Test the RRKJ pseudization routine and check the results against ld1.x (carbon, LDA).

```
[1]
     import numpy as np
     import matplotlib.pyplot as plt
     # add pstudio to the search path
     import sys
     sys.path.append('..')
[2]
     from pstudio import AE, set_output
     from pstudio.RRKJ import pseudize_RRKJ
     #set_output(sys.stdout)
     ae = AE('C', xcname='LDA', relativity='SR')
     ae.run()
     scalar relativistic atomic calculation for C (Carbon, Z=6)
     configuration: 1s2 2s2 2p2, 6 electrons
     exchange-correlation: lda_x+lda_c_pz
     2001 radial gridpoints in [1e-05,100]
    Converged in 63 iterations
     Energy contributions:
     Kinetic:
               +37.269733 Ha
                                 +1014.161102 eV
     Ionic:
                 -87.619337 Ha
                                 -2384.243613 eV
    Hartree:
                 +17.627276 Ha
                                   +479.662609 eV
     XC:
                  -4.732032 Ha
                                   -128.765157 eV
     Total:
                 -37.454308 Ha -1019.183627 eV
     state eigenvalue eigenvalue
                                              rmax
     1s2
               -9.961701 Ha -271.071678 eV
                                              0.175
     2s2
              -0.501784 Ha -13.654238 eV
                                             1.218
              -0.199279 Ha -5.422666 eV
     2p2
                                             1.189
```

```
ldlae = np.loadtxt('LD1_C-LDA-RRKJ/c.wfc')
ldlps = np.loadtxt('LD1_C-LDA-RRKJ/cps.wfc')
```

```
[4]
     # loop over the valence orbitals
     r = ae.rgd.r
     ps = []
     for orb in ae.orbitals[1:]:
         n = orb.n
         l = orb.l
         aeorb = orb.ur
         rc = 1.54
         print('Pseudizing n={0}, l={1}'.format(n,l))
         psorb = pseudize_RRKJ(aeorb, l, rc, ae.rgd, verbose=True)
         ps.append(psorb)
         print()
         plt.figure(figsize=(6,4), dpi=200)
         plt.plot(r, aeorb, color='C1', label='AE PStudio')
         plt.plot(r, psorb, color='C2', label='PS PStudio')
         if l == 0:
             plt.plot(ld1ae[::20,0], -ld1ae[::20,2], linestyle='none',
     marker='o', markersize=4, color='C1', label='AE ld1')
             plt.plot(ld1ps[::20,0], ld1ps[::20,1], linestyle='none',
     marker='o', markersize=4, color='C2', label='PS ld1')
         else:
             plt.plot(ld1ae[::20,0], ld1ae[::20,1], linestyle='none',
     marker='o', markersize=4, color='C1', label='AE ld1')
             plt.plot(ld1ps[::20,0], ld1ps[::20,2], linestyle='none',
     marker='o', markersize=4, color='C2', label='PS ld1')
         plt.axvline(rc, linestyle='dashed', color='black',
     linewidth=0.5)
         plt.xlim(0,5)
         plt.title('C, LDA, n={0}, l={1}'.format(n,l))
         plt.legend()
         plt.show()
         print()
```

```
RRKJ3 pseudization: l=0 rc=1.5382

AE norm within rc : +0.542046

0-th AE derivative at rc: +0.762039

1-th AE derivative at rc: -0.286792

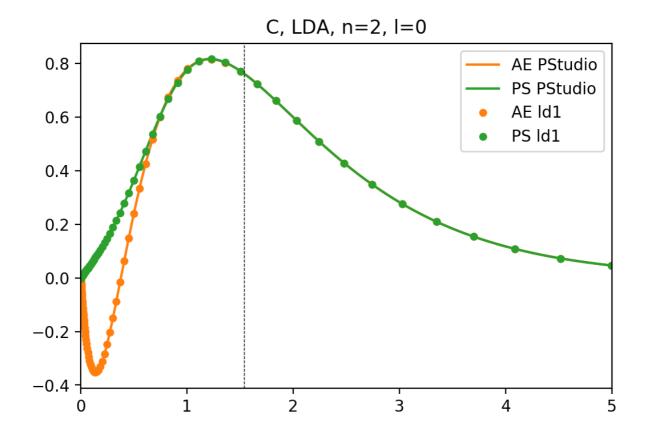
2-th AE derivative at rc: -0.507802

qi: [1.21630921 3.14118728 5.15350027]

estimated cutoff: 13.2793 Ha

RRKJ coefficients: [0.9513780131193765, -0.18781536460118928, -0.23024866834632174]
```

