

**Theorem (2.2.7b).** *Let  $A$  be a set. The empty set dominates set intersection such that  $A \cap \emptyset = \emptyset$ .*

*Proof.* Let  $x$  be an element in  $A \cap \emptyset$ . By the definition for set intersection we have  $(x \in A) \wedge (x \in \emptyset)$ . We know that  $(x \in \emptyset) \equiv \perp$  because the empty set is empty. The logical law of domination gives us that  $(x \in A) \wedge \perp \equiv \perp$ . It immediately follows that  $(x \in A) \wedge (x \in \emptyset) \equiv (x \in \emptyset)$ , which is the definition of  $A \cap \emptyset = \emptyset$ . Thus proves the law of set domination for the intersection of sets. ■