Lesson 10

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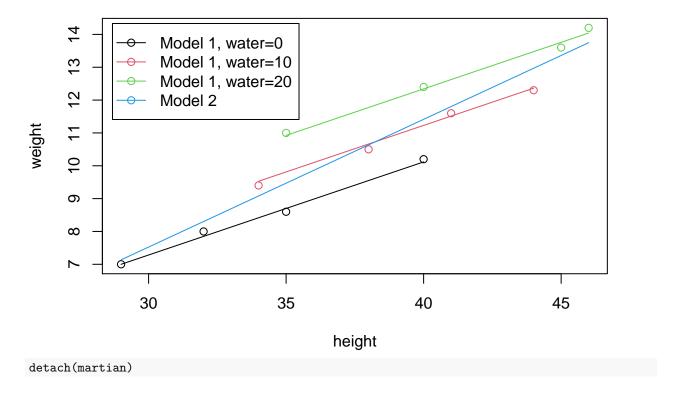
Martians (underspecified model)

Call:

Load the martians data. Fit a multiple linear regression model of weight vs height + water. Fit a simple linear regression model of weight vs height with points marked by water level and regression lines for each model.

```
martian <- read.table("./Data/martian.txt", header=T)</pre>
attach(martian)
model.1 <- lm(weight ~ height + water)</pre>
summary(model.1)
##
## lm(formula = weight ~ height + water)
##
## Residuals:
       Min
                  10
                      Median
                                    30
                                            Max
## -0.16247 -0.10722 0.02955 0.08388 0.15792
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.220194
                           0.320978 -3.801 0.00421 **
## height
                0.283436
                           0.009142 31.003 1.85e-10 ***
## water
                0.111212
                           0.005748 19.348 1.22e-08 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1305 on 9 degrees of freedom
## Multiple R-squared: 0.9972, Adjusted R-squared: 0.9966
## F-statistic: 1592 on 2 and 9 DF, p-value: 3.353e-12
              Estimate Std. Error t value Pr(>|t|)
# (Intercept) -1.220194
                          0.320978 -3.801 0.00421 **
                          0.009142 31.003 1.85e-10 ***
# height
             0.283436
                          0.005748 19.348 1.22e-08 ***
# water
               0.111212
# Residual standard error: 0.1305 on 9 degrees of freedom
model.2 <- lm(weight ~ height)</pre>
summary(model.2)
##
```

```
## lm(formula = weight ~ height)
##
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -1.2140 -0.3943 -0.1359 0.3528 1.5307
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -4.14335
                        1.75340 -2.363 0.0397 *
               0.38893
                          0.04543 8.561 6.48e-06 ***
## height
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.808 on 10 degrees of freedom
## Multiple R-squared: 0.8799, Adjusted R-squared: 0.8679
## F-statistic: 73.28 on 1 and 10 DF, p-value: 6.475e-06
             Estimate Std. Error t value Pr(>|t|)
# (Intercept) -4.14335 1.75340 -2.363 0.0397 *
# height
              0.38893
                         0.04543 8.561 6.48e-06 ***
# ---
# Residual standard error: 0.808 on 10 degrees of freedom
plot(x=height, y=weight, col=water/10+1,
     panel.last = c(lines(sort(height[water==0]),
                         fitted(model.1) [water==0] [order(height[water==0])],
                          col=1),
                   lines(sort(height[water==10]),
                          fitted(model.1) [water==10] [order(height[water==10])],
                          col=2),
                   lines(sort(height[water==20]),
                          fitted(model.1) [water==20] [order(height[water==20])],
                   lines(sort(height), fitted(model.2)[order(height)], col=4)))
legend("topleft", col=1:4, pch=1, lty=1, inset=0.02,
       legend=c("Model 1, water=0", "Model 1, water=10",
                "Model 1, water=20", "Model 2"))
```



Cement hardening (variable selection using stepwise regression)

Load the cement data. Create a scatterplot matrix of the data. Use the add1 and drop1 functions to conduct stepwise regression.

```
cement <- read.table("./Data/cement.txt", header=T)
attach(cement)
pairs(cement)</pre>
```

```
5 10 15 20
                                                  5 10 15 20
                                                                  8
                                          8
                                         ዏ
         y
                                   ° °
                                                   0
                                                  0
                       x1
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                                                                                20
                                       x2
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                      o <sup>de</sup>
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                                                                  9 &
                                                 50
                                                          0
                                         0
          100
                                                                     30
                                                                        50
     80
                                  30
                                        50
                                             70
                                                                 10
model.0 \leftarrow lm(y \sim 1)
add1(model.0, \sim x1 + x2 + x3 + x4, test="F")
## Single term additions
##
## Model:
## y ~ 1
          Df Sum of Sq
                           RSS
                                  AIC F value
## <none>
                       2715.76 71.444
## x1
          1
              1450.08 1265.69 63.519 12.6025 0.0045520 **
## x2
           1
              1809.43 906.34 59.178 21.9606 0.0006648 ***
## x3
           1 776.36 1939.40 69.067 4.4034 0.0597623 .
           1 1831.90 883.87 58.852 22.7985 0.0005762 ***
## x4
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
#y \sim 1
         Df Sum of Sq RSS
                                 AIC F value
#
                                              Pr(>F)
               2715.76 71.444
# x1
          1 1450.08 1265.69 63.519 12.6025 0.0045520 **
# x2
         1 1809.43 906.34 59.178 21.9606 0.0006648 ***
          1 776.36 1939.40 69.067 4.4034 0.0597623 .
# x3
          1 1831.90 883.87 58.852 22.7985 0.0005762 ***
# x4
model.4 \leftarrow lm(y \sim x4)
add1(model.4, \sim . + x1 + x2 + x3, test="F")
## Single term additions
##
## Model:
```

```
## y ~ x4
## Df Sum of Sq RSS AIC F value Pr(>F)
## <none> 883.87 58.852
        1 809.10 74.76 28.742 108.2239 1.105e-06 ***
## x1
## x2
        1
             14.99 868.88 60.629 0.1725 0.6867
## x3
        1 708.13 175.74 39.853 40.2946 8.375e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# y \sim x4
# Df Sum of Sq RSS AIC F value Pr(>F)
            883.87 58.852
        1 809.10 74.76 28.742 108.2239 1.105e-06 ***
            14.99 868.88 60.629 0.1725 0.6867
        1
# x2
        1 708.13 175.74 39.853 40.2946 8.375e-05 ***
# x3
model.14 \leftarrow lm(y \sim x1 + x4)
drop1(model.14, ~ ., test="F")
## Single term deletions
##
## Model:
## y \sim x1 + x4
## Df Sum of Sq RSS
                             AIC F value Pr(>F)
                     74.76 28.742
## <none>
             809.1 883.87 58.852 108.22 1.105e-06 ***
        1
## x1
## x4
        1 1190.9 1265.69 63.519 159.30 1.815e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# y \sim x1 + x4
# Df Sum of Sq RSS AIC F value Pr(>F)
        74.76 28.742
            809.1 883.87 58.852 108.22 1.105e-06 ***
# x1
       1
       1 1190.9 1265.69 63.519 159.30 1.815e-07 ***
# x4
add1(model.14, \sim . + x2 + x3, test="F")
## Single term additions
##
## Model:
## y \sim x1 + x4
## Df Sum of Sq RSS AIC F value Pr(>F)
## <none>
                   74.762 28.742
        1 26.789 47.973 24.974 5.0259 0.05169 .
## x2
## x3
        1 23.926 50.836 25.728 4.2358 0.06969 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# y \sim x1 + x4
# Df Sum of Sq RSS AIC F value Pr(>F)
      74.762 28.742
# x2 1 26.789 47.973 24.974 5.0259 0.05169 .
```

```
# x3 1 23.926 50.836 25.728 4.2358 0.06969 .
model.124 \leftarrow lm(y \sim x1 + x2 + x4)
drop1(model.124, ~ ., test="F")
## Single term deletions
##
## Model:
## y \sim x1 + x2 + x4
                                 AIC F value
##
         Df Sum of Sq
                         RSS
                                                 Pr(>F)
                        47.97 24.974
## <none>
## x1
           1
                820.91 868.88 60.629 154.0076 5.781e-07 ***
## x2
           1
                 26.79 74.76 28.742
                                       5.0259
                                                0.05169 .
## x4
           1
                  9.93 57.90 25.420
                                       1.8633
                                                0.20540
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# y \sim x4 + x1 + x2
        Df Sum of Sq
                       RSS
                                AIC F value
                                                Pr(>F)
                 47.97 24.974
# x1
             820.91 868.88 60.629 154.0076 5.781e-07 ***
         1
# x2
          1
              26.79 74.76 28.742 5.0259
                                              0.05169 .
                 9.93 57.90 25.420 1.8633
                                               0.20540
# x4
          1
model.12 \leftarrow lm(y \sim x1 + x2)
add1(model.12, \sim . + x3 + x4, test="F")
## Single term additions
##
## Model:
## y ~ x1 + x2
         Df Sum of Sq
                         RSS
                                 AIC F value Pr(>F)
                       57.904 25.420
## <none>
                9.7939 48.111 25.011 1.8321 0.2089
## x3
          1
## x4
           1
               9.9318 47.973 24.974 1.8633 0.2054
# Model:
# y \sim x1 + x2
#
        Df Sum of Sq
                        RSS
                                AIC F value Pr(>F)
#
               57.904 25.420
              9.7939 48.111 25.011 1.8321 0.2089
# x3
          1
# x4
              9.9318 47.973 24.974 1.8633 0.2054
          1
detach(cement)
```

