# Lesson 11

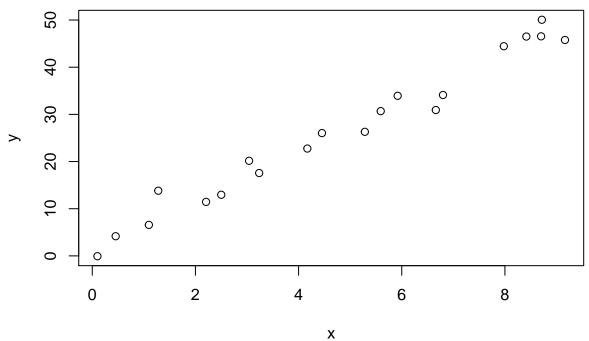
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#### Influence 1 (no influential points)

Load the influence1 data. Create a scatterplot of the data.

```
influence1 <- read.table("./Data/influence1.txt", header=T)
attach(influence1)
plot(x, y)</pre>
```



detach(influence1)

#### Influence 2 (outlier, low leverage, not influential)

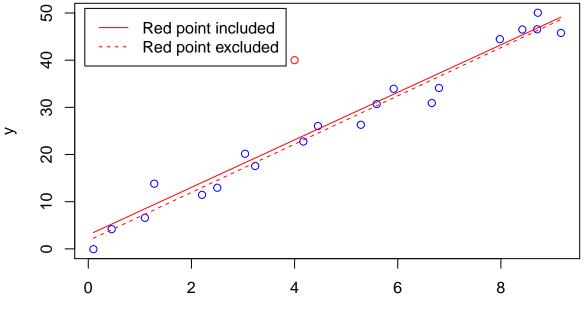
Load the influence data. Create a scatterplot of the data. Fit a simple linear regression model to all the data. Fit a simple linear regression model to the data excluding observation #21. Add regression lines to the scatterplot, one for each model. Calculate leverages, standardized residuals, studentized residuals, DFFITS, Cook's distances.

```
influence2 <- read.table("./Data/influence2.txt", header=T)
attach(influence2)
plot(x, y)</pre>
```

```
50
                                                                       0
                                                                    000
4
                                    0
                                                        0
30
                                               0
                                                        0
                                             0
                                       0
                                     0
20
                             0
                              O
                      0 0
               0
10
              0
         0
       0
      0
                     2
                                    4
                                                   6
                                                                  8
                                        Χ
```

```
model.1 \leftarrow lm(y \sim x)
summary(model.1)
##
## Call:
## lm(formula = y \sim x)
##
## Residuals:
     Min
              1Q Median
                            3Q
                                  Max
## -5.587 -2.620 -1.077 1.157 16.893
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 2.9576
                            2.0091
                                     1.472
                                              0.157
                            0.3633 13.865 2.18e-11 ***
## x
                 5.0373
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.711 on 19 degrees of freedom
## Multiple R-squared: 0.9101, Adjusted R-squared: 0.9053
## F-statistic: 192.2 on 1 and 19 DF, p-value: 2.179e-11
#
              Estimate Std. Error t value Pr(>|t|)
                                   1.472
# (Intercept) 2.9576
                           2.0091
# x
                5.0373
                           0.3633 13.865 2.18e-11 ***
# Residual standard error: 4.711 on 19 degrees of freedom
# Multiple R-squared: 0.9101, Adjusted R-squared: 0.9053
# F-statistic: 192.2 on 1 and 19 DF, p-value: 2.179e-11
model.2 <- lm(y ~ x, subset=1:20) # exclude obs #21
summary(model.2)
```

```
##
## Call:
## lm(formula = y \sim x, subset = 1:20)
##
## Residuals:
                1Q Median
                                3Q
##
       Min
                                       Max
   -4.8911 -1.7580 -0.0998 1.7552 5.5365
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 1.7322
                            1.1205
                                     1.546
                            0.2003 25.551 1.35e-15 ***
                 5.1169
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.592 on 18 degrees of freedom
## Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
## F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
              Estimate Std. Error t value Pr(>|t|)
                           1.1205
# (Intercept)
                1.7322
                                    1.546
# x
                5.1169
                           0.2003 25.551 1.35e-15 ***
# Residual standard error: 2.592 on 18 degrees of freedom
# Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
# F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
plot(x=x, y=y, col=ifelse(Row<=20, "blue", "red"),</pre>
     panel.last = c(lines(sort(x), fitted(model.1)[order(x)], col="red"),
                    lines(sort(x[-21]), fitted(model.2)[order(x[-21])],
                          col="red", lty=2)))
legend("topleft", col="red", lty=c(1,2),
       inset=0.02, legend=c("Red point included", "Red point excluded"))
```



