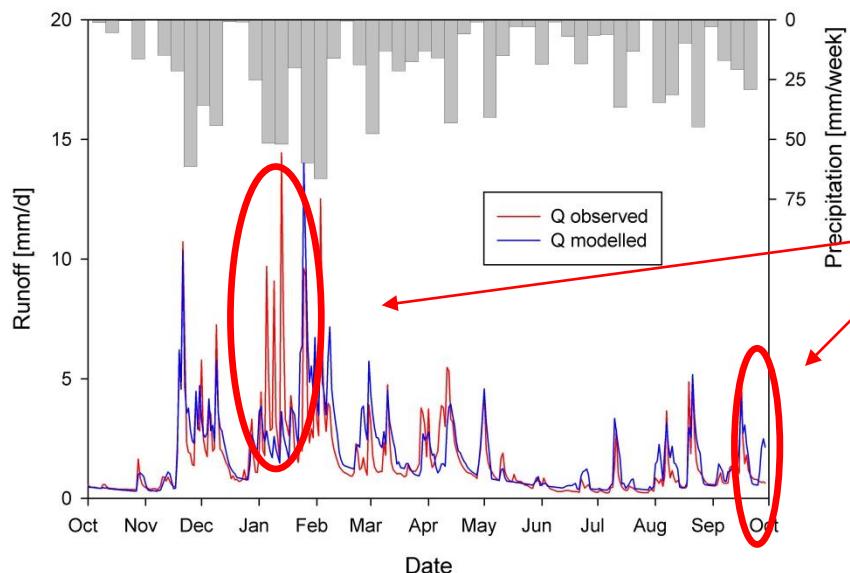
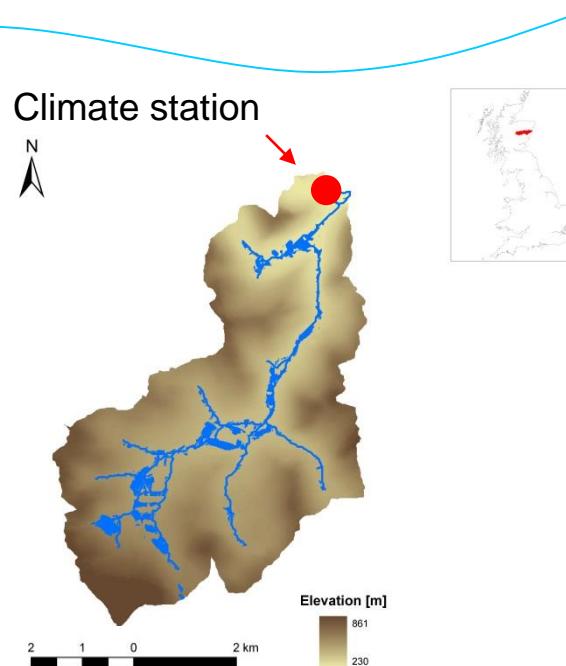
In 10% of the events, only ONE gauge recorded rain, even in this small catchment ( $8\text{ km}^2$ )!!

# Precipitation uncertainty – effect on model

## Girnock Burn experimental catchment

Cairngorm Mountains, Scotland ( $\sim 30 \text{ km}^2$ ),  
one(!) climate station, 1100mm/yr

Several models (5 – 12 parameters),  
NSE  $\sim 0.7$ , NSE-log  $\sim 0.85$



# Precipitation uncertainty – effect on model

## Girnock Burn experimental catchment

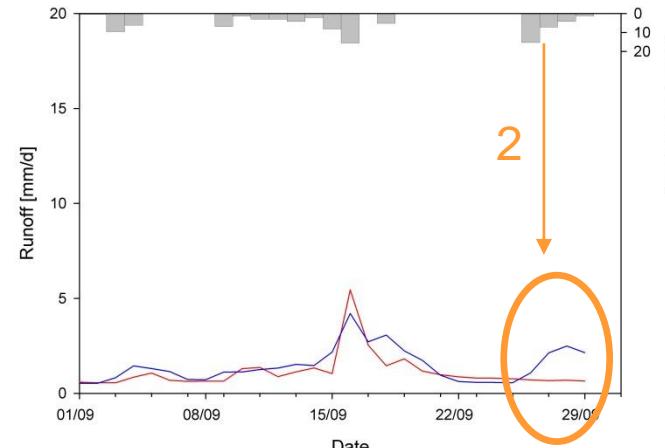
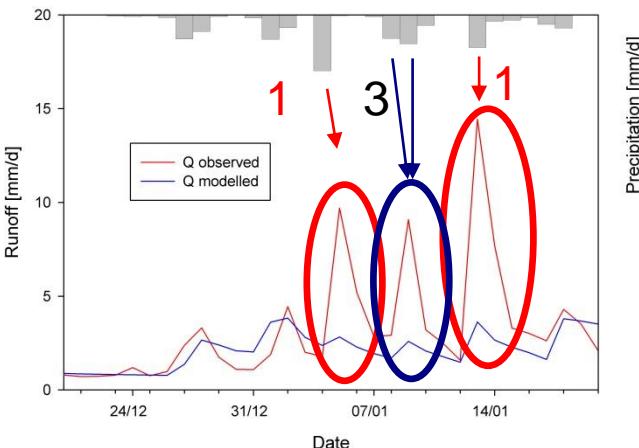
Several different types of potential errors can be identified in these two short periods:



- 1 – Recorded precipitation amount is too low → Q is underestimated
- 2 – Recorded precipitation amount is too high → Q is overestimated

Not only related to the number or position of gauges:

- 3 – Recorded precipitation amount is either too low or rain from the preceding time step t-1 should count towards the peak at t → Q is underestimated



# Temporal resolution of data

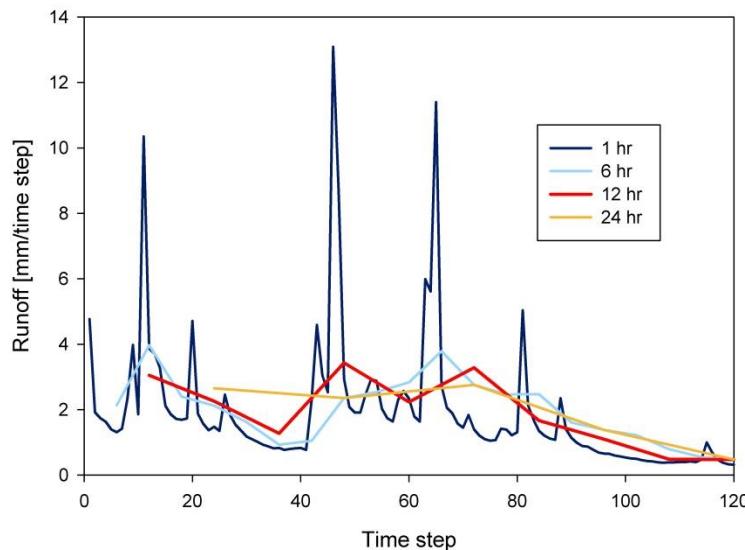
Observation data resolution and discretization

Problem: continuous processes in nature need to be discretized.

Or in other words: observation technology does not allow us to continuously record variables of interest → everything we are observing (e.g. rain, stream flow,...) is averaged over the observation time interval and likely to be subject to a time lag.

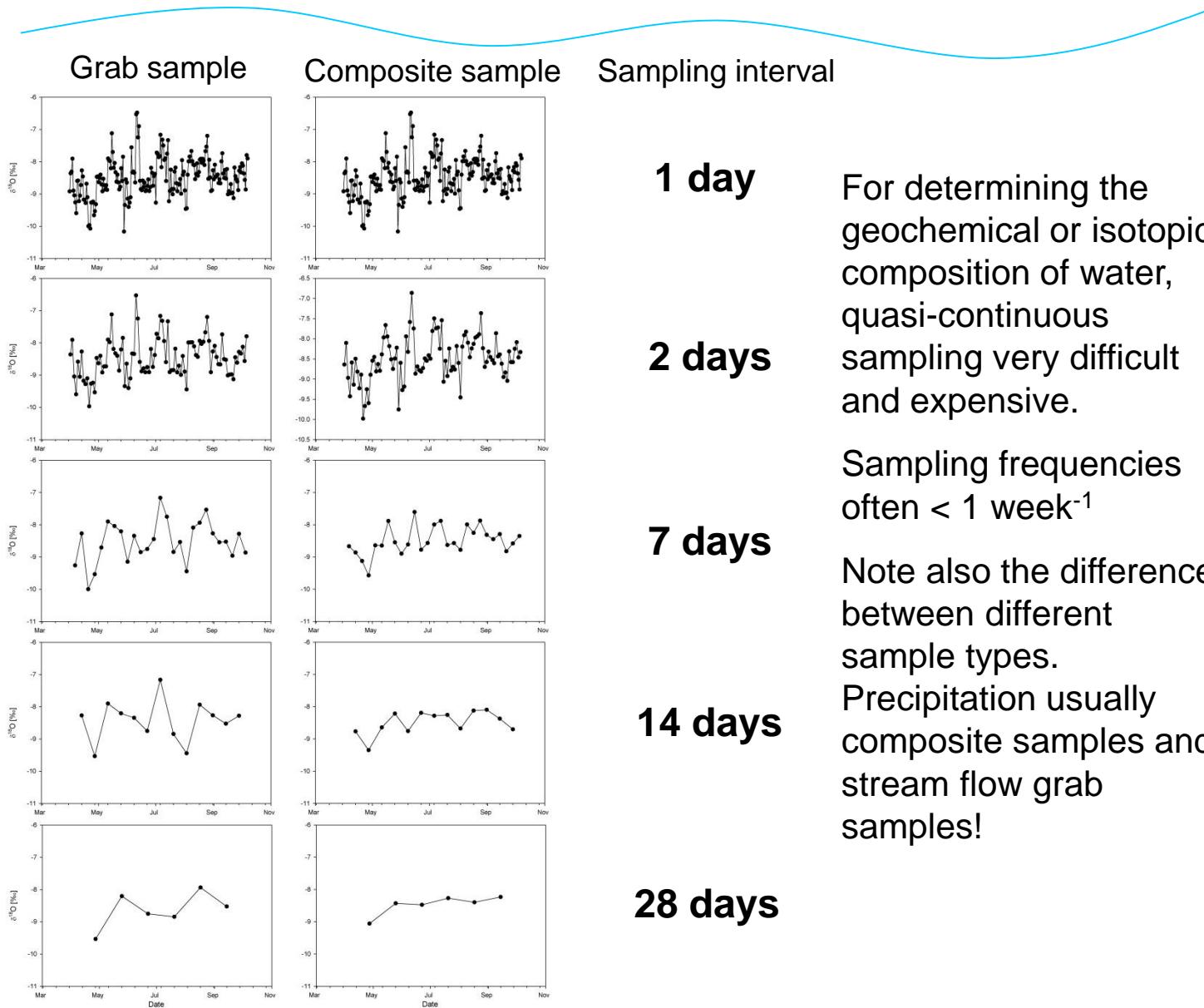
Commercial data loggers can record stream flow with a frequency  $\leq 1 \text{ second}^{-1}$  (in theory!!) and rainfall  $\leq 1 \text{ minute}^{-1}$  (in theory!!).

In reality observation frequencies between  $1 \text{ hr}^{-1}$  and  $1 \text{ day}^{-1}$  are common.

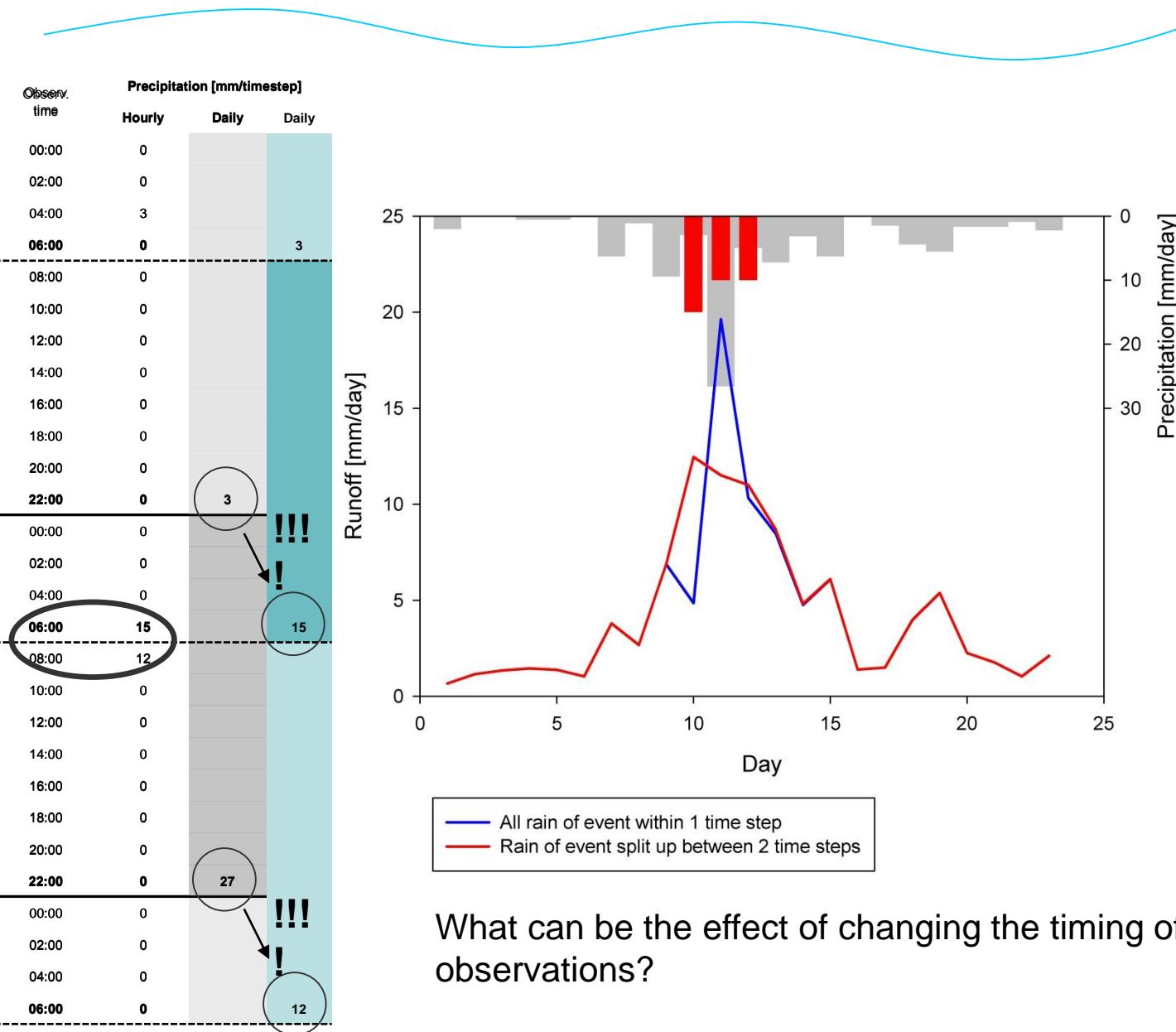


Where only observation frequencies  $\leq 1 \text{ day}^{-1}$  are available → problematic for peak flow estimates and design values

# Temporal resolution of data and sample type



# Timing of observations



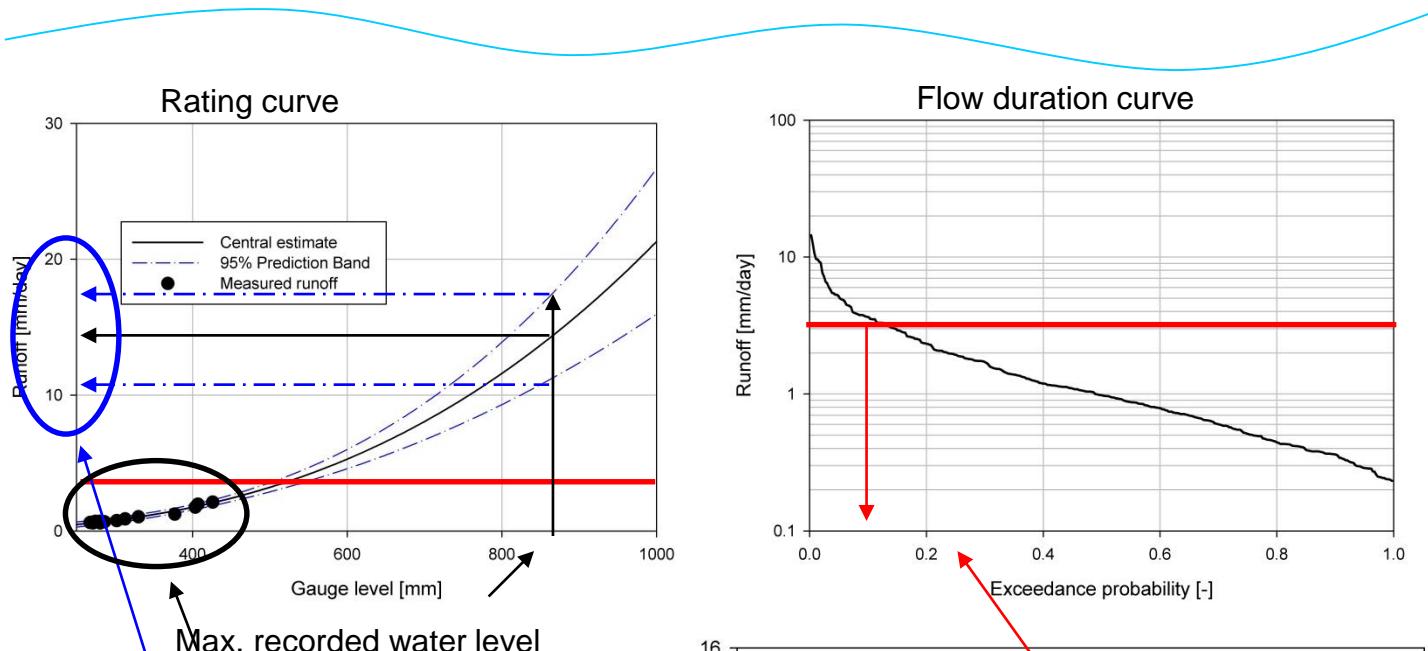
# How to reduce errors from data



## **Attention!**

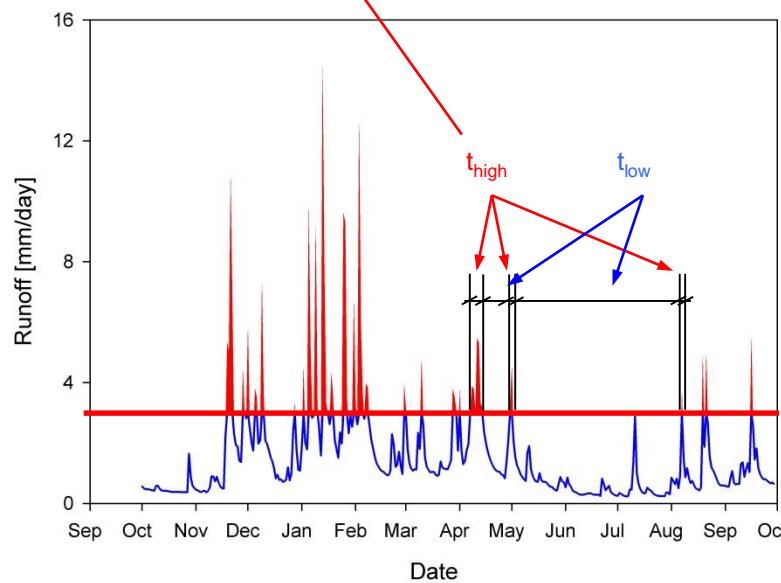
- Be consistent in the use of rain gauges for extrapolation
- Adjust extrapolation method to data available
- Adjust extrapolation method to the objective of the research and to its spatio-temporal scale (e.g. peak flows, groundwater body,...)
- Be careful when using data from different sources
- Be careful if there is a change in the person responsible for operating field equipment
- Be careful if there is a change in the sensors and loggers
- Be careful if there is a change in observation frequency
- Be careful if there is a change in sample type

# Uncertainty in runoff observation

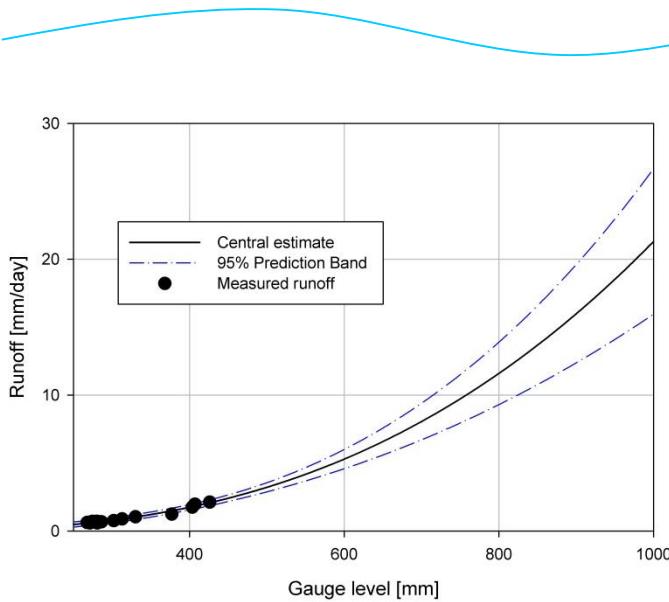


Reasons: Biased runoff –

- biased towards low flow!
- Too few high flow measurements
- Uncertainty in runoff measurement (i.e. wide confidence interval)
  - problematic for extrapolation of high flows