IQ and body size (variable selection using stepwise regression)

Load the iquize data. Create a scatterplot matrix of the data. Use the add1 and drop1 functions to conduct stepwise regression.

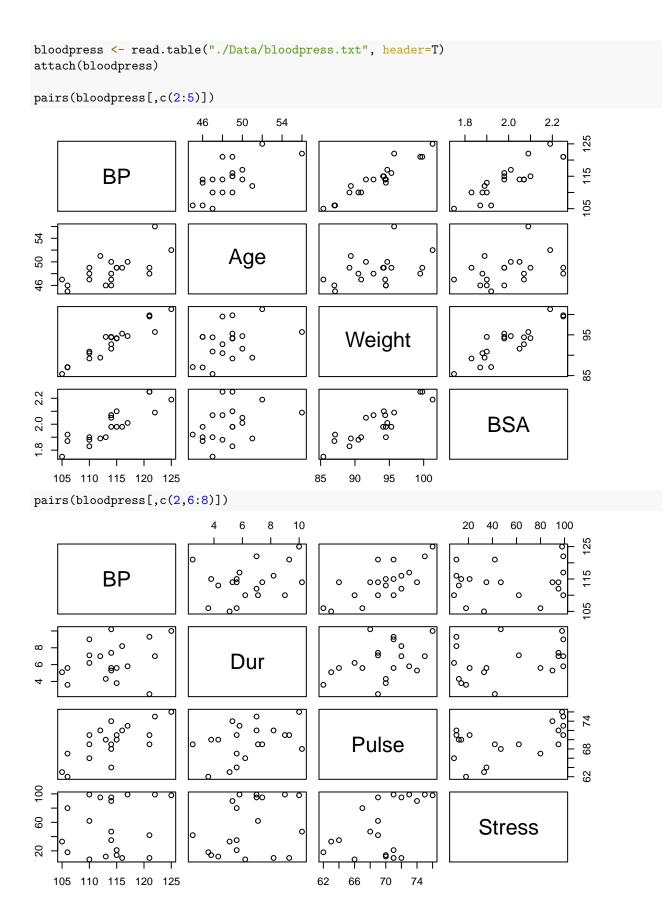
```
iqsize <- read.table("./Data/iqsize.txt", header=T)
attach(iqsize)
pairs(iqsize)</pre>
```

```
80
                          90
                               100
                                                          120
                                                                 160
                                         & 8,880°°
        PIQ
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                                                                     ଚତ
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                                         <sub>ೢ</sub> ಹಂೄಿ ೢ ೢ ಎ ಿ
                          Brain
                                          Height
                                                                    o 8
                                                                          70
                                           ° œ°
              α
                                                            Weight
                     တုိင္ပိ
၀၀
    80 100 120 140
                                         65
                                              70
                                                   75
model.0 \leftarrow lm(PIQ \sim 1)
add1(model.0, ~ Brain + Height + Weight, test="F")
## Single term additions
##
## Model:
## PIQ ~ 1
## Df Sum of Sq RSS
                            AIC F value Pr(>F)
## <none> 18895 237.94
## Brain 1
             2697.09 16198 234.09 5.9945 0.01935 *
## Height 1
             163.97 18731 239.61 0.3151 0.57802
## Weight 1
              0.12 18894 239.94 0.0002 0.98806
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# PIQ ~ 1
       Df Sum of Sq RSS
                             AIC F value Pr(>F)
              18895 237.94
# Brain 1 2697.09 16198 234.09 5.9945 0.01935 *
# Height 1 163.97 18731 239.61 0.3151 0.57802
# Weight 1
              0.12 18894 239.94 0.0002 0.98806
model.1 <- lm(PIQ ~ Brain)</pre>
add1(model.1, ~ . + Height + Weight, test="F")
## Single term additions
##
## Model:
## PIQ ~ Brain
        Df Sum of Sq RSS AIC F value Pr(>F)
```

```
## <none>
                      16198 234.09
## Height 1 2875.65 13322 228.66 7.5551 0.009399 **
## Weight 1 940.94 15256 233.82 2.1586 0.150705
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# PIQ ~ Brain
                             AIC F value
        Df Sum of Sq RSS
#
             16198 234.09
# Height 1 2875.65 13322 228.66 7.5551 0.009399 **
# Weight 1 940.94 15256 233.82 2.1586 0.150705
model.12 <- lm(PIQ ~ Brain + Height)</pre>
drop1(model.12, ~ ., test="F")
## Single term deletions
##
## Model:
## PIQ ~ Brain + Height
       Df Sum of Sq
                       RSS
                              AIC F value
## <none>
                     13322 228.66
## Brain 1
             5408.8 18731 239.61 14.2103 0.0006045 ***
## Height 1 2875.6 16198 234.09 7.5551 0.0093991 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# PIQ ~ Brain + Height
        Df Sum of Sq RSS
                             AIC F value
                                            Pr(>F)
              13322 228.66
# Brain 1
            5408.8 18731 239.61 14.2103 0.0006045 ***
           2875.6 16198 234.09 7.5551 0.0093991 **
# Height 1
add1(model.12, ~ . + Weight, test="F")
## Single term additions
##
## Model:
## PIQ ~ Brain + Height
        Df Sum of Sq
                       RSS
                            AIC F value Pr(>F)
## <none>
                     13322 228.66
## Weight 1 0.0031633 13322 230.66
                                        0 0.9977
# Model:
# PIQ ~ Brain + Height
                             AIC F value Pr(>F)
       Df Sum of Sq RSS
               13322 228.66
# Weight 1 0.0031633 13322 230.66
                                     0 0.9977
detach(iqsize)
```

