linear regression model

March 7, 2023

1 What did Adam do to AMC, and 2023 Earnings Prediction by Linear Regression

```
[]: from matplotlib.collections import PatchCollection from matplotlib.patches import Circle import matplotlib.pyplot as plt import pandas as pd import numpy as np import df2img import math

plt.style.use("dark_background")
```

```
[]: years = list(range(2014, 2023))

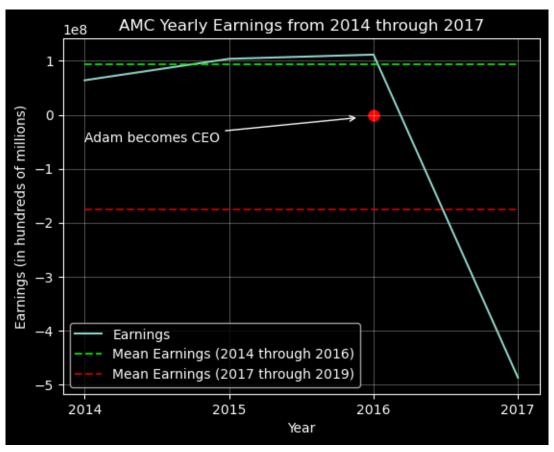
df = pd.read_csv("data.csv", index_col = 0)
```

2 Descriptive Data Visualizations

```
[]: plt.plot(years[:4], df.groupby("year").agg(["sum"])[:2017]["earnings"])
     plt.plot(years[:4], [df.groupby("year").agg(["sum"])[:2016]["earnings"].mean()]

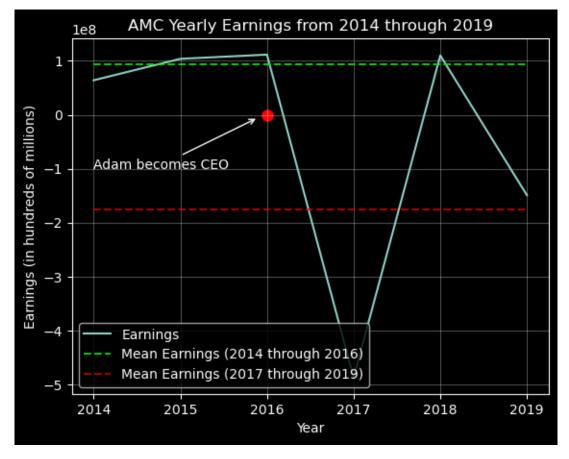
→* 4, color="lime",
              alpha = 0.8, linestyle="--")
     plt.plot(years[:4], [df.groupby("year").agg(["sum"])[2017:2019]["earnings"].
      →mean()] * 4, color="red",
              alpha = 0.7, linestyle="--")
     plt.scatter([2016], [0], color="red", linewidth=3.0, edgecolor="red")
     plt.annotate("Adam becomes CEO", xy=[2015.9, -0.05 * 10**8], xytext=[2014, -0.5]
      →* 10**8], arrowprops={
         "facecolor": "red", "arrowstyle": "->", "connectionstyle": "arc3"})
     plt.legend(["Earnings", "Mean Earnings (2014 through 2016)", "Mean Earnings⊔
     ⇔(2017 through 2019)"])
     plt.grid(True, alpha = 0.3)
     plt.title("AMC Yearly Earnings from 2014 through 2017")
     plt.xlabel("Year")
     plt.ylabel("Earnings (in hundreds of millions)")
```

```
plt.xticks([2014, 2015, 2016, 2017])
plt.savefig("plots/earnings.2014.2017.png")
plt.show()
```

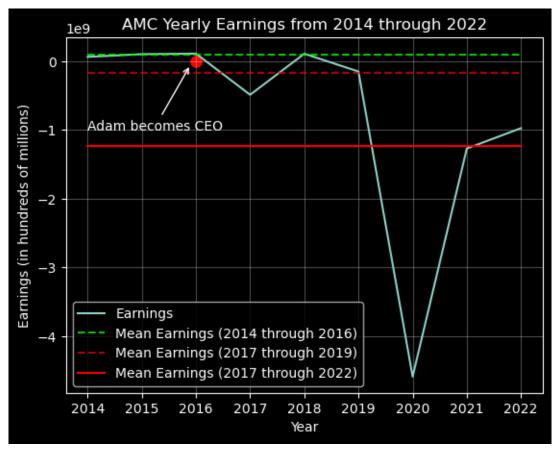


Zooming out for some context.

```
plt.title("AMC Yearly Earnings from 2014 through 2019")
plt.xlabel("Year")
plt.ylabel("Earnings (in hundreds of millions)")
plt.xticks([2014, 2015, 2016, 2017, 2018, 2019])
plt.savefig("plots/earnings.2014.2019.png")
plt.show()
```



The entire dataset.