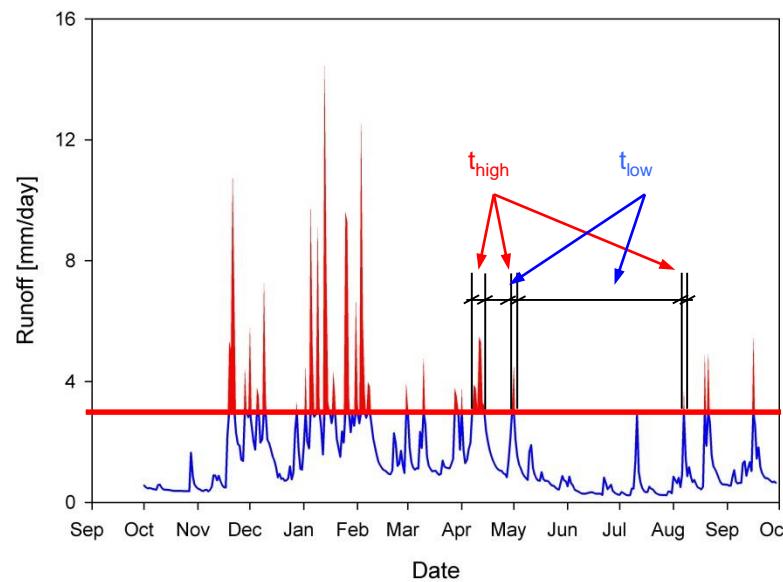


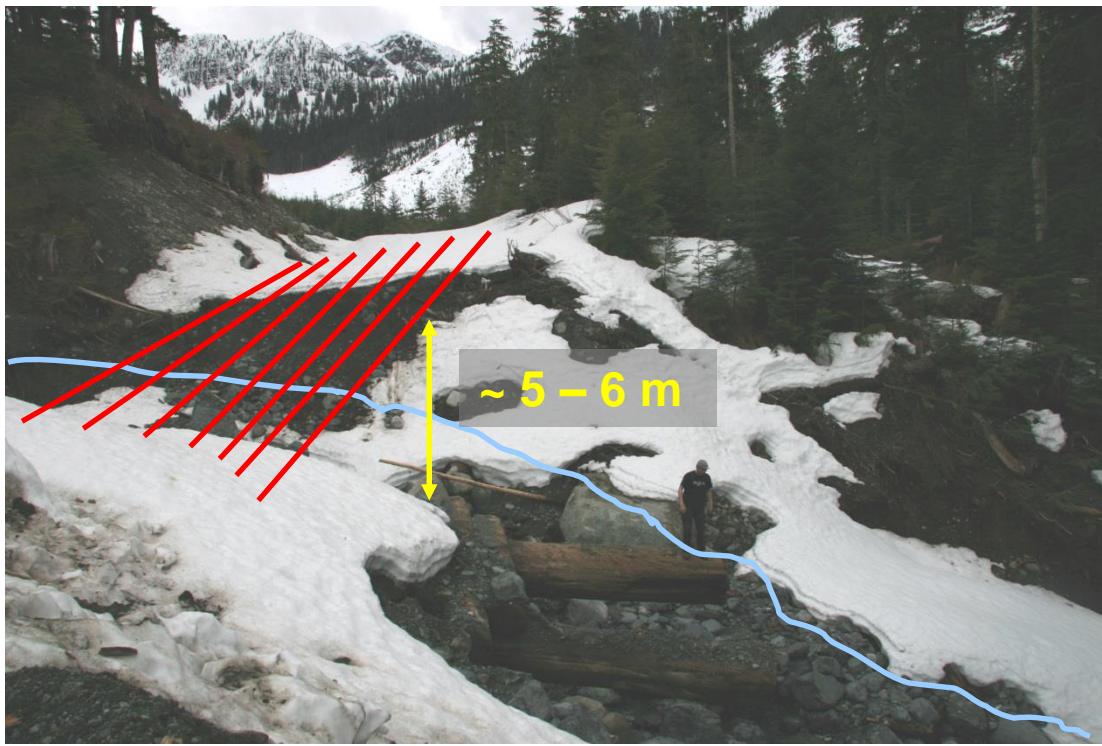
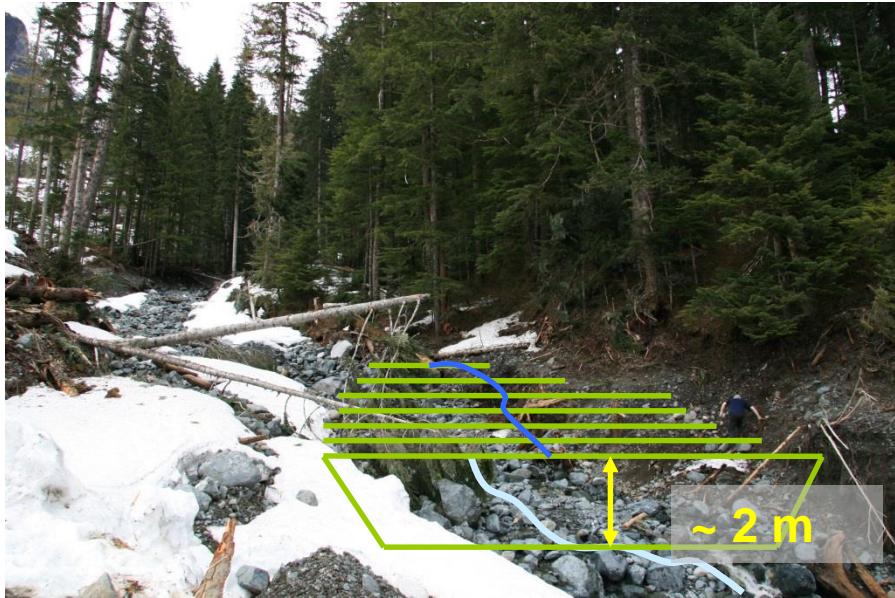
# Uncertainty in runoff observation



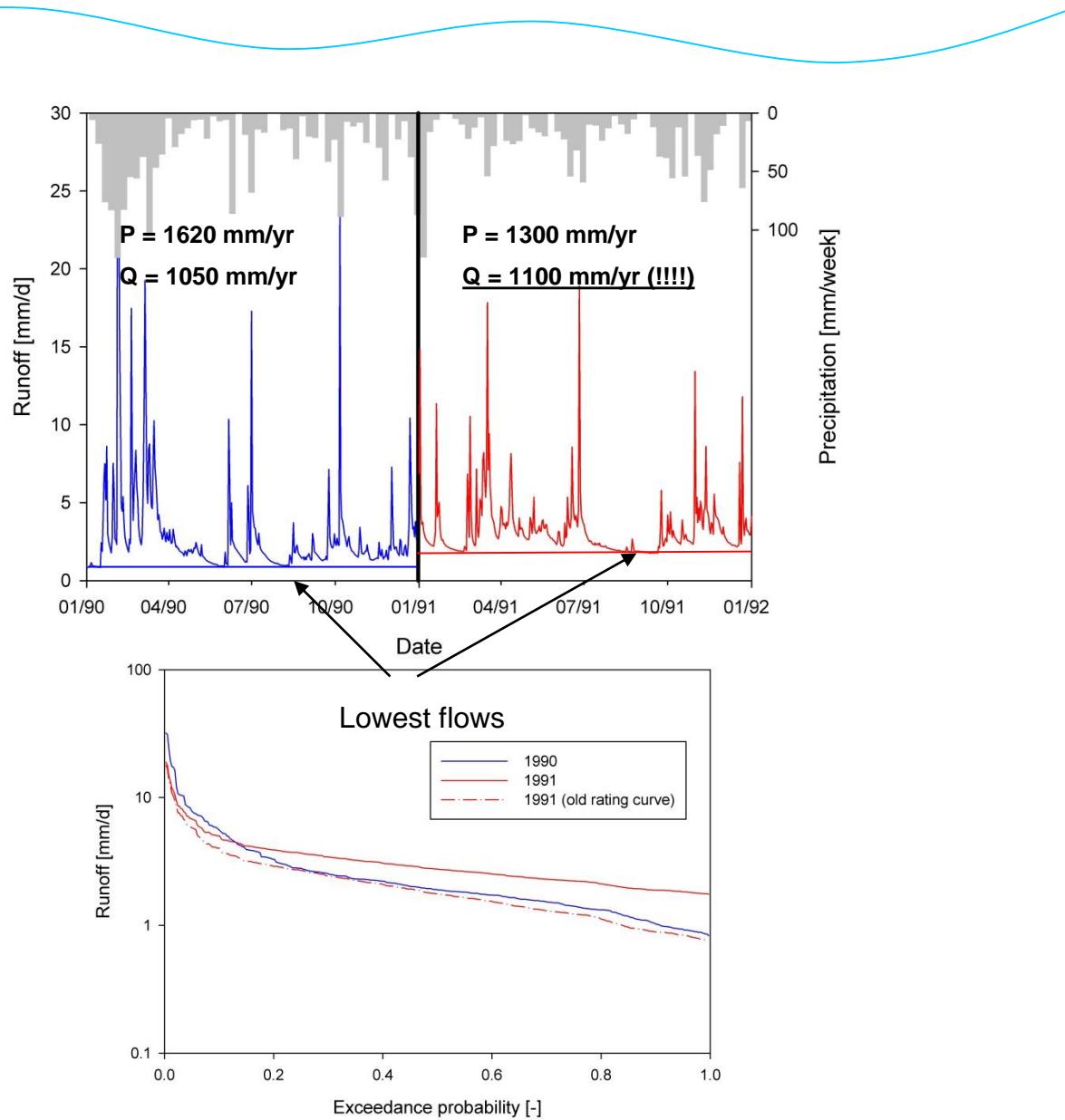
## Other reasons:

- Gradual or instantaneous change of stream cross section by bedload redistribution, river bank erosion or debris caused obstruction

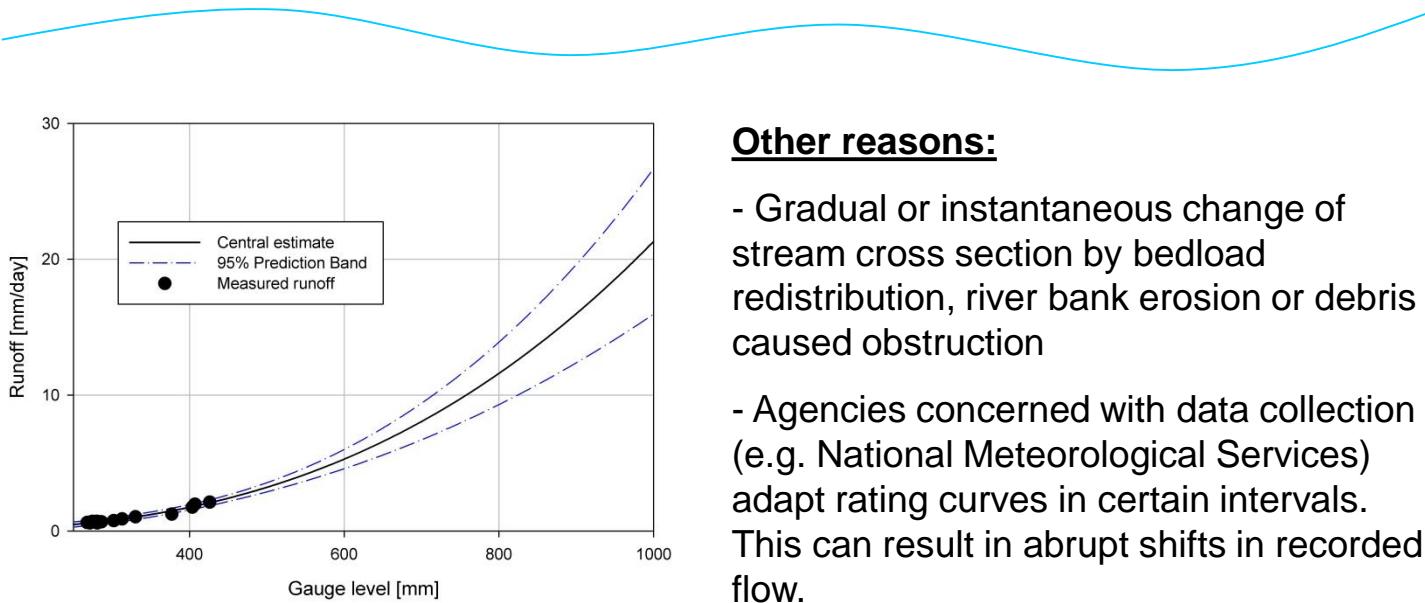




# Uncertainty in runoff observation



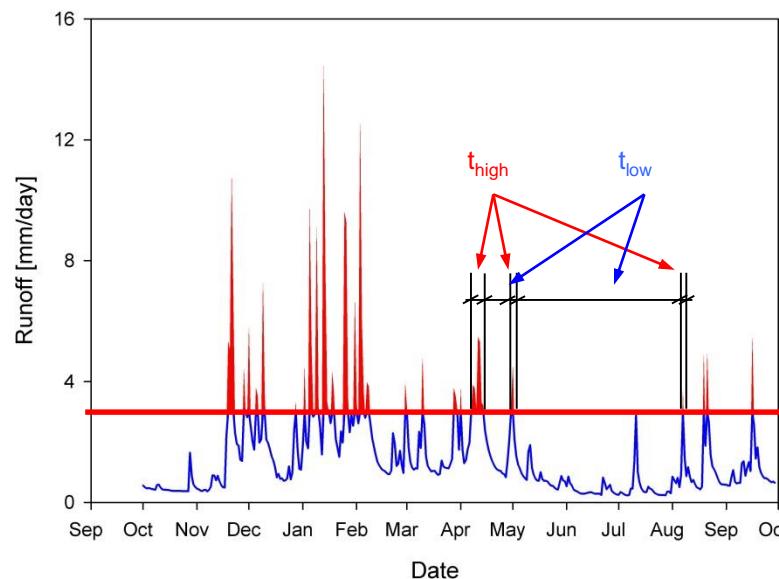
# Uncertainty in runoff observation



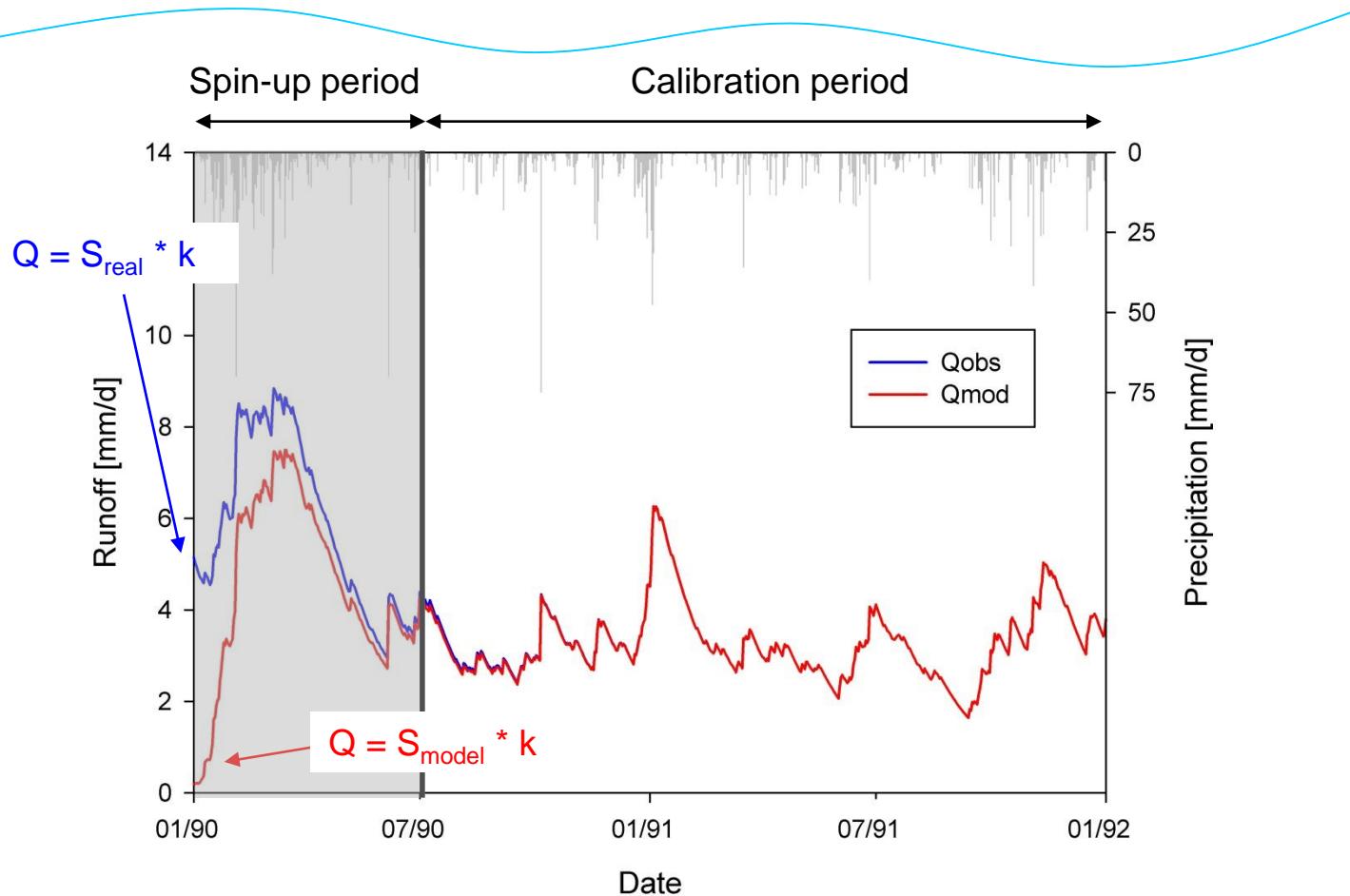
## Other reasons:

- Gradual or instantaneous change of stream cross section by bedload redistribution, river bank erosion or debris caused obstruction
- Agencies concerned with data collection (e.g. National Meteorological Services) adapt rating curves in certain intervals. This can result in abrupt shifts in recorded flow.

- Unless fixed to a solid structure, water level sensors can be subject to movement (e.g. after maintenance, by bedload movement,...)
- Time averaging



# Model spin-up period

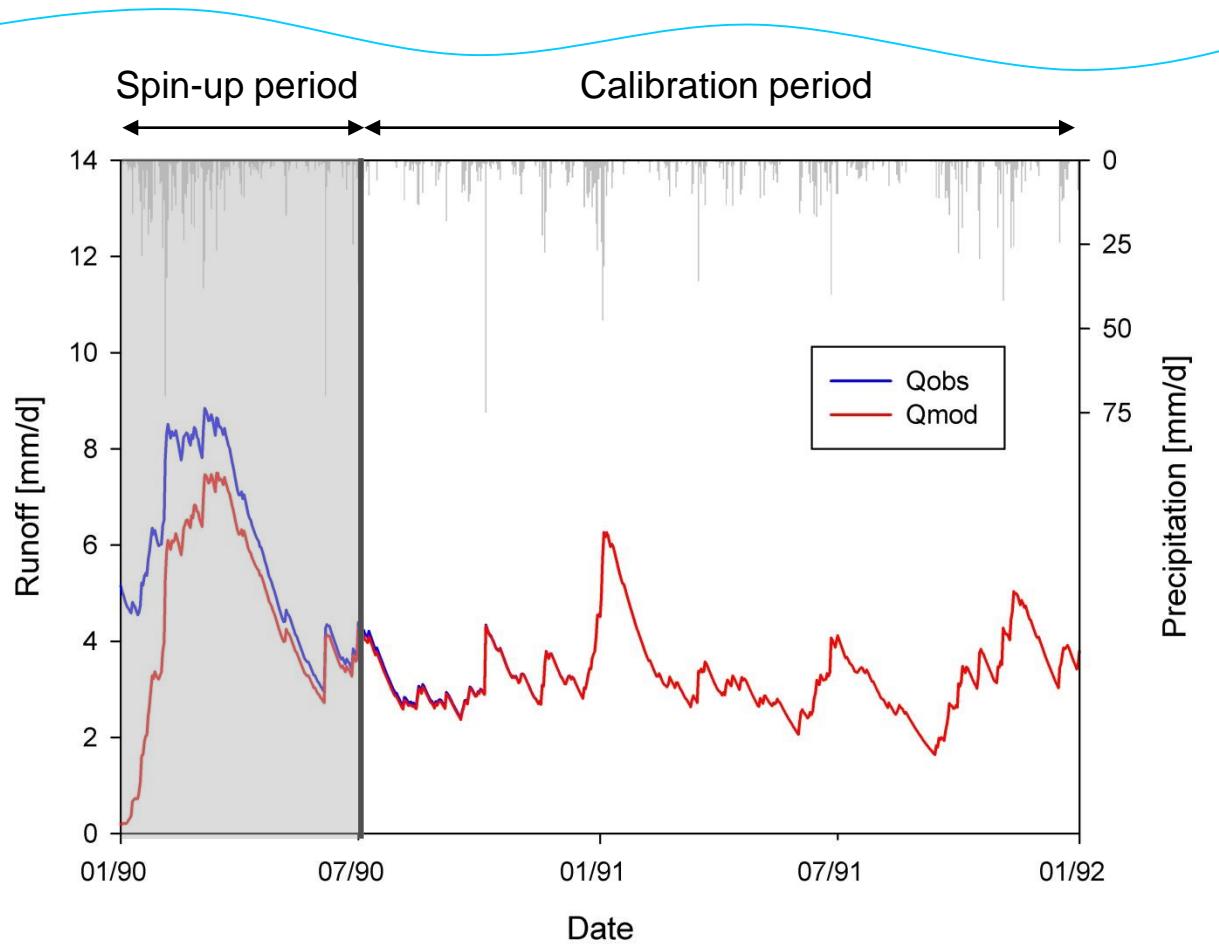


Simple linear reservoir:  $Q = S * k$

Initial condition  $S(0)$  is unknown and arbitrarily chosen, here:  $S(0) = 0$ .

Model needs certain period ("warm-up", "spin-up", "burn-in" period) to bring the system states to values reflecting real world processes, here: storage  $S$  needs to fill up to "real-world" level.

# Model spin-up period

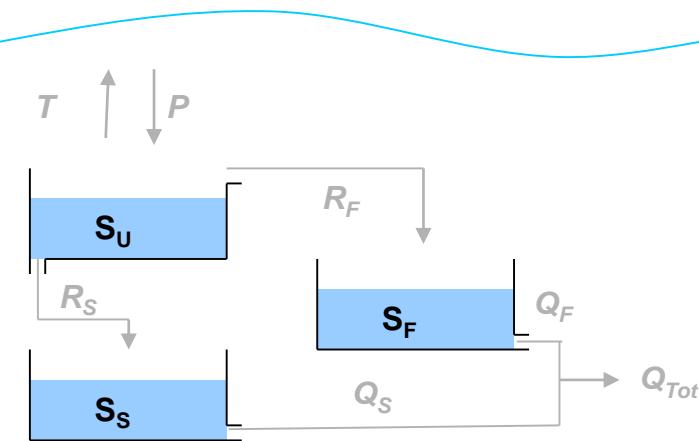


Spin-up period is not considered for calibration. Otherwise, model is forced to compensate for errors due to incorrect  $S(0)!!$

Length of spin-up period is dependent on the catchment but is typically 1 year.