Χ

```
lev <- hatvalues(model.1)</pre>
round(lev, 6)
                  3
                         4
                               5
                                      6
## 0.176297 0.157454 0.127015 0.119313 0.086145 0.077744 0.065028 0.061276
## 9 10 11 12 13 14 15 16
## 0.048147 0.049628 0.049313 0.051829 0.055760 0.069310 0.072580 0.109616
## 17 18 19
                         20 21
## 0.127489 0.141136 0.140453 0.163492 0.050974
# 1 2 3 4 5 6 7 8 9
# 0.176297 0.157454 0.127015 0.119313 0.086145 0.077744 0.065028 0.061276 0.048147
# 10 11 12 13 14 15 16 17 18
# 0.049628 0.049313 0.051829 0.055760 0.069310 0.072580 0.109616 0.127489 0.141136
# 19 20 21
# 0.140453 0.163492 0.050974
sum(lev) # 2
## [1] 2
sta <- rstandard(model.1)</pre>
round(sta, 6)
                         4
             2 3
                                   5
## -0.826351 -0.249154 -0.435445 0.998187 -0.581904 -0.574462 0.413791 -0.371226
   9 10 11 12 13 14 15
## 0.139767 -0.262514 -0.713173 -0.095897 0.252734 -1.229353 -0.683161 0.292644
   17 18 19 20
## 0.262144 0.731458 -0.055615 -0.776800 3.681098
# 1 2 3 4 5 6 7 8
# -0.826351 -0.249154 -0.435445 0.998187 -0.581904 -0.574462 0.413791 -0.371226
# 9 10 11 12 13 14 15 16
# 0.139767 -0.262514 -0.713173 -0.095897 0.252734 -1.229353 -0.683161 0.292644
# 17 18 19 20 21
# 0.262144 0.731458 -0.055615 -0.776800 3.681098
stu <- rstudent(model.1)</pre>
round(stu, 6)
              2
                    3
                            4
                                   5
                                                 7
## -0.819167 -0.242905 -0.425962 0.998087 -0.571499 -0.564060 0.404582 -0.362643
  9 10 11 12 13 14 15
## 0.136110 -0.255977 -0.703633 -0.093362 0.246408 -1.247195 -0.673261 0.285483
##
  17 18 19 20
## 0.255615 0.722190 -0.054136 -0.768382 6.690129
# 1 2 3 4 5 6 7 8
# -0.819167 -0.242905 -0.425962 0.998087 -0.571499 -0.564060 0.404582 -0.362643
  9 10 11 12 13 14 15 16
#
  0.136110 \ -0.255977 \ -0.703633 \ -0.093362 \ 0.246408 \ -1.247195 \ -0.673261 \ 0.285483
# 17 18 19 20 21
# 0.255615 0.722190 -0.054136 -0.768382 6.690129
dffit <- dffits(model.1)</pre>
round(dffit, 6)
```

```
##
                      2
                                 3
                                                      5
                                                                6
           1
   -0.378974 -0.105007 -0.162478 0.367368 -0.175466 -0.163769
                                                                  0.106698 -0.092652
##
##
           9
                     10
                               11
                                          12
                                                     13
                                                               14
                                                                          15
                                              0.059879 -0.340354 -0.188345
##
    0.030612 -0.058495 -0.160254 -0.021828
                                                                              0.100168
##
          17
                     18
                               19
                                          20
                                                     21
##
    0.097710
              0.292757 -0.021884 -0.339696
                                              1.550500
#
          1
                     2
                               3
                                                     5
                                                                6
                                                                                     8
                                          4
                                                                   0.106698 -0.092652
#
  -0.378974 -0.105007 -0.162478
                                   0.367368
                                            -0.175466 -0.163769
#
          9
                                                    13
                                                                                    16
                    10
                              11
                                         12
                                                              14
                                                                         15
#
   0.030612 -0.058495 -0.160254 -0.021828
                                             0.059879 -0.340354 -0.188345 0.100168
#
         17
                    18
                              19
                                         20
                                                    21
   0.097710
             0.292757 -0.021884 -0.339696
cook <- cooks.distance(model.1)</pre>
round(cook, 6)
                    2
##
                             3
                                       4
                                                5
                                                          6
## 0.073076 0.005800 0.013794 0.067493 0.015960 0.013909 0.005954 0.004498
##
                   10
                            11
                                      12
                                               13
                                                         14
                                                                            16
## 0.000494 0.001799 0.013191 0.000251 0.001886 0.056275 0.018262 0.005272
##
                   18
         17
                            19
## 0.005021 0.043960 0.000253 0.058968 0.363914
                   2
                            3
#
                                                5
# 0.073076 0.005800 0.013794 0.067493 0.015960 0.013909 0.005954 0.004498
#
         9
                  10
                           11
                                     12
                                              13
                                                        14
                                                                  15
                                                                           16
#
 0.000494 0.001799 0.013191 0.000251 0.001886 0.056275 0.018262 0.005272
        17
                  18
                           19
                                     20
                                              21
# 0.005021 0.043960 0.000253 0.058968 0.363914
detach(influence2)
```