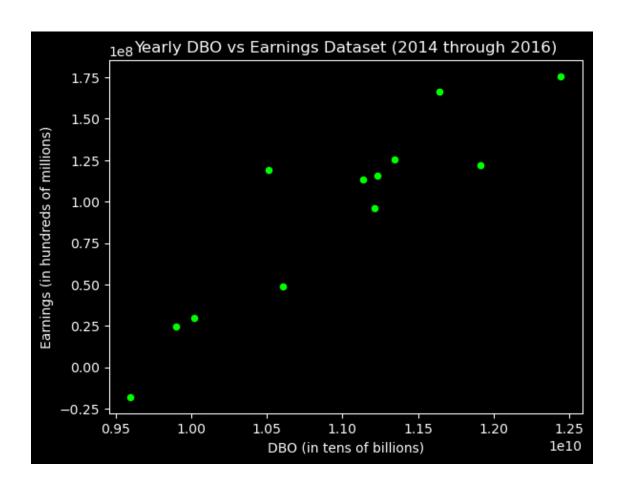


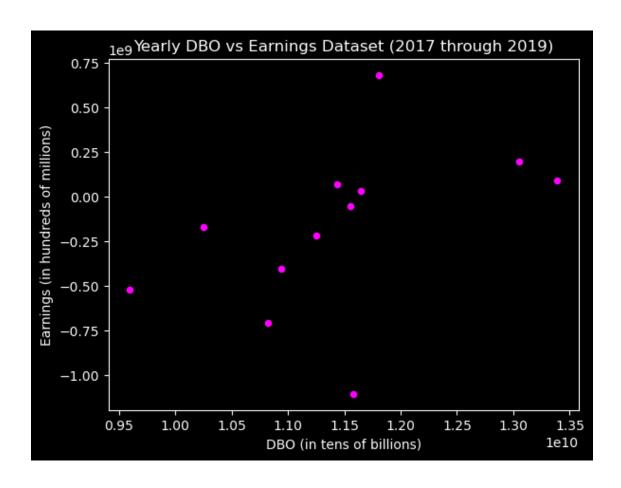
Drop 2020 Q1 outlier, and superfluous columns. Extrapolate quarterly to yearly values. Alias columns with x and y variables.

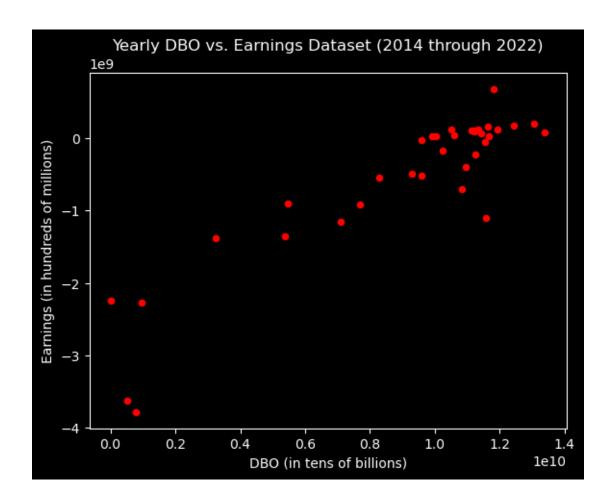
```
[]: columns = ["DBO gross", "earnings"]
try:
    df = df.drop(24)
```

```
df["DBO gross"] = df["DBO gross"] * 4
   df["earnings"] = df["earnings"] * 4
except KeyError: pass
df = df[columns]
x = df["DBO gross"]
y = df["earnings"]
print(df.describe())
df.loc[:11].plot.scatter("DBO gross", "earnings", color="lime")
plt.title("Yearly DBO vs Earnings Dataset (2014 through 2016)")
plt.xlabel("DBO (in tens of billions)")
plt.ylabel("Earnings (in hundreds of millions)")
plt.savefig("plots/dataset.2014.2016.png")
plt.show()
df.loc[12:23].plot.scatter("DBO gross", "earnings", color="magenta")
plt.title("Yearly DBO vs Earnings Dataset (2017 through 2019)")
plt.xlabel("DBO (in tens of billions)")
plt.ylabel("Earnings (in hundreds of millions)")
plt.savefig("plots/dataset.2017.2019.png")
plt.show()
df.plot.scatter("DBO gross", "earnings", color="red")
plt.title("Yearly DBO vs. Earnings Dataset (2014 through 2022)")
plt.xlabel("DBO (in tens of billions)")
plt.ylabel("Earnings (in hundreds of millions)")
plt.savefig("plots/dataset.2014.2022.png")
plt.show()
```

```
DBO gross
                        earnings
count 3.500000e+01 3.500000e+01
      9.074312e+09 -5.603539e+08
mean
      3.788194e+09 1.039427e+09
std
min
      1.890192e+07 -3.784400e+09
25%
      7.982850e+09 -9.022000e+08
    1.060793e+10 -5.400000e+07
50%
75%
     1.149479e+10 1.045160e+08
      1.338965e+10 6.824000e+08
max
```