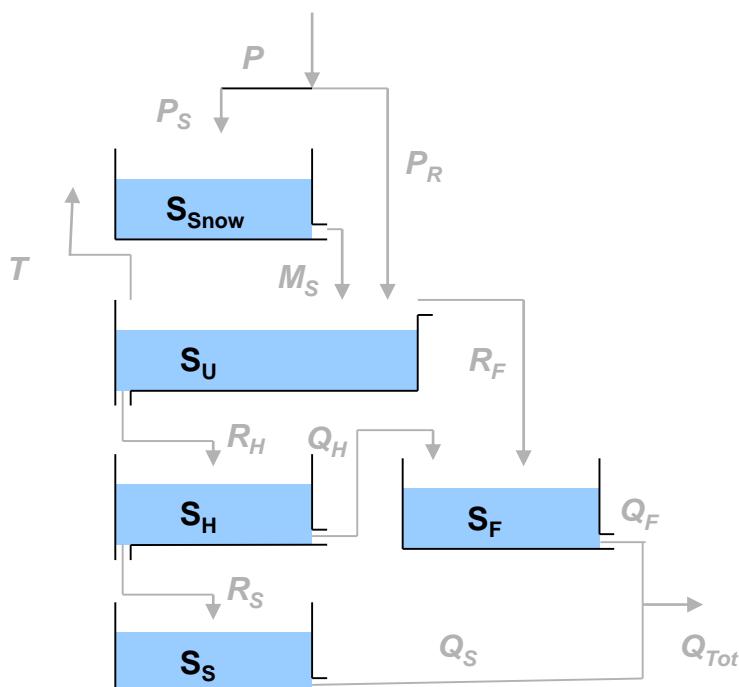
To reduce uncertainty, the calibration period should start in dry season, when  $S \sim 0$

# Model structure



## Model 1

5 Parameters,  
3 states  
(Unsaturated, fast, slow responding storage)

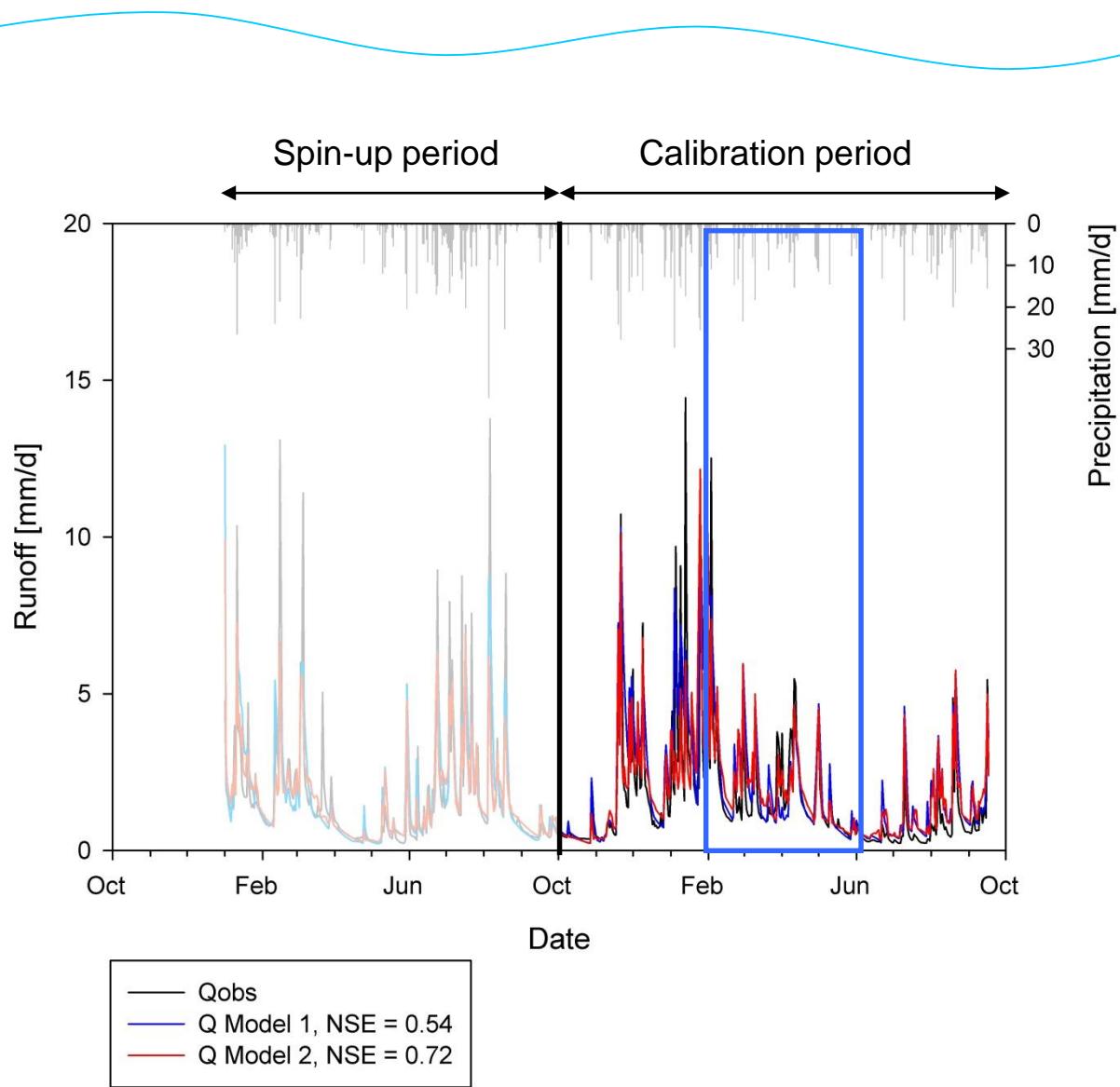


## Model 2

12 Parameters,  
5 states  
(Snow, unsaturated, hillslope, wetland and slow responding storage)

$P$  = precipitation,  $P_S$  = snow,  $P_R$  = rain,  $M_S$  = snow melt,  $T$  = transpiration,  $R_F$  = recharge of fast/wetland storage,  $R_S$  = recharge of slow storage,  $R_H$  = recharge of hillslope storage,  $Q_F$  = flow from fast/wetland storage,  $Q_S$  = Flow from slow storage,  $Q_H$  = flow from hillslope storage,  $Q_{Tot}$  = total runoff;  $S_{Snow}$  = snow storage,  $S_U$  = unsaturated storage,  $S_F$  = fast/wetland storage,  $S_S$  = Slow storage,  $S_H$  = hillslope storage

# Model structure



# Model selection

## Which model is now the “better” model??

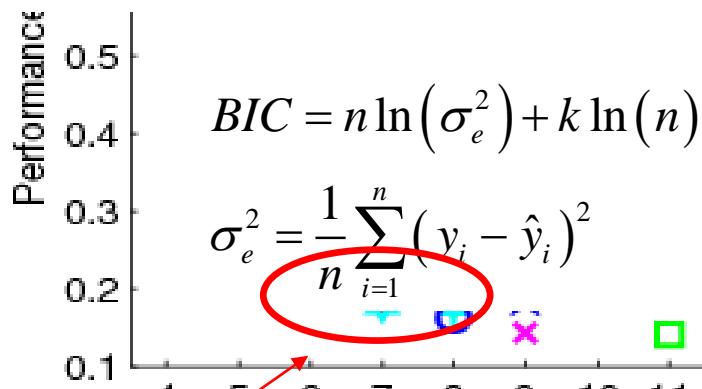
### Bayesian Information Criterion BIC

- Used for selecting the most adequate model among a finite set of models.
- It is a relative metric → Does not give information on the absolute performance of the model
- Most adequate model is the one with the lowest BIC

parameters = 1  
There is no reason to add more parameters

- (1) Check the number of active periods c
- (2) Do additional parameters yes, they

- (3) If testing against  $\mu$  ...  
Where  $n$  = sample size,  $k$  = number of parameters,  $\sigma_e^2$  = the error variance,  $y_i$  = observed data,  $\hat{y}_i$  = modeled output



Models in this region are likely to be the most

As a rule of thumb: if  $BIC_i - BIC_{min} > 5$  there is a difference in the performance of the models

mance (NSE = 0.54) but might be snow storage and melt (!) parameters more.

because more

help in the decision:  
hen certain components for the hydrograph in this e significant  
parameter identifiability? If m climates)

- (5) Independently test the model (e.g. split sample test → validation)

# Numerical implementation

Hydrological models are sets of coupled differential equations of the form

$$\frac{dS(t)}{dt} = f_s(S(t), F(t) | \theta)$$

$$Q(t) = f_Q(S(t), F(t) | \theta)$$

where S = states, F = forcings,  $\theta$  = parameter set, Q = output

Consider a simple linear reservoir:

In the special case of  $F = 0$  (i.e. no precipitation, evaporation or other gains or losses) the system can be solved analytically

$$\frac{dS}{dt} = -Q \quad \text{Rearranging: } \frac{dS}{dt} = -\frac{S}{k}$$

$$Q = \frac{S}{k} \quad \frac{dS}{S} = -\frac{1}{k} dt$$

$$\ln(S) = -\frac{1}{k}t + C$$

$$S = e^{-\frac{t}{k}+C}$$

$$S = e^{-\frac{t}{k}} e^C \quad \text{with } e^C = S_0$$

$$S(t) = S_0 e^{-\frac{t}{k}}$$

$$\text{Rearranging and substituting: } S = Qk$$

$$Qk = S_0 e^{-\frac{t}{k}}$$

$$Q = \frac{S_0}{k} e^{-\frac{t}{k}}$$

$$Q(t) = Q_0 e^{-\frac{t}{k}}$$

# Numerical implementation

For the special case  $F = 0$ , there exists also an analytical solution for nonlinear reservoirs of the form

$$\frac{dS}{dt} = -Q$$
$$Q = \frac{S^\alpha}{k}$$
$$\longrightarrow S(t) = (-kt + k\alpha + S_0^{1-\alpha})^{-(\alpha-1)^{-1}}$$

where  $S$  = states,  $F$  = forcings,  $Q$  = output,  $k$  = timescale and  $\alpha$  = non-linearity parameter

However, generally  $F \neq 0$ , for which no analytical solution exists so far

$$\frac{dS}{dt} = P - E - Q$$
$$Q = \frac{S^\alpha}{k}$$
$$\longrightarrow$$

Numerical solutions must be applied:

- explicit methods
- implicit methods

# Explicit methods

Explicit methods compute the state of the system at a later time based on the state of the system at the present:

$$S(t + \Delta t) = F(S(t))$$

The simplest explicit method is the **forward Euler method**

$$\frac{dS}{dt} = -\frac{S(t)^\alpha}{k}$$

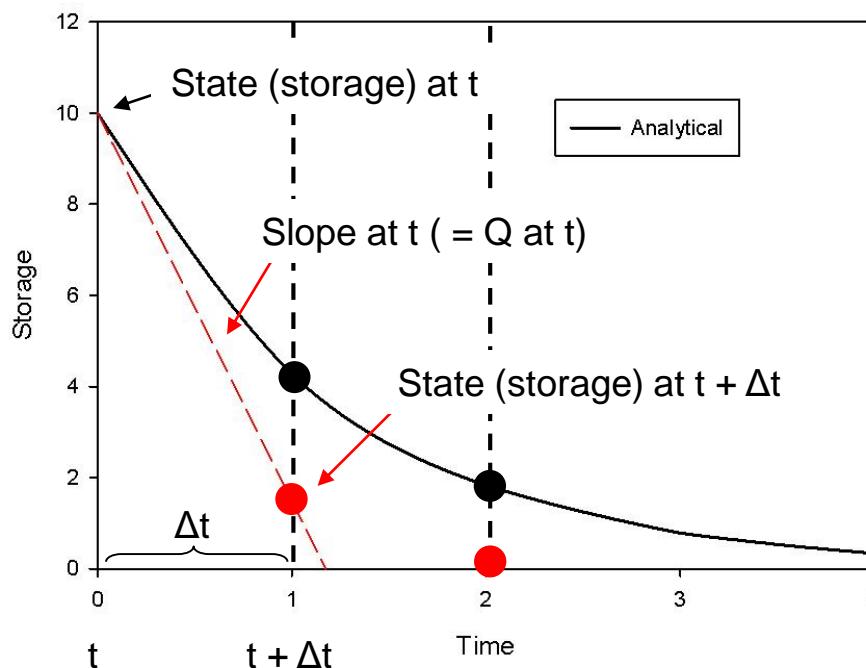
$$\frac{S(t + \Delta t) - S(t)}{\Delta t} = -\frac{S(t)^\alpha}{k}$$

$$S(t + \Delta t) = S(t) - \frac{S(t)^\alpha}{k} \Delta t$$

where  $S$  = states,  $t$  = time,  $k$  = timescale  
and  $\alpha$  = non-linearity parameter

+ can be computed with one iteration

- problematic for large time steps  
and/or steep gradients



# Explicit methods

Better results can generally be obtained by using sub-stepping methods, such as the **classic Runge-Kutta** scheme or RK4.

RK4 uses a weighed average of gradients to estimate the state at  $t + \Delta t$  instead of only the gradient at  $t$  as the forward Euler method does.

$$\frac{dS}{dt} = -\frac{S(t)^\alpha}{k}$$

$$S(t + \Delta t) = S(t) - \frac{1}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

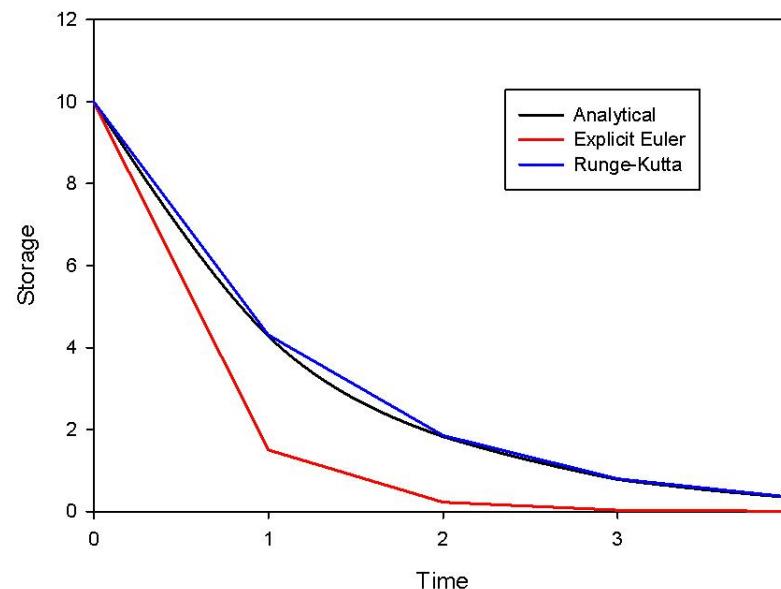
where  $S$  = states,  $t$  = time,  $k$  = timescale  
and  $\alpha$  = non-linearity parameter and

$$k_1 = -\frac{S(t)^\alpha}{k}$$

$$k_2 = S(t) - k_1 \frac{\Delta t}{2}$$

$$k_3 = S(t) - k_2 \frac{\Delta t}{2}$$

$$k_4 = S(t) - k_3 \Delta t$$



# Implicit methods

Implicit methods compute the state of the system at a later time based on the state of the system at the present AND the state of the system at a later time:

$$G(S(t), S(t + \Delta t)) = 0$$

The simplest implicit method is the **backward Euler method**

$$\frac{dS}{dt} = -\frac{S(t)^\alpha}{k}$$

$$\frac{S(t + \Delta t) - S(t)}{\Delta t} = -\frac{S(t + \Delta t)^\alpha}{k}$$

$$S(t + \Delta t)^\alpha \frac{\Delta t}{k} + S(t + \Delta t) - S(t) = 0$$

where S = states, t = time, k = timescale  
and  $\alpha$  = non-linearity parameter

- cannot be computed with one iteration and needs to be solved using root finding algorithms (e.g. Newton method)
- + better approximations
- + more stable

# Reduce parameter uncertainty

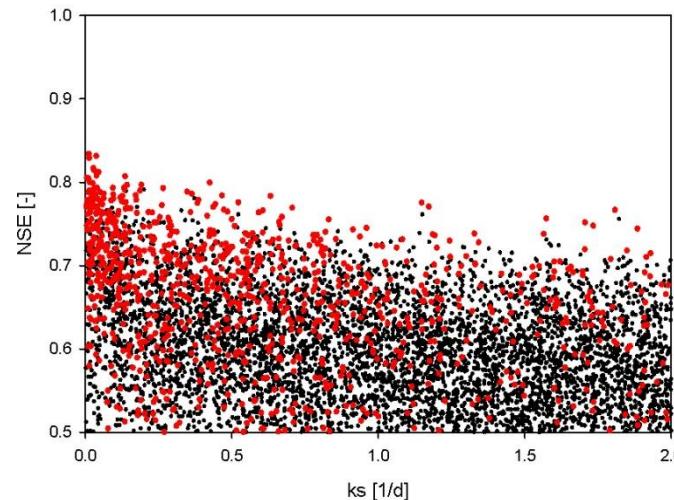
The choice of unsuitable parameters leads to prediction errors → low model realism

Parameter uncertainty is largely caused by:

- (1) Imperfect model structures → parameters compensate for errors
- (2) Overfitting of the model → too few constraints, i.e. too many degrees of freedom
- (3) Temporally changing parameter values, e.g. extent of saturated area

Way forward by increasing number of constraints:

- (1) Multi-objective calibration → more than one objective function
- (2) Multi-criteria calibration → more than one variable to be calibrated  
(e.g. stream flow and tracer concentration)



# Reduce parameter uncertainty

Example of the effects of combined multi-objective and multi-criteria calibration:

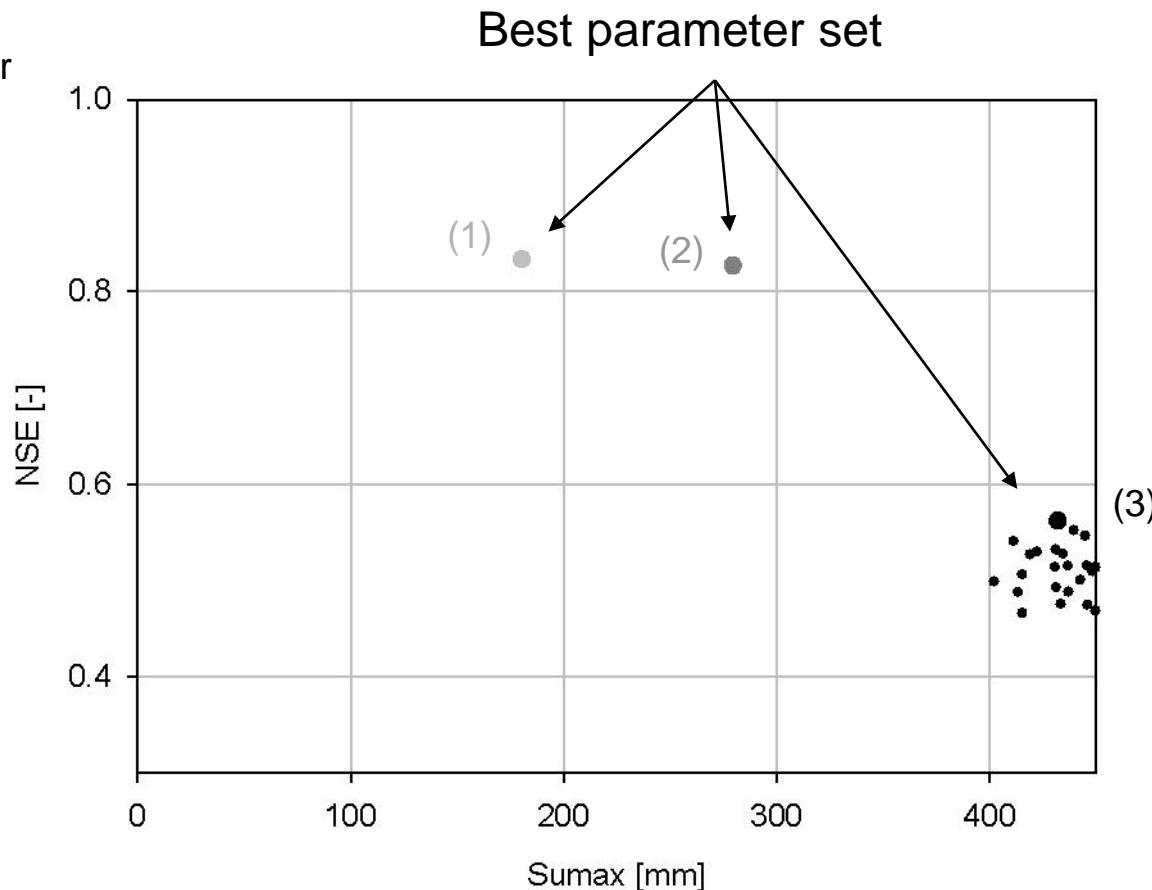
Model calibrated against (1) stream flow using NSE, (2) NSE of log flows and  
(3) NSE of tracer concentration in stream

Feasible parameter sets reduced from

(1) 5077

To (2) 3857

and (3) 24 (!!!)



# Reduce parameter uncertainty

Models should in general aim to predict stream flow with adequate accuracy.

High predictive power is strongly related to how well the model represents reality → model realism

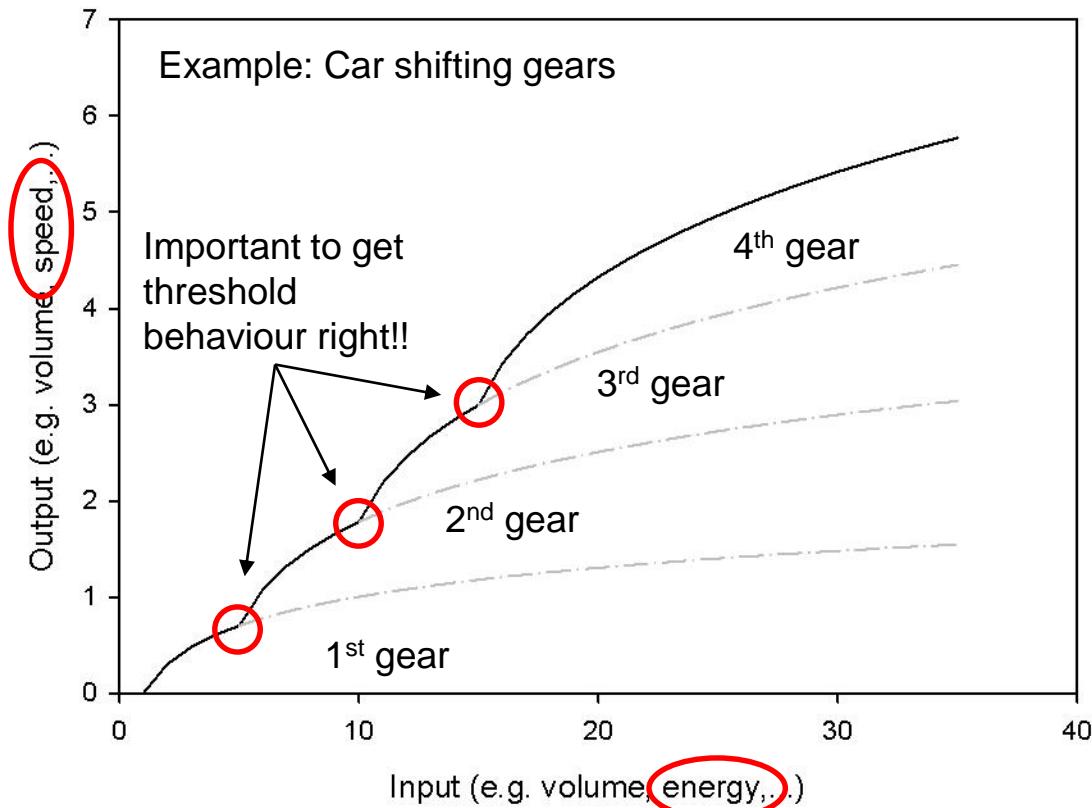
Best parameter set in calibration period not necessarily the most realistic parameter set → performance of parameters in independent test periods (“validation periods”) holds crucial information on model realism

Several strategies to include information from validation periods, e.g.:

- (1) Split sample test: train model using the first part of the available data (e.g. 50%) and then test the model with the remaining part. Frequently applied, very simple, however only limited additional information
- (2) Ordinary differential split sample test: calibrate the model on a dry period and validate it for a wet period, if the model is used to predict wet periods and the other way round if it is to be used for dry period.
- (3) Extended split and differential split sample tests: sequentially train the model on more than one calibration period and test it for the remaining period (e.g. calibrate year 1 - validate year two, calibrate year 2, validate year 1). Use the parameter sets that perform best during ALL calibration and validation periods.

