

$$E = P_i V \left(\ln \left(\frac{P_i}{P_0} \right) + \frac{P_0}{P_i} - 1 \right)$$

$$\Delta P_0 \frac{\partial E}{\partial P_0} = \left(V - \frac{P_i V}{P_0} \right) \Delta P_0$$

$$\Delta P_i \frac{\partial E}{\partial P_i} = V \ln \left(\frac{P_i}{P_0} \right) \Delta P_i$$

$$\Delta V \frac{\partial E}{\partial V} = \left(P_i \ln \left(\frac{P_i}{P_0} \right) + P_0 - P_i \right) \Delta V$$

$$\Delta E = \left| \left(V - \frac{P_i V}{P_0} \right) \Delta P_0 \right| + \left| V \ln \left(\frac{P_i}{P_0} \right) \Delta P_i \right| + \left| \left(P_i \ln \left(\frac{P_i}{P_0} \right) + P_0 - P_i \right) \Delta V \right|$$

$$\frac{E}{L^2} (L^3) \quad F(L) = E$$

$$\begin{aligned} \frac{\partial E}{\partial P_0} &= \left(P_i V \ln \left(\frac{P_i}{P_0} \right) + P_i V \frac{P_0}{P_i} - P_i V \right) \frac{\partial}{\partial P_0} \\ &= \frac{P_i V}{\frac{P_0}{P_0}} \left(\frac{P_i}{P_0^2} \right) + V - 0 = \left(-\frac{P_i V}{P_0} + V \right) \Delta P_0 \end{aligned}$$

$$\frac{\partial E}{\partial P_i} = V \ln \left(\frac{P_i}{P_0} \right) + 0 + 0 - V = \left(V \ln \left(\frac{P_i}{P_0} \right) - V \right) \Delta P_i$$

$$\frac{\partial E}{\partial V} = P_i \ln \left(\frac{P_i}{P_0} \right) + P_0 - P_i = \left(P_i \ln \left(\frac{P_i}{P_0} \right) + P_0 - P_i \right) \Delta V$$