Blood pressure (variable selection using stepwise regression)

Load the bloodpress data. Create scatterplot matrices of the data. Use the add1 and drop1 functions to conduct stepwise regression.



```
model.0 \leftarrow lm(BP \sim 1)
add1(model.0, ~ Age + Weight + BSA + Dur + Pulse + Stress, test="F")
## Single term additions
##
## Model:
## BP ~ 1
        Df Sum of Sq RSS
                             AIC F value
         560.00 68.644
## <none>
            243.27 316.73 59.247 13.8248 0.0015737 **
## Age
         1
            505.47 54.53 24.060 166.8591 1.528e-10 ***
## Weight 1
## BSA
            419.86 140.14 42.938 53.9270 8.114e-07 ***
             48.02 511.98 68.851 1.6883 0.2102216
## Dur
          1
            291.44 268.56 55.946 19.5342 0.0003307 ***
## Pulse 1
## Stress 1 15.04 544.96 70.099 0.4969 0.4898895
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# BP ~ 1
        Df Sum of Sq
                            AIC F value
                    RSS
                                         Pr(>F)
             560.00 68.644
           243.27 316.73 59.247 13.8248 0.0015737 **
# Age
        1
# Weight 1
           505.47 54.53 24.060 166.8591 1.528e-10 ***
# BSA 1 419.86 140.14 42.938 53.9270 8.114e-07 ***
        1
             48.02 511.98 68.851 1.6883 0.2102216
# Pulse 1 291.44 268.56 55.946 19.5342 0.0003307 ***
# Stress 1
            15.04 544.96 70.099 0.4969 0.4898895
model.2 <- lm(BP ~ Weight)</pre>
add1(model.2, ~ . + Age + BSA + Dur + Pulse + Stress, test="F")
## Single term additions
##
## Model:
## BP ~ Weight
                                           Pr(>F)
        Df Sum of Sq RSS
                              AIC F value
         54.528 24.060
## <none>
            49.704 4.824 -22.443 175.1622 2.218e-10 ***
## Age
          1
              2.814 51.714 25.000
## BSA
                                   0.9251
         1
## Dur
         1
             6.095 48.433 23.689
                                   2.1393 0.16181
## Pulse 1
             8.940 45.588 22.478
                                   3.3338 0.08549 .
## Stress 1
             9.660 44.868 22.160
                                  3.6601
                                            0.07273 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# BP ~ Weight
        Df Sum of Sq
                     RSS
                             AIC F value
                                           Pr(>F)
             54.528 24.060
# Age
           49.704 4.824 -22.443 175.1622 2.218e-10 ***
       1
# BSA
             2.814 51.714 25.000 0.9251 0.34962
        1
           6.095 48.433 23.689
# Dur
        1
                                   2.1393 0.16181
# Pulse 1 8.940 45.588 22.478 3.3338 0.08549 .
# Stress 1 9.660 44.868 22.160 3.6601 0.07273 .
```

```
model.12 <- lm(BP ~ Age + Weight)</pre>
drop1(model.12, ~ ., test="F")
## Single term deletions
##
## Model:
## BP ~ Age + Weight
                             AIC F value
        Df Sum of Sq RSS
                                            Pr(>F)
## <none>
                      4.82 -22.443
       1 49.704 54.53 24.060 175.16 2.218e-10 ***
## Age
## Weight 1 311.910 316.73 59.247 1099.20 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
# BP ~ Age + Weight
       Df Sum of Sq RSS
                              AIC F value Pr(>F)
#
               4.82 -22.443
       1 49.704 54.53 24.060 175.16 2.218e-10 ***
# Age
# Weight 1 311.910 316.73 59.247 1099.20 < 2.2e-16 ***
add1(model.12, ~ . + BSA + Dur + Pulse + Stress, test="F")
## Single term additions
##
## Model:
## BP ~ Age + Weight
       Df Sum of Sq RSS AIC F value Pr(>F)
## <none> 4.8239 -22.443
## BSA
        1
            1.76778 3.0561 -29.572 9.2550 0.007764 **
        1 0.17835 4.6456 -21.196 0.6143 0.444639
## Pulse 1 0.49557 4.3284 -22.611 1.8319 0.194719
## Stress 1 0.16286 4.6611 -21.130 0.5591 0.465486
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# BP ~ Age + Weight
                     RSS
                              AIC F value Pr(>F)
       Df Sum of Sq
             4.8239 -22.443
        1 1.76778 3.0561 -29.572 9.2550 0.007764 **
# BSA
# Dur
        1 0.17835 4.6456 -21.196 0.6143 0.444639
# Pulse 1 0.49557 4.3284 -22.611 1.8319 0.194719
# Stress 1 0.16286 4.6611 -21.130 0.5591 0.465486
model.123 <- lm(BP ~ Age + Weight + BSA)</pre>
drop1(model.123, ~ ., test="F")
## Single term deletions
## Model:
## BP ~ Age + Weight + BSA
## Df Sum of Sq RSS
                             AIC F value
## <none>
                      3.056 -29.572
## Age 1 48.658 51.714 25.000 254.740 3.002e-11 ***
```

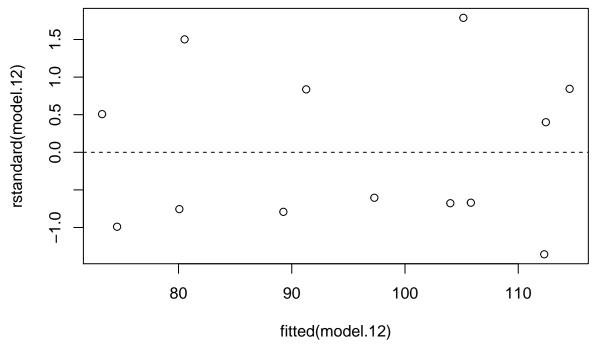
```
65.303 68.359 30.581 341.886 3.198e-12 ***
## Weight 1
           1
                 1.768 4.824 -22.443
                                       9.255 0.007764 **
## BSA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# BP ~ Age + Weight + BSA
#
         Df Sum of Sq
                         RSS
                                 AIC F value
                                                Pr(>F)
#
                 3.056 -29.572
# Age
               48.658 51.714 25.000 254.740 3.002e-11 ***
          1
# Weight
         1
               65.303 68.359 30.581 341.886 3.198e-12 ***
# BSA
          1
               1.768 4.824 -22.443
                                      9.255 0.007764 **
add1(model.123, ~ . + Dur + Pulse + Stress, test="F")
## Single term additions
##
## Model:
## BP ~ Age + Weight + BSA
##
         Df Sum of Sq
                         RSS
                                  AIC F value Pr(>F)
## <none>
                       3.0561 -29.572
## Dur
              0.33510 2.7210 -29.894 1.8473 0.1942
              0.04111 3.0150 -27.842 0.2045 0.6576
## Pulse
          1
              0.21774 2.8384 -29.050 1.1507 0.3004
## Stress
         1
# Model:
# BP ~ Age + Weight + BSA
#
         Df Sum of Sq
                         RSS
                                 AIC F value Pr(>F)
#
                3.0561 -29.572
# Dur
             0.33510 2.7210 -29.894 1.8473 0.1942
             0.04111 3.0150 -27.842 0.2045 0.6576
# Pulse
         1
# Stress 1
              0.21774 2.8384 -29.050 1.1507 0.3004
detach(bloodpress)
```

