[4005-735-01] Parallel Computing I Performance Analysis Results

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Christopher

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Performance Metrics

In this section we list all gathered performance metrics that we collected during our experiments. The program output files used to generate these metrics are provided in the 'output' directory of the TeamSatisfactionDeliverables.jar archive.

Variable Performance Metrics

Exhaustive Program (Speedup)

Exhaustive 3-SAT with Fixed Schedule

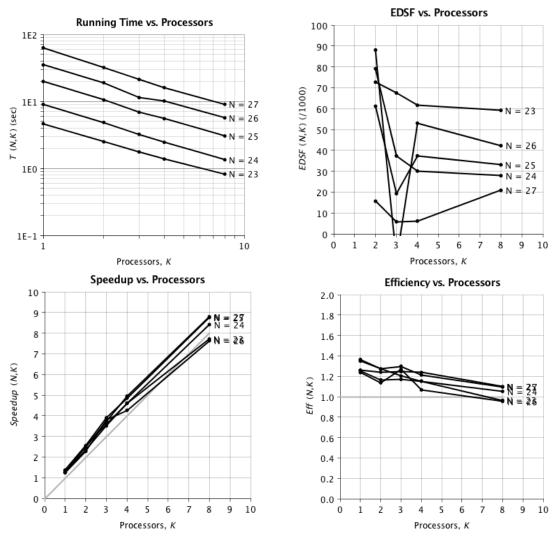


Figure 1. Exhaustive 3-SAT with a fixed schedule.

Table 1. Speedup metrics for exhaustive parallel program with 23 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 6329 | | | |
| 1 | 4639 | 1.364 | 1.364 | |
| 2 | 2488 | 2.544 | 1.272 | 0.073 |
| 3 | 1755 | 3.606 | 1.202 | 0.067 |
| 4 | 1374 | 4.606 | 1.152 | 0.062 |
| 8 | 820 | 7.718 | 0.965 | 0.059 |

Table 2. Speedup metrics for exhaustive parallel program with 24 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 11283 | | | |
| 1 | 8978 | 1.257 | 1.257 | |
| 2 | 4844 | 2.329 | 1.165 | 0.079 |
| 3 | 3216 | 3.508 | 1.169 | 0.037 |
| 4 | 2447 | 4.611 | 1.153 | 0.030 |
| 8 | 1341 | 8.414 | 1.052 | 0.028 |

Table 3. Speedup metrics for exhaustive parallel program with 25 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 26674 | | | |
| 1 | 19779 | 1.349 | 1.349 | |
| 2 | 10494 | 2.542 | 1.271 | 0.061 |
| 3 | 6847 | 3.896 | 1.299 | 0.019 |
| 4 | 5499 | 4.851 | 1.213 | 0.037 |
| 8 | 3045 | 8.760 | 1.095 | 0.033 |

Table 4. Speedup metrics for exhaustive parallel program with 26 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|--------|
| seq | 43213 | | | |
| 1 | 34954 | 1.236 | 1.236 | |
| 2 | 19016 | 2.272 | 1.136 | 0.088 |
| 3 | 11360 | 3.804 | 1.268 | -0.013 |
| 4 | 10128 | 4.267 | 1.067 | 0.053 |
| 8 | 5661 | 7.633 | 0.954 | 0.042 |

Table 5. Speedup metrics for exhaustive parallel program with 27 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 79313 | | | |
| 1 | 62968 | 1.260 | 1.260 | |
| 2 | 31976 | 2.480 | 1.240 | 0.016 |
| 3 | 21233 | 3.735 | 1.245 | 0.006 |
| 4 | 16032 | 4.947 | 1.237 | 0.006 |
| 8 | 9019 | 8.794 | 1.099 | 0.021 |

Exhaustive 3-SAT with Dynamic Schedule

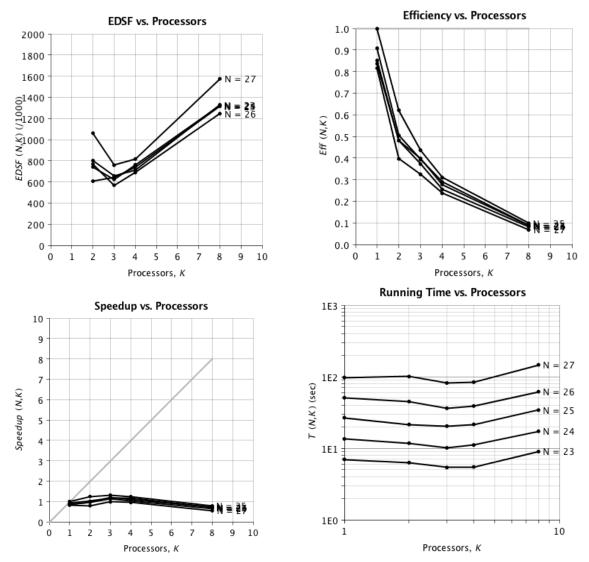


Figure 2. Exhaustive 3-SAT with a dynamic schedule.

Table 6. Speedup metrics for exhaustive parallel program with 23 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 6329 | | | |
| 1 | 6974 | 0.908 | 0.908 | |
| 2 | 6281 | 1.008 | 0.504 | 0.801 |
| 3 | 5375 | 1.177 | 0.392 | 0.656 |
| 4 | 5479 | 1.155 | 0.289 | 0.714 |
| 8 | 8984 | 0.704 | 0.088 | 1.329 |

Table 7. Speedup metrics for exhaustive parallel program with 24 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 11283 | | | |
| 1 | 13495 | 0.836 | 0.836 | |
| 2 | 11752 | 0.960 | 0.480 | 0.742 |
| 3 | 10114 | 1.116 | 0.372 | 0.624 |
| 4 | 11089 | 1.017 | 0.254 | 0.762 |
| 8 | 17281 | 0.653 | 0.082 | 1.321 |

Table 8. Speedup metrics for exhaustive parallel program with 25 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 26674 | | | |
| 1 | 26733 | 0.998 | 0.998 | |
| 2 | 21479 | 1.242 | 0.621 | 0.607 |
| 3 | 20381 | 1.309 | 0.436 | 0.644 |
| 4 | 21541 | 1.238 | 0.310 | 0.741 |
| 8 | 34100 | 0.782 | 0.098 | 1.315 |

Table 9. Speedup metrics for exhaustive parallel program with 26 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 43213 | | | |
| 1 | 50782 | 0.851 | 0.851 | |
| 2 | 44905 | 0.962 | 0.481 | 0.769 |
| 3 | 36204 | 1.194 | 0.398 | 0.569 |
| 4 | 38916 | 1.110 | 0.278 | 0.688 |
| 8 | 61671 | 0.701 | 0.088 | 1.245 |

Table 10. Speedup metrics for exhaustive parallel program with 27 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 79313 | | | |
| 1 | 97234 | 0.816 | 0.816 | |
| 2 | 100179 | 0.792 | 0.396 | 1.061 |
| 3 | 81552 | 0.973 | 0.324 | 0.758 |
| 4 | 83831 | 0.946 | 0.237 | 0.816 |
| 8 | 146151 | 0.543 | 0.068 | 1.575 |

