# Security of Cyber-Physical Systems

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Outline

- Background and motivation

- CPS attack models

- Risk management

- Attack detectability and security metrics

- Attack identification and secure state estimation

ICS-CERT MONIT⊙R

INCIDENT RESPONSE ACTIVITY
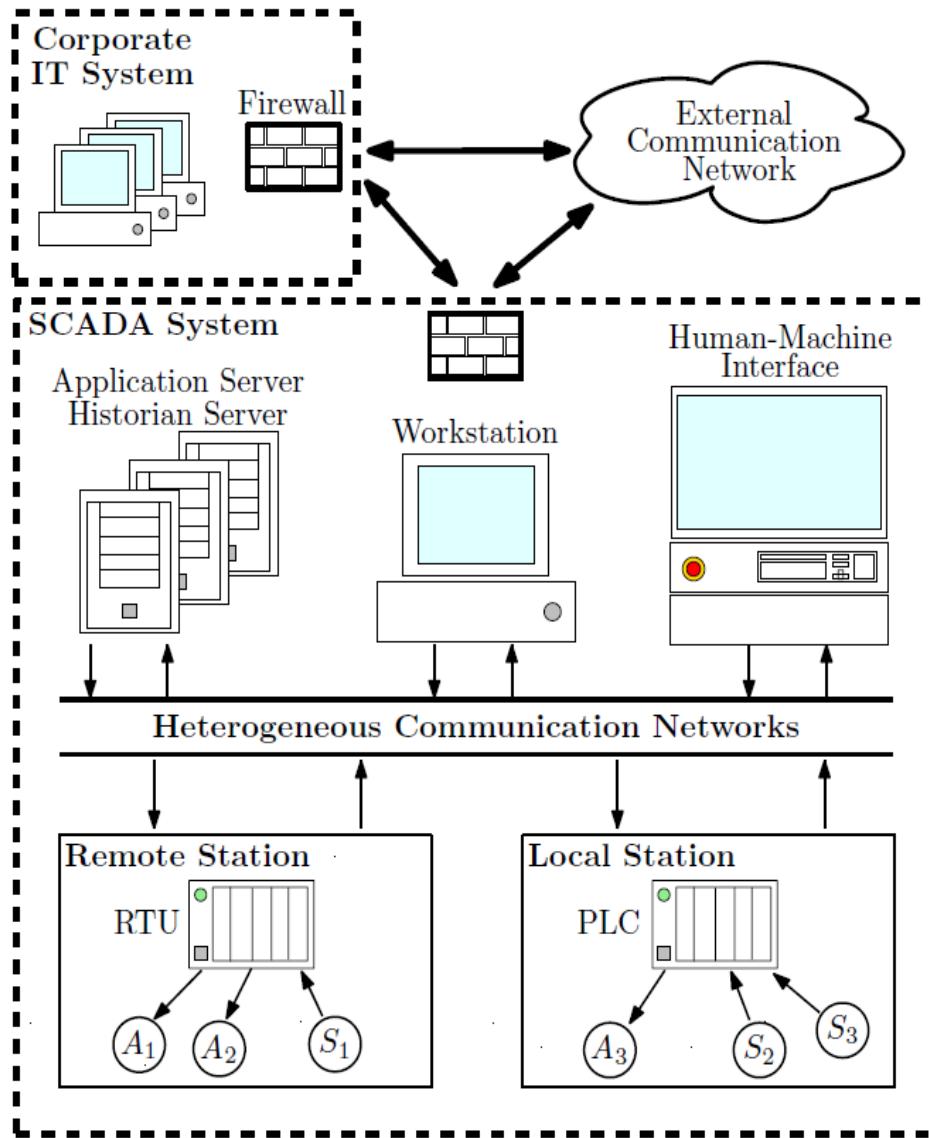
INTERNET ACCESSIBLE CONTROL SYSTEMS AT RISK

Is your control system accessible directly from the Internet? Do you use remote access features to log into your control system network? Are you unsure of the security measures that protect your remote access services? If your answer was yes to any or all these questions, you are at increased risk of cyber attacks including scanning, probes, brute force attempts and unauthorized access to your control environment.