Cement hardening (variable selection using best subsets regression)

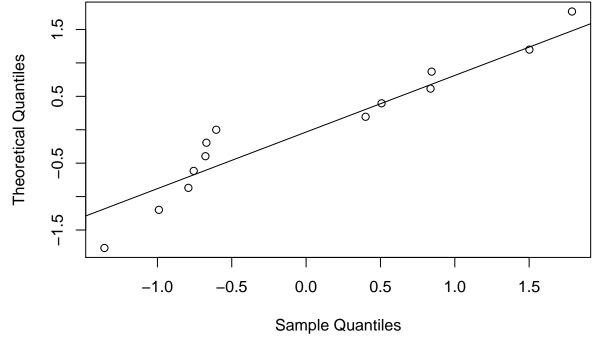
Load the cement data. Use the regsubsets function in the leaps package to conduct variable selection using exhaustive search (i.e., best subsets regression). Note that the nbest=2 argument returns the best two models with 1, 2, ..., k predictors. Fit models with all four predictors (assumed unbiased) and just two predictors to retrieve the information needed to calculate for the model with just two predictors by hand. Fit model with , , and and note the variance inflation factors for and are very high. Fit model with , , and and note the variance inflation factors are acceptable. Fit model with and and note the variance inflation factors are acceptable, adjusted is high, and a residual analysis and normality test yields no concerns.

```
## 2 (1) "*" "*" " " "0.974" "2.7"
## 2 ( 2 ) "*" " " " " " " " " " " " " 5.5"
## 3 (1) "*" "*" " "*" "0.976" "3"
## 3 ( 2 ) "*" "*" "*" " "0.976" "3"
## 4 ( 1 ) "*" "*" "*" "0.974" "5"
           x1 x2 x3 x4
# 1 (1) " " " " " " " " " " " " " " 138.7"
# 1 (2) " " "*" " " " " " 0.636" "142.5"
# 2 (1) "*" "*" " " " "0.974" "2.7"
# 2 ( 2 ) "*" " " " " " " " " " 0.967" "5.5"
# 3 (1) "*" "*" " "*" "0.976" "3"
# 3 (2) "*" "*" "*" " "0.976" "3"
# 4 ( 1 ) "*" "*" "*" "*" "0.974" "5"
model.1234 \leftarrow lm(y \sim x1 + x2 + x3 + x4)
model.12 \leftarrow lm(y \sim x1 + x2)
SSE.k \leftarrow sum(residuals(model.12)^2) # SSE_k = 57.90448
MSE.all <- summary(model.1234)$sigma^2 # MSE_all = 5.982955
params \leftarrow summary(model.12)$df[1] # k+1 = 3
n \leftarrow sum(summary(model.1234)\$df[1:2]) # n = 13
SSE.k/MSE.all + 2*params - n \# Cp = 2.678242
## [1] 2.678242
model.14 \leftarrow lm(y \sim x1 + x4)
SSE.k \leftarrow sum(residuals(model.14)^2) # SSE_k = 74.76211
params \leftarrow summary(model.14)$df[1] # k+1 = 3
SSE.k/MSE.all + 2*params - n # Cp = 5.495851
## [1] 5.495851
model.124 \leftarrow lm(y \sim x1 + x2 + x4)
library(car)
## Loading required package: carData
vif(model.124)
##
         x1
                  x2
## 1.06633 18.78031 18.94008
               x2
       x1
# 1.06633 18.78031 18.94008
model.123 \leftarrow lm(y \sim x1 + x2 + x3)
vif(model.123)
                  x2
## 3.251068 1.063575 3.142125
        x1
                 x2
# 3.251068 1.063575 3.142125
summary(model.12)
```

```
## Call:
## lm(formula = y \sim x1 + x2)
## Residuals:
   Min
            1Q Median
                          3Q
## -2.893 -1.574 -1.302 1.363 4.048
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 52.57735 2.28617 23.00 5.46e-10 ***
             1.46831
                         0.12130 12.11 2.69e-07 ***
                         0.04585 14.44 5.03e-08 ***
## x2
              0.66225
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.406 on 10 degrees of freedom
## Multiple R-squared: 0.9787, Adjusted R-squared: 0.9744
## F-statistic: 229.5 on 2 and 10 DF, p-value: 4.407e-09
             Estimate Std. Error t value Pr(>|t|)
# (Intercept) 52.57735 2.28617 23.00 5.46e-10 ***
                                 12.11 2.69e-07 ***
             1.46831
                        0.12130
# x2
              0.66225
                      0.04585 14.44 5.03e-08 ***
# ---
# Residual standard error: 2.406 on 10 degrees of freedom
# Multiple R-squared: 0.9787, Adjusted R-squared: 0.9744
# F-statistic: 229.5 on 2 and 10 DF, p-value: 4.407e-09
vif(model.12)
##
        x1
## 1.055129 1.055129
# x1 x2
# 1.055129 1.055129
plot(x=fitted(model.12), y=rstandard(model.12),
panel.last = abline(h=0, lty=2))
```



```
qqnorm(rstandard(model.12), main="", datax=TRUE)
qqline(rstandard(model.12), datax=TRUE)
```



```
library(nortest) ad.test(rstandard(model.12)) # A = 0.6136, p-value = 0.08628
```

```
##
## Anderson-Darling normality test
##
## data: rstandard(model.12)
## A = 0.61361, p-value = 0.08628
```

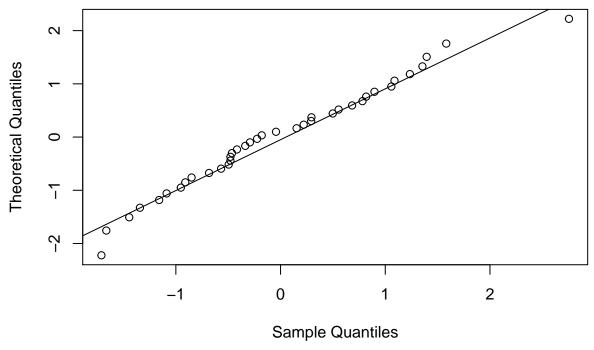
```
detach(cement)
```

IQ and body size (variable selection using best subsets regression)