3 Linear Regressions on the 3 Periods

```
z-scores
```

```
[]: %%latex

$$

\zeta = \frac{x - \mu}{\sigma}

$$
```

$$\zeta = \frac{x - \mu}{\sigma}$$

```
[]: zeta = lambda x: (x - x.mean()) / x.std()

df["z-scoreX1"], df["z-scoreY1"] = zeta(x.iloc[:12]), zeta(y.iloc[:12])

df["z-scoreX2"], df["z-scoreY2"] = zeta(x.iloc[12:24]), zeta(y.iloc[12:24])

df["z-scoreX3"], df["z-scoreY3"] = zeta(x), zeta(y)
```

Pearsons Correlation Coefficient

```
[]: %%latex
$$
\rho = \frac{ \sum{\zeta_x \zeta_y} }{n - 1}
$$
```

$$\rho = \frac{\sum \zeta_x \zeta_y}{n-1}$$

```
[]: r1 = (df["z-scoreX1"] * df["z-scoreY1"]).sum() / (len(df.loc[:11]) - 1)
    r2 = (df["z-scoreX2"] * df["z-scoreY2"]).sum() / (len(df.loc[12:23]) - 1)
    r3 = (df["z-scoreX3"] * df["z-scoreY3"]).sum() / (len(df) - 1)

print(f"For 2014 through 2016, Pearsons Correlation Coefficient is: {r1}")
    print(f"For 2017 through 2019, Pearsons Correlation Coefficient is: {r2}")
    print(f"For 2014 through 2022, Pearsons Correlation Coefficient is: {r3}")
```

For 2014 through 2016, Pearsons Correlation Coefficient is: 0.9118679351959351 For 2017 through 2019, Pearsons Correlation Coefficient is: 0.45365018248882316 For 2014 through 2022, Pearsons Correlation Coefficient is: 0.9066831913698027

The slope of the least-squares line

```
[]: %%latex
$$
  \beta = \frac{
     \sum{ \langle x - \bar{x} \rangle \langle y - \bar{y} \rangle }
}{
     \sum{ \langle x - \bar{x} \rangle^{2} }
}
```

$$\beta = \frac{\sum \langle x - \bar{x} \rangle \langle y - \bar{y} \rangle}{\sum \langle x - \bar{x} \rangle^2}$$

```
[]: slope = lambda x, y: ((x - x.mean()) * (y - y.mean())).sum() / ((x - x.mean())**2).sum()

df["b1"] = b1 = slope(x.iloc[:12], y.iloc[:12])

df["b2"] = b2 = slope(x.iloc[12:24], y.iloc[12:24])

df["b3"] = b3 = slope(x, y)
```

The y-intercept of the least-squares line

```
[]: %%latex
$$
   \alpha = \bar{y} - \beta \bar{x}
$$
```

```
\alpha = \bar{y} - \beta \bar{x}
```

```
[]: intercept = lambda x, y, b: y.mean() - b * x.mean()
    df["a1"] = a1 = intercept(x.iloc[:12], y.iloc[:12], b1)
    df["a2"] = a2 = intercept(x.iloc[12:24], y.iloc[12:24], b2)
    df["a3"] = a3 = intercept(x, y, b3)
```