# Feedback and thresholds

Modelling complex feedback systems can frequently result in surprising results as they are characterized by thresholds. The system response can thus tip from one regime to another with only VERY SMALL changes in the forcings and states (e.g. like horses switch gaits, cars switch gears or distinct storages in a hydrological system are activated and deactivated)



# Feedback and thresholds

Very simple example to illustrate how highly sensitive to changes in the initial system state a feedback system can be:

Verhulst population dynamics model

$$p_n = p_{n-1} + rp_{n-1}(1 - p_{n-1})$$

Where  $p_n$  = size of population as proportion of the maximal population supported by the system and  $r$  = growth rate

Case 1:

$$p_0 = 0.05, r = 3$$

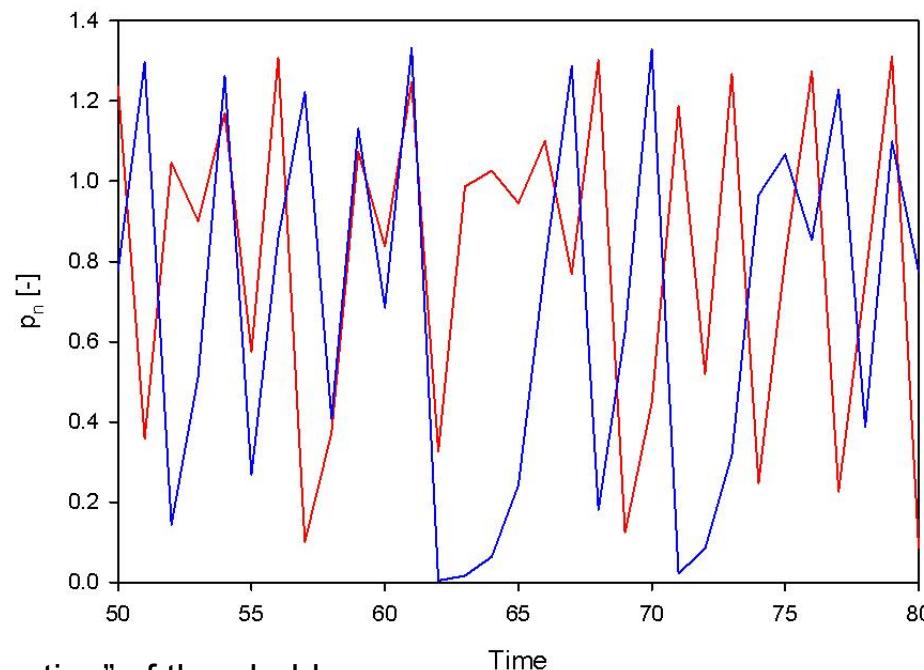
Case 2:

$$p_0 = 0.05 * 0.999999, r = 3$$

Case 3:

$$p_0 = 0.05, r = 3, \text{ but:}$$

$$p_n = (1+r)p_{n-1} - rp_{n-1}^2$$



→ Input, state of the system, “location” of thresholds, computational precision, etc. can strongly affect results!!!!

# Programming essentials



- (1) Prepare a concept and follow it
- (2) Insert as many comment lines as possible, describing in detail what you are doing and why
- (3) Put date and author in comment lines
- (4) Do not include system dependent items in the main code, but isolate these to make changes easier
- (5) Keep old lines as comment lines if you make changes to the code  
describe why you changed it
- (6) Test the code extensively, if possible let also others test it – “There is no code without a bug!”
- (7) Get your units right
- (8) Be accurate
- (9) Avoid rounding and truncation of numbers
- (10) Be careful if the results look “too” good! The better the results seem, the harder bugs are detected

The value of more efficiently  
extracting information from data



OR

Why bother to calibrate??



# Simplicity – Complexity - Information

## Where do we stand?

- There is need to balance process heterogeneity and model parsimony
- **Objective:** more realistic representations of the system
  - > Reduced uncertainty -> Increased predictive power
- Model *performance* vs. model *consistency*
- BUT: in most cases we do not have enough information to improve models!

**STOP!!**



**Is this really true??**

# Kerbernez Research Catchment

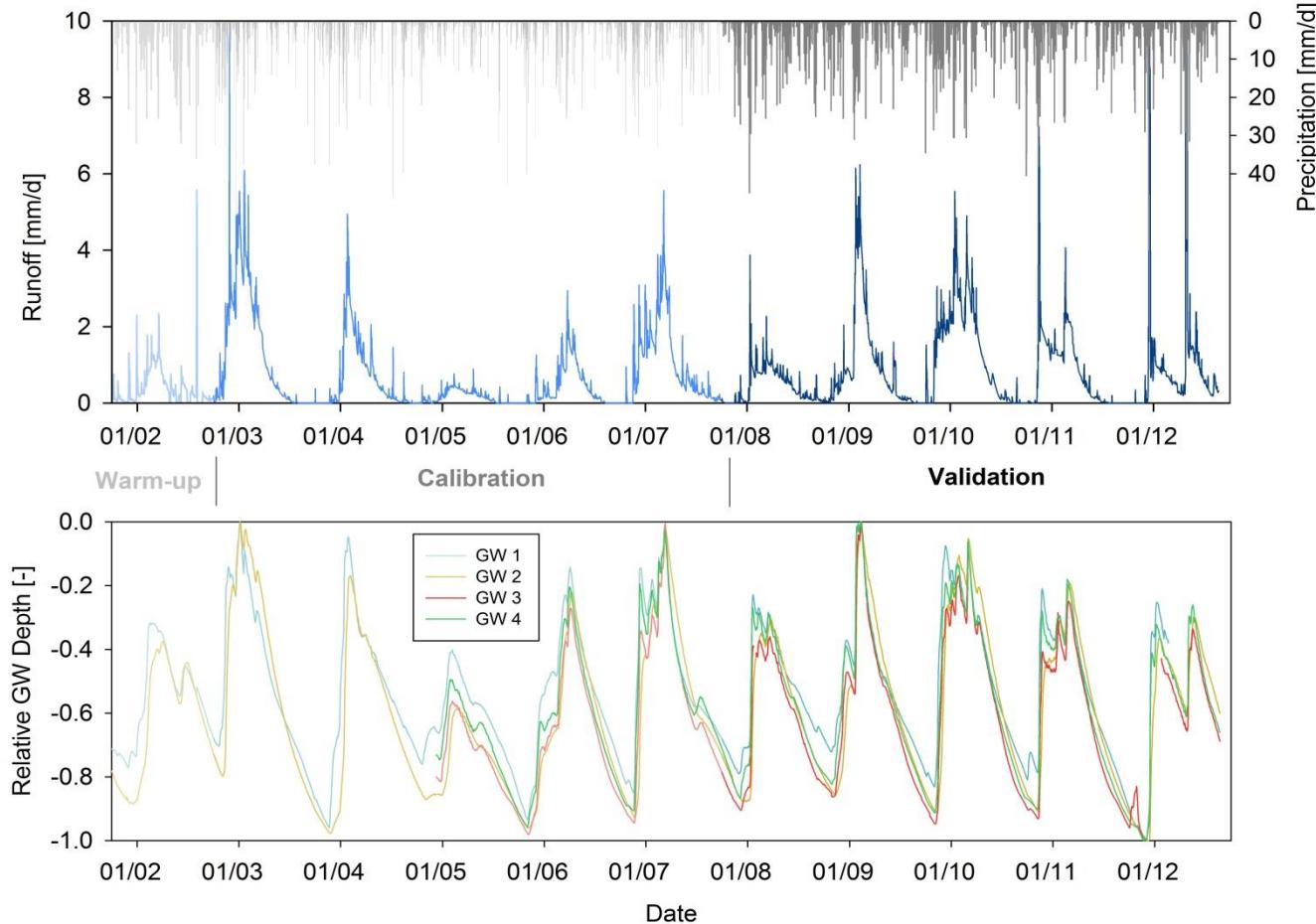
Small catchment in French Brittany

- Catchment area ~11ha
- Average precipitation 1100 mm/yr
- Average Penman Evaporation 700 mm/yr
- Deep, relatively free draining soils
- Underlain by weathered Granite
- Mainly grass- and cropland
- Agriculturally used
- First order, intermittent stream
- Long-term data record
- 5 Piezometers along 2 transects



# Kerbernez Research Catchment

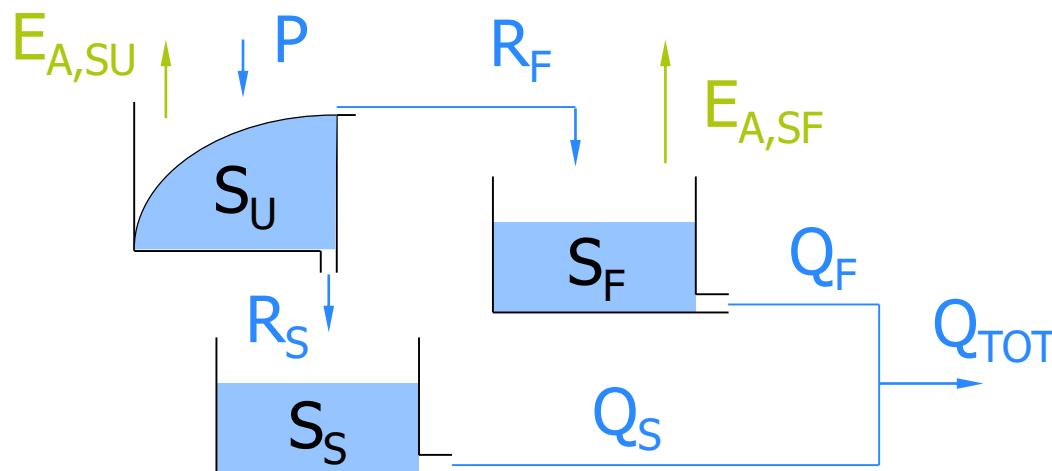
## Small catchment in French Brittany



# M1 - Benchmark Model

## Model 1

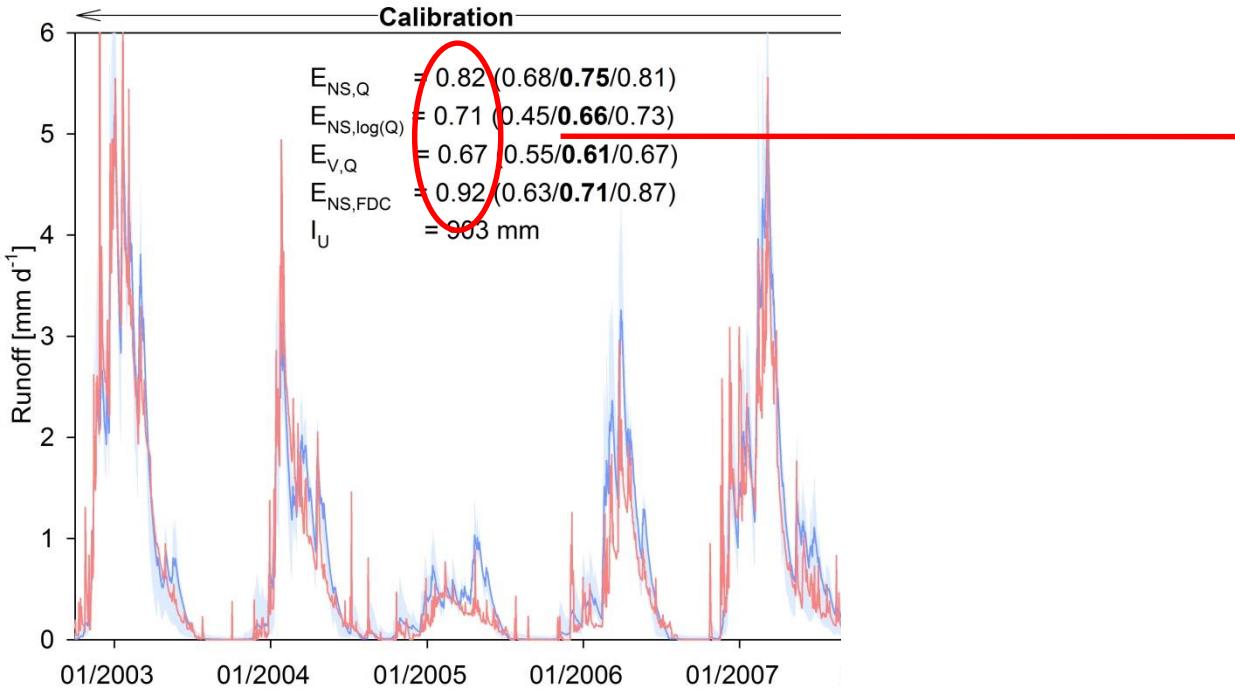
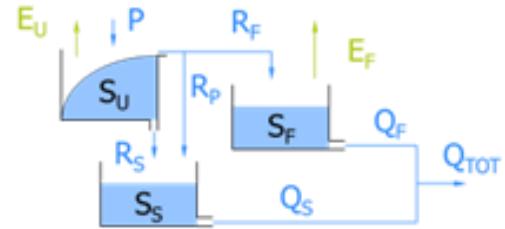
- Ordinary lumped, 3 box HBV-type model
- 6 free calibration parameters
- No constraints
- Multi-objective calibrations:  
NSE Q, NSE log(Q), VE Q and NSE FDC



# M1- Benchmark Model

## Model 1: 6 parameters, no constraints

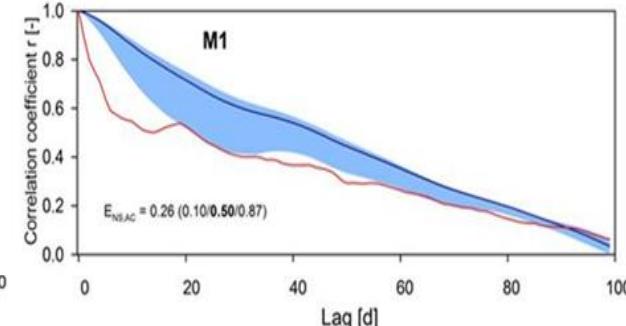
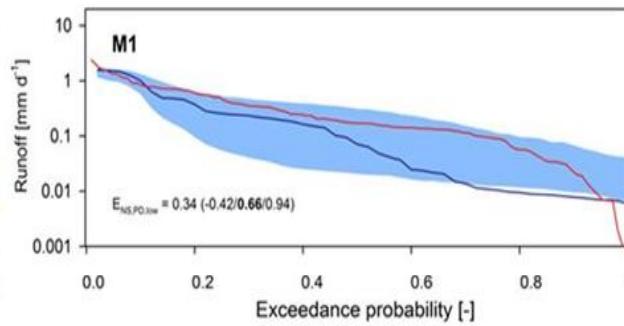
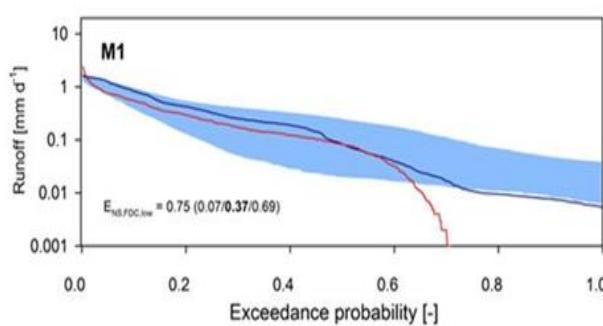
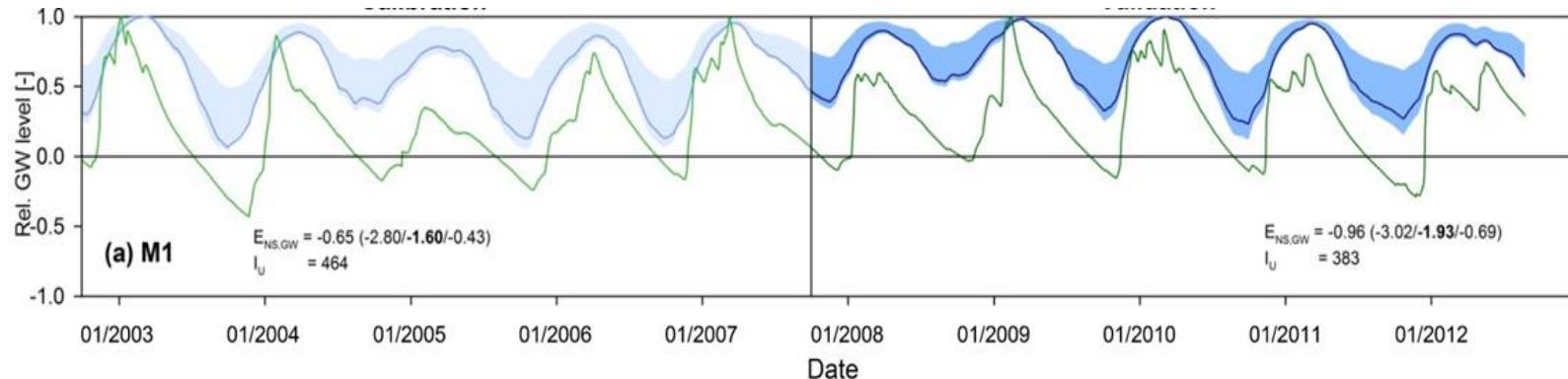
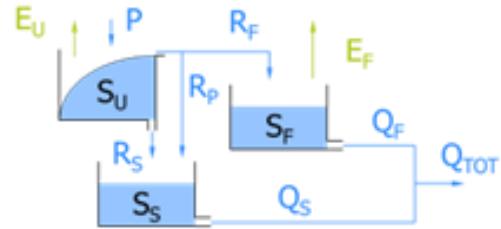
- Good calibration performance
- Well constrained by 4 objective functions
- ~~Yippie - We have a working model!!!~~
- **But: performance in validation decreased**



Hrachowitz et al., 2014, WRR

# M1- Benchmark Model

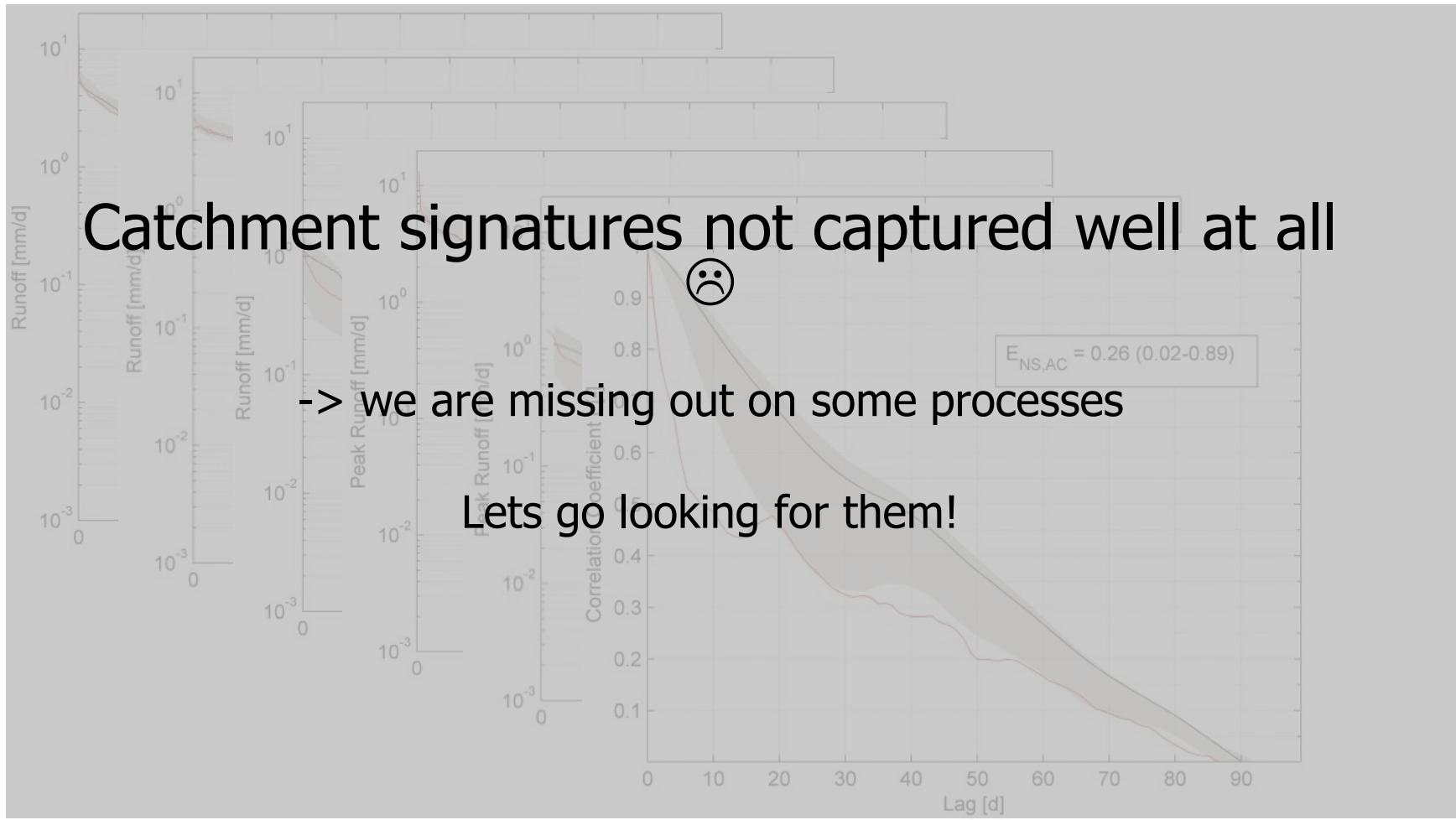
## Model 1: 6 parameters, no constraints



Hrachowitz et al., 2014, WRR

# M1- Benchmark Model

Model 1: 6 Parameters, no constraints



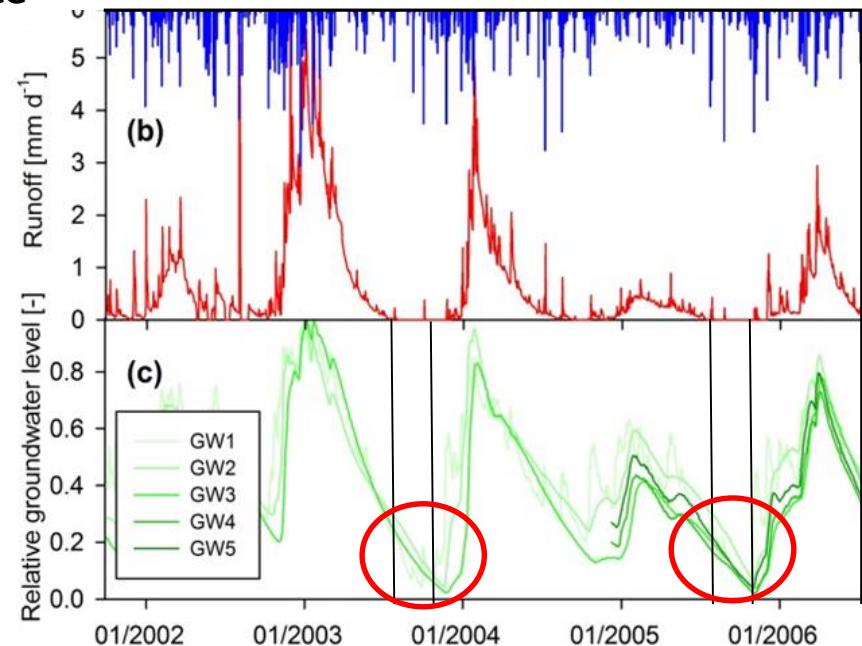
# Additional processes and landscape heterogeneity

What do we know about the catchment?