ICS-CERT = Industrial Control Systems Cyber Emergency Response Team (https://ics-cert.us-cert.gov/)
Part of US Department of Homeland Security

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# Example 1: Industrial Control System (ICS) Infrastructure

Example 2: The Stuxnet Worm (2010)

Targets: Windows, ICS, and PLCs connected to variable-frequency drives
Exploited **4 zero-day flaws**

- **Speculated goal:**
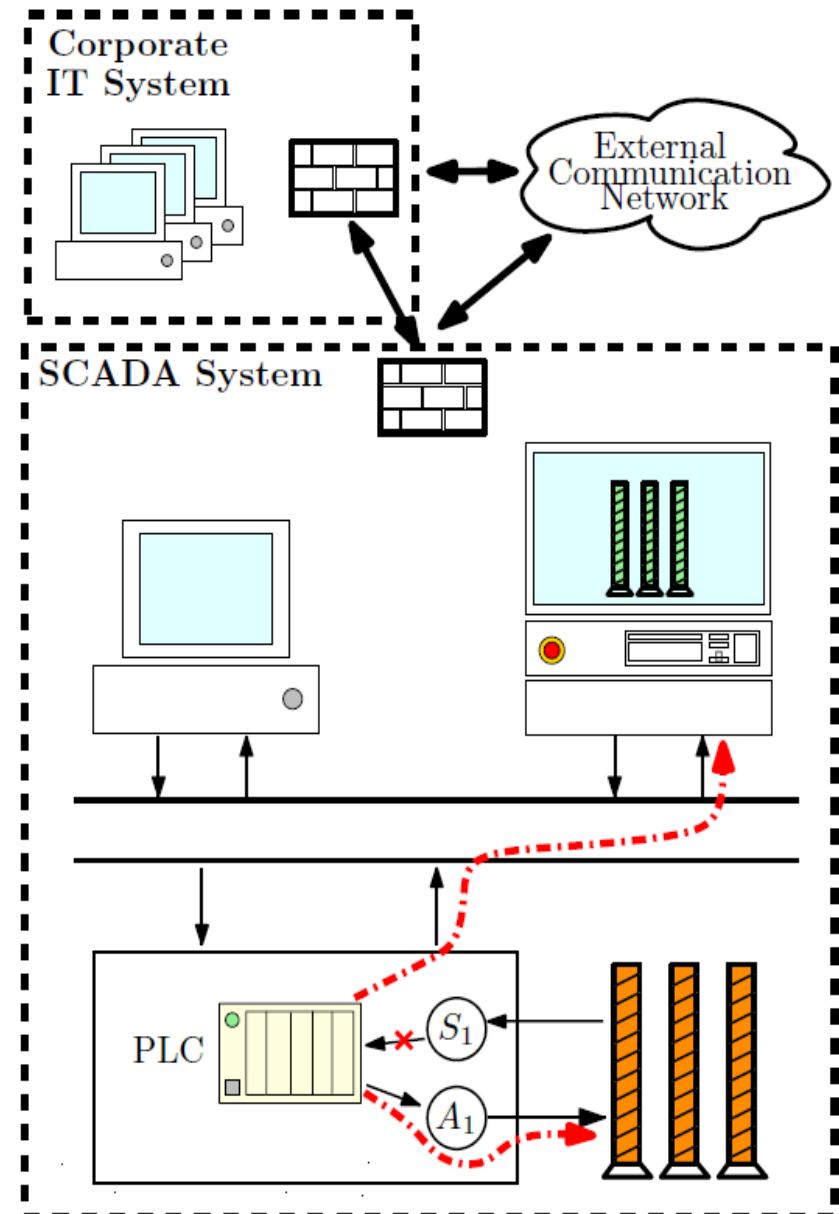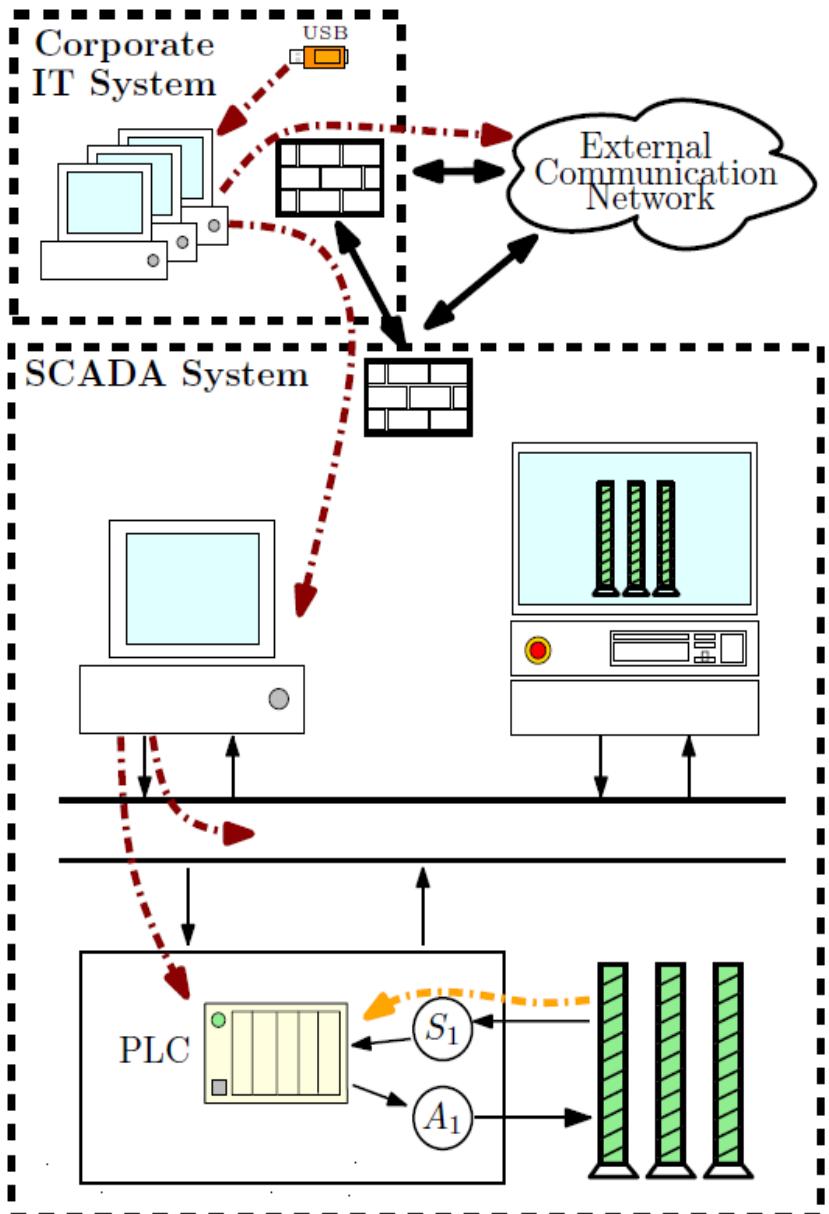
Harm centrifuges at uranium enrichment facility in Iran