The values for α and β

```
[]: print(f"""
For 2014 through 2016:
    a = {a1:,.0f}
    b = {b1}

For 2017 through 2019:
    a = {a2:,.0f}
    b = {b2}

For 2014 through 2022:
    a = {a3:,.0f}
    b = {b3}
    """)
```

```
For 2014 through 2016:

a = -598,645,528

b = 0.06309998813676994

For 2017 through 2019:

a = -2,482,569,804

b = 0.20161160108675694

For 2014 through 2022:

a = -2,817,870,262

b = 0.24878099226102765
```

The function for the least-squares line

```
[]: %%latex
$$
  \hat{y} = f \langle x \rangle = \alpha + \beta x
$$
```

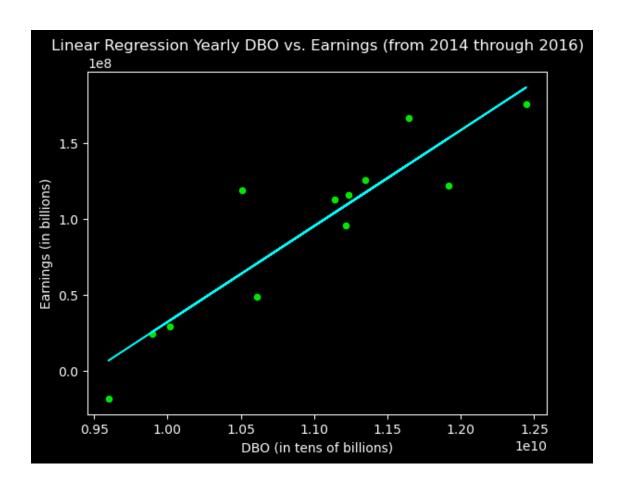
$$\hat{y} = f\langle x \rangle = \alpha + \beta x$$

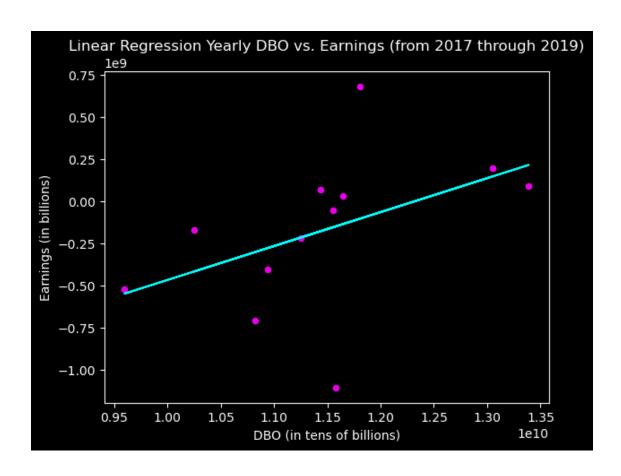
```
[]: hat = lambda a, b, x: a + b * x

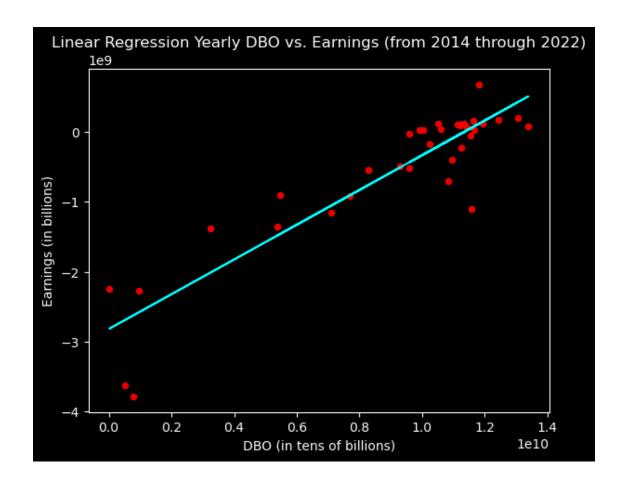
df["y_hat1"] = y_hat1 = hat(a1, b1, x.iloc[:12])
df["y_hat2"] = y_hat2 = hat(a2, b2, x.iloc[12:24])
df["y_hat3"] = y_hat3 = hat(a3, b3, x)
```

