Algorithm 3.1.28 Locate an element from a finite list of increasing integers by recursively splitting the list into four search space partitions.

```
1: procedure QUATERNARY SEARCH(term: integer; a_0, a_1, \ldots, a_n: finite
    list of increasing integers; index = 0: integer)
        endpoint \leftarrow \lfloor \frac{n}{4} \rfloor
 2:
        if endpoint = 0 then
                                              ▶ Bottom of recursion stack reached
 3:
            if term = a_0 then
 4:
                return index
 5:
            else if term = a_1 then
 6:
 7:
                return index + 1
 8:
            else
                return index + 2
 9:
            end if
10:
        else if term < a_{endpoint} then
                                                      ▶ Recur into search partitions
11:
            return QUATERNARY SEARCH(
12:
                                          term,
                                          a_0, a_1, \ldots, a_{(endpoint-1)},
                                          index)
        else if a_{endpoint} \leq term < a_{(endpoint \times 2)} then
13:
            return QUATERNARY SEARCH(
14:
                                          term,
                                          a_{endpoint}, a_{(endpoint+1)}, \dots, a_{(endpoint \times 2)-1},
                                          index + endpoint)
15:
        else if a_{(endpoint \times 2)} \le term < a_{(endpoint \times 3)} then
            return QUATERNARY SEARCH(
16:
                                          term,
                                          a_{(endpoint \times 2)}, a_{(endpoint \times 2)+1)}, \dots, a_{(endpoint \times 3)-1},
                                          index + (endpoint \times 2)
        else if a_{(endpoint \times 3)} \leq term then
17:
            return QUATERNARY SEARCH(
18:
                                          term,
                                          a_{(endpoint\times3)}, a_{(endpoint\times3)+1}, \dots, a_n,
                                          index + (endpoint \times 3)
        else
19:
                                                   ▶ The term was never in the list
20:
            return \perp
        end if
22: end procedure
```