- **Attack mode:**

1. Delivery with USB stick (**no internet connection necessary**)

2. Replay measurements to control center and execute harmful controls

["The Real Story of Stuxnet", IEEE Spectrum, 2013]
(See also http://www.zerodaysfilm.com/)

(a) Infection and data recording.

(b) Covert sabotage.

Example 3: Events in Ukraine (December, 2015)

Analysis confirms coordinated hack attack caused Ukrainian power outage

BlackEnergy was key ingredient used to cause power outage to at least 80k customers.

by **Dan Goodin** - Jan 11, 2016 5:42am GMT

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The people who carried out last month's first known hacker-caused power outage used highly destructive malware to gain a foothold into multiple regional distribution power companies in Ukraine and delay restoration efforts once electricity had been shut off, a newly published analysis confirms.

The malware, known as BlackEnergy, allowed the attackers to gain a foothold on the power company systems, said the report, which was published by a member of the SANS

FURTHER READING

The report stresses there's no evidence BlackEnergy or its recently developed KillDisk component was the direct cause of the outage, which so far has been shown to affect about 80,000 customers. The analysis also cautioned that evidence showing some past BlackEnergy infections relied on booby-trapped Microsoft Office documents to spread are no indication such a vector was used in the recent Ukrainian power grid attacks. Still, this weekend's report leaves little doubt the blackout was the result of a highly coordinated hacker attack that relied on BlackEnergy as a key ingredient.

