

Theorem (2.2.13). *Let A and B be sets. $A \cap (A \cup B) = A$.*

Proof. Let x be an element in $A \cup (A \cap B)$. By the definitions for set union and set intersection we have $(x \in A) \wedge [(x \in A) \vee (x \in B)]$. Treating each parenthesized object as a discrete object we can immediately apply the logical law of absorption to this definition. The result is $x \in A$. Thus it follows directly from the definition that $A \cap (A \cup B) = A$; the consequence of which proves the absorption law for the intersection of a set with the union of itself and another set. ■