

**Theorem (2.2.37a).** *Let  $A$  be a subset of the universal set  $U$ .  $A \oplus A = \emptyset$ .*

*Proof.* By Theorem 2.2.35,  $A \oplus A = (A \cup A) - (A \cap A)$ . By the set idempotent law, that is  $A - A$ , and by Theorem 2.2.19, equivalent to  $A \cap \overline{A}$ . It follows immediately from the set complementation law that  $A \oplus A = \emptyset$ . ■