## (a) Long-term water balance deficit

- Bit of a no-brainer: check water balance  
-> find substantial losses
- Add loss term to model

P	1035 mm
- Q	- 274 mm
- $E_p$	- 692 mm
Loss	68 mm



Hrachowitz et al., 2014, WRR

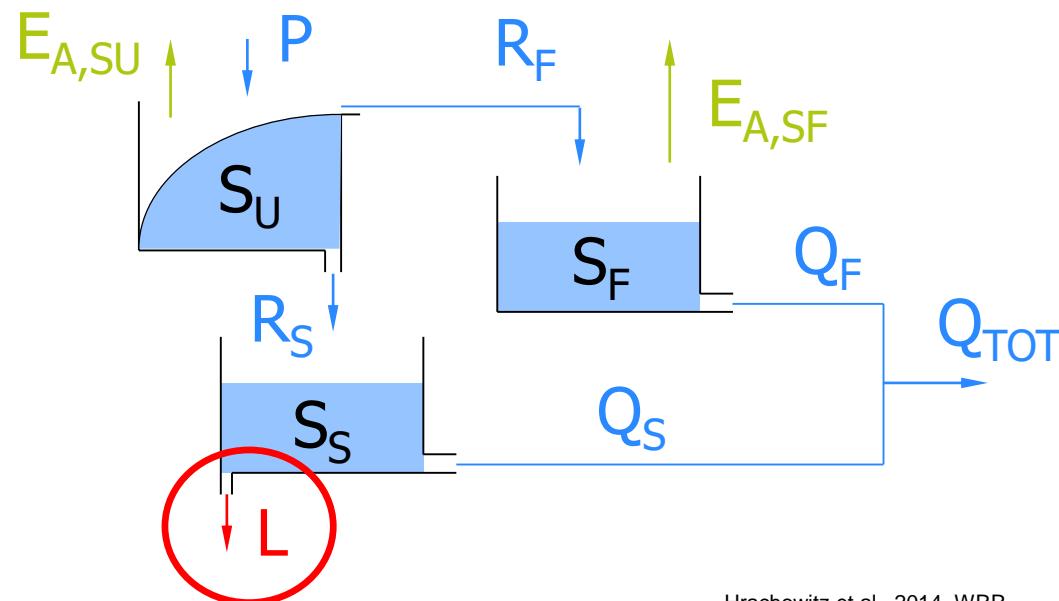
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Hrachowitz et al., 2014, WRR

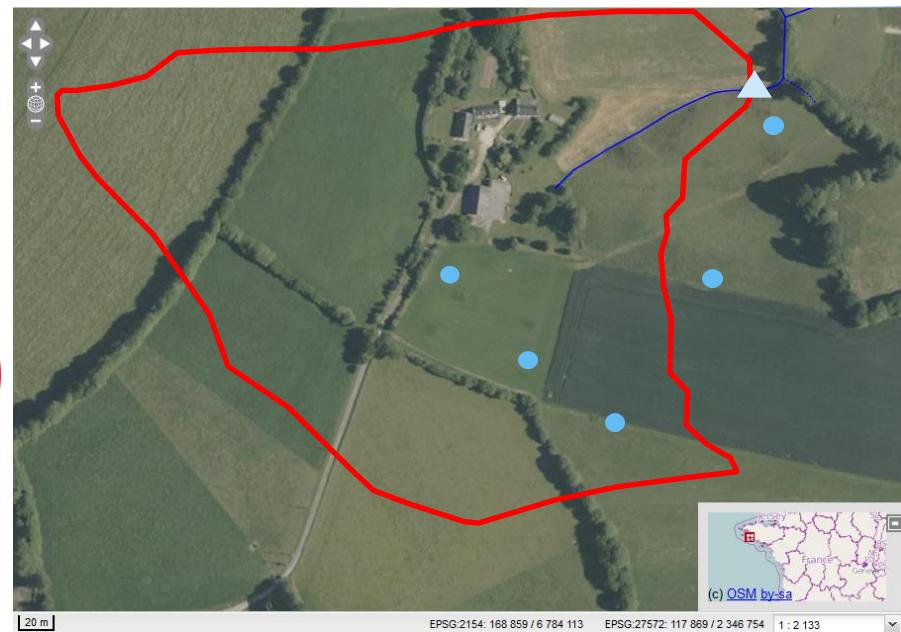
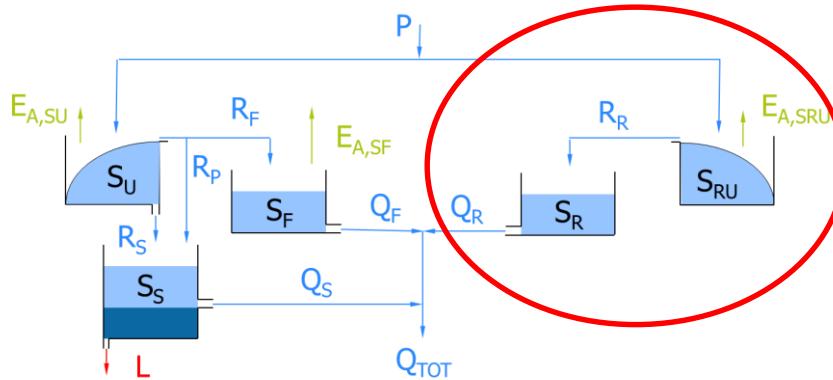
# Additional processes and landscape heterogeneity

What do we know about the catchment?

(a) Long-term water balance deficit

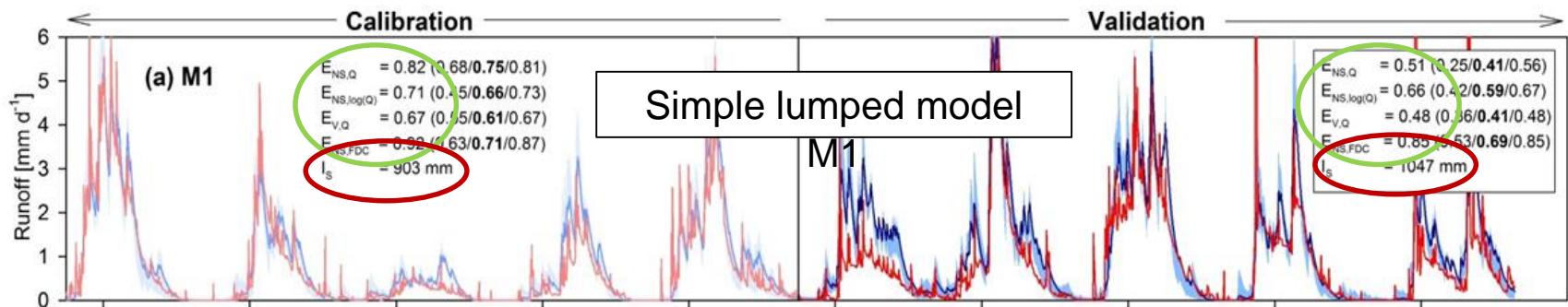
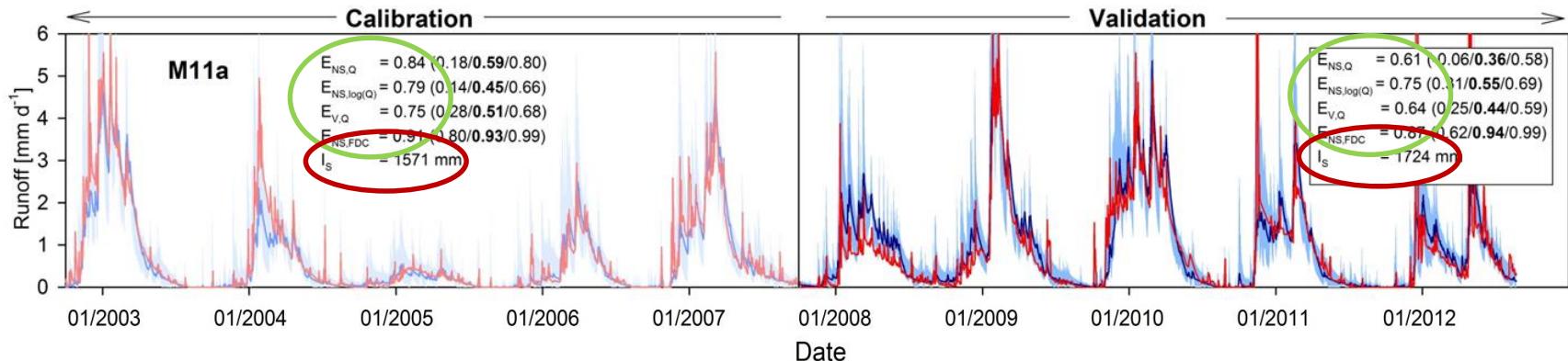
(b) Presence of extended riparian zone / wetland

- Wetlands often show distinct process dynamics than hillslopes.
- Add wetland component to model



# Model evaluation

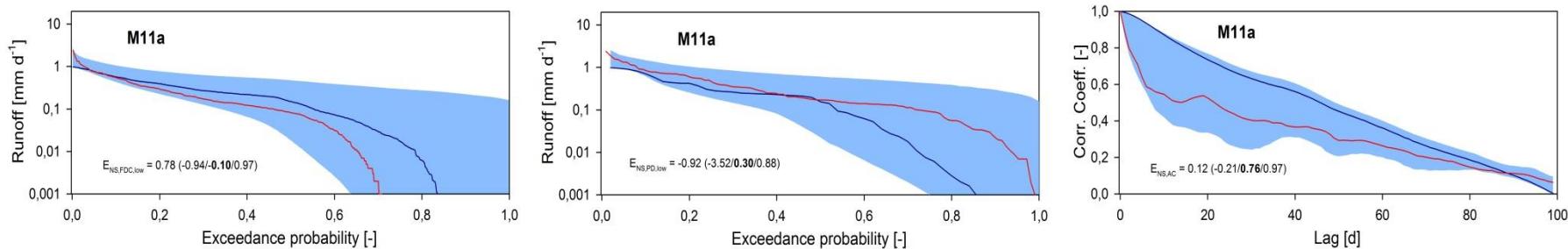
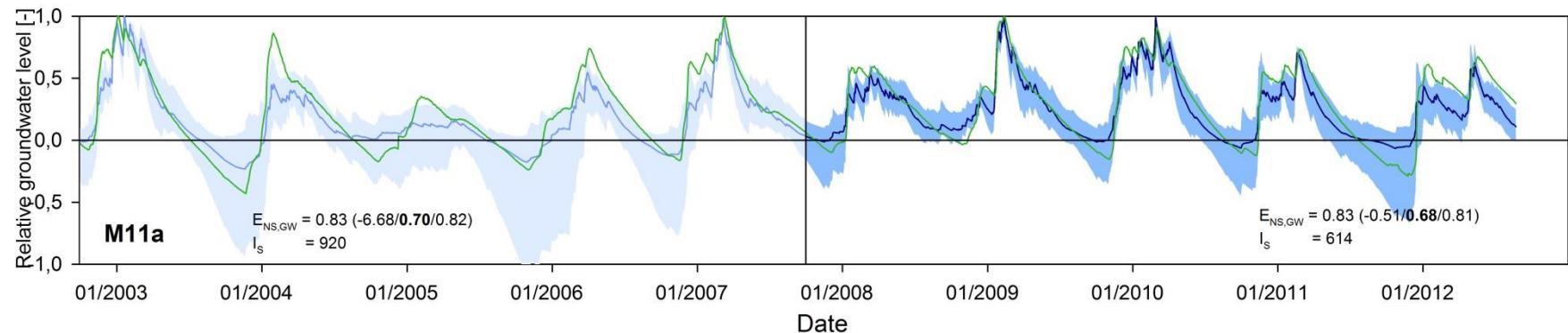
M11a – Improved performance but higher uncertainty



Hrachowitz et al., 2014, WRR

# Model evaluation

M11a – Improved performance but higher uncertainty



Hrachowitz et al., 2014, WRR

# Simplicity – Complexity - Information

Let us have a closer look

- Traditional steps: data -> model -> calibration
- Nothing wrong with that
- **Except:** even simple models are usually over-parameterized
  - > Too many degrees of freedom  
or  
not enough criteria to constrain model
  - > Good performances but high uncertainty  
or  
bad performances and lower uncertainty



## What can we do????

# Simplicity – Complexity - Information

Let us have a closer look

- Traditional steps: data -> model -> calibration

**We need to be more efficient in exploiting**

- Except: even simple models are usually over-parameterized

**our knowledge to maximize the**

-> Too many degrees of freedom

or

**information we can extract.**

not enough criteria to constrain model

-> Good performances but high uncertainty

or

**There are many things we KNOW  
Need to use them more systematically!**

**Signatures – Constraints – Expert knowledge**

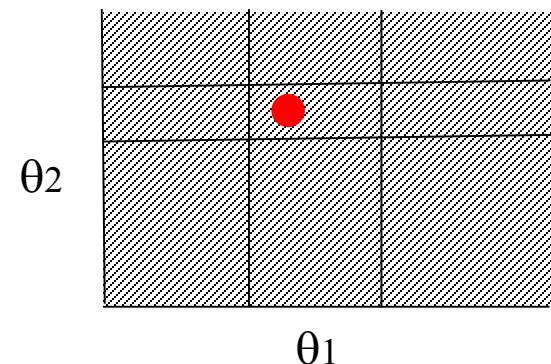
# Simplicity – Complexity - Information

## The value of prior information as model constraints

Models often ill-posed, inverse problems, i.e. no unique solution can be found from a pre-defined model space.

### Strategies to reduce the problem:

- Reduce number of parameters
- Evaluate against multiple objectives/criteria
- Prior constraints
  - a) Prior information on parameter range  
(e.g.  $K_s$ ,  $S_{max}$ )
  - b) Regularization/Regionalization



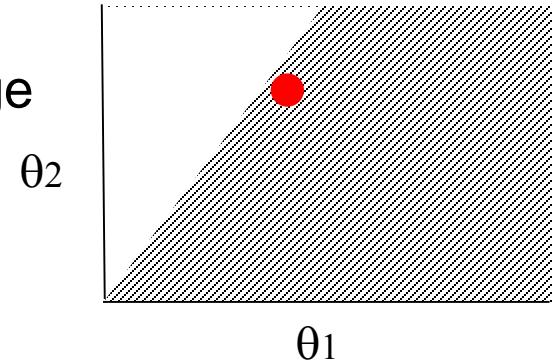
But there are more possibilities....

# Prior Constraints

## Relational parameter constraints

Similar to regularization, but:

- Based on semi-quantitative expert knowledge
- No additional data required
- Easy implementation
- Allows overlapping prior distributions



### Examples:

- Storage coefficient of slow reservoir smaller than of fast reservoir:
- Root zone storage capacity larger in hillslopes than in wetlands:
- Interception capacity higher in forests than in grasslands (e.g. based on LAI differences):

$$K_s < K_f$$

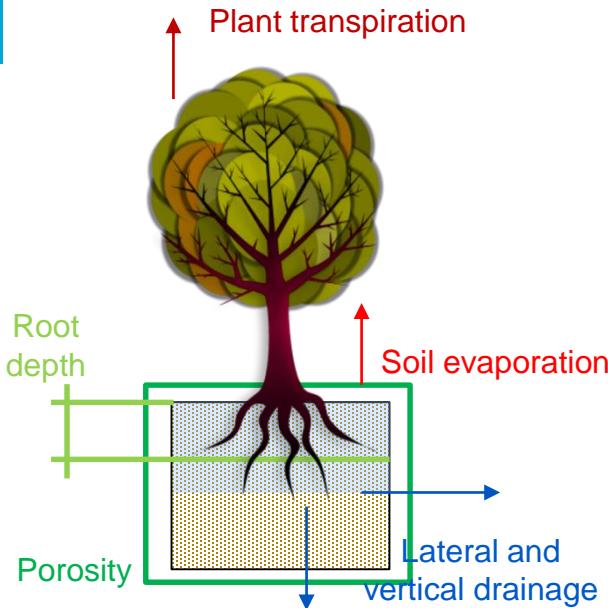
$$S_{\text{umax},H} > S_{\text{umax},W}$$

$$I_{\text{max},F} > I_{\text{max},G}$$

Gharari et al., 2014, HESS  
Gao et al., 2014, HESS

# Prior Constraints

## Root zone storage capacity - How to quantify at catchment-scale?



Water holding capacity in the root zone  $S_R$  is a core parameter in any hydrological system:

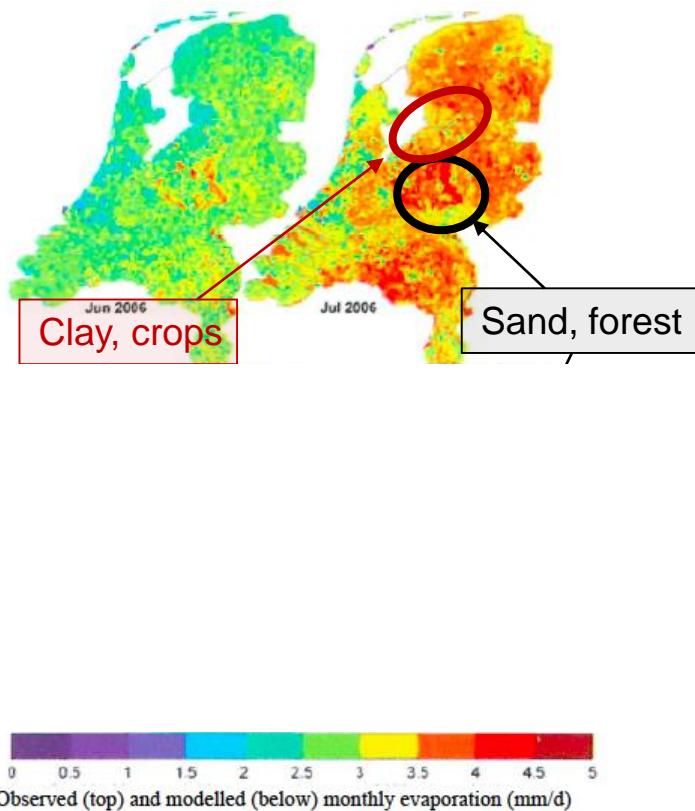
- (1) It provides storage below field capacity  
→ principal source of non-linearity in the system
- (2) It controls how water fluxes are partitioned into **evaporation/transpiration** and **drainage**

How is  $S_R$  determined?

