

**Theorem (2.2.11b).** *Let  $A$  and  $B$  be sets. The intersection of  $A$  and  $B$  is commutative.*

*Proof.* Let  $x$  be an element in  $A \cap B$ . By the definition of intersection,  $(x \in A) \wedge (x \in B)$ . Because logical conjunction is commutative, the definition is equivalently stated as  $(x \in B) \wedge (x \in A)$ . Meaning that  $x \in (B \cap A)$ . So  $A \cap B = B \cap A$ , and indeed the intersection of two sets is commutative. ■