#### Influence 3 (high leverage, not an outlier, not influential)

Load the influence3 data. Create a scatterplot of the data. Fit a simple linear regression model to all the data. Fit a simple linear regression model to the data excluding observation #21. Add regression lines to the scatterplot, one for each model. Calculate leverages, DFFITS, Cook's distances.

```
influence3 <- read.table("./Data/influence3.txt", header=T)
attach(influence3)
plot(x, y)</pre>
```

```
0
     9
     50
                                                   0000
     40
                              000
     30
     20
                           0
                      00
                  0
     10
                 0
              0
                      2
            0
                                4
                                          6
                                                    8
                                                             10
                                                                       12
                                                                                 14
                                               Χ
model.1 \leftarrow lm(y \sim x)
```

```
summary(model.1)
##
## Call:
## lm(formula = y \sim x)
##
## Residuals:
      Min
##
               1Q Median
                               ЗQ
                                      Max
## -4.3636 -1.8607 -0.5376 2.2987 5.0434
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                2.4679
                           1.0757
                                    2.294
## (Intercept)
                                            0.0333 *
## x
                4.9272
                           0.1719 28.661
                                            <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.709 on 19 degrees of freedom
## Multiple R-squared: 0.9774, Adjusted R-squared: 0.9762
## F-statistic: 821.4 on 1 and 19 DF, p-value: < 2.2e-16
             Estimate Std. Error t value Pr(>|t|)
# (Intercept)
              2.4679
                          1.0757
                                  2.294
                                          0.0333 *
# x
               4.9272
                          0.1719 28.661
                                           <2e-16 ***
# Residual standard error: 2.709 on 19 degrees of freedom
# Multiple R-squared: 0.9774, Adjusted R-squared: 0.9762
\# F-statistic: 821.4 on 1 and 19 DF, p-value: < 2.2e-16
model.2 <- lm(y ~ x, subset=1:20) # exclude obs #21
summary(model.2)
```

```
##
## Call:
## lm(formula = y \sim x, subset = 1:20)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -4.8911 -1.7580 -0.0998 1.7552 5.5365
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.7322
                           1.1205
                                   1.546
                           0.2003 25.551 1.35e-15 ***
                5.1169
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.592 on 18 degrees of freedom
## Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
## F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
             Estimate Std. Error t value Pr(>|t|)
                          1.1205
# (Intercept)
              1.7322
                                  1.546
# x
                5.1169
                          0.2003 25.551 1.35e-15 ***
# Residual standard error: 2.592 on 18 degrees of freedom
# Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
# F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
plot(x=x, y=y, col=ifelse(Row<=20, "blue", "red"),</pre>
     panel.last = c(lines(sort(x), fitted(model.1)[order(x)], col="red"),
                   lines(sort(x[-21]), fitted(model.2)[order(x[-21])],
                         col="red", lty=2)))
legend("topleft", col="red", lty=c(1,2),
      inset=0.02, legend=c("Red point included", "Red point excluded"))
```