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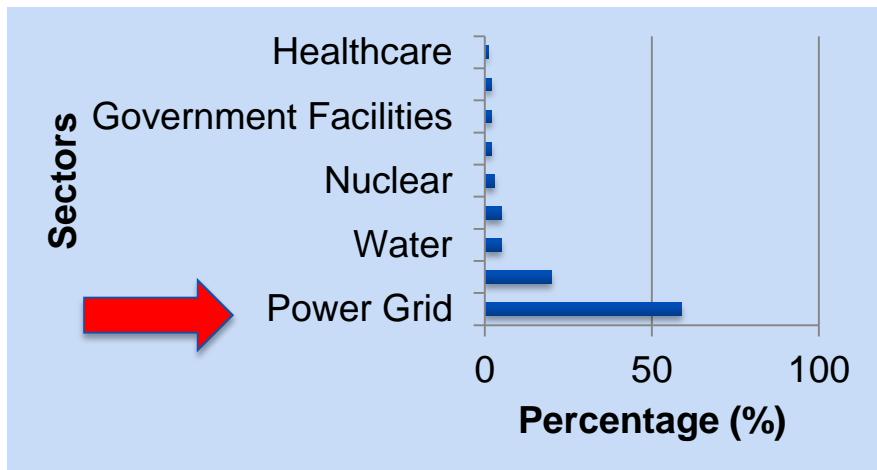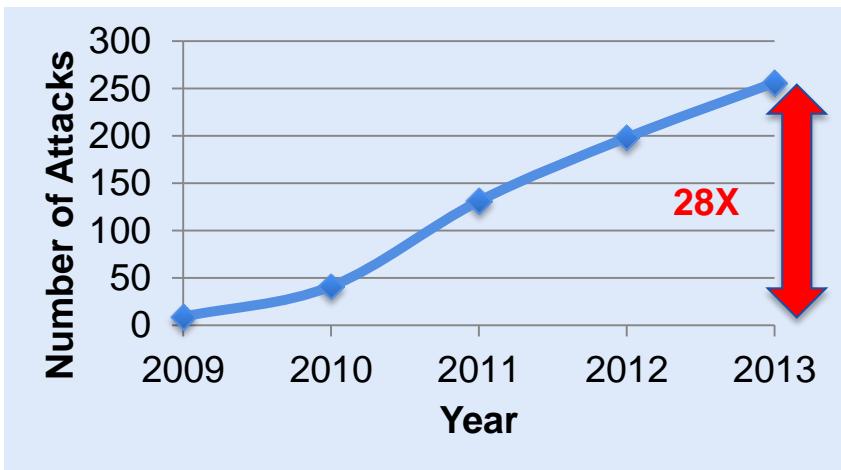
Example 3: Events in Ukraine (December, 2015)

- BlackEnergy (2007-)
- From arstechnica.com:
  - "In 2014 … targeted the North Atlantic Treaty Organization, Ukrainian and Polish government agencies, and a variety of sensitive European industries"
  - "booby-trapped macro functions embedded in Microsoft Office documents"
  - "render infected computers unbootable"
  - "KillDisk, which destroys critical parts of a computer hard drive"
  - "backdoored secure shell (SSH) utility that gives attackers permanent access to infected computers"
- More advanced, more autonomous, follow-up attack in 2016: "Crash Override"

Some Statistics

Cyber incidents in critical infrastructures in the US
(Voluntarily reported to ICS-CERT)

