

Homework 5 Responses

Chris Crabtree

Sept. 30, 2021

I chose to try and use R for this homework (I always use python and am new to R). Learning the syntax and proper functions to manipulate data common data structures became very time consuming and I was not able to finish all the problems.

1

1.a

The plot for importance resampling for $n = 100$ can be found in Figure 1. The plot for $n = 10000$ can be found in Figure 2.

1.b

n=100

For $n = 100$, my estimate $\hat{\mu} = -0.119$.

For the t distribution with 3 degrees of freedom, t_3 , the mean should be 0.

My s^2 estimate for the variance was 1.25915827778705

For the t_3 distribution this variance is 3.

These do not seem like very good estimate so I would like to explain my calculation. I calculated the mean by using the dot product of my proposal samples and the normalized 'weights', where each weight is the proposal density divided by the t_3 (true) density of a each sample.

For the sample variance I element-wise multiplied the samples by each corresponding weight, then subtracted my mean estimate, square, summed, and divided by $n - 1$.

These calculations seemed correct to me and my resampling looked good

n=10000

The same caluculations as above produces $\hat{\mu} = -0.0499$ and $s^2 = 13.7920400662904$. There was clearly something wrong with my calculation, but I could not figure out what. My resampling plots looked good so I couldn't figure out the issue.

2

I used a burn in of 20 and a thinning stride of 4. The plot of the samples along with the contour plot can be seen in Figure 3. When I calculated the posterior means by hand I got $\mathbb{E}[X_1|X_2] = \mu_1 - .75(x_2 - 2)$, but this caused a negative correlation in the variables so I manually flipped the sign. Still, I'm unsure where my calculation went wrong.

The trace plot for the first variable (mean=0) is in Figure 4 and the autocorrelation (after thinning) for the same variable is in Figure 5.