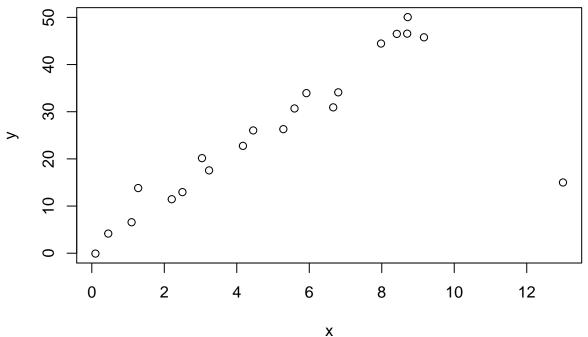
```
Red point included
                Red point excluded
    50
    40
    20
    10
                 2
         0
                                6
                                        8
                                                10
                                                       12
                                                               14
                                    Χ
lev <- hatvalues(model.1)</pre>
round(lev, 6)
                      3
       1
               2
                             4
                                     5
## 0.153481 0.139367 0.116292 0.110382 0.084374 0.077557 0.066879 0.063589
## 9
              10 11
                             12 13 14
                                              15
## 0.050033 0.052121 0.047632 0.048156 0.049557 0.055893 0.057574 0.078121
       17
              18
                     19
                             20
## 0.088549 0.096634 0.096227 0.110048 0.357535
# 1 2 3
                            4 5 6 7 8 9
# 0.153481 0.139367 0.116292 0.110382 0.084374 0.077557 0.066879 0.063589 0.050033
# 10 11 12 13 14 15 16 17 18
# 0.052121 0.047632 0.048156 0.049557 0.055893 0.057574 0.078121 0.088549 0.096634
# 0.096227 0.110048 0.357535
sum(lev) # 2
## [1] 2
dffit <- dffits(model.1)</pre>
round(dffit, 6)
                2
                        3
                                         5
                                                         7
## -0.525036 -0.083882 -0.182326 0.758981 -0.218230 -0.201548 0.277728 -0.082294
##
      9
                                        13
                                                14
               10
                        11
                                12
                                                        15
  0.138643 -0.022210 -0.184873 0.055235 0.197411 -0.424484 -0.172490 0.299173
                        19
##
       17
              18
                                20
   0.309606 \quad 0.630493 \quad 0.149474 \quad -0.250945 \quad -1.238416
  1 2 3 4 5 6 7
# -0.525036 -0.083882 -0.182326 0.758981 -0.218230 -0.201548 0.277728 -0.082294
  9 10 11 12 13 14 15 16
 0.138643 -0.022210 -0.184873 0.055235 0.197411 -0.424484 -0.172490 0.299173
  17 18 19 20 21
```

```
cook <- cooks.distance(model.1)</pre>
round(cook, 6)
                  2
                           3
                                    4
                                             5
                                                      6
                                                               7
                                                                       8
## 0.134157 0.003705 0.017302 0.241690 0.024433 0.020879 0.038412 0.003555
##
                 10
                                                     14
                          11
                                   12
                                            13
                                                              15
##
  0.009943\ 0.000260\ 0.017379\ 0.001605\ 0.019748\ 0.081344\ 0.015289\ 0.044620
                                   20
        17
                 18
                          19
                                            21
##
  0.047961 0.173901 0.011656 0.032322 0.701965
#
                 2
                          3
                                            5
# 0.134157 0.003705 0.017302 0.241690 0.024433 0.020879 0.038412 0.003555
                                           13
                                                             15
#
        9
                10
                         11
                                  12
                                                    14
                                                                      16
# 0.009943 0.000260 0.017379 0.001605 0.019748 0.081344 0.015289 0.044620
       17
                18
                         19
                                  20
                                           21
# 0.047961 0.173901 0.011656 0.032322 0.701965
detach(influence3)
```