[ICS-CERT, 2013]
[S. Zonouz, 2014]
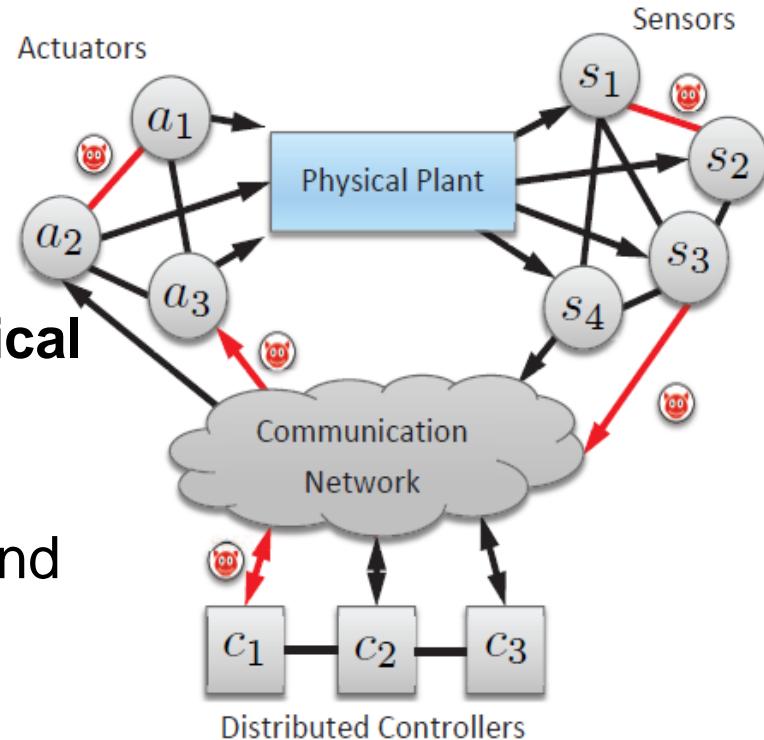
Cyber-Physical Security

Networked control systems

- are being **integrated with business/corporate networks**
- have many potential points of **cyber-physical attack**
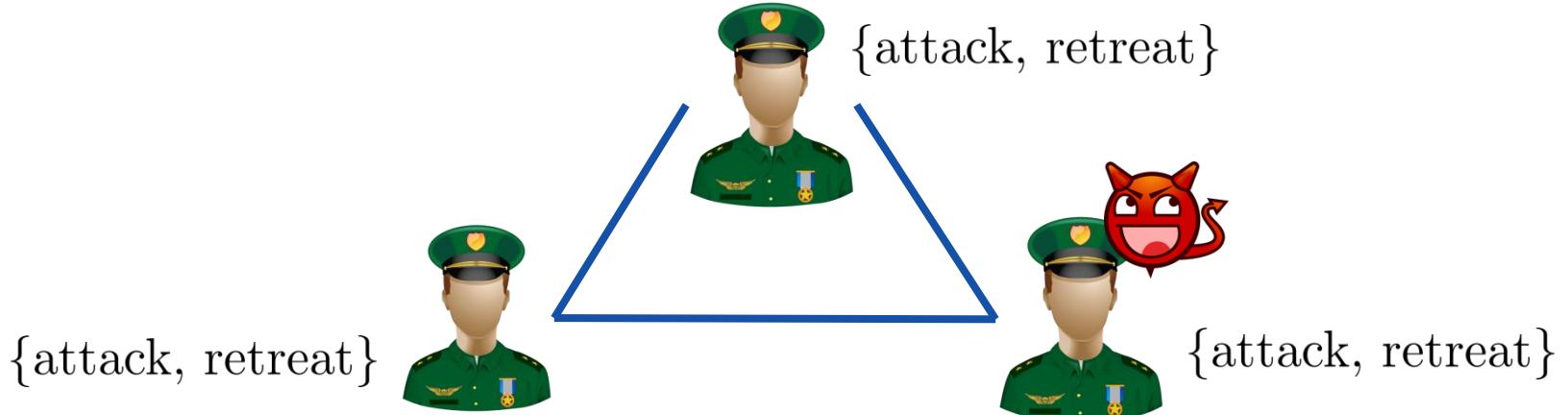
Need tools and strategies to understand and mitigate attacks:

- Which threats should we care about?
- What impact can we expect from attacks?
- Which resources should we protect (more), and how?

Is it enough to apply cyber (IT) security solutions?