Decision Program (Speedup)

Decision 3-SAT with a Fixed Schedule

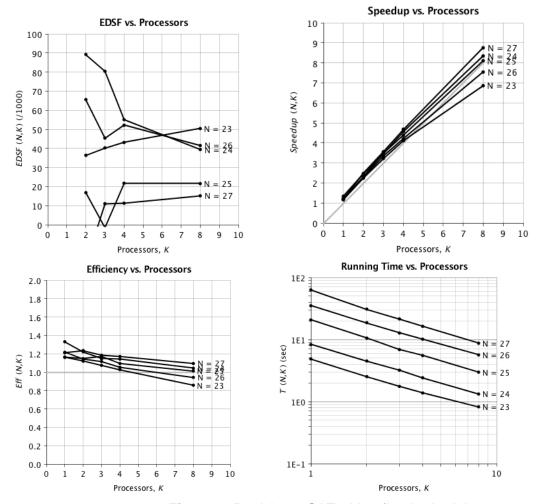


Figure 3. Decision 3-SAT with a fixed schedule.

Table 11. Speedup metrics for decision parallel program with 23 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 5645 | | | |
| 1 | 4867 | 1.160 | 1.160 | |
| 2 | 2522 | 2.238 | 1.119 | 0.036 |
| 3 | 1753 | 3.220 | 1.073 | 0.040 |
| 4 | 1374 | 4.108 | 1.027 | 0.043 |
| 8 | 823 | 6.859 | 0.857 | 0.050 |

Table 12. Speedup metrics for decision parallel program with 24 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 11019 | | | |
| 1 | 8283 | 1.330 | 1.330 | |
| 2 | 4511 | 2.443 | 1.221 | 0.089 |
| 3 | 3205 | 3.438 | 1.146 | 0.080 |
| 4 | 2413 | 4.567 | 1.142 | 0.055 |
| 8 | 1321 | 8.341 | 1.043 | 0.039 |

Table 13. Speedup metrics for decision parallel program with 25 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|--------|
| seq | 24097 | | | |
| 1 | 20675 | 1.166 | 1.166 | |
| 2 | 10511 | 2.293 | 1.146 | 0.017 |
| 3 | 6872 | 3.507 | 1.169 | -0.001 |
| 4 | 5506 | 4.376 | 1.094 | 0.022 |
| 8 | 2974 | 8.103 | 1.013 | 0.022 |

Table 14. Speedup metrics for decision parallel program with 26 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 42555 | | | |
| 1 | 34987 | 1.216 | 1.216 | |
| 2 | 18641 | 2.283 | 1.141 | 0.066 |
| 3 | 12721 | 3.345 | 1.115 | 0.045 |
| 4 | 10114 | 4.208 | 1.052 | 0.052 |
| 8 | 5644 | 7.540 | 0.942 | 0.042 |

Table 15. Speedup metrics for decision parallel program with 27 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|--------|
| seq | 76206 | | | |
| 1 | 62987 | 1.210 | 1.210 | |
| 2 | 30853 | 2.470 | 1.235 | -0.020 |
| 3 | 21458 | 3.551 | 1.184 | 0.011 |
| 4 | 16279 | 4.681 | 1.170 | 0.011 |
| 8 | 8709 | 8.750 | 1.094 | 0.015 |

Decision 3-SAT with a Dynamic Schedule

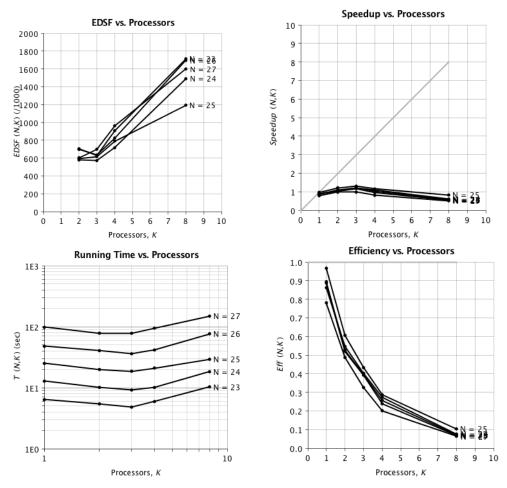


Figure 4. Decision 3-SAT with a dynamic schedule.

Table 16. Speedup metrics for decision parallel program with 23 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 5645 | | | |
| 1 | 6366 | 0.887 | 0.887 | |
| 2 | 5426 | 1.040 | 0.520 | 0.705 |
| 3 | 4800 | 1.176 | 0.392 | 0.631 |
| 4 | 5922 | 0.953 | 0.238 | 0.907 |
| 8 | 10342 | 0.546 | 0.068 | 1.714 |

Table 17. Speedup metrics for decision parallel program with 24 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 11019 | | | |
| 1 | 12791 | 0.861 | 0.861 | |
| 2 | 10093 | 1.092 | 0.546 | 0.578 |
| 3 | 9135 | 1.206 | 0.402 | 0.571 |
| 4 | 10063 | 1.095 | 0.274 | 0.716 |
| 8 | 18275 | 0.603 | 0.075 | 1.490 |

Table 18. Speedup metrics for decision parallel program with 25 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 24097 | | | |
| 1 | 24946 | 0.966 | 0.966 | |
| 2 | 19888 | 1.212 | 0.606 | 0.594 |
| 3 | 18573 | 1.297 | 0.432 | 0.617 |
| 4 | 21028 | 1.146 | 0.286 | 0.791 |
| 8 | 29166 | 0.826 | 0.103 | 1.193 |

Table 19. Speedup metrics for decision parallel program with 26 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 42555 | | | |
| 1 | 47627 | 0.894 | 0.894 | |
| 2 | 40395 | 1.053 | 0.527 | 0.696 |
| 3 | 35986 | 1.183 | 0.394 | 0.633 |
| 4 | 41408 | 1.028 | 0.257 | 0.826 |
| 8 | 76571 | 0.556 | 0.069 | 1.695 |

Table 20. Speedup metrics for decision parallel program with 27 variables and 1000 clauses.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 76206 | | | |
| 1 | 97636 | 0.781 | 0.781 | |
| 2 | 78312 | 0.973 | 0.487 | 0.604 |
| 3 | 78046 | 0.976 | 0.325 | 0.699 |
| 4 | 94828 | 0.804 | 0.201 | 0.962 |
| 8 | 148841 | 0.512 | 0.064 | 1.599 |

Exhaustive Program (Sizeup)

Exhaustive 3-SAT with Fixed Schedule

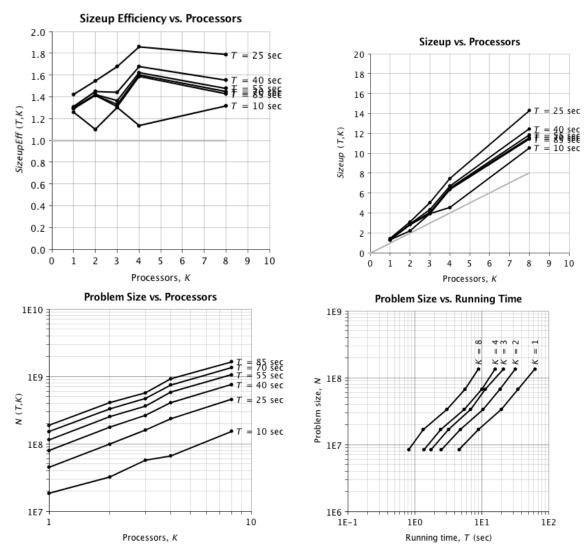


Figure 5. Exhaustive 3-SAT with a fixed schedule.