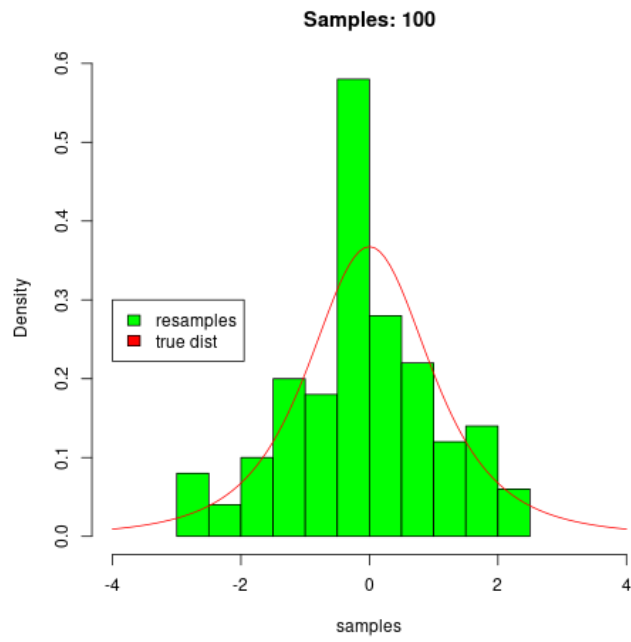


Figure 1: Importance sampling. $n=100$

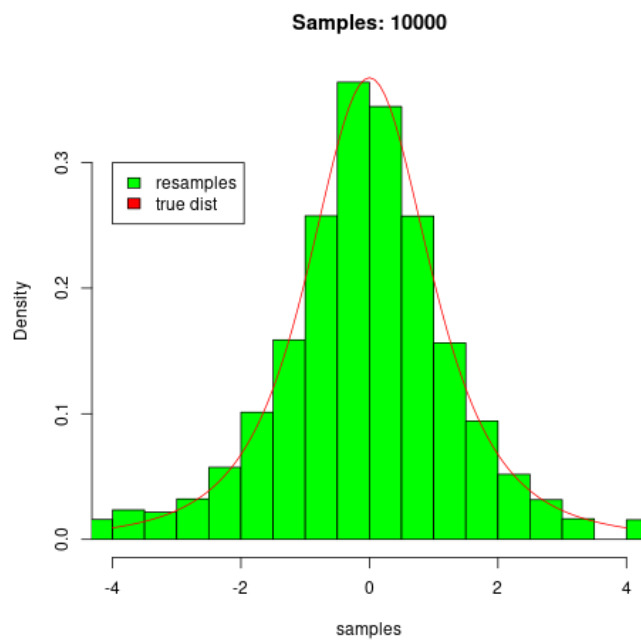


Figure 2: Importance sampling. $n=100$

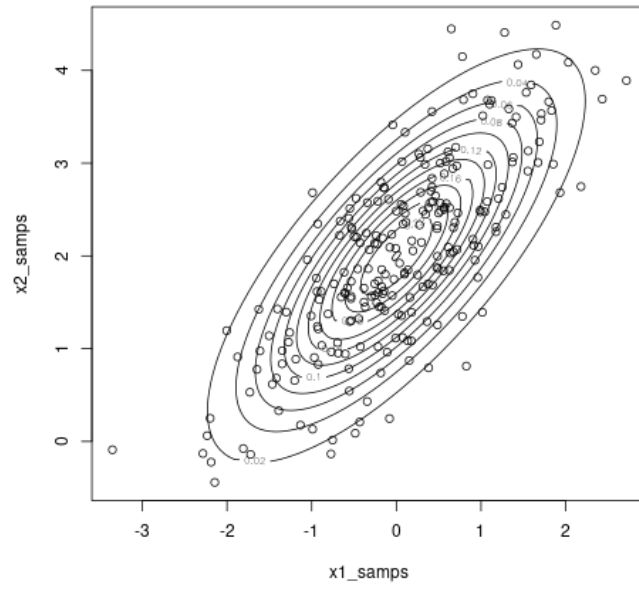


Figure 3: Results of Gibbs sampling.

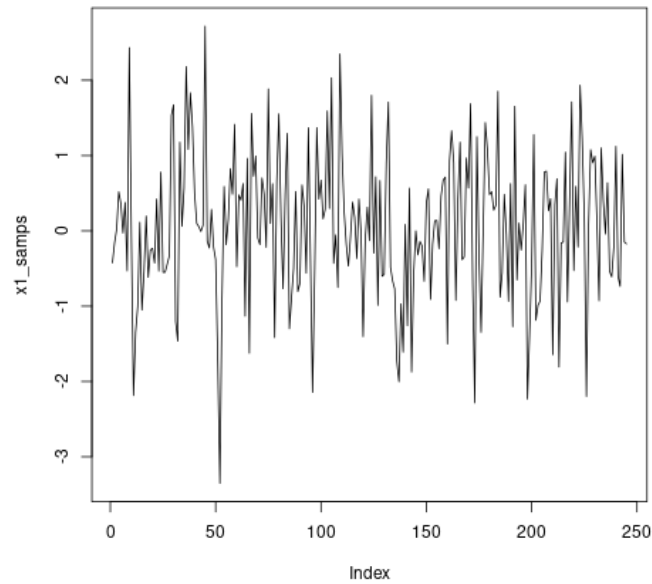


Figure 4: Trace plot of the MCMC samples from the first variable

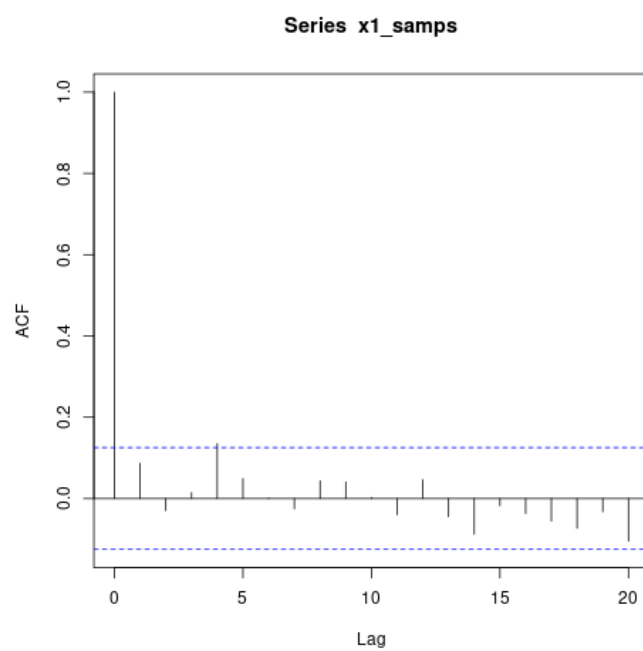


Figure 5: Autocorrelation plot of the MCMC samples of the first variable