

Template matching for pattern-based clique finding

- P_u : the set of nodes in pattern P
- F_u : the set of all nodes in all patterns
- Base = {i,k}
- $T = \{C_{i,k} \cup \{i, k\}\}$, the nodes in the triangles of a projector matrix entry & base
- MissingP = $P_u \setminus T$: nodes in one pattern that are not in the nodes of triangles from a projector matrix entry
- Missing* = MissingP \cap q*: the nodes in a pattern core that are not in the nodes of triangles of a projector matrix entry
- Jold* = $q^* \cap C_{i,k}$: the nodes in a pattern core that are in the projector matrix entry
- Clique_check(P, T): returns true if P reflects T as if it were a clique
- Tri_covd(P, $C_{i,k}$, i, k): returns true if P reflects every triangle with i,k as base and an element of $C_{i,k}$ as 3d node (called triangles_covered in code)

	Process the Base Process only if i, k not in same core for some pattern. First, Loop through all the patterns and if clique_check(P, T) or tri_covd(P, $C_{i,k}$, i, k), then stop (do not process column). Loop through all the patterns and if we find a trigger for an Action, perform it and stop.	Process the Projectors Process only if $C_{i,k} \setminus F_u \neq \{\}$ Loop through all the patterns and apply the actions in the templates.	Adjust the Patterns (optional?) Process only if $F_u \setminus T \neq \{\}$ First, loop through all patterns and if $P_u \setminus T = \{\}$ or clique_check(P, T) or tri_covd(P, $C_{i,k}$, i, k), then stop (do not process column). Loop through all the patterns and apply the actions in the templates.
$i, k \notin P_u$	Action 1: New pattern, $q^* = T$, $q\# = \{\}$	No action	No action
$i, k \in q^*$	No action	Action 3: $P_{new} = C_{i,k} \setminus P_u$ if $P_{new} \neq \{\}$ if $ P_{new} = 1$ New pattern, $q^* = [i, k, P_{new}]$, $q\# = \{\}$ else $M = C_{i,k} \cap q^*$ if $ M = 1$ new $q\# = P_{new} \cup M$ $q^* = q^* / M$ else new $q\# = P_{new}$ else No action	Action 4: if $ Missing^* = 1$ remove Missing* else move Missing* to new $q\#$
$i, k \in Q\#$.	No action	Action 3	No action
one of $i, k \notin P_u$, the other $\in q^*$	Action 2 if $ C_{i,k} = 1$ or (Jold* $\neq \{\}$ and $ q^* \leq 3$): Action 1 else No action	No action	Action 5 if MissingP $\neq \{\}$ $M = (\text{one of } i, k \notin P_u \text{ and MissingP})$ if there is exactly one $q\#$ that contains nodes in MissingP, move M to that $q\#$ else move M to a new $q\#$ else No action
one of $i, k \notin P_u$, the other $\in q\#$	Action 2	No Action	Action 6 if MissingP \ nodes in the “other” $q\# \neq \{\}$ $M = (\text{one of } i, k \notin P_u \text{ and MissingP}) \setminus \text{nodes in the “other” } q\#$ if there is exactly one $q\#$ that contains nodes in M, move M to that $q\#$ else move M to a new $q\#$ else No action
one of $i, k \in q^*$, the other $\in q\#$	Action 2' If Jold* $\neq \{\}$ and $ q^* < 3$: Action 1 Else No action	Action 3	Action 7 if Missing* $\neq \{\}$ move Missing* to “other” $q\#$ else No action