- (1) Water filled **porosity** at field capacity
- (2) Average **root depth**

# Prior Constraints

## Root zone storage capacity - Effect of the traditional method

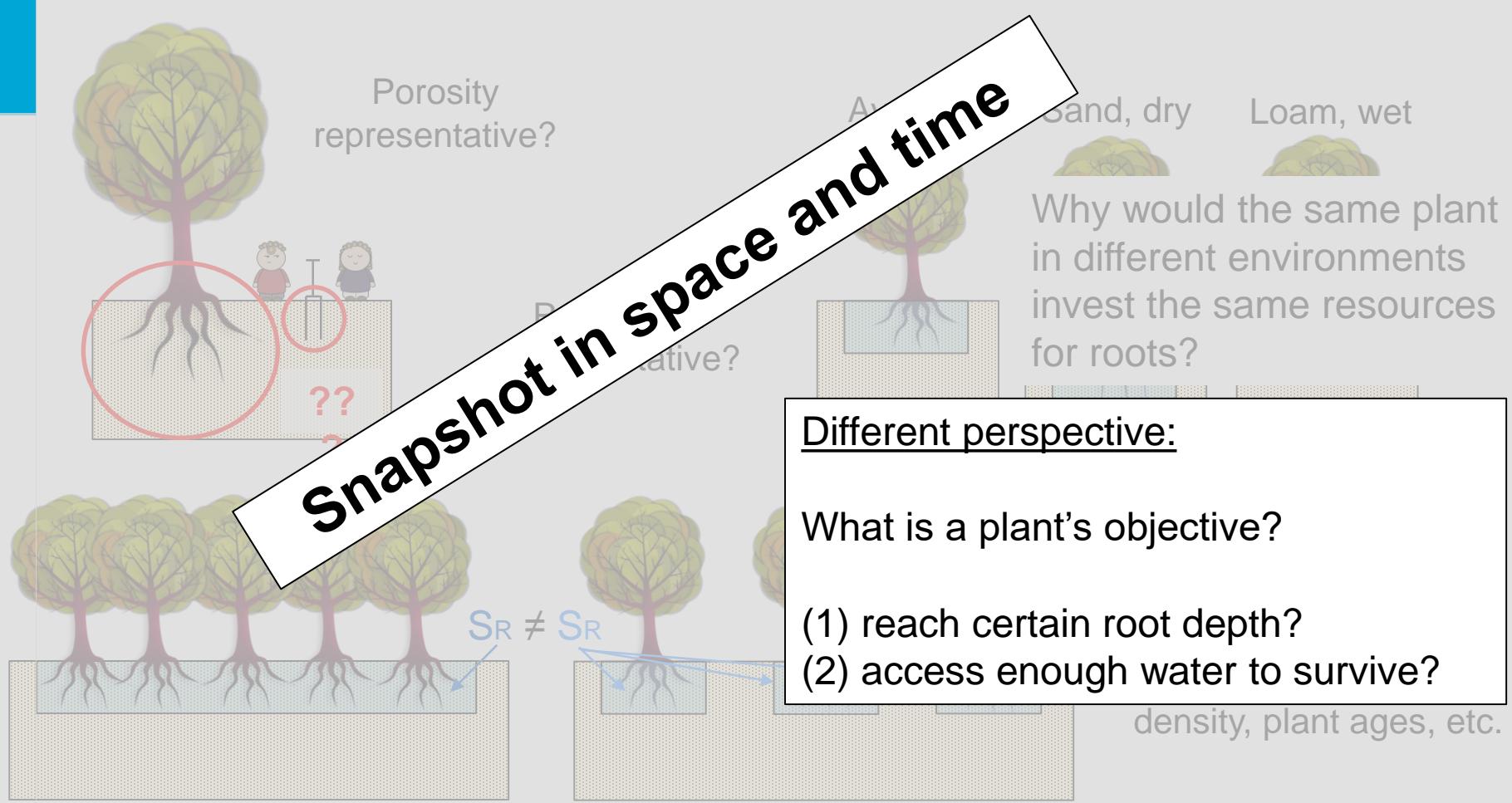


- Observed evaporation: upscaled eddy-covariance and lysimeter observations
- Modelled evaporation: physically-based, distributed NHI model
- Difference in spatial pattern
- Similar vegetation (mostly forest)
- Model only reflects differences in soils
- In sand, deeper roots are necessary to satisfy water demand during water limited conditions!

Beekman et al., 2014, Stromingen

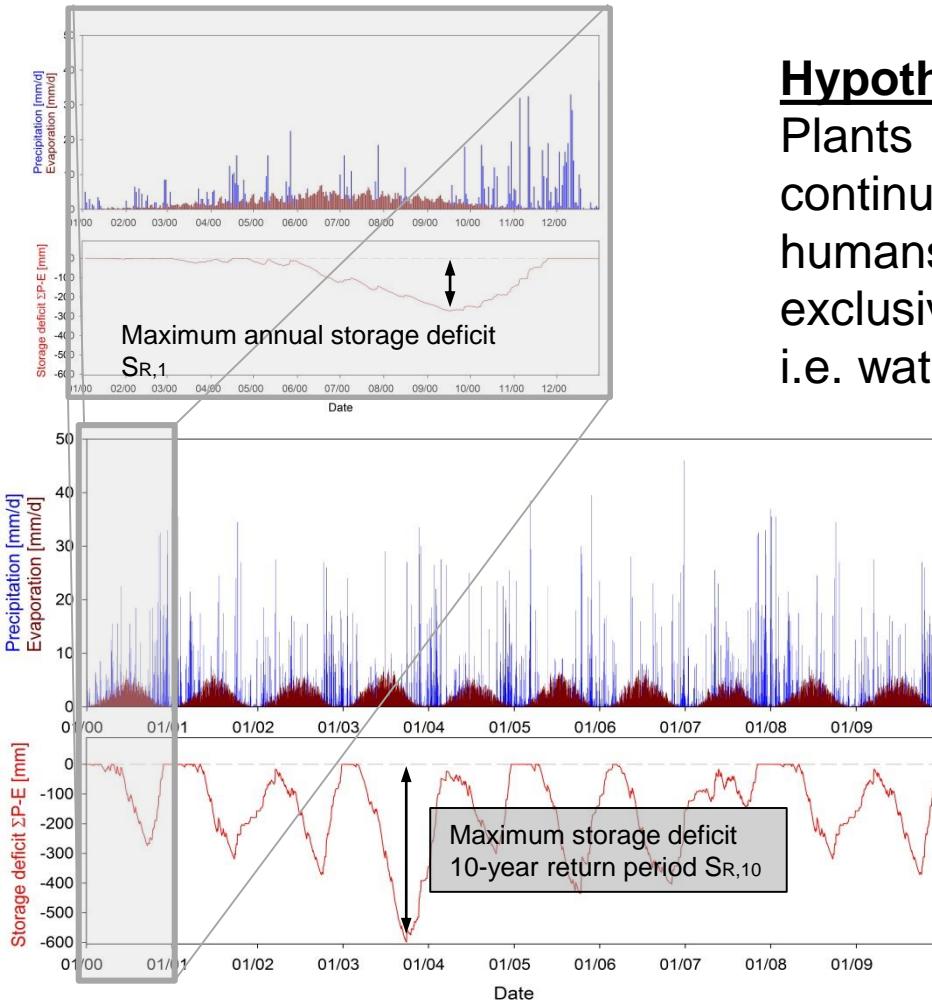
# Prior Constraints

Root zone storage capacity - Effect of the traditional method



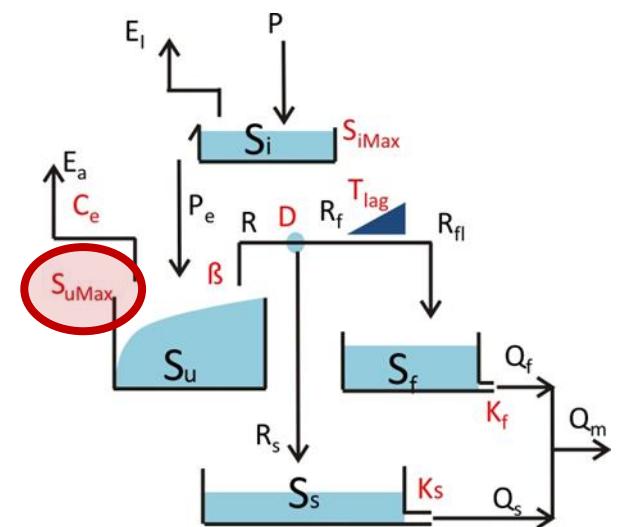
# Prior Constraints

## Root zone storage capacity - Estimation from water balance



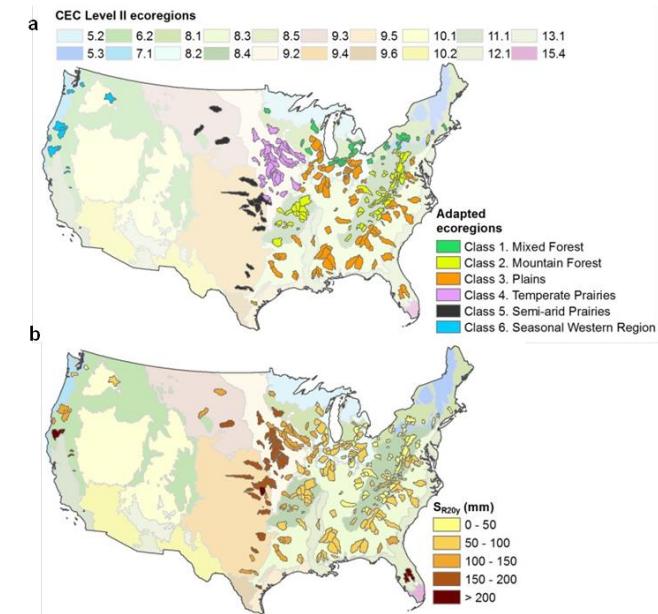
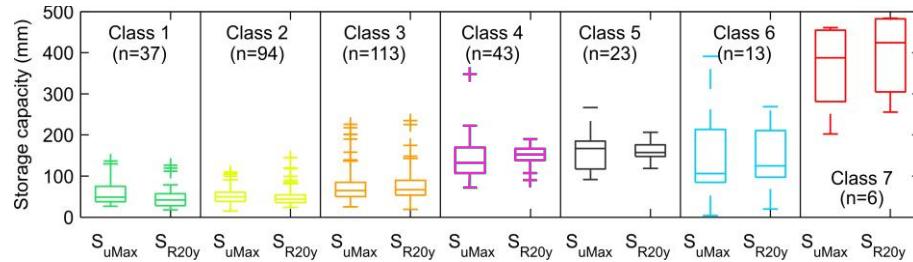
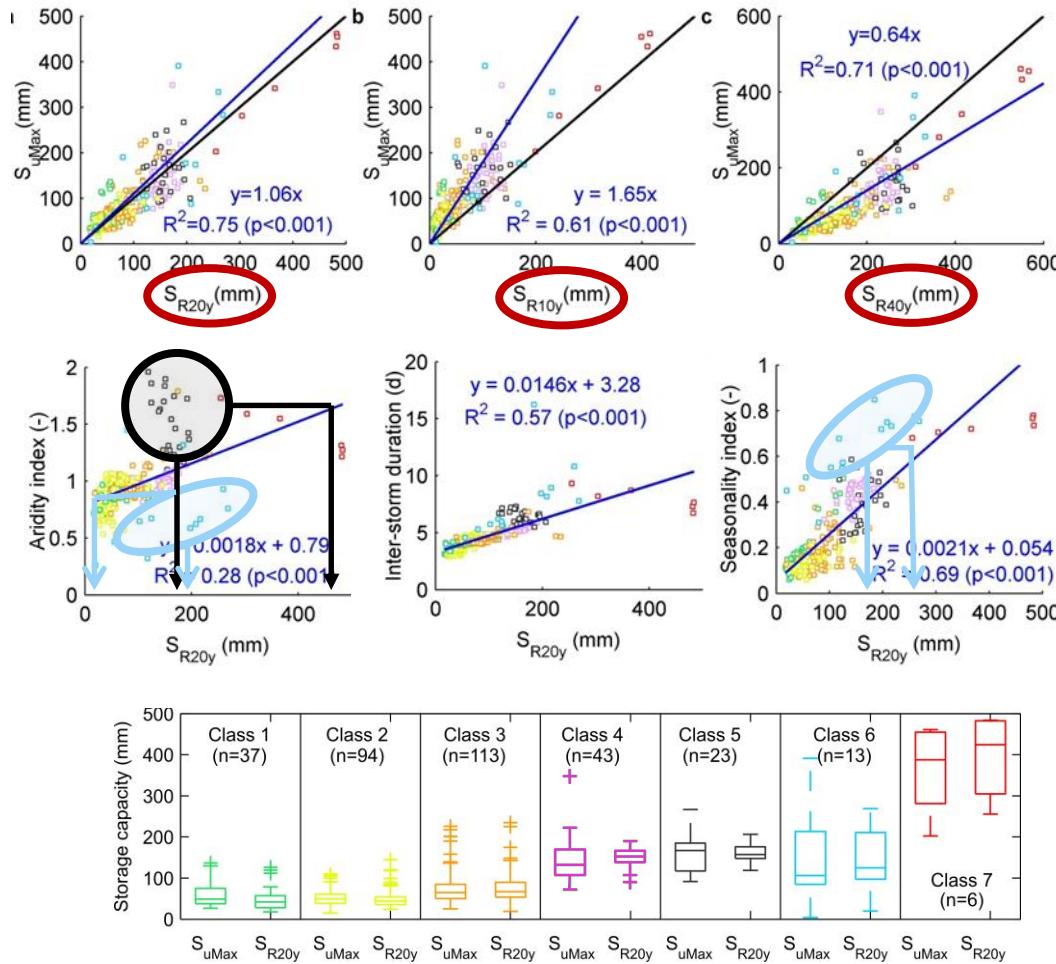
### Hypothesis:

Plants design root systems to guarantee continuous access to water similar to how humans design water reservoirs, exclusively based on supply and demand, i.e. water balance.



# Prior Constraints

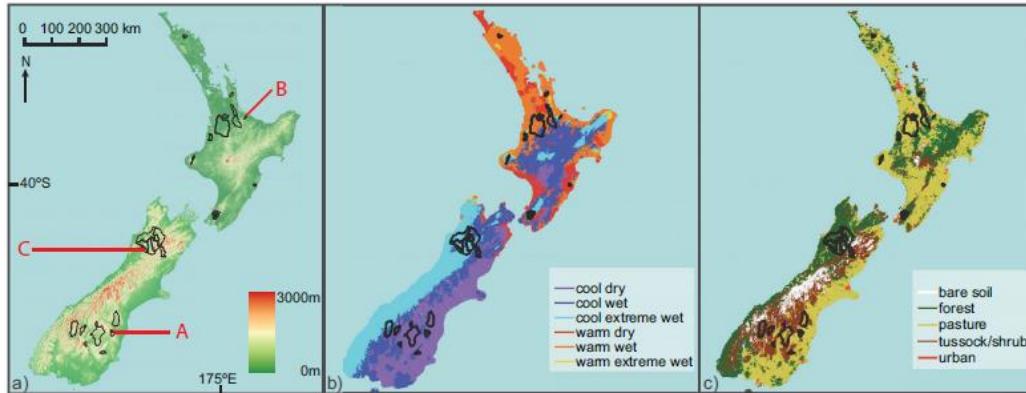
## Root zone storage capacity - What is controlling?



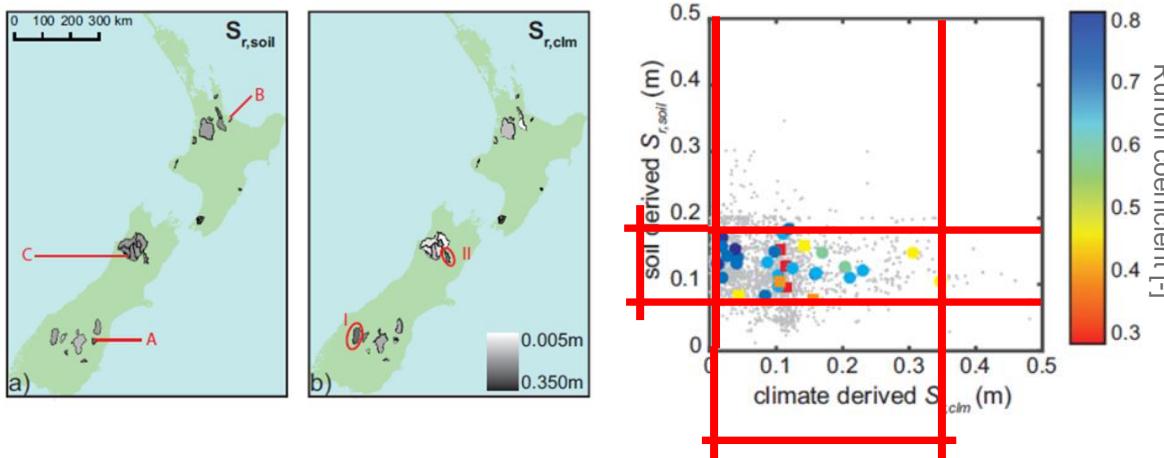
Gao et al., 2014, GRL

# Prior Constraints

Root zone storage capacity - And what about soil/root data?



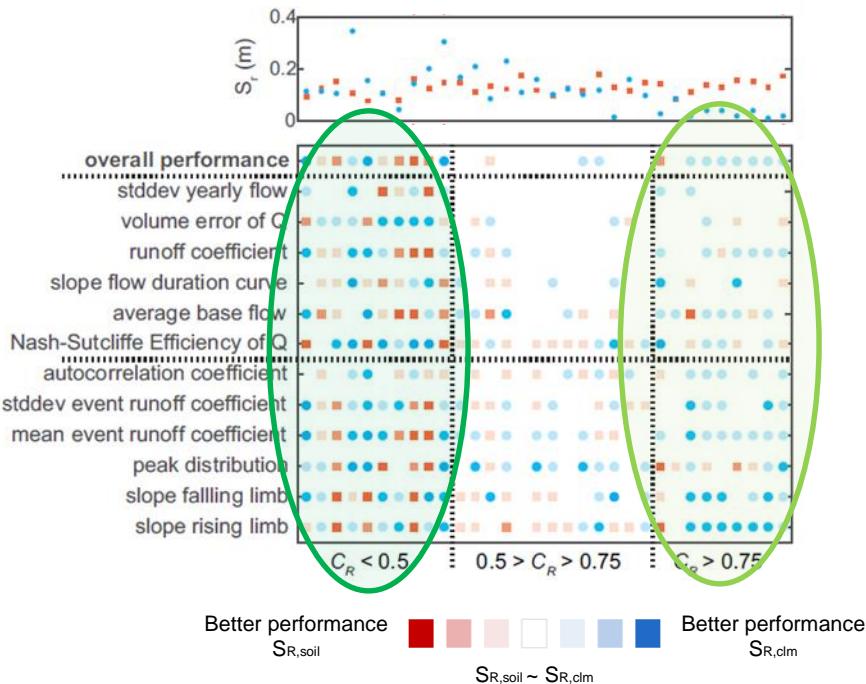
- 30 catchments in contrasting regions in New Zealand
- Higher variability in water balance derived  $S_{R,clm}$  estimates than in soil derived ones  $S_{R,soil}$
- The lower runoff coefficient the higher  $S_R$



deBoer-Euser et al., 2016, WRR

# Prior Constraints

## Root zone storage capacity - Water balance vs. soil/root derived estimates



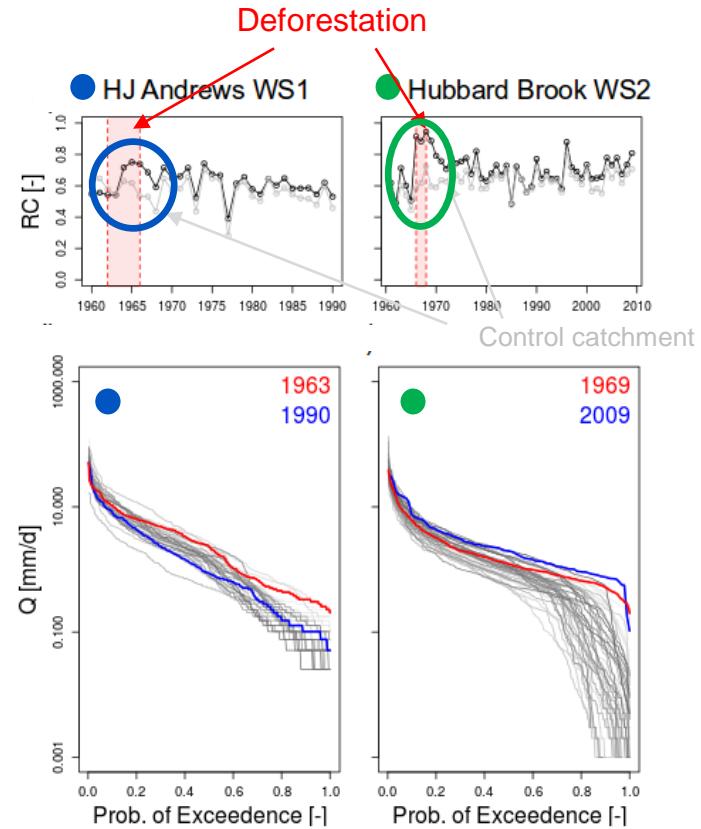
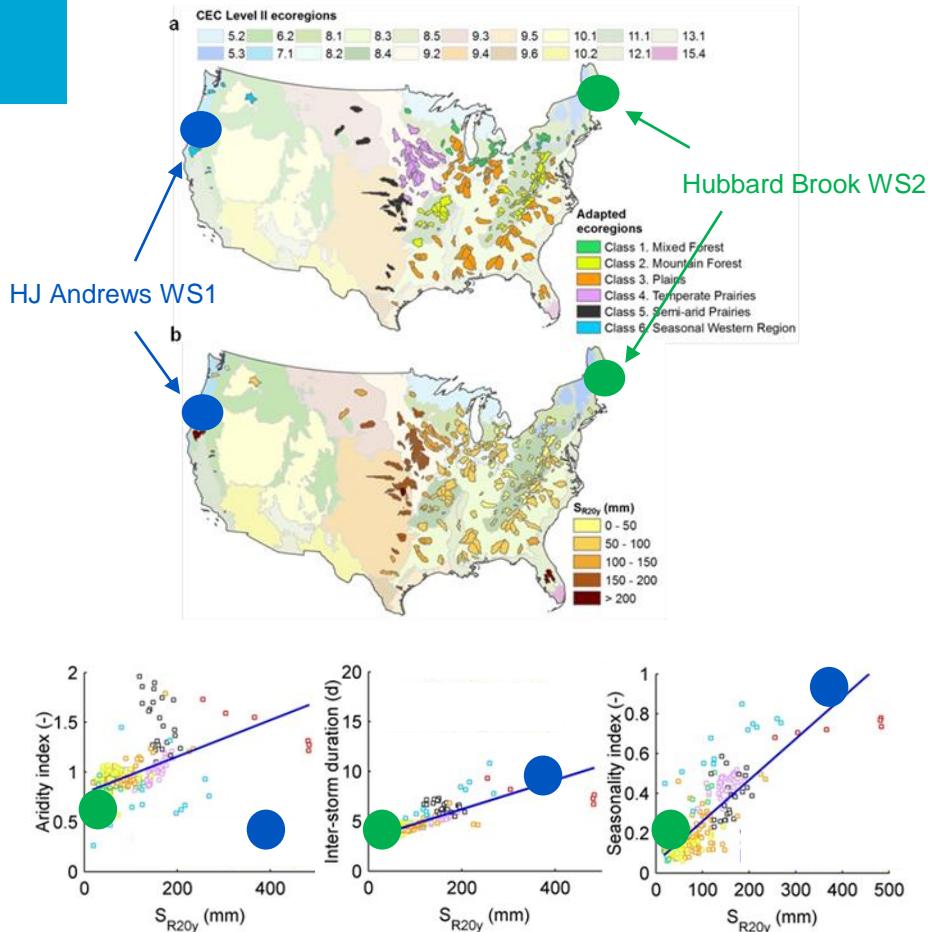
- TopNet model
- UNCALIBRATED!
- Compare model's ability to reproduce wide range of hydrological signatures with  $S_{R,soil}$  and  $S_{R,clm}$

On balance, model performances with  $S_{R,clm}$  at least **as good as** with  $S_{R,soil}$ , in regions with high runoff coefficients even considerably **better**.

deBoer-Euser et al., 2016, WRR

# Prior Constraints

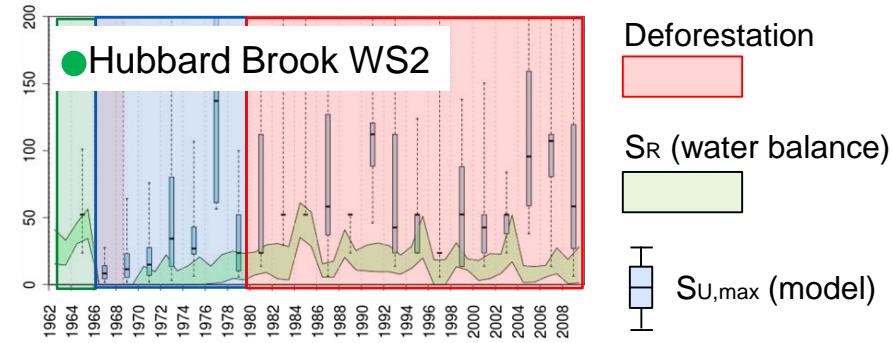
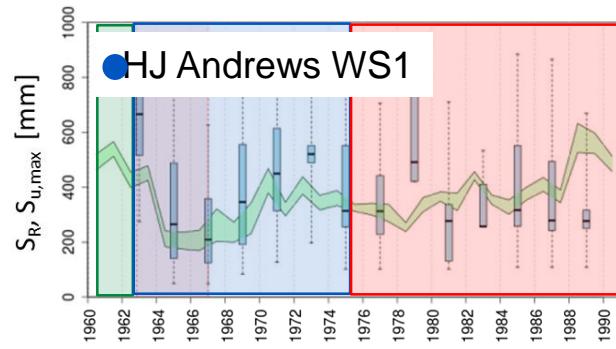
## Root zone storage capacity – Influence of deforestation?



