ME EN 2450 HW2b

Name:		
I declare that the knowledged.	e assignment here submitted is original ex	cept for source material explicitly ac-
I also acknowledge that I am aware of University policy and regulations on honesty in academic work, and of the disciplinary guidelines and procedures applicable to breaches of such policy and regulations, as contained in the University website.		
Name		_
Signature		Student ID

Score

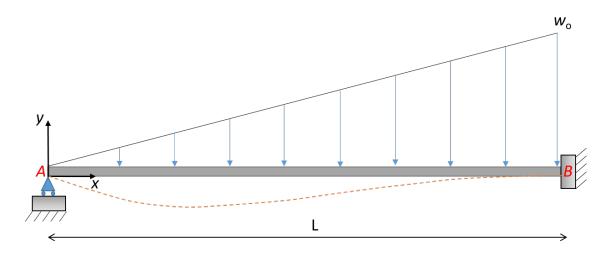
Total:

Q1 - 8 pts

Determine the maximum deflection of a beam. You will not need any previous knowledge of structural mechanics to solve this problem. The beam illustration and problem statement are only here to provide engineering context to the polynomial for which you will be determining roots.

A beam with uniform cross section is carrying a load that increases linearly from the pinned end (point A) to the fixed end (point B). The beam has the following properties:

- $E = 29 \times 10^4 \ psi$ (Young's modulus)
- $I = 723 in^4$ (Cross-section moment of inertia)
- $w_o = 3000 \frac{lbs}{ft}$ (applied load, see figure)
- L = 15 ft (beam length, see figure)



The deformed shape of the beam, y(x), (illustrated by the orange dashed line in the figure) is given by the following equation (note, the origin is placed at A):

$$y(x) = \frac{w_o}{(120EIL)} \left(-x^5 + 2L^2x^3 - L^4x \right)$$

- a. Analytically derive the first derivative of y(x) with respect to x, i.e. $\frac{dy(x)}{dx}$.
- b. Next, the maximum deflection can be determined by setting $\frac{dy}{dx}=0$ and solving for the root (the value of x where $\frac{dy}{dx}=0$). Write a matlab or python script to determine the root using the Newton-Raphson method. Report the root in inches. Submit your code, along with what you used as the initial guess, tolerance, and how many iterations were required to achieve your tolerance.
- c. Verify your obtained root using the built-in Matlab function fzero, Python function scipy.optimize.fsolve or scipy.optimize.root, or by solving analytically. Report a comparison of this result to that from your Newton-Raphson code.

Q2: (10 pts)

You now work on a new project to design compressed air tanks for energy storage:

Estimating Work Potential

Before creating machines that take advantage of sustainable energy sources, it is desirable to determine whether it would be feasible to do so. Such feasibility studies can take into account economic factors, such as setup or maintenance costs and expected profits, as well as more traditional engineer-ing factors, such as the safety of designs and the ease of replacing damaged parts. One such factor that should be considered is called exergy, which is an estimate of the maximum amount of useful work that we could expect to get from that source. (Exergy has the same units as energy, so in SI units it is in Joules, while in English units it may be in foot-pounds, calories, or Btu. Note: you should convert all measurements to SI units for your reported calculation.)

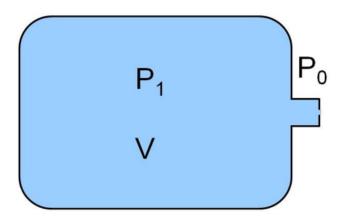


Figure 1: Schematic of a Compressed Air Tank. P1 indicates the pressure inside the tank, P0 the atmospheric pressure outside of the tank, and V is the tank volume.

In the case of a tank of compressed air (Figure 1), exergy is the maximum amount of useful work we could expect to do by bringing the gas to the same state (i.e., pressure and temperature) as the environment. The work potential (exergy) of compressed air in a fixed-volume tank at the same temperature as its environment can be estimated using the formula:

$$X = P_1 V \left(\ln \left(\frac{P_1}{P_0} \right) + \frac{P_0}{P_1} - 1 \right) \tag{1}$$

where P_1 and P_0 are the pressure inside the tank and in the surrounding atmosphere, respectively, while V is the volume of the tank and X is the exergy. (Note that this is not a guarantee of the actual amount of energy you will be able to extract from the tank. It is an estimate of the most work that could be done if we used the gas in the most efficient way possible.)

Analyzing Error

Suppose that on a given day, the atmospheric pressure in Salt Lake City is $P_0=26.02$ inches Hg. You fill the tank with compressed air until the pressure gauge reads 50 psi (i.e., $P_1=50$ psi above the atmospheric pressure). For this calculation, choose a tank size of radius r=4.5 inches, and a length h=0.55 meters. Suppose you have a ruler capable of measuring the size of your tank with markings every 1/16-inch - i.e., the measurement error is in the range of -1/16-inch to +1/16-inch. The pressure gauge on the pump you use to fill the tank has markings every 2 psi. The local atmospheric pressure is reported to the hundredths of an inch of mercury (in Hg).

(10 points) Perform an error propagation analysis on the exergy equation (using Equation 1) to determine (It would be much easier if you first convert everything into SI units):

- where the largest source of error is (1 pt), and
- if it's worth your time and money to invest in better sensors (1 pt).

Note that you need to first perform the symbolic analytical derivations by hand (4 pts) before calculating the numbers (4 pts) either by coding (recommended), or using calculators.