Load the iqsize data. Use the regsubsets function in the leaps package to conduct variable selection using exhaustive search (i.e., best subsets regression). Fit model with Brain and Height and note the variance inflation factors are acceptable, adjusted is as good as it gets with this dataset, and a residual analysis and normality test yields no concerns.

```
iqsize <- read.table("./Data/iqsize.txt", header=T)</pre>
attach(iqsize)
subset <- regsubsets(PIQ ~ Brain + Height + Weight, method="exhaustive", nbest=2, data=iqsize)</pre>
cbind(summary(subset)$outmat, round(summary(subset)$adjr2, 3), round(summary(subset)$cp, 1))
##
            Brain Height Weight
                         11 11
                                "0.119" "7.3"
     (1)"*"
## 1
     (2)""
                  "*"
                         11 11
## 1
                                "-0.019" "13.8"
                  "*"
                         11 11
## 2 (1) "*"
                                "0.255"
                                         "2"
                  11 11
                         "*"
## 2 (2) "*"
                                "0.146"
                                         "6.9"
## 3 (1) "*"
                         "*"
                                "0.233"
                                         "4"
           Brain Height Weight
                               "0.119" "7.3"
# 1 (1) "*"
#1 (2)""
                 "*"
                        11 11
                               "-0.019" "13.8"
                 "*"
                        H - H
#2 (1) "*"
                               "0.255"
                                        "2"
#2 (2) "*"
                 11 11
                        11*11
                               "0.146"
                                        "6.9"
#3 (1) "*"
                 "*"
                        "*"
                               "0.233" "4"
model.12 <- lm(PIQ ~ Brain + Height)</pre>
summary(model.12)
##
## Call:
## lm(formula = PIQ ~ Brain + Height)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -32.750 -12.090 -3.841 14.174 51.690
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 111.2757
                           55.8673
                                     1.992 0.054243 .
                 2.0606
                            0.5466
                                     3.770 0.000604 ***
## Brain
## Height
                -2.7299
                            0.9932 -2.749 0.009399 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.51 on 35 degrees of freedom
## Multiple R-squared: 0.2949, Adjusted R-squared: 0.2546
## F-statistic: 7.321 on 2 and 35 DF, p-value: 0.002208
              Estimate Std. Error t value Pr(>|t|)
# (Intercept) 111.2757
                          55.8673
                                    1.992 0.054243 .
# Brain
                2.0606
                           0.5466
                                    3.770 0.000604 ***
```

```
# Height
                -2.7299 0.9932 -2.749 0.009399 **
# ---
# Residual standard error: 19.51 on 35 degrees of freedom
# Multiple R-squared: 0.2949, Adjusted R-squared: 0.2546
\mbox{\# F-statistic: 7.321 on 2 and 35 DF, } \mbox{ p-value: 0.002208}
vif(model.12)
##
      Brain
               Height
## 1.529463 1.529463
     Brain
              Height
# 1.529463 1.529463
plot(x=fitted(model.12), y=rstandard(model.12),
     panel.last = abline(h=0, lty=2))
                      0
      \alpha
rstandard(model.12)
                                  0
                                                              0
                                      0
                                 0
                            0
                                     00
                                                   0
                                                            0
                                              00
                                                                    0
      0
                                               0
             00
                       00
                                 0
                                                                                 0
                                                       0
                                                                                     0
      7
                                \infty
                              0
                                            0
                                                      0
                             0
                                0
                                                  0
              90
                                        110
                                                      120
                                                                   130
                                                                                140
                           100
                                         fitted(model.12)
qqnorm(rstandard(model.12), main="", datax=TRUE)
qqline(rstandard(model.12), datax=TRUE)
```



```
ad.test(rstandard(model.12)) # A = 0.2629, p-value = 0.6829

##
## Anderson-Darling normality test
##
## data: rstandard(model.12)
## A = 0.26289, p-value = 0.6829

detach(iqsize)
```

Blood pressure (variable selection using best subsets regression)

Load the bloodpress data. Use the regsubsets function in the leaps package to conduct variable selection using exhaustive search (i.e., best subsets regression). Fit model with Age and Weight and note the variance inflation factors are acceptable, adjusted can't get much better, and a residual analysis and normality test yields no concerns.

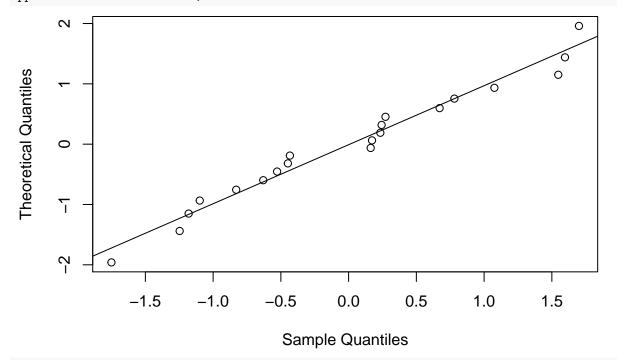
```
##
             Age Weight BSA Dur Pulse Stress
                                               "0.897" "312.8"
## 1
      ( 1
          )
                                        11 11
                                               "0.736" "829.1"
##
  1
        2
             11
                                        11 11
      (1
                                               "0.99" "15.1"
      (2
                                               "0.91" "256.6"
## 3
        1
                                               "0.994" "6.4"
                                        11 11
## 3
        2
          )
                                               "0.991" "14.1"
          ) "*" "*"
                                        11 11
      ( 1
                                               "0.994" "6.4"
                                               "0.994" "7.1"
     (2) "*" "*"
```

```
## 5 (1) "*" "*"
                    "*" " " "*"
                                    "*"
                                          "0.994" "7"
## 5 (2) "*" "*"
                      "*" "*" "*"
                                    11 11
                                          "0.994" "7.7"
                                    "*"
## 6 (1) "*" "*"
                      "*" "*" "*"
                                          "0.994" "7"
          Age Weight BSA Dur Pulse Stress
# 1 (1) " " "*"
                    " " " " " " " "0.897" "312.8"
#1 (2) " " " "
                     11*11 11 11 11
                                          "0.736" "829.1"
# 2 (1) "*" "*"
                     H = H = H = H = H
                                   11 11
                                          "0.99" "15.1"
                                       "0.91" "256.6"
#2 (2) " " "*"
                     H = H = H = H = H
                                   "*"
                                   H = H
# 3 (1) "*" "*"
                    n_*" " " " " "
                                         "0.994" "6.4"
# 3 (2) "*" "*"
                     11 11 11 11<sub>*</sub>11
                                   H = H
                                          "0.991" "14.1"
# 4 (1) "*" "*"
                     "*" "*" " "
                                   11 11
                                          "0.994" "6.4"
                     "*" " " " "
                                         "0.994" "7.1"
#4 (2) "*" "*"
                                   "*"
# 5 (1) "*" "*"
                     "*" " " "*"
                                   "*"
                                         "0.994" "7"
# 5 (2) "*" "*"
                   "*" "*" "*"
                                   11 11
                                          "0.994" "7.7"
                                         "0.994" "7"
# 6 (1) "*" "*"
                     "*" "*" "*"
                                   "*"
model.12 <- lm(BP ~ Age + Weight)</pre>
summary(model.12)
##
## Call:
## lm(formula = BP ~ Age + Weight)
##
## Residuals:
                1Q Median
##
                                  3Q
       Min
                                          Max
## -0.89968 -0.35242 0.06979 0.35528 0.82781
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -16.57937
                          3.00746 -5.513 3.80e-05 ***
                           0.05351 13.235 2.22e-10 ***
                0.70825
## Age
                1.03296
                           0.03116 33.154 < 2e-16 ***
## Weight
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.5327 on 17 degrees of freedom
## Multiple R-squared: 0.9914, Adjusted R-squared: 0.9904
## F-statistic: 978.2 on 2 and 17 DF, p-value: < 2.2e-16
             Estimate Std. Error t value Pr(>|t|)
# (Intercept) -16.57937 3.00746 -5.513 3.80e-05 ***
                        0.05351 13.235 2.22e-10 ***
# Age
             0.70825
                          0.03116 33.154 < 2e-16 ***
# Weight
               1.03296
# Residual standard error: 0.5327 on 17 degrees of freedom
# Multiple R-squared: 0.9914, Adjusted R-squared: 0.9904
# F-statistic: 978.2 on 2 and 17 DF, p-value: < 2.2e-16
vif(model.12)
       Age
             Weight
## 1.198945 1.198945
      Age Weight
# 1.198945 1.198945
```

```
plot(x=fitted(model.12), y=rstandard(model.12),
      panel.last = abline(h=0, lty=2))
                                                                             0
      1.5
                                                0
                0
                                                 0
rstandard(model.12)
                                                  0
                                                              0
      0.5
                   0
                                           0
                                                                                                0
               0
                                                                                    0
      -0.5
                                                     0
                                                                                 0
                                    0
                                                         0
                                                              0
                                      0
                                                  0
```

fitted(model.12)

qqnorm(rstandard(model.12), main="", datax=TRUE)
qqline(rstandard(model.12), datax=TRUE)



ad.test(rstandard(model.12)) # A = 0.275, p-value = 0.6225

##
Anderson-Darling normality test
##

-1.5

```
## data: rstandard(model.12)
## A = 0.27496, p-value = 0.6225
detach(bloodpress)
```