Linear regression plots

```
[]: df.iloc[:12].plot.scatter("DBO gross", "earnings", alpha = 0.9, color="lime")
    plt.plot(x.iloc[:12], y_hat1, linewidth=1.5, color = "cyan")
     plt.title("Linear Regression Yearly DBO vs. Earnings (from 2014 through 2016)")
     plt.xlabel("DBO (in tens of billions)")
     plt.ylabel("Earnings (in billions)")
     plt.savefig("plots/regression.2014.2016.png")
     plt.show()
     df.iloc[12:24].plot.scatter("DBO gross", "earnings", alpha = 0.9,
      ⇔color="magenta")
     plt.plot(x.iloc[12:24], y_hat2, linewidth=1.5, color = "cyan")
     plt.title("Linear Regression Yearly DBO vs. Earnings (from 2017 through 2019)")
     plt.xlabel("DBO (in tens of billions)")
     plt.ylabel("Earnings (in billions)")
     plt.savefig("plots/regression.2017.2019.png")
     plt.show()
     df.plot.scatter("DBO gross", "earnings", alpha = 0.9, color="red")
     plt.plot(x, y_hat3, linewidth=1.5, color = "cyan")
     plt.title("Linear Regression Yearly DBO vs. Earnings (from 2014 through 2022)")
     plt.xlabel("DBO (in tens of billions)")
     plt.ylabel("Earnings (in billions)")
     plt.savefig("plots/regression.2014.2022.png")
     plt.show()
```



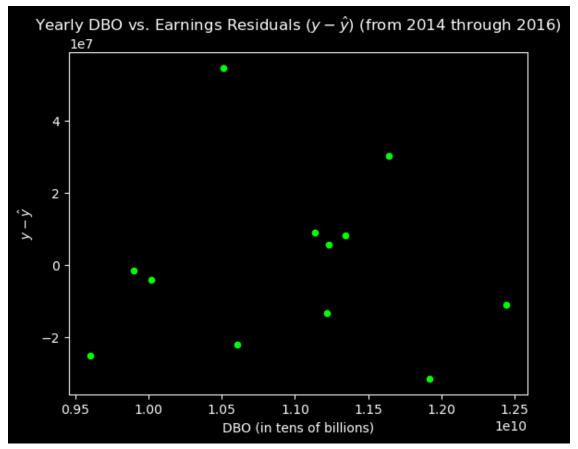


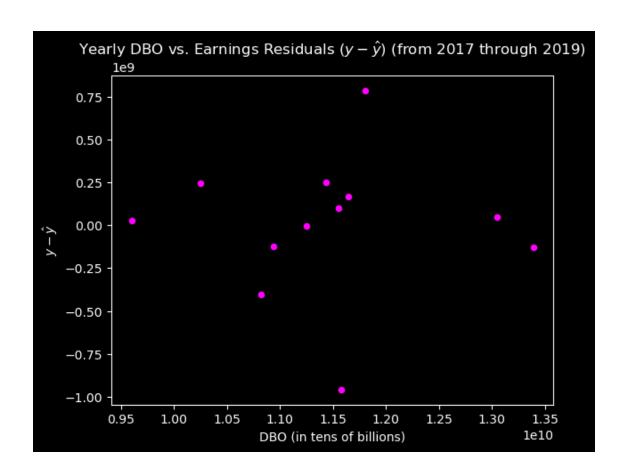


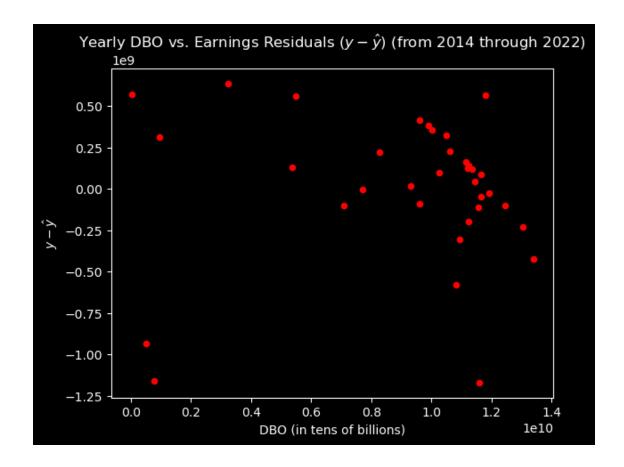
Residuals

```
[]: %%latex
$$
y - \hat{y}
$$
```

$$y - \hat{y}$$







The total sum of squares

```
[]: %%latex
$$
   \tau = \sum{ \langle y - \bar{y} \rangle^{2}}
$$
```

$$\tau = \sum{\langle y - \bar{y} \rangle^2}$$

```
[]: squares = lambda y: (y - y.mean())**2

df["squares1"] = squares1 = squares(y.iloc[:12])
    df["squares2"] = squares2 = squares(y.iloc[12:24])
    df["squares3"] = squares3 = squares(y)

t1 = squares1.sum()
    t2 = squares2.sum()
    t3 = squares3.sum()
```