Table 21. Sizeup metrics for the exhaustive parallel program with 23 variables and fixed clause size.

| Т | K | N | Sizeup | SizeupEff |
|-------|-----|----------|--------|-----------|
| 10000 | seq | 14604712 | | |
| 10000 | 1 | 18364691 | 1.257 | 1.257 |
| 10000 | 2 | 32087539 | 2.197 | 1.099 |
| 10000 | 3 | 56997181 | 3.903 | 1.301 |

| 10000 | 4 | 66181025 | 4.531 | 1.133 |
|-------|-----|------------|--------|-------|
| 10000 | 8 | 153822789 | 10.532 | 1.317 |
| 25000 | seq | 31729660 | | |
| 25000 | 1 | 45098926 | 1.421 | 1.421 |
| 25000 | 2 | 98094932 | 3.092 | 1.546 |
| 25000 | 3 | 159822822 | 5.037 | 1.679 |
| 25000 | 4 | 236154092 | 7.443 | 1.861 |
| 40000 | seq | 60590308 | | |
| 40000 | 1 | 79196796 | 1.307 | 1.307 |
| 40000 | 2 | 175767228 | 2.901 | 1.450 |
| 40000 | 3 | 261780986 | 4.321 | 1.440 |
| 40000 | 4 | 406654254 | 6.712 | 1.678 |
| 40000 | 8 | 753365946 | 12.434 | 1.554 |
| 55000 | seq | 89020559 | | |
| 55000 | 1 | 115130007 | 1.293 | 1.293 |
| 55000 | 2 | 253439525 | 2.847 | 1.423 |
| 55000 | 3 | 363739151 | 4.086 | 1.362 |
| 55000 | 4 | 577154417 | 6.483 | 1.621 |
| 55000 | 8 | 1053137524 | 11.830 | 1.479 |
| 70000 | seq | 116905128 | | |
| 70000 | 1 | 151063217 | 1.292 | 1.292 |
| 70000 | 2 | 331111821 | 2.832 | 1.416 |
| 70000 | 3 | 465697316 | 3.984 | 1.328 |
| 70000 | 4 | 747654580 | 6.395 | 1.599 |

| 70000 | 8 | 1352909103 | 11.573 | 1.447 |
|-------|-----|------------|--------|-------|
| 85000 | seq | 144789698 | | |
| 85000 | 1 | 186996428 | 1.292 | 1.292 |
| 85000 | 2 | 408784117 | 2.823 | 1.412 |
| 85000 | 3 | 567655481 | 3.921 | 1.307 |
| 85000 | 4 | 918154742 | 6.341 | 1.585 |
| 85000 | 8 | 1652680681 | 11.414 | 1.427 |

Exhaustive 3-SAT with Dynamic Schedule

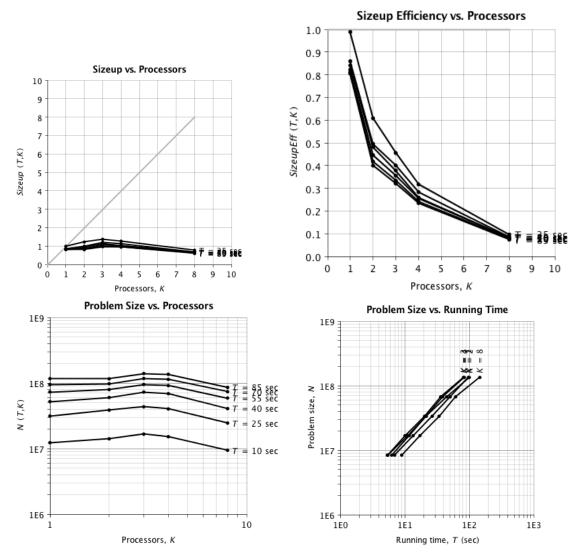


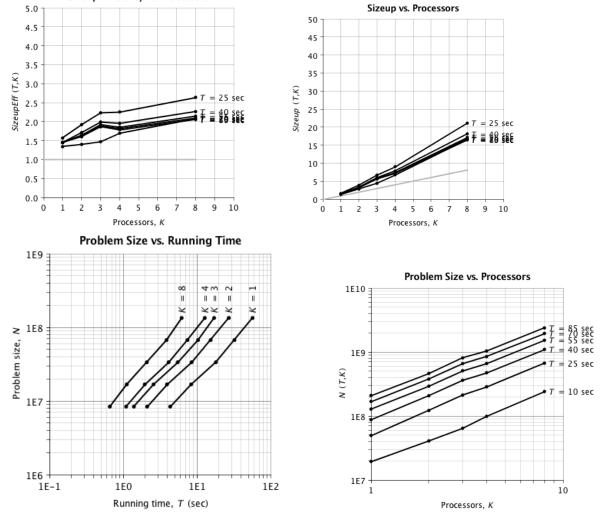
Figure 6. Exhaustive 3-SAT with a dynamic schedule.

Table 22. Sizeup metrics for the exhaustive parallel program with 23 variables and fixed clause size.

| Т | K | N | Sizeup | SizeupEff |
|-------|-----|----------|--------|-----------|
| 10000 | seq | 14604712 | | |
| 10000 | 1 | 12281251 | 0.841 | 0.841 |
| 10000 | 2 | 14090899 | 0.965 | 0.482 |
| 10000 | 3 | 16575422 | 1.135 | 0.378 |
| 10000 | 4 | 15148839 | 1.037 | 0.259 |
| 10000 | 8 | 9415826 | 0.645 | 0.081 |
| 25000 | seq | 31729660 | | |
| 25000 | 1 | 31358110 | 0.988 | 0.988 |
| 25000 | 2 | 38597767 | 1.216 | 0.608 |
| 25000 | 3 | 43349535 | 1.366 | 0.455 |
| 25000 | 4 | 40234419 | 1.268 | 0.317 |
| 25000 | 8 | 24477039 | 0.771 | 0.096 |
| 40000 | seq | 60590308 | | |
| 40000 | 1 | 52065249 | 0.859 | 0.859 |
| 40000 | 2 | 60083145 | 0.992 | 0.496 |
| 40000 | 3 | 72726427 | 1.200 | 0.400 |
| 40000 | 4 | 68728501 | 1.134 | 0.284 |
| 40000 | 8 | 40734844 | 0.672 | 0.084 |
| 55000 | seq | 89020559 | | |
| 55000 | 1 | 73202578 | 0.822 | 0.822 |
| 55000 | 2 | 79365331 | 0.892 | 0.446 |
| 55000 | 3 | 94924384 | 1.066 | 0.355 |
| 55000 | 4 | 91140456 | 1.024 | 0.256 |

| 55000 | 8 | 58990130 | 0.663 | 0.083 |
|-------|-----|-----------|-------|-------|
| 70000 | seq | 116905128 | | |
| 70000 | 1 | 94872968 | 0.812 | 0.812 |
| 70000 | 2 | 97577022 | 0.835 | 0.417 |
| 70000 | 3 | 117122341 | 1.002 | 0.334 |
| 70000 | 4 | 113552411 | 0.971 | 0.243 |
| 70000 | 8 | 73725220 | 0.631 | 0.079 |
| 85000 | seq | 144789698 | | |
| 85000 | 1 | 116543358 | 0.805 | 0.805 |
| 85000 | 2 | 115788712 | 0.800 | 0.400 |
| 85000 | 3 | 139320298 | 0.962 | 0.321 |
| 85000 | 4 | 135964366 | 0.939 | 0.235 |
| 85000 | 8 | 85640856 | 0.591 | 0.074 |

