

**Theorem (2.2.18b).** *Let  $A$ ,  $B$  and  $C$  be sets.  $(A \cap B \cap C) \subseteq (A \cap B)$ .*

*Proof.* Let  $x$  be an element in  $(A \cap B \cap C)$ . The definition of this expression is  $(x \in A) \wedge (x \in B) \wedge (x \in C)$ . From that, obviously  $(x \in A) \wedge (x \in B)$ , being the definition for  $(A \cap B)$ . It necessarily follows that  $(A \cap B \cap C) \subseteq (A \cap B)$ . ■