Pseudizing n=2, l=0



Pseudizing n=2, l=1

RRKJ3 pseudization: l=1 rc=1.5382

AE norm within rc : +0.475565

0-th AE derivative at rc: +0.675043

1-th AE derivative at rc: -0.161338

2-th AE derivative at rc: -0.287611

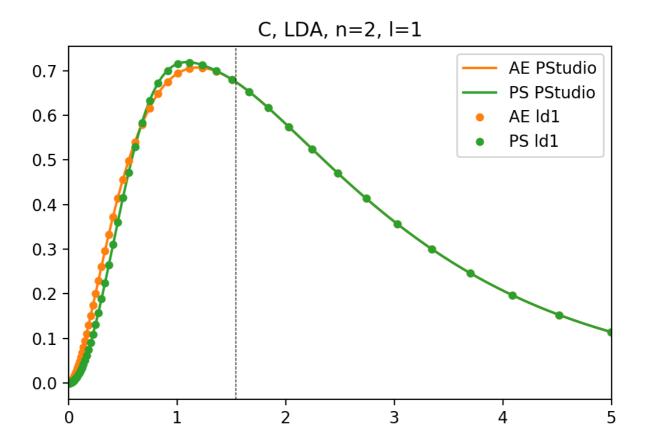
qi: [1.89253656 4.01747709 6.08313793]

estimated cutoff: 18.5023 Ha

RRKJ coefficients: [1.5167470899198419, 0.7727605389870011,

0.1600184575839441]

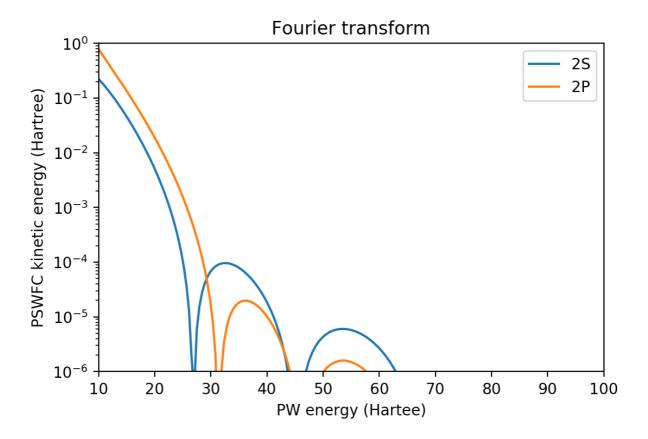
norm error : -1.2323475573339238e-14



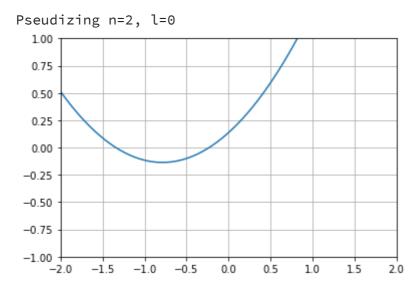
5

```
[5]
     plt.figure(figsize=(6,4), dpi=200)
     q, fq = ae.rgd.fft(ps[0], l=0)
     plt.plot(0.5*q*q, 0.5*fq*fq*q*q, label='2S')
     q, fq = ae.rgd.fft(ps[1], l=1)
     plt.plot(0.5*q*q, 0.5*fq*fq*q*q, label='2P')
     plt.xlim(10,100)
     plt.xlabel('PW energy (Hartee)')
     plt.ylim(1e-6, 1)
     plt.yscale('log')
     plt.ylabel('PSWFC kinetic energy (Hartree)')
     plt.title('Fourier transform')
     plt.legend()
     plt.show()
```

0



```
for orb in ae.orbitals[1:]:
    n = orb.n
    l = orb.l
    aeorb = orb.ur
    print('Pseudizing n={0}, l={1}'.format(n,l))
    psorb = pseudize_RRKJ(aeorb, l, 1.54, ae.rgd, verbose=False,
plot_c2=True)
    plt.xlim(-2,2)
    plt.ylim(-1,1)
    plt.show()
    print()
```



Pseudizing n=2, l=1