Exhaustive 3-SAT with Guided Schedule



Sizeup Efficiency vs. Processors

Figure 7. Exhaustive 3-SAT with a dynamic schedule.

Table 23. Sizeup metrics for the exhaustive parallel program with 23 variables and fixed clause size.

| Т | K | N | Sizeup | SizeupEff |
|-------|-----|-----------|--------|-----------|
| 10000 | seq | 14604712 | | |
| 10000 | 1 | 19542277 | 1.338 | 1.338 |
| 10000 | 2 | 40846331 | 2.797 | 1.398 |
| 10000 | 3 | 64378965 | 4.408 | 1.469 |
| 10000 | 4 | 98871645 | 6.770 | 1.692 |
| 10000 | 8 | 241797258 | 16.556 | 2.070 |

| 25000 | seq | 31729660 | | |
|-------|-----|------------|--------|-------|
| 25000 | 1 | 49672838 | 1.566 | 1.566 |
| 25000 | 2 | 121820518 | 3.839 | 1.920 |
| 25000 | 3 | 212325763 | 6.692 | 2.231 |
| 25000 | 4 | 286152196 | 9.018 | 2.255 |
| 25000 | 8 | 669605571 | 21.103 | 2.638 |
| 40000 | seq | 60590308 | | |
| 40000 | 1 | 87751074 | 1.448 | 1.448 |
| 40000 | 2 | 207200752 | 3.420 | 1.710 |
| 40000 | 3 | 361500772 | 5.966 | 1.989 |
| 40000 | 4 | 473432747 | 7.814 | 1.953 |
| 40000 | 8 | 1097413884 | 18.112 | 2.264 |
| 55000 | seq | 89020559 | | |
| 55000 | 1 | 128406686 | 1.442 | 1.442 |
| 55000 | 2 | 292580986 | 3.287 | 1.643 |
| 55000 | 3 | 510675780 | 5.737 | 1.912 |
| 55000 | 4 | 660713297 | 7.422 | 1.856 |
| 55000 | 8 | 1525222197 | 17.133 | 2.142 |
| 70000 | seq | 116905128 | | |
| 70000 | 1 | 169062298 | 1.446 | 1.446 |
| 70000 | 2 | 377961220 | 3.233 | 1.617 |
| 70000 | 3 | 659850789 | 5.644 | 1.881 |
| 70000 | 4 | 847993848 | 7.254 | 1.813 |
| 70000 | 8 | 1953030510 | 16.706 | 2.088 |
| 85000 | seq | 144789698 | | |
| 85000 | 1 | 209717910 | 1.448 | 1.448 |
| 85000 | 2 | 463341454 | 3.200 | 1.600 |
| L | 1 | I . | I . | |

| 85000 | 3 | 809025798 | 5.588 | 1.863 |
|-------|---|------------|--------|-------|
| 85000 | 4 | 1035274399 | 7.150 | 1.788 |
| 85000 | 8 | 2380838822 | 16.443 | 2.055 |

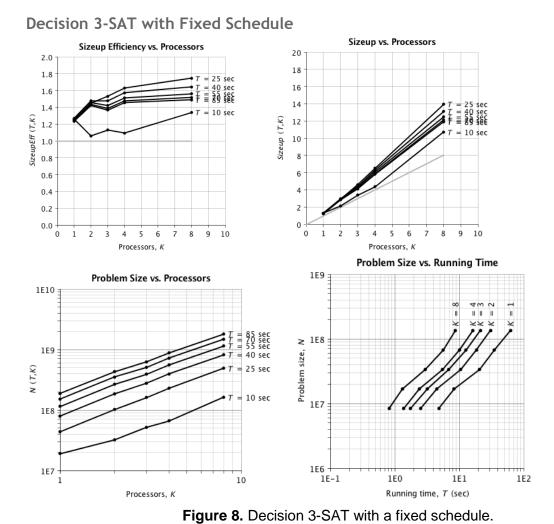


Table 24. Sizeup metrics for the decision parallel program with 23 variables and fixed clause size.

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|-------|-----|----------|--------|-----------|
| т | K | N | Sizeup | SizeupEff |
| 10000 | seq | 15186596 | | |
| 10000 | 1 | 19101819 | 1.258 | 1.258 |
| 10000 | 2 | 32125572 | 2.115 | 1.058 |
| 10000 | 3 | 51499083 | 3.391 | 1.130 |

| 10000 | 4 | 66278741 | 4.364 | 1.091 |
|-------|-----|------------|--------|--------|
| 10000 | 8 | 162484463 | 10.699 | 1.337 |
| 25000 | seq | 35195978 | | |
| 25000 | 1 | 43694379 | 1.241 | 13.948 |
| 25000 | 2 | 102053612 | 2.900 | 1.450 |
| 25000 | 3 | 161423817 | 4.586 | 1.529 |
| 25000 | 4 | 229149829 | 6.511 | 1.628 |
| 25000 | 8 | 490912835 | 13.948 | 1.743 |
| 40000 | seq | 62464180 | | |
| 40000 | 1 | 79123747 | 1.267 | 1.267 |
| 40000 | 2 | 184483432 | 2.953 | 1.477 |
| 40000 | 3 | 276638760 | 4.429 | 1.476 |
| 40000 | 4 | 392431737 | 6.283 | 1.571 |
| 40000 | 8 | 1476197951 | 13.117 | 1.640 |
| 55000 | seq | 91927437 | | |
| 55000 | 1 | 115074925 | 1.252 | 1.252 |
| 55000 | 2 | 266913252 | 2.904 | 1.452 |
| 55000 | 3 | 391853703 | 4.263 | 1.421 |
| 55000 | 4 | 555713644 | 6.045 | 1.511 |
| 55000 | 8 | 1147769579 | 12.486 | 1.561 |
| 70000 | seq | 121841347 | | |
| 70000 | 1 | 151026102 | 1.240 | 1.240 |
| 70000 | 2 | 349343072 | 2.867 | 1.434 |
| 70000 | 3 | 507068647 | 4.162 | 1.387 |

| 70000 | 4 | 718995552 | 5.901 | 1.475 |
|-------|-----|------------|--------|-------|
| 70000 | 8 | 1476197951 | 12.116 | 1.514 |
| 85000 | seq | 151755256 | | |
| 85000 | 1 | 186977279 | 1.232 | 1.232 |
| 85000 | 2 | 431772892 | 2.845 | 1.423 |
| 85000 | 3 | 622283590 | 4.101 | 1.367 |
| 85000 | 4 | 882277459 | 5.814 | 1.453 |
| 85000 | 8 | 1804626323 | 11.892 | 1.486 |

