

**Theorem** (1.6.10). *The product of two rational numbers is rational.*

*Proof.* Let  $m$  and  $n$  be rational numbers. By definition there exist integers  $a$ ,  $b$ ,  $c$ , and  $d$  such that  $m = \frac{a}{b}$  and  $n = \frac{c}{d}$ . The product of  $m$  and  $n$  is  $\frac{ac}{bd}$ . Since the product of integers is an integer,  $ac$  and  $bd$  are integers. Thus  $mn$  is rational by definition. ■