


In[1]:=  **Derivative of  $f(x) = (.5/(\sqrt{1 + x^2})) - \sqrt{1 + x^2}(1 - (.5/(1 + x^2))) + x$**

Derivative:

Show steps +

$$\frac{d}{dx} \left( f(x) = \frac{0.5}{\sqrt{1+x^2}} - \sqrt{1+x^2} \left( 1 - \frac{0.5}{1+x^2} \right) + x \right) = \left( f'(x) = \frac{x(-x^2-2.)}{(x^2+1)^{3/2}} + 1 \right)$$

Alternate form:

+


$$f'(x) = \frac{x^4 + 2. x^2 - 2. \sqrt{x^2 + 1} x - \sqrt{x^2 + 1} x^3 + 1.}{(x^2 + 1.)^2}$$

Expanded form:

Show steps +

$$f'(x) = -\frac{2. x}{(x^2 + 1)^{3/2}} - \frac{x^3}{(x^2 + 1)^{3/2}} + 1$$

WolframAlpha +

In[5]:=  **Derivative of  $f(x) = ((x (-x^2 - 2.))/(x^2 + 1)^{(3/2)} + 1)$**

Derivative:

Show steps +

$$\frac{d}{dx} \left( f(x) = \frac{x(-x^2-2.)}{(x^2+1)^{3/2}} + 1 \right) = \left( f'(x) = \frac{x^2-2.}{\sqrt{x^2+1} (x^2+1.)^2} \right)$$

Alternate forms:

+

$$f'(x) = \frac{x^2-2}{(x^2+1)^{5/2}}$$

$$f'(x) = \frac{(x^2-2.) \sqrt{x^2+1}}{(x^2+1.)^3}$$

$$f'(x) = \frac{x^2}{\sqrt{x^2+1} (x^2+1.)^2} - \frac{2.}{\sqrt{x^2+1} (x^2+1.)^2}$$

Alternate form assuming x is real:

+

$$f'(x) = \frac{x^2}{\sqrt{x^2+1} (x^2+1.)^2} - \frac{2.}{\sqrt{x^2+1} (x^2+1.)^2} + 0. i$$

WolframAlpha +

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In[48]:= FirstDerivative[x_] := ((x (- (x^2) - 2)) / ((x^2) + 1)^(3/2)) + 1
FirstD[x_] := (x (-x^2 - 2.)) / (x^2 + 1)^(3/2) + 1

In[9]:= FirstDerivative[0.6]
Out[9]= 0.107199


In[46]:= SecondDerivative[x_] := ((x^2) - 2) / ((Sqrt[(x^2) + 1]) (x^2) + 1)^2
SecondD[x_] := (x^2 - 2.) / (Sqrt[x^2 + 1] (x^2 + 1.)^2)

In[11]:= SecondDerivative[0.6]
Out[11]= -0.76032

In[32]:= 0.6 - (FirstDerivative[0.6] / SecondDerivative[0.6])
Out[32]= 0.740991

In[35]:= % - (FirstDerivative[%] / SecondDerivative[%])
In[50]:= 0.7861314312243325`
In[52]:= 0.7861314312243325`
0.6 - (FirstD[0.6] / SecondD[0.6])
Out[52]= 0.786131

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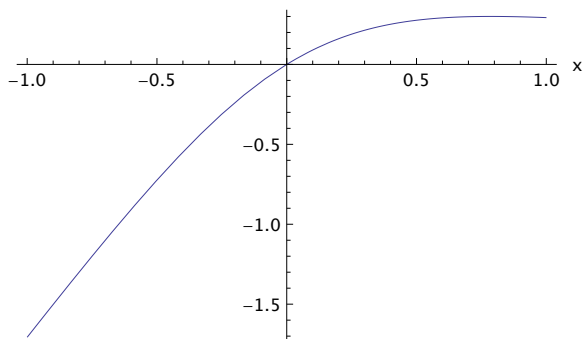
In[51]:=  Plot  $f(x) = (.5/(\sqrt{1 + x^2})) - \sqrt{1 + x^2}(1 - (.5/(1 + x^2))) + x$



Input interpretation:

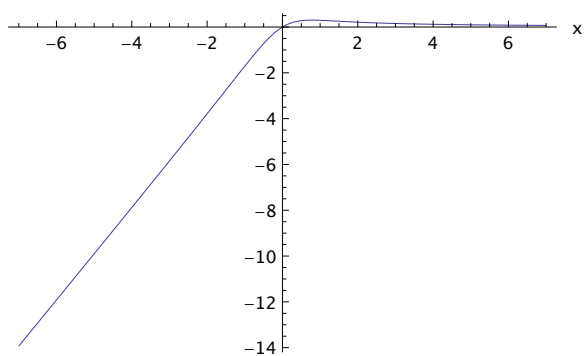
plot



$$f(x) = \frac{0.5}{\sqrt{1 + x^2}} - \sqrt{1 + x^2} \left( 1 - \frac{0.5}{1 + x^2} \right) + x$$

Plots:



min  max 



min  max 

WolframAlpha 

In[64]:= 0.6 - (FirstD[0.6] / SecondD[0.6])

Out[64]= 0.740991

In[73]:= % - (FirstD[%] / SecondD[%])

Out[73]= 0.786151

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In[74]:= % - (FirstD[%] / SecondD[%])  
Out[74]= 0.786151  
  
In[75]:= % - (FirstD[%] / SecondD[%])  
Out[75]= 0.786151  
  
In[76]:= % - (FirstD[%] / SecondD[%])  
Out[76]= 0.786151  
  
In[77]:= % - (FirstD[%] / SecondD[%])  
Out[77]= 0.786151  
  
In[78]:= .786151 - (FirstD[.786151] / SecondD[.786151])  
Out[78]= 0.786151
```