Peruvian blood pressure (variable selection using best subsets regression)

Load the peru data. Use the regsubsets function in the leaps package to conduct variable selection using exhaustive search (i.e., best subsets regression). Fit the best 5-predictor and 4-predictor models. Calculate AIC and BIC by hand. Use the stepAIC function in the MASS package to conduct variable selection using a stepwise algorithm based on AIC or BIC.

```
##
             Age Years fraclife Weight Height Chin Forearm Pulse
                                                                     "0.272" "0.252"
      (1)
            "*"
## 1
      (2)""
                                                               11 11
                                                                     "0.076" "0.051"
## 1
                        11 * 11
## 2
      (1)""
                                  "*"
                                                               11 11
                                                                     "0.473" "0.444"
      (2)""
                                  11 * 11
                                         11 11
                                                               11 11
## 2
                                                                     "0.421" "0.389"
                                  "*"
                                         .. ..
                                                               11 11
## 3
      (1)
                                                                      "0.503" "0.461"
      (2
                                  11 * 11
                                                               11 11
          )
## 3
                                                                      "0.49"
                                                                              "0.447"
      (1
                                  "*"
                                                               11 11
## 4
          )
                                                                     "0.597" "0.55"
          ) "*"
                                  11 11
                                         "*"
                                                               11 11
      (2
                                                                     "0.525" "0.469"
## 5
      (1
                                         .. ..
                                                      11 11
                                                               11 11
                                                                      "0.639" "0.584"
                                  11 🕌 11
                                                 11 11
                                                               11 11
      (2
                                                                      "0.631" "0.576"
## 5
          )
      (1
                                  "*"
                                         11 11
                                                 "*"
                                                               11 11
                                                                     "0.649" "0.583"
##
                                                               11 11
                                  "*"
                                                 11 🕌 11
      ( 2
                                         " * "
                                                                     "0.643" "0.576"
                                                               11 11
## 7
      (1)
                                  "*"
                                         "*"
                                                                      "0.661" "0.584"
## 7
      (2)
                                  "*"
                                         11 11
                                                 "*"
                                                               "*"
                                                                      "0.655" "0.577"
      (1)"*"
                                  "*"
                                                               "*"
## 8
                                                                     "0.666" "0.577"
##
## 1
      (1) "30.5" "11.3376"
      (2) "48.1" "12.7697"
      (1) "14.4" "9.7772"
      (2) "19.1" "10.2512"
## 3
      (1) "13.7" "9.6273"
## 3
      (2) "14.8" "9.7509"
      (1) "7.2"
                    "8.7946"
      (2) "13.7" "9.5502"
      (1) "5.5"
## 5
                    "8.4571"
## 5
      (2) "6.1"
                    "8.5417"
     (1) "6.6"
                    "8.4663"
                    "8.5337"
## 6 (2) "7.1"
```

```
## 7 (1) "7.5"
                   "8.4556"
## 7 (2) "8"
                   "8.522"
                   "8.5228"
## 8 (1) "9"
           Age Years fraclife Weight Height Chin Forearm Pulse
#1 (1) """"
                     11 11
                              11*11
                                             H = H = H = H
                                                        11 11
                                                                "0.272" "0.252" "30.5" "11.3376"
    (2)""""
                                                                "0.076" "0.051" "48.1" "12.7697"
# 1
# 2
    (1)""""
                     "*"
                               11 * 11
                                                          11 11
                                                                "0.473" "0.444" "14.4" "9.7772"
#2 (2)"""*"
                     11 11
                              11 * 11
                                                                "0.421" "0.389" "19.1" "10.2512"
    (1)""""
                     "*"
                               "*"
                                      11 11
                                                          11 11
                                                                "0.503" "0.461" "13.7" "9.6273"
    (2)"""*"
                                                                "0.49" "0.447" "14.8" "9.7509"
                     "*"
                               "*"
# 3
                                      11 11
                                                                "0.597" "0.55" "7.2" "8.7946"
    (1) "*" "*"
                     11*11
                               "*"
                                             H - H
    (2) "*" "*"
                              H = H
                                      11 * 11
                                             H = H
                                                          H = H
                                                                "0.525" "0.469" "13.7" "9.5502"
                     11 * 11
# 5
    (1) "*" "*"
                     "*"
                              "*"
                                      11 11
                                             "*"
                                                          11 11
                                                                "0.639" "0.584" "5.5"
                                                                                        "8.4571"
    (2) "*" "*"
                     "*"
                              "*"
                                      11 11
                                             11 11
                                                  11411
                                                          11 11
                                                                "0.631" "0.576" "6.1"
# 5
                                                                                        "8.5417"
                                                  "*"
                     "*"
                              "*"
                                      11 11
                                             "*"
    (1) "*" "*"
                                                                "0.649" "0.583" "6.6"
# 6
                                                                                       "8.4663"
    (2) "*" "*"
                                             "*"
                                                 11 11
                                                          11 11
                                                                "0.643" "0.576" "7.1"
                     "*"
                              "*"
                                      11 * 11
                                                                                        "8.5337"
#7 (1) "*" "*"
                               "*"
                                                          11 11
                     11*11
                                      11*11
                                             "*"
                                                  "*"
                                                                "0.661" "0.584" "7.5"
                                                                                        "8.4556"
# 7
    (2) "*" "*"
                     "*"
                               "*"
                                      11 11
                                             "*"
                                                  "*"
                                                          "*"
                                                                "0.655" "0.577" "8"
                                                                                        "8.522"
#8 (1) "*" "*"
                     "*"
                              "*"
                                      11 * 11
                                             "*"
                                                  "*"
                                                          "*"
                                                                "0.666" "0.577" "9"
                                                                                        "8.5228"
model.5 <- lm(Systol ~ Age + Years + fraclife + Weight + Chin)</pre>
summary(model.5)
##
## Call:
## lm(formula = Systol ~ Age + Years + fraclife + Weight + Chin)
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -14.520 -6.640 -1.093
                             4.893 16.366
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 109.3590
                            21.4843
                                     5.090 1.41e-05 ***
## Age
                 -1.0120
                             0.3059 -3.308 0.002277 **
## Years
                  2.4067
                             0.7426
                                     3.241 0.002723 **
                            27.2795 -4.062 0.000282 ***
## fraclife
               -110.8112
## Weight
                  1.0976
                             0.2980
                                     3.683 0.000819 ***
## Chin
                 -1.1918
                             0.6140 -1.941 0.060830 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.457 on 33 degrees of freedom
## Multiple R-squared: 0.6386, Adjusted R-squared: 0.5839
## F-statistic: 11.66 on 5 and 33 DF, p-value: 1.531e-06
               Estimate Std. Error t value Pr(>|t|)
# (Intercept) 109.3590
                           21.4843
                                    5.090 1.41e-05 ***
                           0.3059 -3.308 0.002277 **
# Age
                -1.0120
# Years
                 2.4067
                           0.7426
                                    3.241 0.002723 **
# fraclife
              -110.8112
                           27.2795
                                    -4.062 0.000282 ***
                          0.2980
                                    3.683 0.000819 ***
# Weight
                1.0976
# Chin
                -1.1918
                            0.6140 -1.941 0.060830 .
```

```
# Residual standard error: 8.457 on 33 degrees of freedom
# Multiple R-squared: 0.6386, Adjusted R-squared: 0.5839
# F-statistic: 11.66 on 5 and 33 DF, p-value: 1.531e-06
k < -5
n*log(sum(residuals(model.5)^2))-n*log(n)+2*(k+1) # AIC = 172.0151
## [1] 172.0151
n*log(sum(residuals(model.5)^2))-n*log(n)+log(n)*(k+1) # BIC = 181.9965
## [1] 181.9965
model.4 <- lm(Systol ~ Age + Years + fraclife + Weight)</pre>
summary(model.4)
##
## Call:
## lm(formula = Systol ~ Age + Years + fraclife + Weight)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -16.890 -5.976
                   0.058
                            5.407 16.835
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 116.8354 21.9797
                                   5.316 6.69e-06 ***
## Age
                -0.9507
                            0.3164 -3.004 0.004971 **
## Years
                2.3393
                           0.7714 3.032 0.004621 **
## fraclife
              -108.0728 28.3302 -3.815 0.000549 ***
## Weight
                 0.8324
                            0.2754
                                   3.022 0.004742 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.795 on 34 degrees of freedom
## Multiple R-squared: 0.5974, Adjusted R-squared:
## F-statistic: 12.61 on 4 and 34 DF, p-value: 2.142e-06
              Estimate Std. Error t value Pr(>|t|)
                          21.9797 5.316 6.69e-06 ***
# (Intercept) 116.8354
                         0.3164 -3.004 0.004971 **
# Age
               -0.9507
                2.3393
                          0.7714 3.032 0.004621 **
# Years
# fraclife
             -108.0728
                          28.3302 -3.815 0.000549 ***
                                   3.022 0.004742 **
# Weight
                0.8324
                          0.2754
# Residual standard error: 8.795 on 34 degrees of freedom
# Multiple R-squared: 0.5974, Adjusted R-squared: 0.55
# F-statistic: 12.61 on 4 and 34 DF, p-value: 2.142e-06
k < -4
n*log(sum(residuals(model.4)^2))-n*log(n)+2*(k+1) # AIC = 174.2316
## [1] 174.2316
n*log(sum(residuals(model.4)^2))-n*log(n)+log(n)*(k+1) # BIC = 182.5494
```

