

4005-800 ALGORITHMS

HOMEWORK 7

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PROBLEM 1 - 34.2-1. Consider the language $\text{GRAPH-ISOMORPHISM} = \{\langle G_1, G_2 \rangle : G_1 \text{ and } G_2 \text{ are isomorphic graphs}\}$. Prove that $\text{GRAPH-ISOMORPHISM} \in NP$ by describing a polynomial-time algorithm to verify the language.

Solution.

PROBLEM 2 - 34.2-10. Prove that if $NP \neq \text{co-}NP$, then $P \neq NP$.

Solution.

PROBLEM 3 - 34.3-1. Verify that the circuit in Figure 34.8(b) is unsatisfiable.

Solution.

PROBLEM 4 - 34.4-5. Show that the problem of determining the satisfiability of boolean formulas in disjunctive normal form is polynomial-time solvable.

Solution.

PROBLEM 5 - 34.5-5. The *set-partition problem* takes as input a set S of numbers. The question is whether the numbers can be partitioned into two sets A and $A' = S - A$ such that $\sum_{x \in A} x = \sum_{x \in A'} x$. Show that the set-partition problem is NP -complete.

Solution.