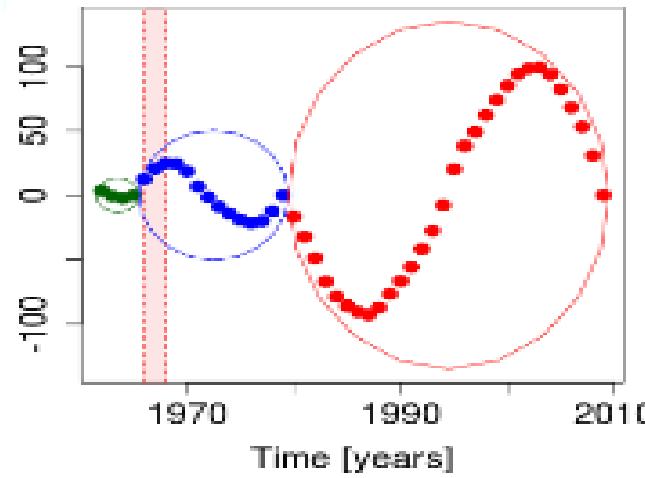
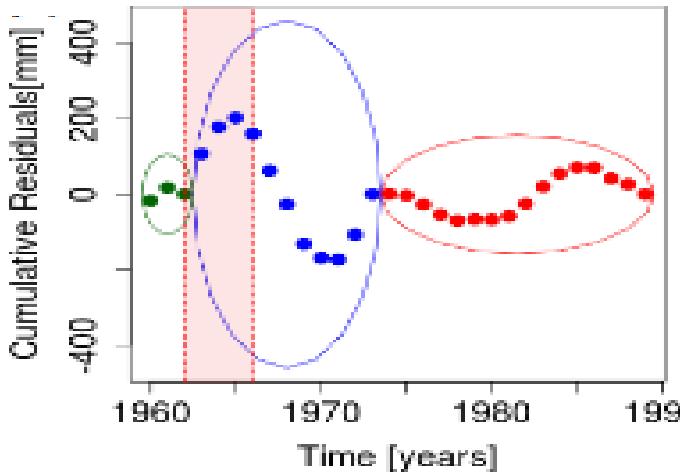
Nijzink et al., 2016, HESS

# Prior Constraints

## Root zone storage capacity – Influence of deforestation?



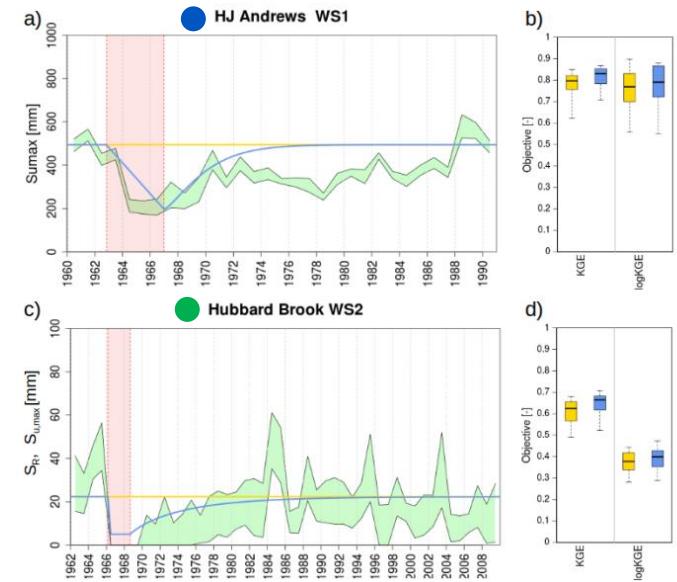
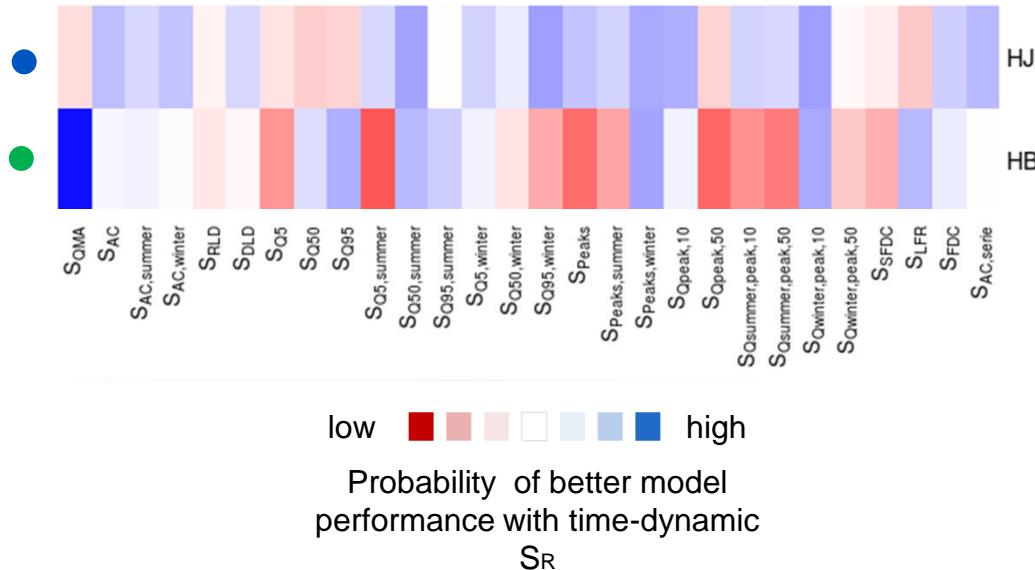
Deforestation  
SR (water balance)  
SU,max (model)



Nijzink et al., 2016, HESS

# Prior Constraints

## Root zone storage capacity – A step towards dynamic models?



- Effect stronger in HJ Andrews WS1 → higher absolute  $S_R$
  - What is needed?
    - (1) Climate projections  
How will precipitation and potential evaporation change?
    - (2) Understanding of how vegetation adapts to climatic conditions  
(trade time vs. space!)

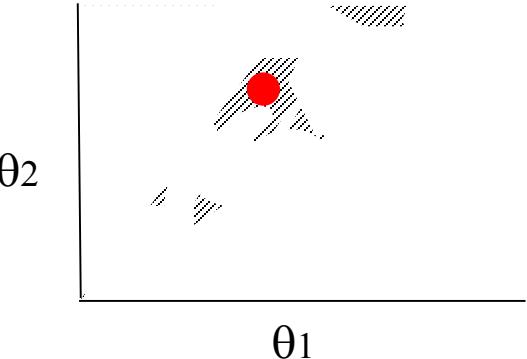
Nijzink et al., 2016, HESS

# Prior Constraints

## Relational process constraints

Limit of Acceptability approaches to extend multiple objective/criteria strategies:

- Expert knowledge and/or semi-quantitative, anecdotal information sufficient
- Ensures plausible (internal) model dynamics
- Easy implementation



### Examples:

- Modelled long-term actual evaporation should reflect estimate from Budyko curve:
- Modelled long-term base flow contribution should reflect digital filter baseflow estimates:
- During dry periods higher peak flow contribution from riparian zones than from hillslopes:

$$E_{A,Bud,low} < E_{A,m} < E_{A,Bud,high}$$

$$C_{B,low} < C_{B,m} < C_{B,high}$$

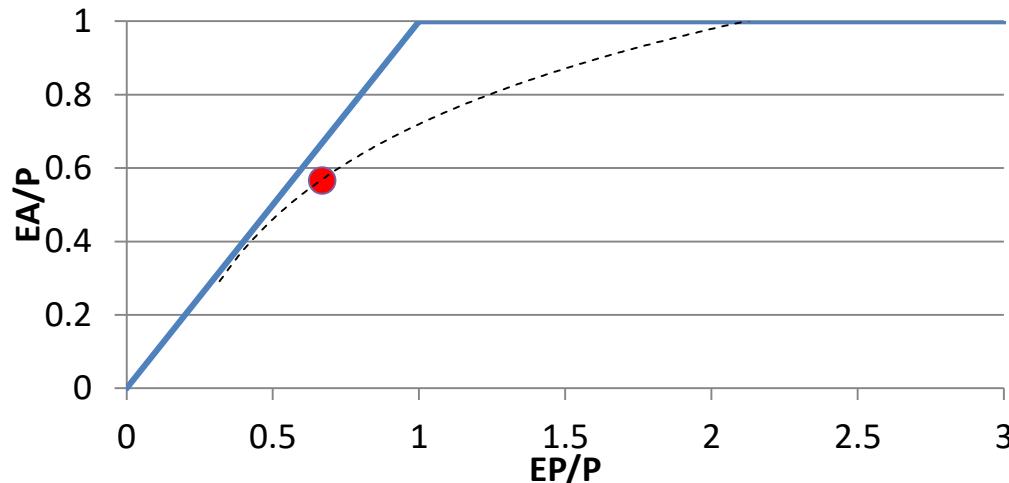
$$Q_{R,dry,avg} > Q_{H,dry,avg}$$

Gharari et al., 2014, HESS  
Gao et al., 2014, HESS

# What to do next?

## Model constraints

- Use long-term water balance to constrain parameterization and reduce model uncertainty
- We know: Mean annual runoff coefficient must be satisfied.
- Where there not enough data: estimate actual evaporation from Budyko framework
- From that we can get even more: upper and lower bounds on losses!

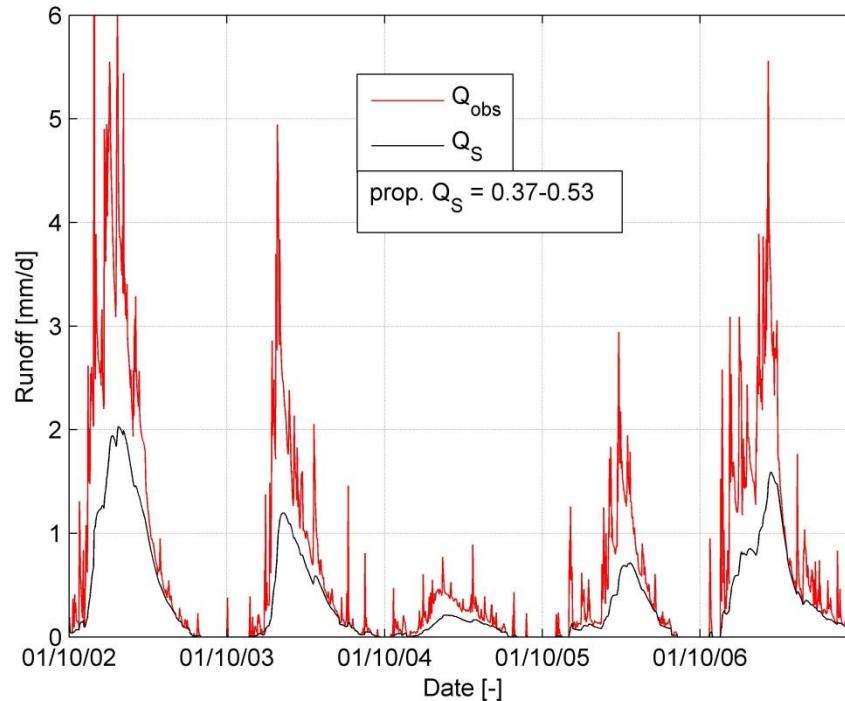


P	1035 mm	1035 mm
- Q	- 274 mm	- 274 mm
- $E_P$	- 692 mm	
- $E_A$		- 584 mm
Loss	68 mm	176 mm

# Constrain contribution of GW

## Model constraints

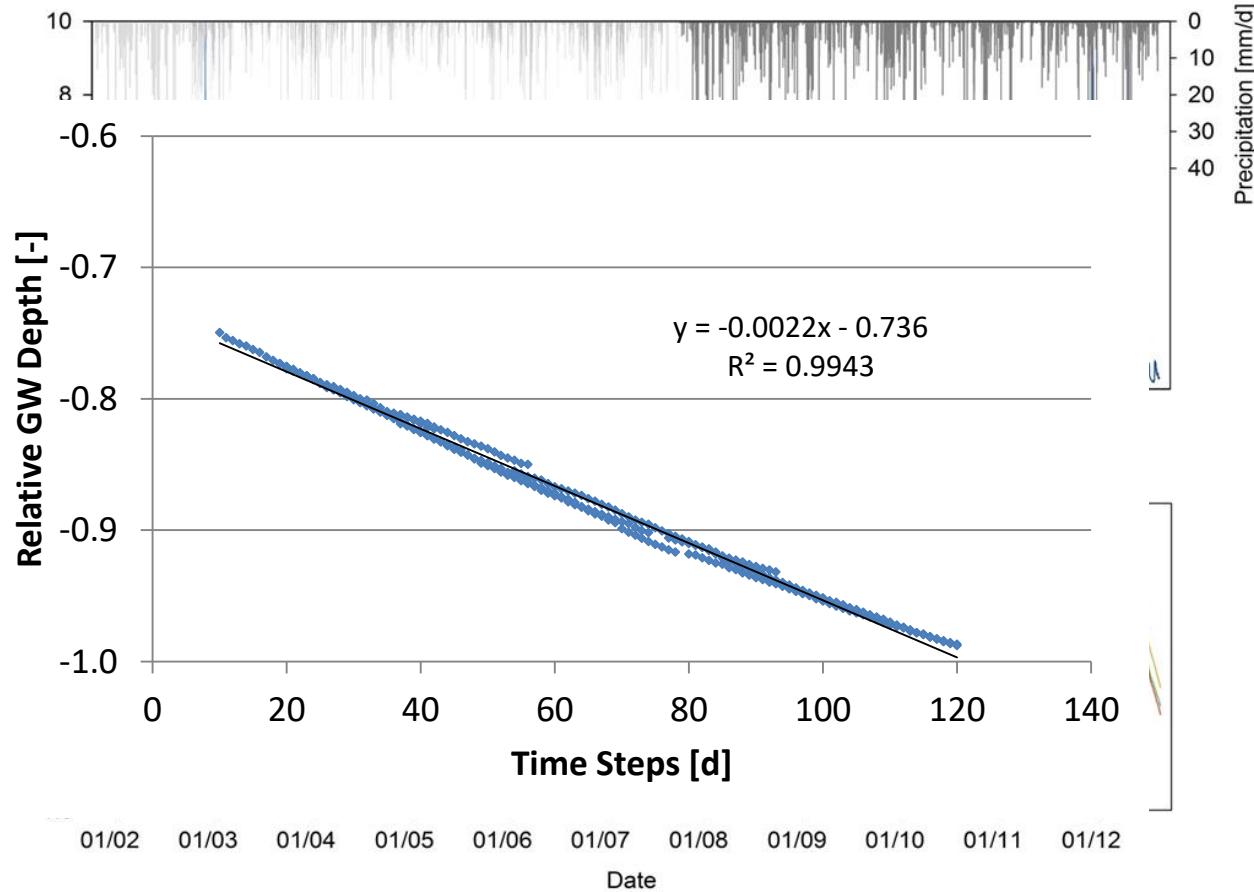
- Use of digital filter or other techniques to get rough estimate of  $Q_s$   
-> upper/lower bounds



# But there is more we know....

## Model constraints

- Lucky: at scale of interest GW falling at an approx. constant rate



# ...and yet more!

## Model constraints

- From fact that we have 0-flow periods, constant loss rate can be directly estimated
- When loss rate is known,  $K_S$  can also be estimated using a Master Recession Curve
- -> reduce free calibration parameters by 3 ( $K_S$ ,  $K_L$ ,  $S_{uP}$ )

# Do not forget landscape heterogeneity!

## Model constraints

- Wetland in catchment: different process  
-> increase process heterogeneity
- Expert knowledge

### • **Parameter Constraints:**

- 1) proportion  $f$  of wetland known
- 2)  $S_{U\max} > S_{U\max,WL}$

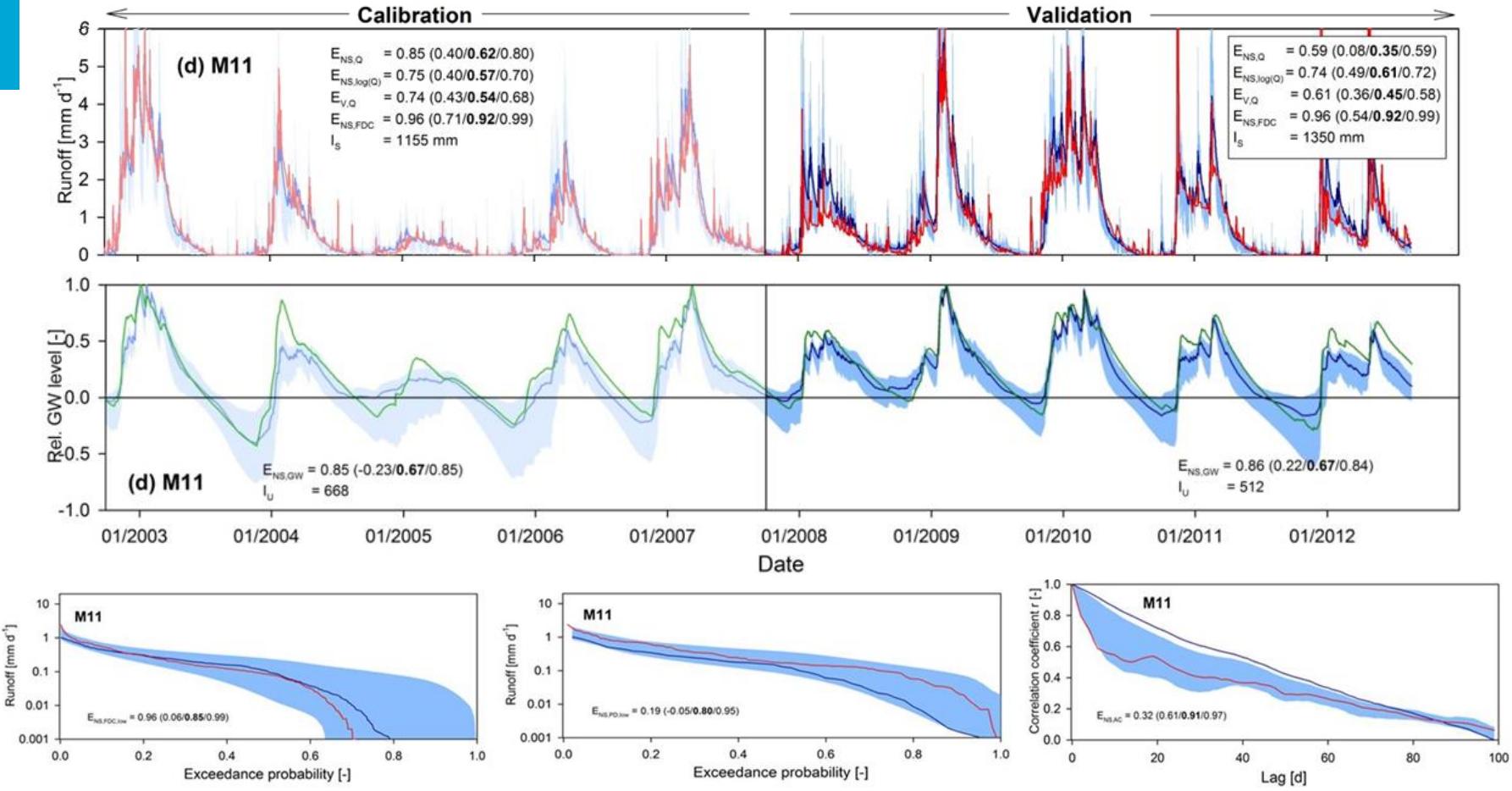
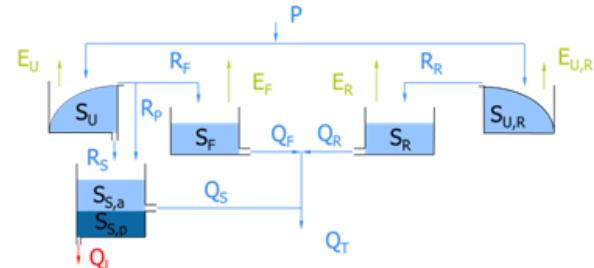
### • **Process constraints:**

- 3)  $\sum Q_{WL} > \sum Q_F$  in dry periods
- 4)  $\sum Q_F > \sum Q_{WL}$  in wet periods



