

**Theorem (2.2.16d).** *Let  $A$  and  $B$  be sets.  $A \cap (B - A) = \emptyset$ .*

*Proof.* Let  $x$  be an element in  $A \cap (B - A)$ . Note that  $(B - A) \equiv (B \cap \overline{A})$ . Because set intersection is associative we can drop the parentheses, giving us  $A \cap B \cap \overline{A}$ . This is logically defined as  $(x \in A) \wedge (x \in B) \wedge (x \notin A) \equiv \perp$ . Because this statement is false  $\forall x$  in the domain,  $A \cap (B - A)$  is empty. ■