The residual sum of squares

```
[]: %%latex
$$
  \epsilon = \sum{ \langle y - \hat{y} \rangle^{2}}
$$
```

$$\epsilon = \sum{\langle y - \hat{y} \rangle^2}$$

```
[]: df["residual squares1"] = df["residuals1"]**2
df["residual squares2"] = df["residuals2"]**2
df["residual squares3"] = df["residuals3"]**2

e1 = df["residual squares1"].sum()
e2 = df["residual squares2"].sum()
e3 = df["residual squares3"].sum()
```

Coefficient of Determination

```
[]: %%latex
$$
r^{2} = 1 - \frac{\epsilon}{\tau}
$$
```

$$r^2 = 1 - \frac{\epsilon}{\tau}$$

```
[]: r_2_1 = 1 - (e1 / t1)
r_2_2 = 1 - (e2 / t2)
r_2_3 = 1 - (e3 / t3)
print(f"""
For 2014 through 2016:
   The Coefficient of Determination is: {r_2_1}

For 2017 through 2019:
   The Coefficient of Determination is: {r_2_2}

For 2014 through 2022:
   The Coefficient of Determination is: {r_2_3}
""")
```

```
For 2014 through 2016:
The Coefficient of Determination is: 0.8315031312384981
```

For 2017 through 2019:

The Coefficient of Determination is: 0.2057984880721423

```
For 2014 through 2022:
The Coefficient of Determination is: 0.8220744095125301
```

The standard deviation about the least-squares line σ_{ϵ}

```
[]: %%latex
$$
\sigma_{\epsilon} = \sqrt{ \frac{\epsilon}{n - 2} }
$$
```

$$\sigma_\epsilon = \sqrt{\frac{\epsilon}{n-2}}$$

```
[]: rssd = lambda e, df: math.sqrt((e / (len(df) - 2)))
    sd1 = y.loc[:12].std()
    sd2 = y.loc[12:24].std()
    sd3 = y.std()
        = rssd(e1, df.iloc[:12])
    r1
    r2 = rssd(e2, df.iloc[12:24])
        = rssd(e3, df)
    r3
    print(f"""
    For 2014 through 2016:
     The Standard deviation about y is: {sd1:,.7f}
     The Standard deviation about the least-squares line: {r1:,.8f}
    For 2017 through 2019:
     The Standard deviation about y is: {sd2:,.7f}
     The Standard deviation about the least-squares line: {r2:,.8f}
    For 2014 through 2022:
     The Standard deviation about y is: {sd3:,.7f}
     The Standard deviation about the least-squares line: {r3:,.8f}
     """)
```

```
For 2014 through 2016:
The Standard deviation about y is: 59,186,777.5202432
The Standard deviation about the least-squares line: 25,554,998.54506667

For 2017 through 2019:
The Standard deviation about y is: 465,442,163.1875729
The Standard deviation about the least-squares line: 435,038,226.38255721
```

```
For 2014 through 2022:
The Standard deviation about y is: 1,039,426,652.4898386
The Standard deviation about the least-squares line: 445,036,411.52865213
```

The DBO minimum and maximum predictive range for all 3 models together is: minimum = 9,600,109,748 maximum = 12,445,502,384