Decision 3-SAT with Dynamic Schedule

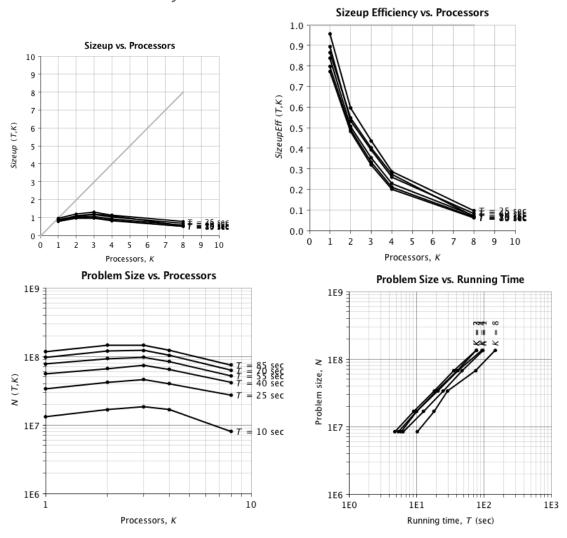


Figure 9. Decision 3-SAT with a dynamic schedule.

Table 25. Sizeup metrics for the decision parallel program with 23 variables and fixed clause size.

| Т | K | N | Sizeup | SizeupEff |
|-------|-----|----------|--------|-----------|
| 10000 | seq | 15186596 | | |
| 10000 | 1 | 13133231 | 0.865 | 0.865 |
| 10000 | 2 | 16610055 | 1.094 | 0.547 |
| 10000 | 3 | 18314861 | 1.206 | 0.402 |
| 10000 | 4 | 16649594 | 1.096 | 0.274 |
| 10000 | 8 | 8026966 | 0.529 | 0.066 |
| 25000 | seq | 35195978 | | |
| 25000 | 1 | 33634320 | 0.956 | 0.956 |
| 25000 | 2 | 41918905 | 1.191 | 0.596 |
| 25000 | 3 | 45939106 | 1.305 | 0.435 |
| 25000 | 4 | 40094089 | 1.139 | 0.285 |
| 25000 | 8 | 27136850 | 0.771 | 0.096 |
| 40000 | seq | 62464180 | | |
| 40000 | 1 | 55825426 | 0.894 | 0.894 |
| 40000 | 2 | 66462548 | 1.064 | 0.532 |
| 40000 | 3 | 73513405 | 1.177 | 0.392 |
| 40000 | 4 | 64790678 | 1.037 | 0.259 |
| 40000 | 8 | 41223005 | 0.660 | 0.082 |
| 55000 | seq | 91927437 | | |
| 55000 | 1 | 77002956 | 0.838 | 0.838 |
| 55000 | 2 | 92958086 | 1.011 | 0.506 |

| 55000 | 3 | 97446666 | 1.060 | 0.353 |
|-------|-----|-----------|-------|-------|
| 55000 | 4 | 84183811 | 0.916 | 0.229 |
| 55000 | 8 | 51840376 | 0.564 | 0.070 |
| 70000 | seq | 121841347 | | |
| 70000 | 1 | 97131992 | 0.797 | 0.797 |
| 70000 | 2 | 119506414 | 0.981 | 0.490 |
| 70000 | 3 | 121379927 | 0.996 | 0.332 |
| 70000 | 4 | 103027558 | 0.846 | 0.211 |
| 70000 | 8 | 62457748 | 0.513 | 0.064 |
| 85000 | seq | 151755256 | | |
| 85000 | 1 | 117261028 | 0.773 | 0.773 |
| 85000 | 2 | 146054743 | 0.962 | 0.481 |
| 85000 | 3 | 145313188 | 0.958 | 0.319 |
| 85000 | 4 | 121871305 | 0.803 | 0.201 |
| 85000 | 8 | 74935910 | 0.494 | 0.062 |

Decision 3-SAT with Guided Schedule

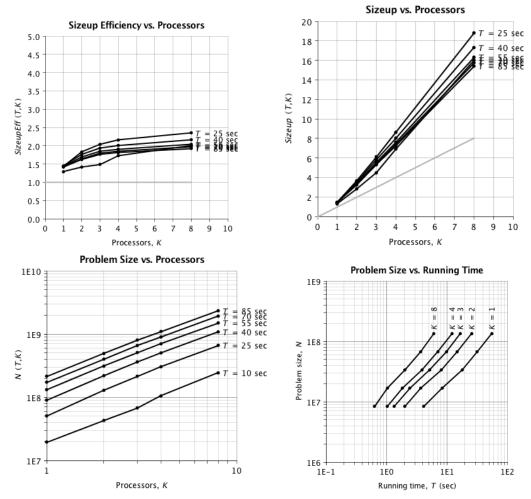


Figure 10. Decision 3-SAT with a guided schedule.

Table 26. Sizeup metrics for the decision parallel program with 23 variables and fixed clause size.

| Т | K | N | Sizeup | SizeupEff |
|-------|-----|-----------|--------|-----------|
| 10000 | seq | 15186596 | | |
| 10000 | 1 | 19544430 | 1.287 | 1.287 |
| 10000 | 2 | 42998164 | 2.831 | 1.416 |
| 10000 | 3 | 67815376 | 4.465 | 1.488 |
| 10000 | 4 | 104942759 | 4.465 | 1.728 |
| 10000 | 8 | 243245196 | 16.017 | 2.002 |
| 25000 | seq | 35195978 | | |

| 25000 | 1 | 50665492 | 1.440 | 1.440 |
|-------|-----|------------|--------|-------|
| 25000 | 2 | 128654581 | 3.655 | 1.828 |
| 25000 | 3 | 215005457 | 6.109 | 2.036 |
| 25000 | 4 | 303372280 | 8.620 | 2.155 |
| 25000 | 8 | 662151962 | 18.813 | 2.352 |
| 40000 | seq | 62464180 | | |
| 40000 | 1 | 90182386 | 1.444 | 1.444 |
| 40000 | 2 | 219456760 | 3.513 | 1.757 |
| 40000 | 3 | 362195537 | 5.798 | 1.933 |
| 40000 | 4 | 501801801 | 8.033 | 2.008 |
| 40000 | 8 | 1081058729 | 17.307 | 2.163 |
| 55000 | seq | 91927437 | | |
| 55000 | 1 | 131751305 | 1.433 | 1.433 |
| 55000 | 2 | 310258940 | 3.375 | 1.688 |
| 55000 | 3 | 509385618 | 5.541 | 1.688 |
| 55000 | 4 | 700231322 | 7.617 | 1.904 |
| 55000 | 8 | 1499965495 | 16.317 | 2.040 |
| 70000 | seq | 121841347 | | |
| 70000 | 1 | 173320225 | 1.423 | 1.423 |
| 70000 | 2 | 401061119 | 3.292 | 1.646 |
| 70000 | 3 | 656575698 | 5.389 | 1.796 |
| 70000 | 4 | 898660843 | 7.376 | 1.844 |
| 70000 | 8 | 1918872262 | 15.749 | 1.969 |
| 85000 | seq | 151755256 | | |
| 85000 | 1 | 214889145 | 1.416 | 1.416 |
| | | | | |

| 85000 | 2 | 491863298 | 3.241 | 1.621 |
|-------|---|------------|--------|-------|
| 85000 | 3 | 803765778 | 5.296 | 1.765 |
| 85000 | 4 | 1097090364 | 7.229 | 1.807 |
| 85000 | 8 | 2337779028 | 15.405 | 1.807 |