[1] 182.5494

```
library(MASS)
## Attaching package: 'MASS'
## The following object is masked _by_ '.GlobalEnv':
##
      cement
subset.aic <- stepAIC(lm(Systol ~ Age + Years + fraclife + Weight + Height +
                          Chin + Forearm + Pulse), direction="both", k=2)
## Start: AIC=174.9
## Systol ~ Age + Years + fraclife + Weight + Height + Chin + Forearm +
##
      Pulse
##
##
             Df Sum of Sq
                             RSS
                                    AIC
## - Pulse
              1
                    37.31 2216.4 173.56
                    72.23 2251.3 174.17
## - Height
              1
## <none>
                          2179.1 174.90
                   130.95 2310.1 175.18
## - Chin
              1
## - Forearm
              1
                   146.06 2325.2 175.43
## - Years
              1
                   677.20 2856.3 183.46
## - Weight
                 829.55 3008.7 185.48
              1
                  873.30 3052.4 186.04
## - Age
              1
## - fraclife 1
                 1103.76 3282.9 188.88
## Step: AIC=173.56
## Systol ~ Age + Years + fraclife + Weight + Height + Chin + Forearm
             Df Sum of Sq
                             RSS
                    77.26 2293.7 172.90
## - Height
              1
## - Forearm 1
                   113.91 2330.3 173.52
## <none>
                          2216.4 173.56
## - Chin
                   152.11 2368.5 174.15
              1
                   37.31 2179.1 174.90
## + Pulse
              1
## - Years
                   651.50 2867.9 181.61
              1
## - Age
              1
                 856.29 3072.7 184.30
## - Weight
              1
                880.23 3096.7 184.61
                  1067.91 3284.3 186.90
## - fraclife 1
##
## Step: AIC=172.9
## Systol ~ Age + Years + fraclife + Weight + Chin + Forearm
##
             Df Sum of Sq
                             RSS
                                    AIC
## - Forearm
                    66.53 2360.2 172.01
             1
                   114.02 2407.7 172.79
## - Chin
              1
## <none>
                          2293.7 172.90
## + Height
                   77.26 2216.4 173.56
              1
## + Pulse
                   42.35 2251.3 174.17
              1
## - Years
                 811.30 3105.0 182.71
              1
## - Age
                  848.93 3142.6 183.18
              1
## - Weight
              1 1036.53 3330.2 185.44
## - fraclife 1 1246.44 3540.1 187.83
```