4 Predictions

4.0.1 First, let's compare predictive models

```
[]: clean = lambda v: f"{v:,.0f}"

X = list(range(9600000000, 12500000000, 250000000))
Y1 = pd.Series([a1 + b1 * x for x in X])
Y2 = pd.Series([a2 + b2 * x for x in X])
Y3 = pd.Series([a3 + b3 * x for x in X])
X = [clean(x) for x in X]

mY1 = Y1.mean(), Y1.min(), Y1.max()
mY2 = Y2.mean(), Y2.min(), Y2.max()
mY3 = Y3.mean(), Y3.min(), Y3.max()

Y1 = [clean(y) for y in Y1]
Y2 = [clean(y) for y in Y2]
Y3 = [clean(y) for y in Y3]

columns = ["DBO", "Earnings (2014 - 2016)", "Earnings (2017 - 2019)", "Earnings_\( \text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\te
```

```
[]: bg = "#333333"
     font = "Arial"
     fig = df2img.plot_dataframe(predictions,
         title={"text": "All Predictions", "font_color": "purple", "font_size": 32,
                "font_family": font, "x": 0.41, "yanchor": "middle"},
         tbl_header = {"align": "center", "fill_color": bg, "font_color": L

¬"darkviolet",
                       "font_size": 20, "line": {"color": bg}, "font_family": font},
         tbl_cells = {"align": "center", "fill_color": bg, "font_color": "cyan",
                      "font_size": 16, "line": {"color": bg}, "height": 28, __

¬"font_family": font},
                      row_fill_color = (bg, "purple"),
         print_index = False,
         paper_bgcolor = bg,
         fig_size = (1000, 420),
         col_width = 6)
     df2img.save_dataframe(fig = fig, filename = "dataframes/all.predictions.png")
```

All Predictions								
DBO								
9,600,000,000	7,114,358	-547,098,434	-429,572,737					
9,850,000,000	22,889,355	-496,695,534	-367,377,489					
10,100,000,000	38,664,352	-446,292,633	-305,182,240					
10,350,000,000	54,439,349	-395,889,733	-242,986,992					
10,600,000,000	70,214,346	-345,486,833	-180,791,744					
10,850,000,000	85,989,343	-295,083,933	-118,596,496					
11,100,000,000	101,764,340	-244,681,032	-56,401,248					
11,350,000,000	117,539,337	-194,278,132	5,794,000					
11,600,000,000	133,314,334	-143,875,232	67,989,248					
11,850,000,000	149,089,331	-93,472,332	130,184,496					
12,100,000,000	164,864,329	-43,069,431	192,379,744					
12,350,000,000	180,639,326	7,333,469	254,574,992					

Clearly AMC was fundamentally in a much better position prior to Adam Aron becoming CEO. Since far less DBO was required to turn a profit.

```
[]: print(f"""
Approximate descriptive statistics of the predicted earnings.

For 2014 through 2016:
```

```
{mY1[0]:,.0f}
    mean:
            {mY1[1]:,.0f}
    min:
            {mY1[2]:,.0f}
    max:
For 2017 through 2019:
            {mY2[0]:,.0f}
    mean:
            {mY2[1]:,.0f}
    min:
            {mY2[2]:,.0f}
    max:
For 2014 through 2022:
            {mY3[0]:,.0f}
    mean:
            {mY3[1]:,.0f}
    min:
            {mY3[2]:,.0f}
    max:
""")
```

Approximate descriptive statistics of the predicted earnings.

For 2014 through 2016:

mean: 93,876,842 min: 7,114,358 max: 180,639,326

For 2017 through 2019:

mean: -269,882,483 min: -547,098,434 max: 7,333,469

For 2014 through 2022:

mean: -87,498,872 min: -429,572,737 max: 254,574,992

4.0.2 2023 Yearly Earnings Predictions from DBO Isolate

```
[]: minimum = int(max(df["DBO gross"].min(), 7500000000))
    maximum = int(df["DBO gross"].max())
    inc = 500000000
    X = list(range(minimum, maximum + inc, inc))
    Y = pd.Series([a3 + b3 * x for x in X])
    DB0
             = X
    Lowest
             = Y - (2 * r3)
             = Y - r3
    Low
    Earnings = Y
    High
            = Y + r3
    Highest = Y + (2 * r3)
    DB0
             = [clean(x) for x in DBO]
    Lowest = [clean(s) for s in Lowest]
             = [clean(s) for s in Low]
    Earnings = [clean(y) for y in Earnings]
    High = [clean(s) for s in High]
    Highest = [clean(s) for s in Highest]
    columns = ["DBO", "Lowest", "Low", "Earnings", "High", "Highest"]
    prediction2 = pd.DataFrame(np.array([DBO, Lowest, Low, Earnings, High, ⊔
      →Highest]).T,
                                columns = columns)
```

```
print_index = False,
  paper_bgcolor = bg,
  fig_size = (1000, 450),
  col_width = 6)

df2img.save_dataframe(fig = fig, filename = "dataframes/2023.prediction.png")
```

