

# Part A

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```
1 A <-- Array // An array that has enough space to contain all elements in
  the tree
2 count <-- 0
3
4 // Traverse the tree in order and put values in an array
5 function inorder_traversal(tree):
6     if (tree != NULL):
7         if (tree->val1 != NULL):
8             inorder_traversal(tree->child0)
9             A[count] = tree->val1
10            count <-- count + 1
11            inorder_traversal(tree->child1)
12
13        if (tree->val2 != NULL):
14            inorder_traversal(tree->child2)
15            A[count] = tree->val2
16            count <-- count + 1
17
18        if (tree->val3 != NULL):
19            inorder_traversal(tree->child4)
20            A[count] = tree->val3
21            count <-- count + 1
22
23 function find_median(A[0...n]):
24     return A[(n + 1) / 2]
```

## Part B

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```
1 function count_descendants(node):  
2     num_descendant <-- 0  
3     for not null child in node->childrens:  
4         num_descendant <-- num_descendant + child->num_vals + child-  
>num_descendant  
5     return num_descendant
```

# Part C

```
1 total_val_count <-- tree->num_descendants + tree->num_vals // number of
  values in the tree
2 target_count <-- (total_val_count + 1) / 2 // index of the median
3 temp = 0 // used to store number of values of each child
4
5 // check through each child and value in each level
6 // to find where the median index is located
7 function find_median_efficient(tree):
8     if (tree->child0 != NULL):
9         temp = tree->child0->num_descendants + tree->child0->num_vals
10    if (total_val_count - temp < target_count):
11        return find_median_efficient(tree->child0)
12    else if (total_val_count - temp == target_count):
13        return tree->val0
14    total_val_count = total_val_count - temp - 1
15    temp = 0
16
17    if (tree->child1 != NULL):
18        temp = tree->child1->num_descendants + tree->child1->num_vals //
Number of values in the second node
19    else if (total_val_count - temp < target_count):
20        return find_median_efficient(tree->child1)
21    else if (total_val_count - temp == target_count):
22        return tree->val1
23    total_val_count = total_val_count - temp - 1
24    temp = 0
25
26    if (tree->child2 != NULL):
27        temp = tree->child2->num_descendants + tree->child2->num_vals //
Number of values in the third node
28    else if (total_val_count - temp < target_count):
29        return find_median_efficient(tree->child2)
30    else if (total_val_count - temp == target_count):
31        return tree->val2
32    total_val_count = total_val_count - temp - 1
33    temp = 0
34
35    // Median must be in the last child
36    return find_median_efficient(tree->child3)
37
```

## Part D

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Since `num_descendants` and `num_vals` are computed before running the find median algorithm and included in the tree structure, it will only take  $O(1)$  time to get them.

In the best case, in which the median is the first value of the root, it will only take  $O(1)$  time to get the result.

Since there are at most 4 children of each node, it will take  $O(1)$  time to travel through them

In the worst case, the median is in the leaf node of the longest branch of the tree, and that branch is located in the right most child. Since travelling through children in a level will only take  $O(1)$  time, the algorithm will take  $\theta(h)$  time to travel to the bottom of the tree, where  $h$  represents the height of the tree.

In terms of space complexity, neglecting the memory usage for recursion, the algorithm will take  $O(1)$  space since it doesn't require any external storage besides several variables that store temporary data.