##

```
## Step: AIC=172.02
## Systol ~ Age + Years + fraclife + Weight + Chin
##
##
             Df Sum of Sq
                          RSS
                                   AIC
## <none>
                         2360.2 172.01
## + Forearm 1
                   66.53 2293.7 172.90
## + Height 1
                  29.88 2330.3 173.52
            1
## + Pulse
                   9.84 2350.4 173.85
## - Chin
             1
                  269.48 2629.7 174.23
## - Years
            1 751.19 3111.4 180.79
## - Age
              1 782.65 3142.9 181.18
## - Weight
                 970.26 3330.5 183.44
              1
## - fraclife 1 1180.14 3540.4 185.83
# Step: AIC=172.02
# Systol ~ Age + Years + fraclife + Weight + Chin
subset.bic <- stepAIC(lm(Systol ~ Age + Years + fraclife + Weight + Height +</pre>
                         Chin + Forearm + Pulse), direction="both", k=log(n))
## Start: AIC=189.87
## Systol ~ Age + Years + fraclife + Weight + Height + Chin + Forearm +
##
      Pulse
##
##
             Df Sum of Sq
                            RSS
                                   AIC
                   37.31 2216.4 186.87
## - Pulse
             1
## - Height
              1
                   72.23 2251.3 187.48
              1 130.95 2310.1 188.49
## - Chin
## - Forearm 1 146.06 2325.2 188.74
## <none>
                         2179.1 189.87
## - Years
            1
                  677.20 2856.3 196.76
## - Weight
              1 829.55 3008.7 198.79
              1 873.30 3052.4 199.35
## - Age
## - fraclife 1 1103.76 3282.9 202.19
## Step: AIC=186.87
## Systol ~ Age + Years + fraclife + Weight + Height + Chin + Forearm
##
##
             Df Sum of Sq
                            RSS
                                   AIC
## - Height
            1 77.26 2293.7 184.54
## - Forearm 1
                  113.91 2330.3 185.16
## - Chin
             1 152.11 2368.5 185.80
                         2216.4 186.87
## <none>
## + Pulse
            1
                  37.31 2179.1 189.87
## - Years
              1 651.50 2867.9 193.26
## - Age
              1 856.29 3072.7 195.95
## - Weight
           1 880.23 3096.7 196.25
## - fraclife 1 1067.91 3284.3 198.55
##
## Step: AIC=184.54
## Systol ~ Age + Years + fraclife + Weight + Chin + Forearm
##
             Df Sum of Sq
                            RSS
                                   AIC
## - Forearm 1 66.53 2360.2 182.00
## - Chin
            1
                  114.02 2407.7 182.77
```

```
## <none>
                           2293.7 184.54
## + Height
                     77.26 2216.4 186.87
               1
## + Pulse
                     42.35 2251.3 187.48
## - Years
                    811.30 3105.0 192.69
               1
## - Age
               1
                    848.93 3142.6 193.16
## - Weight
                   1036.53 3330.2 195.42
               1
                   1246.44 3540.1 197.81
## - fraclife 1
##
## Step: AIC=182
## Systol ~ Age + Years + fraclife + Weight + Chin
                              RSS
##
              Df Sum of Sq
                                     AIC
## <none>
                           2360.2 182.00
## - Chin
               1
                    269.48 2629.7 182.55
## + Forearm
                     66.53 2293.7 184.54
               1
## + Height
               1
                     29.88 2330.3 185.16
## + Pulse
                     9.84 2350.4 185.50
               1
## - Years
                    751.19 3111.4 189.11
               1
## - Age
                    782.65 3142.9 189.50
               1
## - Weight
                    970.26 3330.5 191.76
## - fraclife 1
                   1180.14 3540.4 194.15
# Step: AIC=182
# Systol ~ Age + Years + fraclife + Weight + Chin
detach(peru)
```

Measurements of college students (variable selection using stepwise regression)

Load the Physical data. Use the add1 and drop1 functions to conduct stepwise regression. Use the regsubsets function to conduct variable selection using backward elimination. Use the regsubsets function to conduct variable selection using forward selection.

```
physical <- read.table("./Data/Physical.txt", header=T)</pre>
attach(physical)
gender <- ifelse(Sex=="Female",1,0)</pre>
model.0 <- lm(Height ~ 1)</pre>
add1(model.0, ~ LeftArm + LeftFoot + LeftHand + HeadCirc + nose + gender, test="F")
## Single term additions
##
## Model:
## Height ~ 1
##
           Df Sum of Sq
                             RSS
                                    AIC F value
                                                    Pr(>F)
## <none>
                         1054.75 164.46
                  590.21 464.53 121.35 67.3396 5.252e-11 ***
## LeftArm
             1
## LeftFoot
                  707.42
                          347.33 105.36 107.9484 2.172e-14 ***
            1
## LeftHand 1
                  143.59 911.15 158.41
                                          8.3525 0.005570 **
## HeadCirc 1
                  189.24 865.51 155.58 11.5880 0.001272 **
## nose
                  85.25 969.49 161.82
                                         4.6605 0.035412 *
             1
                  533.24 521.51 127.72 54.1923 1.181e-09 ***
## gender
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
# Model:
# Height ~ 1
         Df Sum of Sq
                        RSS
                               AIC F value Pr(>F)
              1054.75 164.46
#
# LeftArm 1 590.21 464.53 121.35 67.3396 5.252e-11 ***
# LeftFoot 1 707.42 347.33 105.36 107.9484 2.172e-14 ***
# LeftHand 1 143.59 911.15 158.41 8.3525 0.005570 **
# HeadCirc 1 189.24 865.51 155.58 11.5880 0.001272 **
               85.25 969.49 161.82 4.6605 0.035412 *
# nose 1
# qender 1
            533.24 521.51 127.72 54.1923 1.181e-09 ***
model.2 <- lm(Height ~ LeftFoot)</pre>
add1(model.2, ~ . + LeftArm + LeftHand + HeadCirc + nose + gender, test="F")
## Single term additions
##
## Model:
## Height ~ LeftFoot
         Df Sum of Sq RSS AIC F value Pr(>F)
## <none>
                      347.33 105.361
## LeftArm 1 107.143 240.18 87.074 23.1967 1.305e-05 ***
## LeftHand 1 15.359 331.97 104.874 2.4059 0.1269
## HeadCirc 1 2.313 345.01 106.994 0.3486
                                             0.5575
## nose 1
               1.449 345.88 107.131 0.2178
                                             0.6427
## gender 1 15.973 331.35 104.772 2.5066
                                             0.1194
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# Height ~ LeftFoot
       Df Sum of Sq RSS
                             AIC F value Pr(>F)
               347.33 105.361
# LeftArm 1 107.143 240.18 87.074 23.1967 1.305e-05 ***
# LeftHand 1 15.359 331.97 104.874 2.4059 0.1269
              2.313 345.01 106.994 0.3486 0.5575
# HeadCirc 1
               1.449 345.88 107.131 0.2178 0.6427
# nose 1
# gender 1 15.973 331.35 104.772 2.5066 0.1194
model.12 <- lm(Height ~ LeftArm + LeftFoot)</pre>
drop1(model.12, ~ ., test="F")
## Single term deletions
##
## Model:
## Height ~ LeftArm + LeftFoot
          Df Sum of Sq
                        RSS
                                AIC F value Pr(>F)
                      240.18 87.074
## <none>
## LeftArm 1
               107.14 347.33 105.361 23.197 1.305e-05 ***
               224.35 464.53 121.353 48.572 5.538e-09 ***
## LeftFoot 1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Model:
# Height ~ LeftArm + LeftFoot
# Df Sum of Sq RSS AIC F value Pr(>F)
```

```
240.18 87.074
# LeftArm 1 107.14 347.33 105.361 23.197 1.305e-05 ***
# LeftFoot 1 224.35 464.53 121.353 48.572 5.538e-09 ***
add1(model.12, ~ . + LeftHand + HeadCirc + nose + gender, test="F")
## Single term additions
##
## Model:
## Height ~ LeftArm + LeftFoot
         Df Sum of Sq RSS AIC F value Pr(>F)
## <none>
                       240.18 87.074
## LeftHand 1 3.7854 236.40 88.200 0.8167 0.3704
## HeadCirc 1 1.4016 238.78 88.752 0.2994 0.5867
## nose
          1 0.4463 239.74 88.971 0.0950 0.7592
## gender 1 3.7530 236.43 88.207 0.8096 0.3725
# Model:
# Height ~ LeftArm + LeftFoot
        Df Sum of Sq RSS AIC F value Pr(>F)
                240.18 87.074
# LeftHand 1 3.7854 236.40 88.200 0.8167 0.3704
# HeadCirc 1 1.4016 238.78 88.752 0.2994 0.5867
# nose 1 0.4463 239.74 88.971 0.0950 0.7592
# gender 1 3.7530 236.43 88.207 0.8096 0.3725
subset <- regsubsets(Height ~ LeftArm + LeftFoot + LeftHand + HeadCirc + nose + gender,
                   method="backward", data=physical)
subset <- regsubsets(Height ~ LeftArm + LeftFoot + LeftHand + HeadCirc + nose + gender,</pre>
                   method="forward", data=physical)
detach(physical)
```