Clause Performance Metrics

Exhaustive 3-SAT with Fixed Schedule

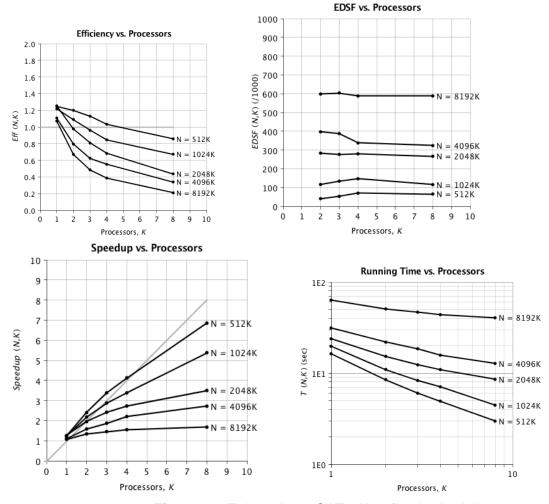


Figure 11. Exhaustive 3-SAT with a fixed schedule.

Table 27. Speedup metrics for the exhaustive parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 20409 | | | |
| 1 | 16345 | 1.249 | 1.249 | |
| 2 | 8507 | 2.399 | 1.200 | 0.041 |
| 3 | 6027 | 3.386 | 1.129 | 0.053 |
| 4 | 4942 | 4.130 | 1.032 | 0.070 |
| 8 | 2979 | 6.851 | 0.856 | 0.065 |

Table 28. Speedup metrics for the exhaustive parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23986 | | | |
| 1 | 19714 | 1.217 | 1.217 | |
| 2 | 11004 | 2.180 | 1.090 | 0.116 |
| 3 | 8336 | 2.877 | 0.959 | 0.134 |
| 4 | 7096 | 3.380 | 0.845 | 0.147 |
| 8 | 4458 | 5.380 | 0.673 | 0.116 |

Table 29. Speedup metrics for the exhaustive parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 29890 | | | |
| 1 | 23863 | 1.253 | 1.253 | |
| 2 | 15312 | 1.952 | 0.976 | 0.283 |
| 3 | 12353 | 2.420 | 0.807 | 0.276 |
| 4 | 10968 | 2.725 | 0.681 | 0.279 |

| 8 | 8549 | 3.496 | 0.437 | 0.267 |
|---|------|-------|-------|-------|
| ľ | 00.0 | 00 | 0.101 | 0.20. |

Table 30. Speedup metrics for the exhaustive parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 34727 | | | |
| 1 | 31344 | 1.108 | 1.108 | |
| 2 | 21892 | 1.586 | 0.793 | 0.397 |
| 3 | 18544 | 1.873 | 0.624 | 0.387 |
| 4 | 15760 | 2.203 | 0.551 | 0.337 |
| 8 | 12786 | 2.716 | 0.340 | 0.323 |

Table 31. Speedup metrics for the exhaustive parallel program with 8192K clauses and a fixed number of variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67998 | | | |
| 1 | 63510 | 1.071 | 1.071 | |
| 2 | 50749 | 1.340 | 0.670 | 0.598 |
| 3 | 46750 | 1.455 | 0.485 | 0.604 |
| 4 | 43875 | 1.550 | 0.387 | 0.588 |
| 8 | 40588 | 1.675 | 0.209 | 0.588 |

Decision 3-SAT with Fixed Schedule

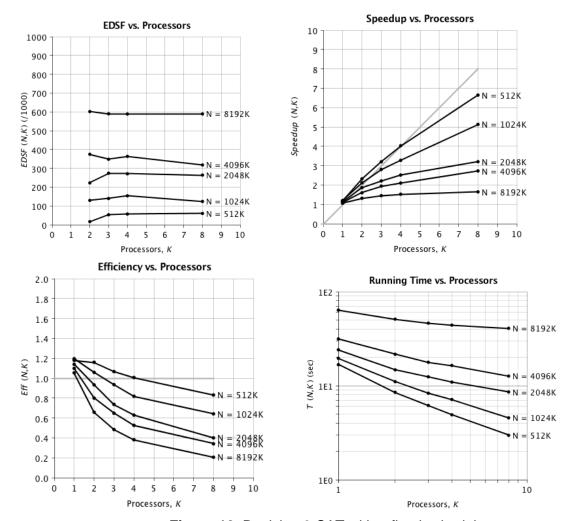


Figure 12. Decision 3-SAT with a fixed schedule.

Table 32. Speedup metrics for the decision parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 19720 | | | |
| 1 | 16732 | 1.179 | 1.179 | |
| 2 | 8504 | 2.319 | 1.159 | 0.016 |
| 3 | 6167 | 3.198 | 1.066 | 0.053 |
| 4 | 4898 | 4.026 | 1.007 | 0.057 |
| 8 | 2968 | 6.644 | 0.831 | 0.060 |

Table 33. Speedup metrics for the decision parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23340 | | | |
| 1 | 19526 | 1.195 | 1.195 | |
| 2 | 11025 | 2.117 | 1.059 | 0.129 |
| 3 | 8325 | 2.804 | 0.935 | 0.140 |
| 4 | 7132 | 3.273 | 0.818 | 0.154 |
| 8 | 4551 | 5.129 | 0.641 | 0.124 |

Table 34. Speedup metrics for the decision parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 27449 | | | |
| 1 | 24093 | 1.139 | 1.139 | |
| 2 | 14726 | 1.864 | 0.932 | 0.222 |
| 3 | 12432 | 2.208 | 0.736 | 0.274 |
| 4 | 10918 | 2.514 | 0.629 | 0.271 |
| 8 | 8574 | 3.201 | 0.400 | 0.264 |

Table 35. Speedup metrics for the decision parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 34501 | | | |
| 1 | 31407 | 1.099 | 1.099 | |
| 2 | 21584 | 1.598 | 0.799 | 0.374 |
| 3 | 17757 | 1.943 | 0.648 | 0.348 |
| 4 | 16410 | 2.102 | 0.526 | 0.363 |
| 8 | 12659 | 2.725 | 0.341 | 0.318 |