## Influence 4 (outlier, high leverage, influential)

Load the influence data. Create a scatterplot of the data. Fit a simple linear regression model to all the data. Fit a simple linear regression model to the data excluding observation #21. Add regression lines to the scatterplot, one for each model. Calculate leverages, DFFITS, Cook's distances.

```
influence4 <- read.table("./Data/influence4.txt", header=T)
attach(influence4)
plot(x, y)</pre>
```



```
model.1 <- lm(y ~ x)
summary(model.1)</pre>
```

```
##
## Call:
## lm(formula = y \sim x)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -36.662 -3.851 1.063 5.779 12.617
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                8.5046
                           4.2224
                                    2.014 0.058374 .
                                    4.838 0.000114 ***
                3.3198
                           0.6862
## x
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 10.45 on 19 degrees of freedom
## Multiple R-squared: 0.5519, Adjusted R-squared: 0.5284
## F-statistic: 23.41 on 1 and 19 DF, p-value: 0.0001143
             Estimate Std. Error t value Pr(>|t|)
# (Intercept)
              8.5046
                          4.2224
                                   2.014 0.058374 .
# x
               3.3198
                          0.6862
                                   4.838 0.000114 ***
# Residual standard error: 10.45 on 19 degrees of freedom
# Multiple R-squared: 0.5519, Adjusted R-squared: 0.5284
# F-statistic: 23.41 on 1 and 19 DF, p-value: 0.0001143
model.2 <- lm(y ~ x, subset=1:20) # exclude obs #21
summary(model.2)
##
## Call:
## lm(formula = y \sim x, subset = 1:20)
## Residuals:
               1Q Median
      Min
                               3Q
                                      Max
## -4.8911 -1.7580 -0.0998 1.7552 5.5365
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.7322
                           1.1205
                                   1.546
## x
                5.1169
                           0.2003 25.551 1.35e-15 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.592 on 18 degrees of freedom
## Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
## F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
             Estimate Std. Error t value Pr(>|t|)
# (Intercept) 1.7322
                         1.1205
                                  1.546
                                             0.14
# x
               5.1169
                          0.2003 25.551 1.35e-15 ***
# ---
# Residual standard error: 2.592 on 18 degrees of freedom
# Multiple R-squared: 0.9732, Adjusted R-squared: 0.9717
```

```
\# F-statistic: 652.8 on 1 and 18 DF, p-value: 1.353e-15
plot(x=x, y=y, col=ifelse(Row<=20, "blue", "red"),</pre>
     panel.last = c(lines(sort(x), fitted(model.1)[order(x)], col="red"),
                    lines(sort(x[-21]), fitted(model.2)[order(x[-21])],
                          col="red", lty=2)))
legend("topleft", col="red", lty=c(1,2),
      inset=0.02, legend=c("Red point included", "Red point excluded"))
     50
                                                     0,000
                    Red point included
                    Red point excluded
     4
     30
     20
                                                                               0
     10
                      2
           0
                                4
                                           6
                                                     8
                                                               10
                                                                          12
                                              Χ
lev <- hatvalues(model.1)</pre>
round(lev, 6)
         1
                   2
                            3
                                     4
                                              5
                                                       6
                                                                7
## 0.158964 0.143985 0.119522 0.113263 0.085774 0.078589 0.067369 0.063924
                                    12
                  10
                           11
                                             13
                                                      14
## 0.049897 0.052019 0.047667 0.048354 0.049990 0.057084 0.058943 0.081446
                  18
                                    20
         17
                           19
## 0.092800 0.101587 0.101146 0.116146 0.311532
#
        1
                  2
                           3
                                             5
                                                  6
                                                         7
# 0.158964 0.143985 0.119522 0.113263 0.085774 0.078589 0.067369 0.063924 0.049897
                         12
                                  13
                                            14
                                                15
                                                              16
                                                                       17
        10
                11
# 0.052019 0.047667 0.048354 0.049990 0.057084 0.058943 0.081446 0.092800 0.101587
        19
                 20
# 0.101146 0.116146 0.311532
sum(lev) # 2
## [1] 2
dffit <- dffits(model.1)</pre>
round(dffit, 6)
##
## -0.402761 -0.243756 -0.205848
                                      0.037612 -0.131355 -0.109593
```