2023 Earnings from DBO Prediction							
DBO					Highest		
7,500,000,000	-1,842,085,643	-1,397,049,232	-952,012,820	-506,976,409	-61,939,997		
8,000,000,000	-1,717,695,147	-1,272,658,736	-827,622,324	-382,585,913	62,450,499		
8,500,000,000	-1,593,304,651	-1,148,268,240	-703,231,828	-258,195,417	186,840,995		
9,000,000,000	-1,468,914,155	-1,023,877,743	-578,841,332	-133,804,920	311,231,491		
9,500,000,000	-1,344,523,659	-899,487,247	-454,450,836	-9,414,424	435,621,987		
10,000,000,000	-1,220,133,163	-775,096,751	-330,060,340	114,976,072	560,012,483		
10,500,000,000	-1,095,742,667	-650,706,255	-205,669,844	239,366,568	684,402,980		
11,000,000,000	-971,352,170	-526,315,759	-81,279,347	363,757,064	808,793,476		
11,500,000,000	-846,961,674	-401,925,263	43,111,149	488,147,560	933,183,972		
12,000,000,000	-722,571,178	-277,534,767	167,501,645	612,538,056	1,057,574,468		
12,500,000,000	-598,180,682	-153,144,271	291,892,141	736,928,553	1,181,964,964		
13,000,000,000	-473,790,186	-28,753,774	416,282,637	861,319,049	1,306,355,460		
13,500,000,000	-349,399,690	95,636,722	540,673,133	985,709,545	1,430,745,956		

- The projected 2023 domestic box office is expected to be \$9B
- The 'Earnings' column is the prediction
- There is an approximate 68% chance that the actual earnings will fall within the range 'Low' to 'High'
- There is an approximate 98% chance that the actual earnings will fall within the range 'Lowest' to 'Highest'

This model has incredibly strong predictive power.

```
[]: df.to_csv("model.csv", index=True)
```

5 Float Size History Since 2016

```
[]: df = pd.read_csv("float_history.csv", index_col=0)

# 2016 to 2020 (excluding 2020) float size increase
f1 = df.loc[4].float / df.loc[0].float

# 2020 to 2023 float size increase
f2 = df.loc[11].float / df.loc[4].float

# Since 2016 float size increase
```

```
# If reverse split passes
f4 = 1.032 * 10**9 / df.loc[0].float

print(f"\nFrom 2016 through 2019 Adam increased the float {f1 * 100:,.2f}%")
print(f"From 2020 to 2023, only, Adam increased the float {f2 * 100:,.2f}%")
print(f"Adams total float increase is {f3 * 100:,.2f}%")
print(f"If rs-c passed the total float increase would be {f4 * 100:,.2f}%")

sbefore the split")
print(f"\nThat is nearly {47.7557:,.2f} times the size of the float "

"before Adam took over AMC.")
```

From 2016 through 2019 Adam increased the float 240.86% From 2020 to 2023, only, Adam increased the float 992.93% Adams total float increase is 2,391.58% If rs-c passed the total float increase would be 4,775.57% before the split

That is nearly 47.76 times the size of the float before Adam took over AMC.

```
[ ]: | # a = pi r^2
     \# a / pi = r^2
     # sqrt(a / pi) = r
     scale = 40000
     area = df.loc[0].float
     r1 = math.sqrt(area / math.pi) / scale
     r2 = math.sqrt((area * f1) / math.pi) / scale
     area = df.loc[4].float
     r3 = math.sqrt((area * f2) / math.pi) / scale
     area = df.loc[0].float
     r4 = math.sqrt((area * f4) / math.pi) / scale
     fig, ax = plt.subplots()
     patches = []
     c1 = Circle((r1*2, r1*2), r1)
     c2 = Circle((r2*.5*17, r2*1.4*6), r2)
     c3 = Circle((r3*.6*4, r3*.25*4), r3)
     c4 = Circle((r4*.2*4, r4*.3*4), r4)
     patches.extend([c1, c2, c3, c4])
     p = PatchCollection(patches, alpha=0.7)
     colors = [.72, .5, .2, .0, 1, .0]
     p.set_array(colors)
```

```
ax.add_collection(p)
fig.colorbar(p, ax=ax)
plt.title("Scaled Visualization of Float Sizes")
plt.savefig("plots/dilution.png")
plt.show()
```