Table 36. Speedup metrics for the decision parallel program with 8192K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67132 | | | |
| 1 | 63681 | 1.054 | 1.054 | |
| 2 | 50996 | 1.316 | 0.658 | 0.602 |
| 3 | 46274 | 1.451 | 0.484 | 0.590 |
| 4 | 44029 | 1.525 | 0.381 | 0.589 |

| 8 | 40782 | 1.646 | 0.206 | 0.589 |
|---|-------|-------|-------|-------|
| ~ | 10.02 | 11010 | 0.200 | 0.000 |

Exhaustive 3-SAT with Dynamic Schedule

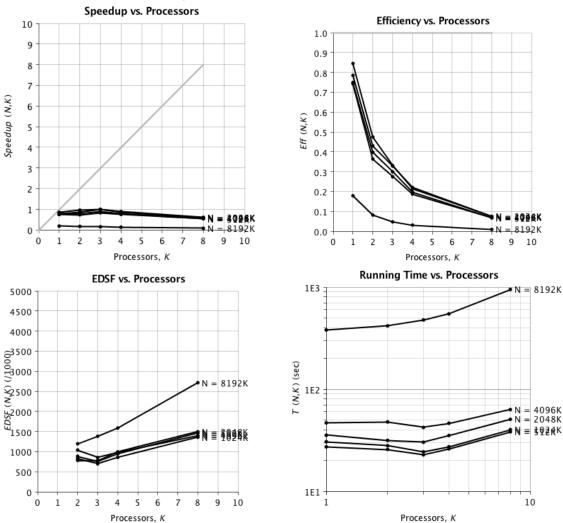


Figure 13. Exhaustive 3-SAT with a dynamic schedule.

Table 37. Speedup metrics for the exhaustive parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 20409 | | | |
| 1 | 27245 | 0.749 | 0.749 | |
| 2 | 27245 | 0.795 | 0.397 | 0.885 |

| 3 | 22761 | 0.897 | 0.299 | 0.753 |
|---|-------|-------|-------|-------|
| 4 | 26067 | 0.783 | 0.196 | 0.942 |
| 8 | 38264 | 0.533 | 0.067 | 1.462 |

Table 38. Speedup metrics for the exhaustive parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23986 | | | |
| 1 | 30566 | 0.785 | 0.785 | |
| 2 | 27921 | 0.859 | 0.430 | 0.827 |
| 3 | 24347 | 0.985 | 0.328 | 0.695 |
| 4 | 27276 | 0.879 | 0.220 | 0.856 |
| 8 | 40156 | 0.597 | 0.075 | 1.359 |

Table 39. Speedup metrics for the exhaustive parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 29890 | | | |
| 1 | 35395 | 0.844 | 0.844 | |
| 2 | 31511 | 0.949 | 0.474 | 0.781 |
| 3 | 30175 | 0.991 | 0.330 | 0.779 |
| 4 | 35179 | 0.850 | 0.212 | 0.992 |
| 8 | 50720 | 0.589 | 0.074 | 1.495 |

Table 40. Speedup metrics for the exhaustive parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|------|
| seq | 34727 | | | |

| 1 | 46796 | 0.742 | 0.742 | |
|---|-------|-------|-------|-------|
| 2 | 47744 | 0.727 | 0.364 | 1.041 |
| 3 | 42179 | 0.823 | 0.274 | 0.852 |
| 4 | 46389 | 0.749 | 0.187 | 0.988 |
| 8 | 63198 | 0.549 | 0.069 | 1.401 |

Table 41. Speedup metrics for the exhaustive parallel program with 8192K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67998 | | | |
| 1 | 380129 | 0.179 | 0.179 | |
| 2 | 417345 | 0.163 | 0.081 | 1.196 |
| 3 | 477144 | 0.143 | 0.048 | 1.383 |
| 4 | 547297 | 0.124 | 0.031 | 1.586 |
| 8 | 950297 | 0.072 | 0.009 | 2.714 |

Decision 3-SAT with Dynamic Schedule

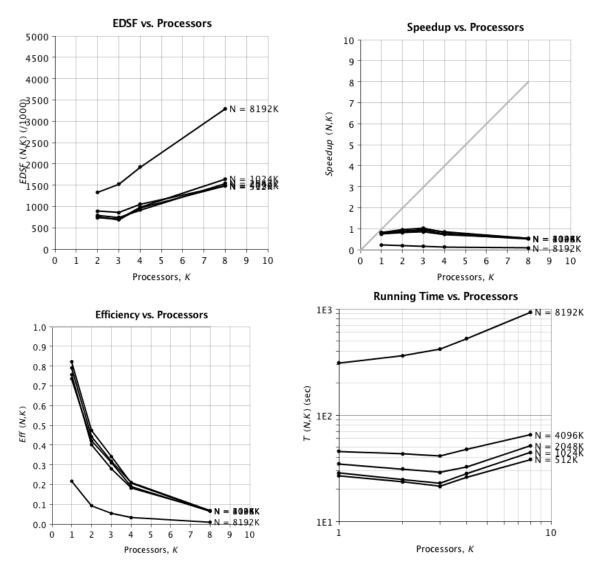


Figure 14. Decision 3-SAT with a dynamic schedule.

Table 42. Speedup metrics for the decision parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 19720 | | | |
| 1 | 26811 | 0.736 | 0.736 | |
| 2 | 23433 | 0.842 | 0.421 | 0.748 |
| 3 | 21218 | 0.929 | 0.310 | 0.687 |
| 4 | 26051 | 0.757 | 0.189 | 0.962 |

|--|

Table 43. Speedup metrics for the decision parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23340 | | | |
| 1 | 28400 | 0.822 | 0.822 | |
| 2 | 24624 | 0.948 | 0.474 | 0.734 |
| 3 | 22813 | 1.023 | 0.341 | 0.705 |
| 4 | 28131 | 0.830 | 0.207 | 0.987 |
| 8 | 44323 | 0.527 | 0.066 | 1.641 |

Table 44. Speedup metrics for the decision parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 27449 | | | |
| 1 | 34721 | 0.791 | 0.791 | |
| 2 | 31081 | 0.883 | 0.442 | 0.790 |
| 3 | 28752 | 0.955 | 0.318 | 0.742 |
| 4 | 32599 | 0.842 | 0.211 | 0.919 |
| 8 | 51276 | 0.535 | 0.067 | 1.545 |

Table 45. Speedup metrics for the decision parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 34501 | | | |
| 1 | 45623 | 0.756 | 0.756 | |
| 2 | 43018 | 0.802 | 0.401 | 0.886 |
| 3 | 41152 | 0.838 | 0.279 | 0.853 |
| 4 | 47518 | 0.726 | 0.182 | 1.055 |

|--|

Table 46. Speedup metrics for the decision parallel program with 8192K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67132 | | | |
| 1 | 310079 | 0.216 | 0.216 | |
| 2 | 361244 | 0.186 | 0.093 | 1.330 |
| 3 | 418479 | 0.160 | 0.053 | 1.524 |
| 4 | 525520 | 0.128 | 0.032 | 1.926 |
| 8 | 931440 | 0.072 | 0.009 | 3.290 |