0.040473

```
##
            8
                                   10
                                               11
                                                           12
                                                                       13
                                                                                   14
                             0.009181
##
    -0.042401
                 0.060224
                                         0.005430
                                                     0.078165
                                                                0.127828
                                                                            0.007230
##
           15
                       16
                                   17
                                               18
                                                           19
                                                                       20
                                                                                   21
     0.073067
                 0.280501
                             0.323599
                                         0.436114
                                                     0.308869
                                                                0.249206 -11.467011
##
#
           1
                      2
                                  3
                                                          5
                                                                      6
#
  -0.402761
              -0.243756
                          -0.205848
                                       0.037612
                                                 -0.131355
                                                             -0.109593
                                                                          0.040473
#
          8
                      9
                                 10
                                             11
                                                         12
                                                                     13
                                                                                 14
#
  -0.042401
                           0.009181
                                       0.005430
                                                   0.078165
                                                              0.127828
                                                                          0.007230
               0.060224
#
         15
                     16
                                 17
                                             18
                                                                     20
                                                                                 21
                                                         19
   0.073067
                           0.323599
                                                              0.249206 -11.467011
#
               0.280501
                                       0.436114
                                                   0.308869
cook <- cooks.distance(model.1)</pre>
round(cook, 6)
                    2
                              3
                                                 5
##
                                        4
                                                           6
                                                                              8
## 0.081718 0.030755 0.021983 0.000746 0.009014 0.006290 0.000863 0.000947
                   10
                             11
                                       12
                                                13
                                                          14
                                                                              16
## 0.001907 0.000044 0.000016 0.003203 0.008478 0.000028 0.002804 0.039575
         17
                   18
                             19
                                       20
## 0.052293 0.091802 0.048085 0.031938 4.048013
                   2
                             3
#
          1
                                                5
# 0.081718 0.030755 0.021983 0.000746 0.009014 0.006290 0.000863 0.000947
                  10
                            11
                                     12
                                               13
                                                         14
                                                                   15
                                                                            16
# 0.001907 0.000044 0.000016 0.003203 0.008478 0.000028 0.002804 0.039575
        17
                  18
                            19
                                     20
                                               21
# 0.052293 0.091802 0.048085 0.031938 4.048013
detach(influence4)
```

# Foot length and height (outlier, high leverage, influential)

Load the height\_foot data. Create a scatterplot of the data. Fit a simple linear regression model to all the data. Fit a simple linear regression model to the data excluding observation #28. Calculate DFFITS and Cook's distance for obs #28.

```
heightfoot <- read.table("./Data/height_foot.txt", header=T)
attach(heightfoot)
plot(height, foot)</pre>
```

```
0
31
                                              0
                                                          0
29
                                  000 0
                   0
                          0
                                                  0
28
                              00
                          8
                              0
                                  8
27
         0
                                                                             0
                          0
                       0
       0
                       0
25
               0
                   0
                      70
                                         75
                                                             80
                                       height
```

```
model.1 <- lm(foot ~ height)
summary(model.1)</pre>
```

```
##
## Call:
## lm(formula = foot ~ height)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -3.5447 -0.8100 0.1903 0.7897
                                   2.3559
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.93577
                          4.43778
                                    2.464 0.019477 *
## height
               0.23344
                          0.06151
                                    3.795 0.000643 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.286 on 31 degrees of freedom
## Multiple R-squared: 0.3173, Adjusted R-squared: 0.2952
## F-statistic: 14.41 on 1 and 31 DF, p-value: 0.0006428
             Estimate Std. Error t value Pr(>|t|)
# (Intercept) 10.93577
                         4.43778
                                   2.464 0.019477 *
                                   3.795 0.000643 ***
# height
              0.23344
                          0.06151
# Residual standard error: 1.286 on 31 degrees of freedom
# Multiple R-squared: 0.3173, Adjusted R-squared: 0.2952
# F-statistic: 14.41 on 1 and 31 DF, p-value: 0.0006428
which(height>80) # 28
```

