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**Algorithm 3.1.59** Solve the deferred acceptance/stable marriage problem.  $M_x$  is a preference list such that  $M_{x_1}$  is a man, and the elements  $M_{x_2}, M_{x_3}, \dots, M_{x_y}$  are ranked preference women. The output match list is the most stable system.

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1: procedure DEFERRED ACCEPTANCE( $M_1, M_2, \dots, M_n$ : a list of prefer-
   ence lists;  $W_1, W_2, \dots, W_n$ : a list of preference lists)
2:    $match\ list \leftarrow$  empty list
3:    $P \leftarrow \emptyset$ 
4:    $\odot \leftarrow 0$ 
5:   while  $\odot \neq n$  do
6:     for  $\Delta = 1$  to  $n$  do
7:        $man \leftarrow M_{\Delta_1}$ 
8:       if  $man \notin \{m | \langle m, w \rangle \in match\ list\}$  then
9:          $lady \leftarrow M_{\Delta_2}$ 
10:        if  $lady \in P$  then  $\triangleright$   $lady$  already paired.
11:           $\forall \phi([ (0 < \phi \leq \odot) \in \mathbb{N} \wedge (match\ list_{\phi_2} = lady)]) \implies$ 
12:             $preference \leftarrow match\ list_{\phi}$ 
13:           $\forall \lambda([ (0 < \lambda \leq n) \in \mathbb{N} \wedge (W_{\lambda} = lady)]) \implies \delta \leftarrow \lambda$ 
14:           $\forall \lambda([ (1 < \lambda \leq n) \in \mathbb{N} \wedge$ 
15:             $\{(W_{\delta_{\lambda}} = preference) \vee (W_{\delta_{\lambda}} = man)\}]) \implies$ 
16:             $preference \leftarrow W_{\delta_{\lambda}}$ 
17:           $match\ list_{\phi} \leftarrow \langle preference, lady \rangle$ 
18:        else
19:           $\odot += 1$ 
20:           $match\ list_{\odot} \leftarrow \langle man, lady \rangle$ 
21:           $P \leftarrow P \cup \{lady\}$ 
22:           $M_{\Delta} \leftarrow M_{\Delta_1}, M_{\Delta_3}, M_{\Delta_4}, \dots, M_{\Delta_{(|M_{\Delta}| - 1)}}$ 
23:        end if
24:      end if
25:    end for
26:  end while
27:  return  $match\ list$ 
28: end procedure

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