Exhaustive 3-SAT with Guided Schedule

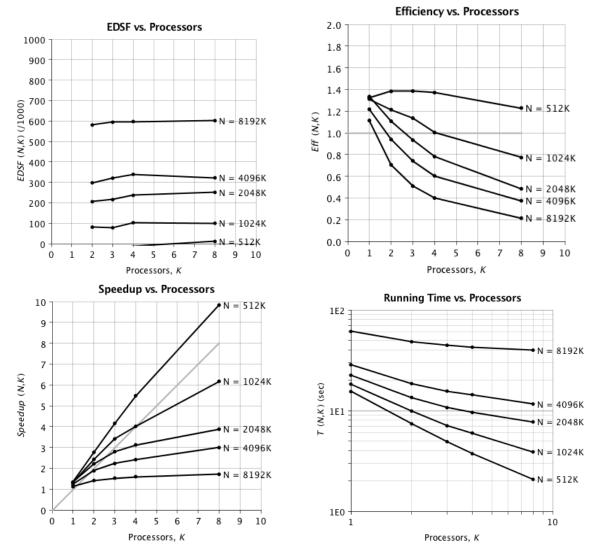


Figure 15. Exhaustive 3-SAT with a guided schedule.

Table 47. Speedup metrics for the exhaustive parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|--------|
| seq | 20409 | | | |
| 1 | 15417 | 1.324 | 1.324 | |
| 2 | 7383 | 2.764 | 1.382 | -0.042 |
| 3 | 4913 | 4.154 | 1.385 | -0.022 |
| 4 | 3722 | 5.483 | 1.371 | -0.011 |

| 1-2.2 | 8 | 2076 | 9.831 | 1.229 | 0.011 |
|-------|---|------|-------|-------|-------|
|-------|---|------|-------|-------|-------|

Table 48. Speedup metrics for the exhaustive parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23986 | | | |
| 1 | 18293 | 1.311 | 1.311 | |
| 2 | 9883 | 2.427 | 1.213 | 0.081 |
| 3 | 7043 | 3.406 | 1.135 | 0.078 |
| 4 | 5980 | 4.011 | 1.003 | 0.103 |
| 8 | 3887 | 6.171 | 0.771 | 0.100 |

Table 49. Speedup metrics for the exhaustive parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 29890 | | | |
| 1 | 22405 | 1.334 | 1.334 | |
| 2 | 13500 | 2.214 | 1.107 | 0.205 |
| 3 | 10686 | 2.797 | 0.932 | 0.215 |
| 4 | 9572 | 3.123 | 0.781 | 0.236 |
| 8 | 7716 | 3.874 | 0.484 | 0.251 |

Table 50. Speedup metrics for the exhaustive parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 34727 | | | |
| 1 | 28528 | 1.217 | 1.217 | |
| 2 | 18510 | 1.876 | 0.938 | 0.298 |

| 3 | 15601 | 2.226 | 0.742 | 0.320 |
|---|-------|-------|-------|-------|
| 4 | 14384 | 2.414 | 0.604 | 0.339 |
| 8 | 11610 | 2.991 | 0.374 | 0.322 |

Table 51. Speedup metrics for the exhaustive parallel program with 8192K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67998 | | | |
| 1 | 61070 | 1.113 | 1.113 | |
| 2 | 48248 | 1.409 | 0.705 | 0.580 |
| 3 | 44535 | 1.527 | 0.509 | 0.594 |
| 4 | 42617 | 1.596 | 0.399 | 0.597 |
| 8 | 39781 | 1.709 | 0.214 | 0.602 |

Decision 3-SAT with Guided Schedule

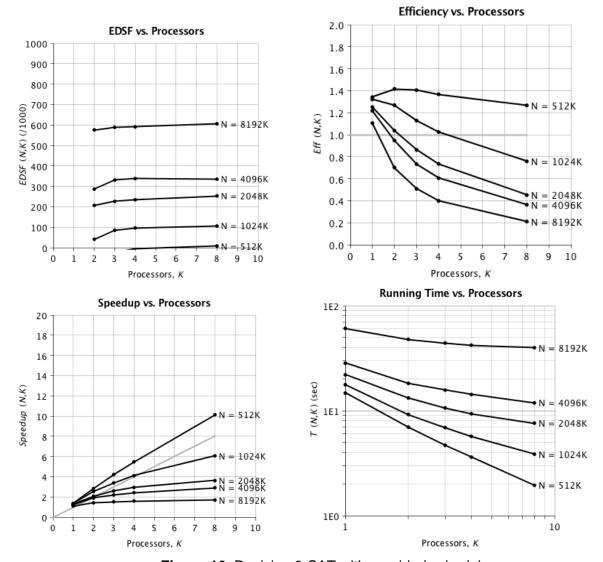


Figure 16. Decision 3-SAT with a guided schedule.

Table 52. Speedup metrics for the decision parallel program with 512K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|--------|
| seq | 19720 | | | |
| 1 | 14706 | 1.341 | 1.341 | |
| 2 | 6961 | 2.833 | 1.416 | -0.053 |
| 3 | 4681 | 4.213 | 1.404 | -0.023 |
| 4 | 3605 | 5.470 | 1.368 | -0.006 |
| 8 | 1947 | 10.128 | 1.266 | 0.008 |

Table 53. Speedup metrics for the decision parallel program with 1024K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 23340 | | | |
| 1 | 17677 | 1.320 | 1.320 | |
| 2 | 9202 | 2.536 | 1.268 | 0.041 |
| 3 | 6895 | 3.385 | 1.128 | 0.085 |
| 4 | 5695 | 4.098 | 1.025 | 0.096 |
| 8 | 3850 | 6.062 | 0.758 | 0.106 |

Table 54. Speedup metrics for the decision parallel program with 2048K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 27449 | | | |
| 1 | 21942 | 1.251 | 1.251 | |
| 2 | 13240 | 2.073 | 1.037 | 0.451 |
| 3 | 10620 | 2.585 | 0.862 | 0.226 |
| 4 | 9344 | 2.938 | 0.734 | 0.234 |
| 8 | 7600 | 3.612 | 0.451 | 0.253 |

Table 55. Speedup metrics for the decision parallel program with 4096K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|------|
| seq | 34501 | | | |
| 1 | 28332 | 1.218 | 1.218 | |

| 2 | 18216 | 1.894 | 0.947 | 0.286 |
|---|-------|-------|-------|-------|
| 3 | 15693 | 2.198 | 0.733 | 0.331 |
| 4 | 14254 | 2.420 | 0.605 | 0.337 |
| 8 | 11850 | 2.911 | 0.605 | 0.335 |

Table 56. Speedup metrics for the decision parallel program with 8192K clauses and 25 variables.

| NT | Time (ms) | Speedup | Efficiency | ESDF |
|-----|-----------|---------|------------|-------|
| seq | 67132 | | | |
| 1 | 60751 | 1.105 | 1.105 | |
| 2 | 47867 | 1.402 | 0.701 | 0.576 |
| 3 | 44082 | 1.523 | 0.508 | 0.588 |
| 4 | 42085 | 1.595 | 0.399 | 0.590 |
| 8 | 39800 | 1.687 | 0.211 | 0.606 |