## [1] 28

```
model.2 <- lm(foot ~ height, subset=(1:33)[-28]) # exclude obs #28
summary(model.2)
##
## Call:
## lm(formula = foot ~ height, subset = (1:33)[-28])
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    3Q
                                            Max
## -1.74925 -0.81825 0.07875 0.58075
                                        2.25075
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.25313
                           4.33232
                                     0.058
                                              0.954
               0.38400
                           0.06038
                                     6.360 5.12e-07 ***
## height
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.028 on 30 degrees of freedom
## Multiple R-squared: 0.5741, Adjusted R-squared: 0.5599
## F-statistic: 40.45 on 1 and 30 DF, p-value: 5.124e-07
              Estimate Std. Error t value Pr(>|t|)
# (Intercept) 0.25313
                          4.33232
                                    0.058
                                             0.954
# height
               0.38400
                          0.06038
                                    6.360 5.12e-07 ***
# ---
# Residual standard error: 1.028 on 30 degrees of freedom
# Multiple R-squared: 0.5741, Adjusted R-squared: 0.5599
# F-statistic: 40.45 on 1 and 30 DF, p-value: 5.124e-07
dffit <- dffits(model.1)</pre>
dffit[28] # -3.200223
          28
##
## -3.200223
cook <- cooks.distance(model.1)</pre>
cook[28] # 3.274466
##
         28
## 3.274466
detach(heightfoot)
```

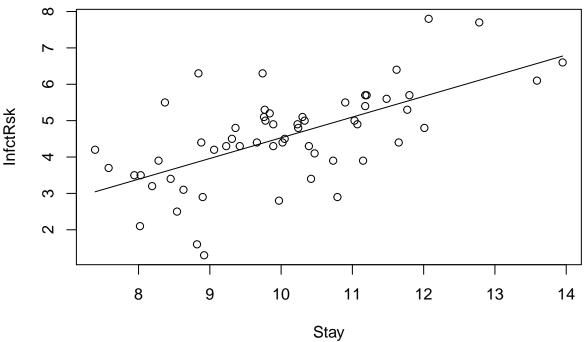
## Hospital infection risk (two outliers, high leverages)

Load the infection risk data. Fit a simple linear regression model to all the data. Create a scatterplot of the data and add the regression line. Display influence measures for influential points, including DFFITS, Cook's distances, and leverages (hat).

```
infectionrisk <- read.table("./Data/infectionrisk.txt", header=T)
attach(infectionrisk)

model <- lm(InfctRsk ~ Stay)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = InfctRsk ~ Stay)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
  -2.6145 -0.4660 0.1388 0.4970
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.15982
                          0.95580 -1.213
                          0.09416
                                    6.041 1.3e-07 ***
## Stay
               0.56887
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.024 on 56 degrees of freedom
## Multiple R-squared: 0.3946, Adjusted R-squared: 0.3838
## F-statistic: 36.5 on 1 and 56 DF, p-value: 1.302e-07
plot(x=Stay, y=InfctRsk,
    panel.last = lines(sort(Stay), fitted(model)[order(Stay)]))
                                                            0
                                                                   0
```



summary(influence.measures(model))

```
## Potentially influential observations of
    lm(formula = InfctRsk ~ Stay) :
##
##
     dfb.1_ dfb.Stay dffit cov.r
##
                                   cook.d hat
## 2
      0.33 -0.28
                      0.44 0.86_* 0.09
                                           0.03
## 12 0.16 -0.17
                     -0.18 1.17_*
                                   0.02
                                           0.12_*
## 26 0.07
           -0.07
                     -0.08 1.21 *
                                   0.00
                                           0.15 *
                     -0.41 0.89_*
## 27 -0.31
             0.27
                                   0.08
                                           0.03
## 55 -0.34
             0.29
                     -0.46 0.83_* 0.10
                                           0.03
```

```
# dfb.1_- dfb.Stay dffit cov.r cook.d hat
# 2 - 0.13  0.09  -0.23  0.94_- * 0.02  0.01
# 34_- 0.04_- 0.05_- 0.05_- 1.07_- * 0.00_- 0.05_-
# 40_- 0.20_- 0.17_- 0.27_- 0.94_- * 0.04_- 0.01_-
# 47_- 0.85_- 0.90_- 0.92_- * 1.30_- * 0.42_- 0.25_- *
# 53_- 0.16_- 0.20_- 0.30_- 0.94_- * 0.04_- 0.02_-
# 93_- 0.14_- 0.09_- 0.25_- 0.92_- * 0.03_- 0.01_-
# 104_- 0.11_- 0.12_- 0.14_- 1.07_- * 0.01_- 0.05_- *
# 112_- 0.64_- 0.68_- 0.70_- * 1.19_- * 0.24_- 0.18_- *
detach(infectionrisk)
```