

**Theorem (2.2.12).** *Let  $A$  and  $B$  be sets.  $A \cup (A \cap B) = A$ .*

*Proof.* Let  $x$  be an element in  $A \cup (A \cap B)$ . By the definitions for set union and set intersection we have  $(x \in A) \vee [(x \in A) \wedge (x \in B)]$ . Treating each parenthesized object as a discrete object we can immediately apply the logical law of absorption to this definition. The result is  $x \in A$ . Thus it follows directly from the definition that  $A \cup (A \cap B) = A$ ; the consequence of which proves the absorption law for the union of a set with the intersection of itself and another set. ■