# M11 – Nonlinear wetland

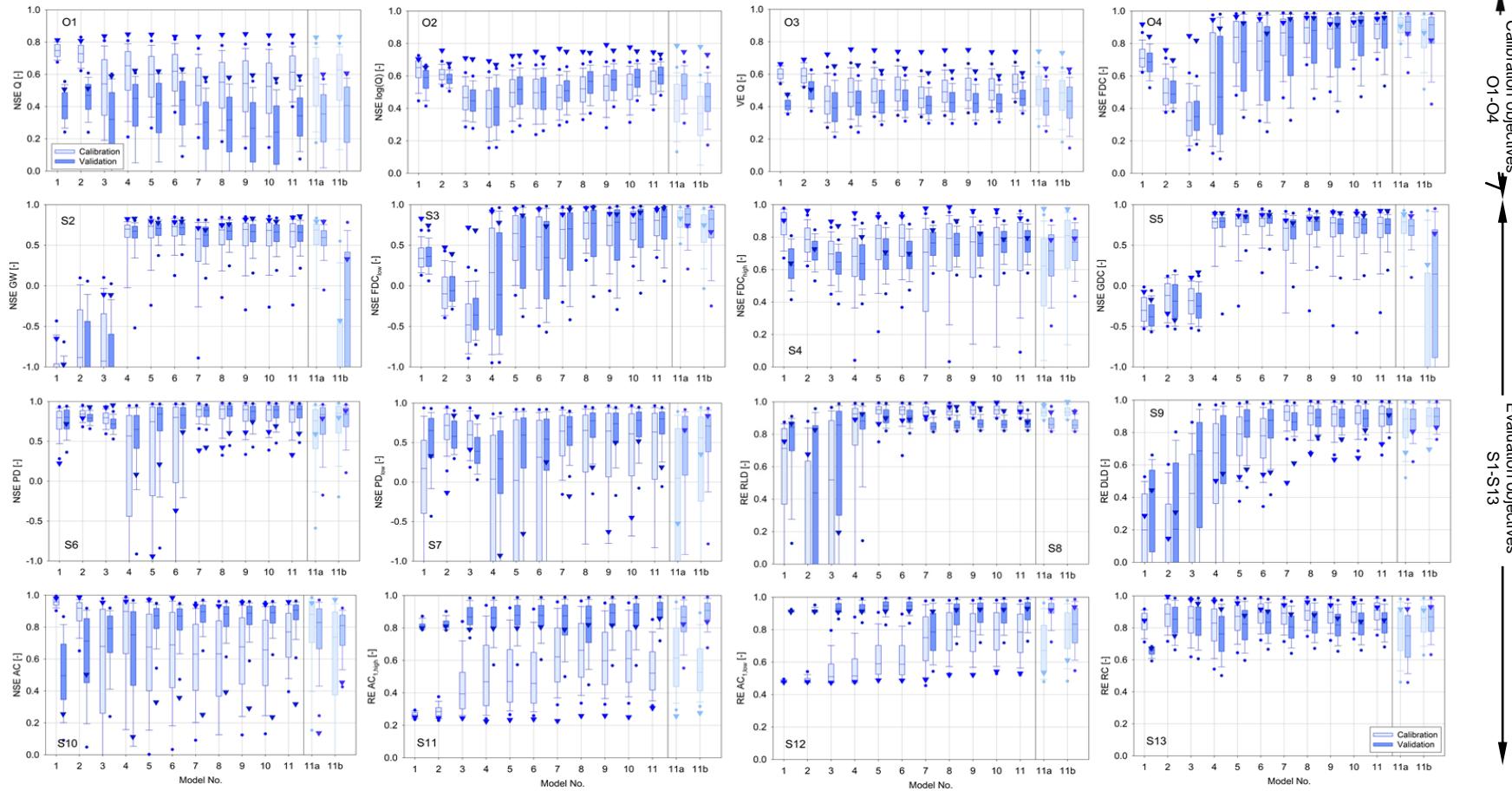
Model 11: 12 parameters, 8 constraints



Hrachowitz et al., 2014, WRR

# Model evaluation

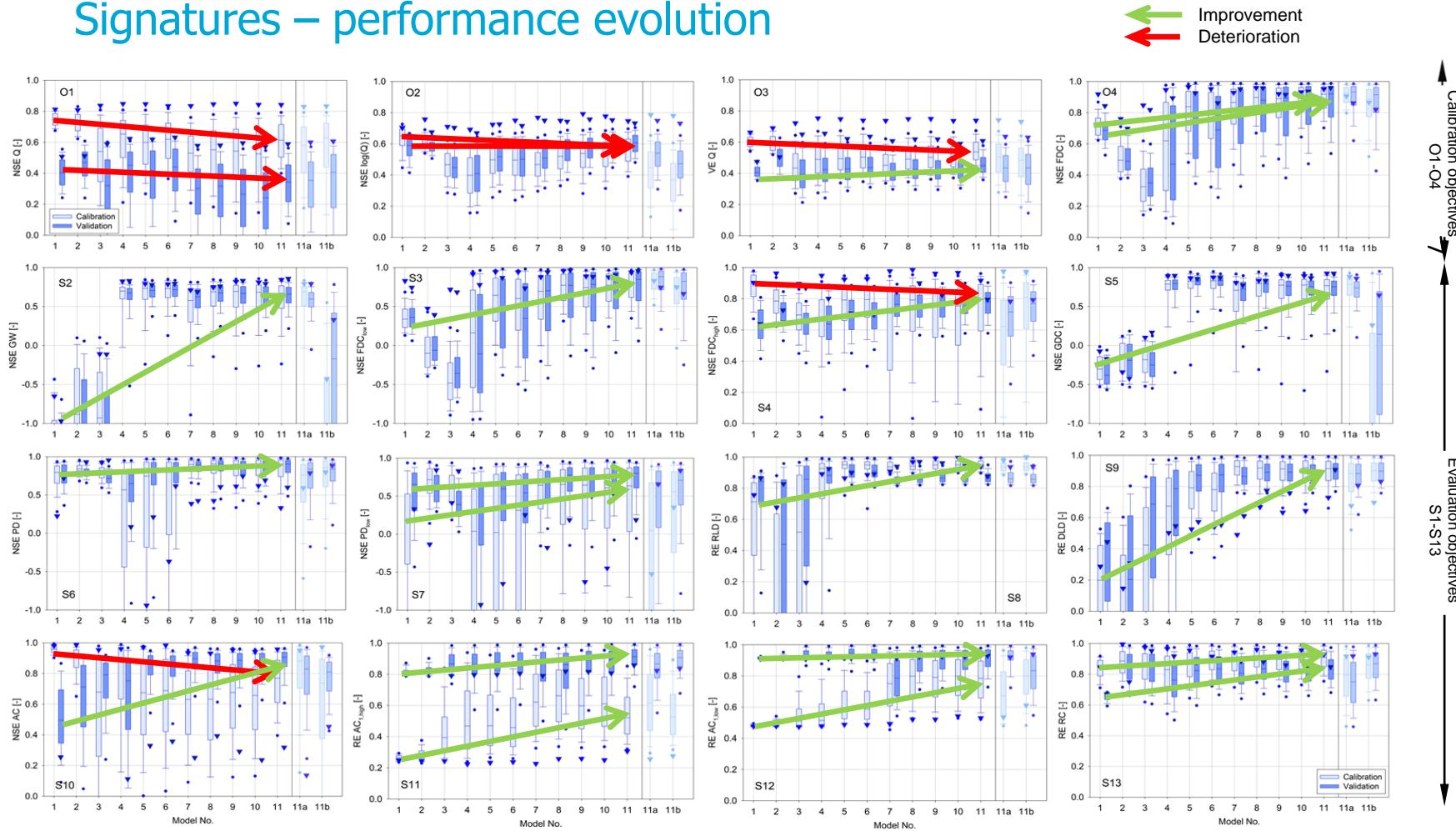
## Signatures



Hrachowitz et al., 2014, WRR

# Model evaluation

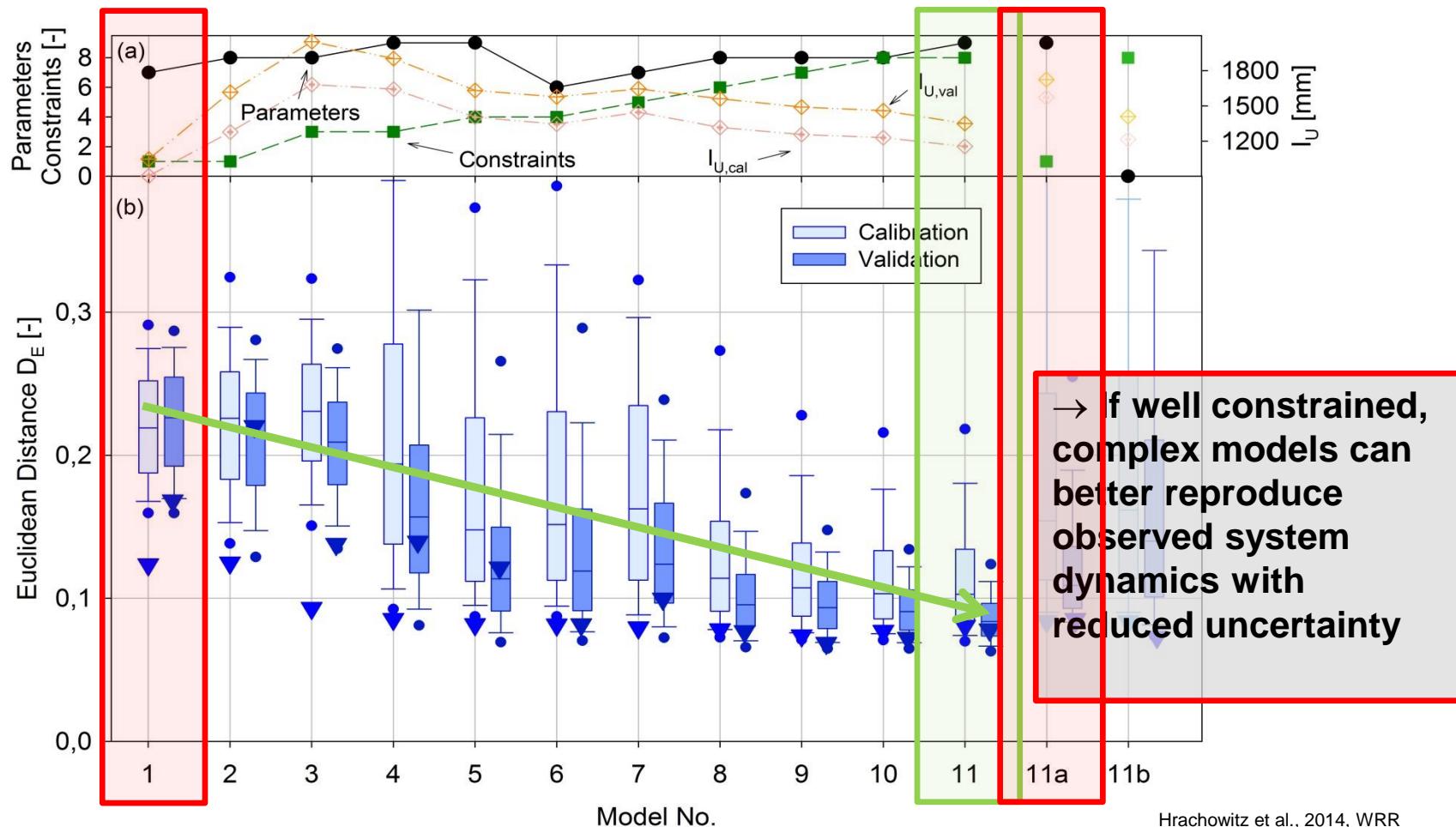
## Signatures – performance evolution



Hrachowitz et al., 2014, WRR

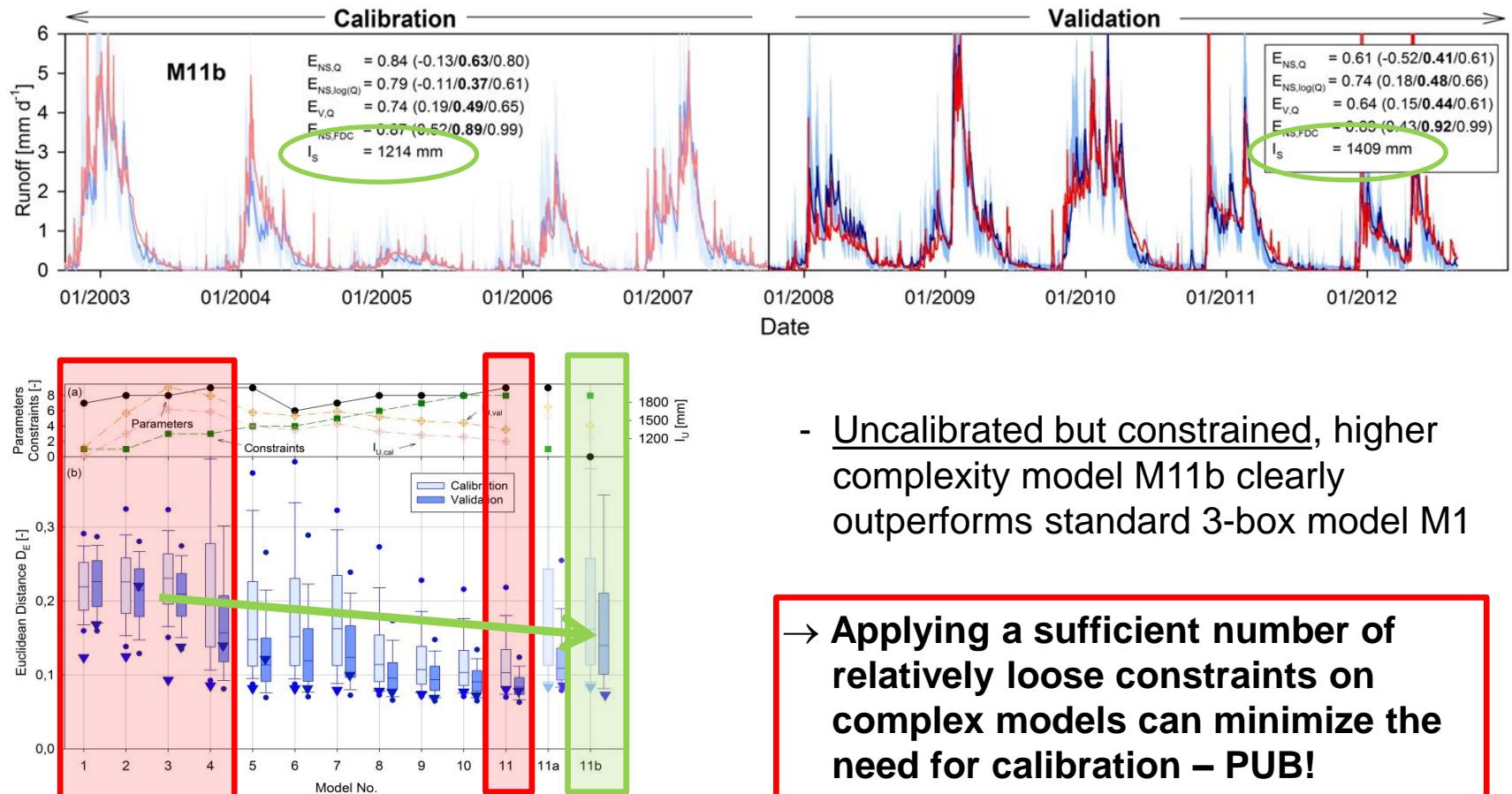
# Model evaluation

Overall performance evolution using 20 system signatures



# Model evaluation

## M11b – Uncalibrated but all constraints applied



Hrachowitz et al., 2014, WRR

# Model transferability

How well can a calibrated model be transferred to another catchment?

- Relevant where no data for calibration are available
- Strong test for a model's ability to capture dominant processes

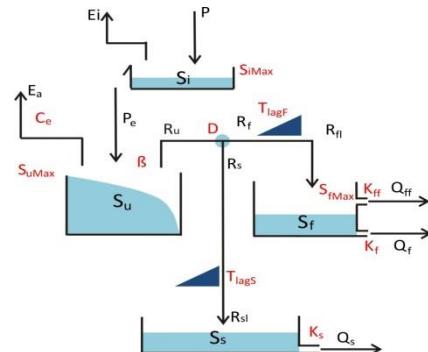


Gao et al., 2016, WRR

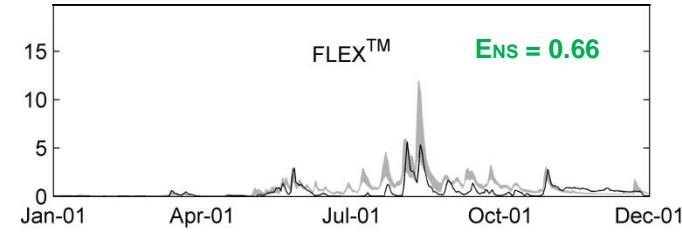
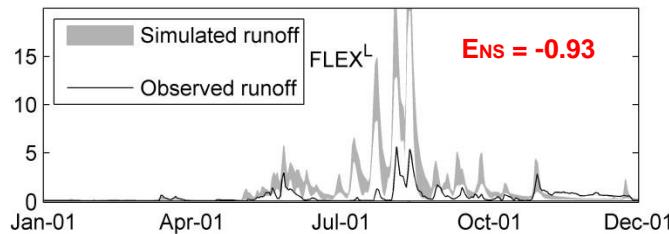
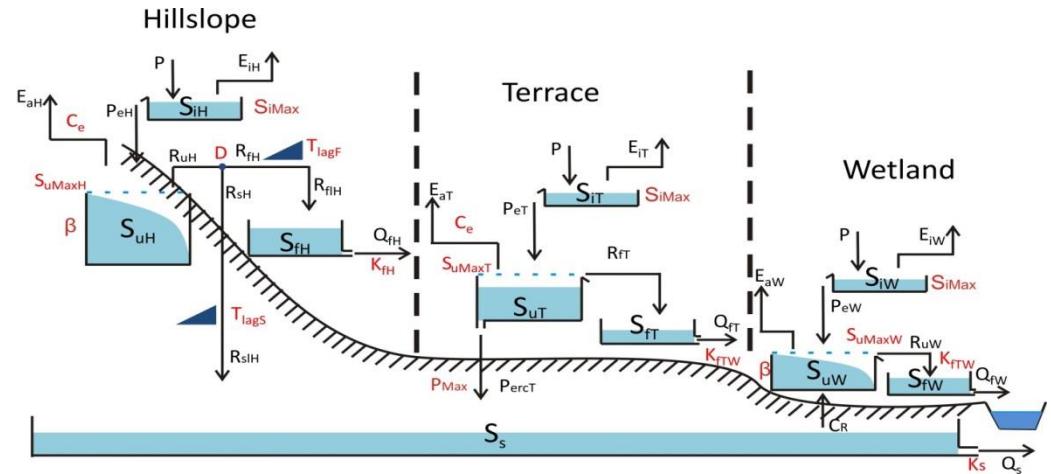
# Model transferability

The value of a more complete system representation

Lumped model



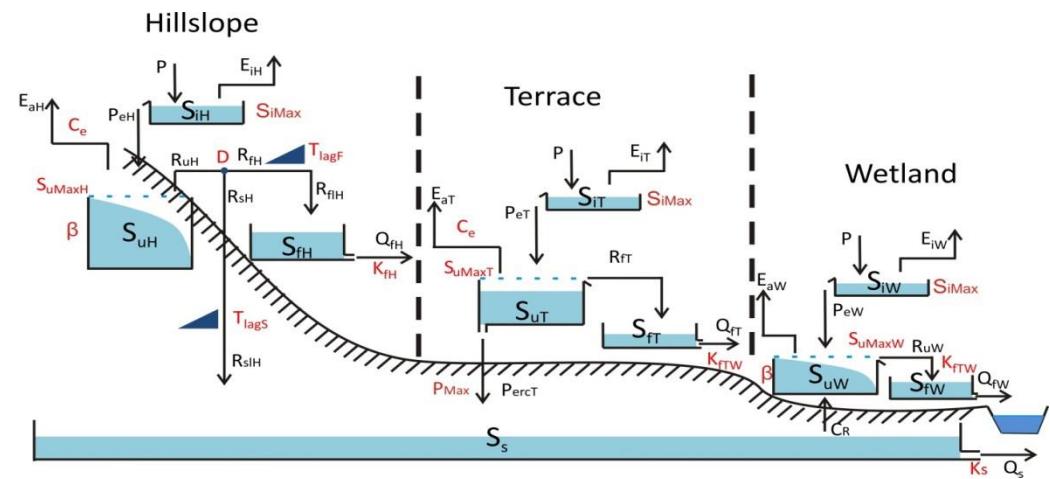
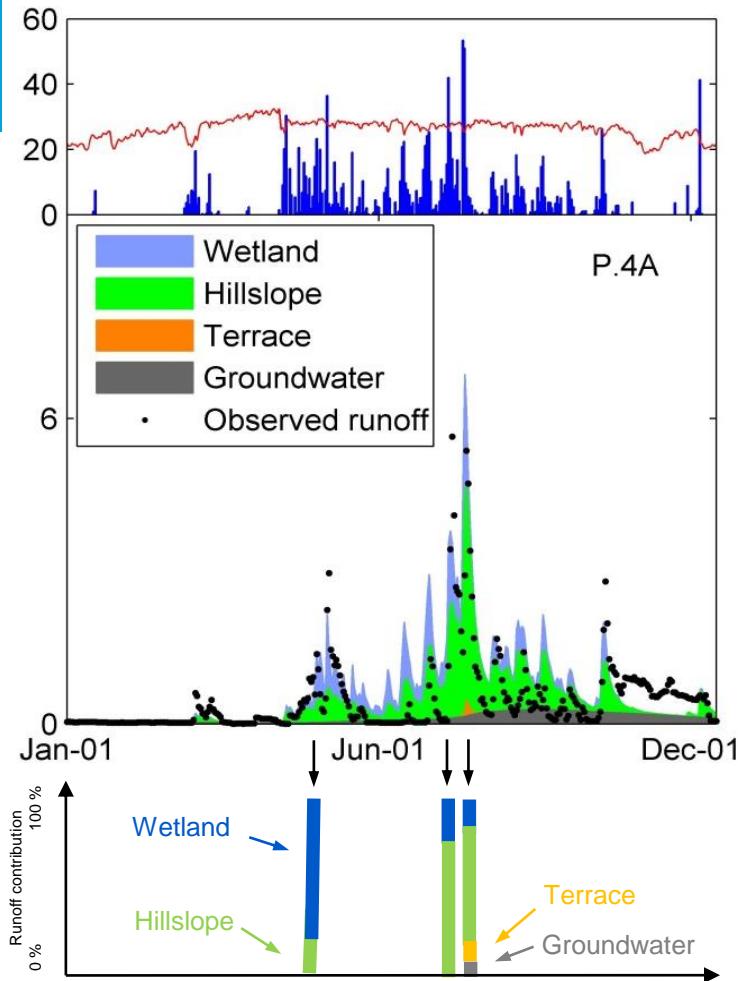
Semi-distributed, constrained model



Gao et al., 2016, WRR

# System internal dynamics

The value of a more complete system representation



Gao et al., 2016, WRR

# In a nutshell

- Need for more realistic representations of the system
- Value of carefully and efficiently exploiting available data to more efficiently extract relevant information
- Combination of
  - (1) process heterogeneity
  - (2) hydrologic signatures
  - (3) expert knowledge and eventually
  - (4) additional data critical for improving models
- Need to have a closer look at available information!
- We KNOW more than we typically think we do!

# **THANK YOU!!**