Example of Classic Cyber Security:
The Byzantine Generals Problem
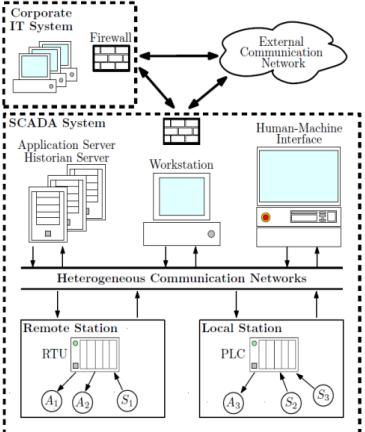
- Consider n generals and q unknown traitors among them. Can the $n - q$ loyal generals always reach an agreement?
- Traitors ("Byzantine faults") can do anything: different message to different generals, send no message, change forwarded message,…
- Agreement protocol exists iff $n \geq 3q + 1$
- If loyal generals use unforgeable signed messages ("authentication") then agreement protocol exists for any q! [Lamport *et al.*, ACM TOPLAS, 1982]

- Application to linear consensus computations: See [Pasqualetti *et al.*, CDC, 2007], [Sundaram and Hadjicostis, ACC, 2008]

Special Controls Perspective Needed?

Clearly cyber (IT) security is needed: Authentication, encryption, firewalls, etc.

But not sufficient…

Interaction between physical and cyber systems make control systems different from normal IT systems

Malicious actions can enter anywhere in the closed loop and cause harm, whether channels secured or not

Can we trust the interfaces and channels are really secured? (see OpenSSL Heartbleed bug…)

[Cardenas *et al*., 2008]

Security Challenges in ICS
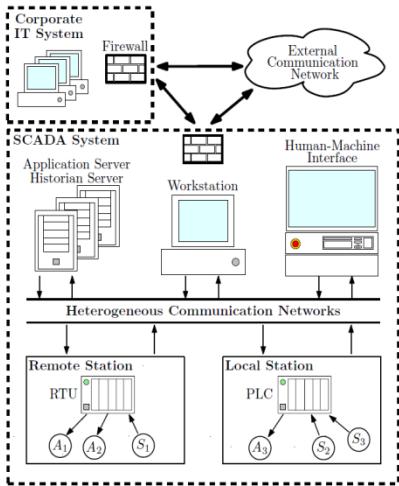
"New" vulnerabilities and "new" threats:

- **Controllers are computers** (Relays → Microprocessors)
- **Networked** (Access from corporate network)
- **Commodity IT solutions** (Windows, TCP/IP,…)
- **Open design** (Protocols known)
- **Increasing size and functionality** (New services, wireless,...)
- **Large and highly skilled IT global workforce** (More IT knowledge)
- **Cybercrime** (Attack tools available)

[Cardenas *et al*., 2008]

Security Challenges in ICS

Differences to traditional IT systems:

- **Patching and frequent updates are not well suited for control systems**

- **Real-time availability** (Strict operational environment)

- **Legacy systems** (Often no authentication or encryption)

- **Protection of information and physical world** (Estimation and control algorithms)

- **Simpler network dynamics** (fixed topology, regular communication, limited number of protocols,…)
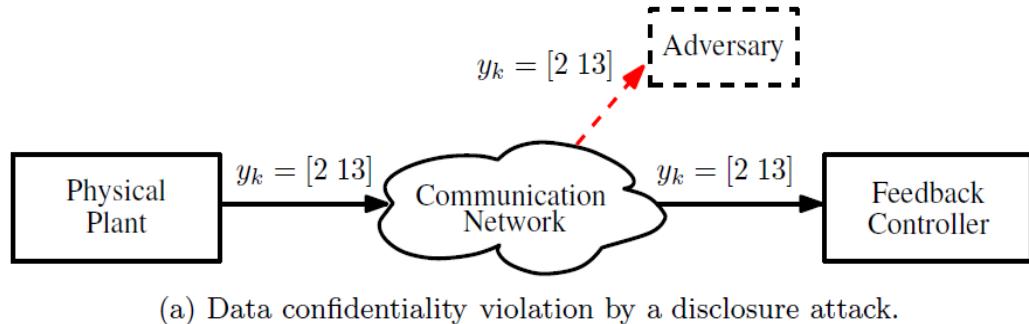
[Cardenas *et a*l., 2008]

CIA in Cyber Security [Bishop, 2002]

C – Confidentiality
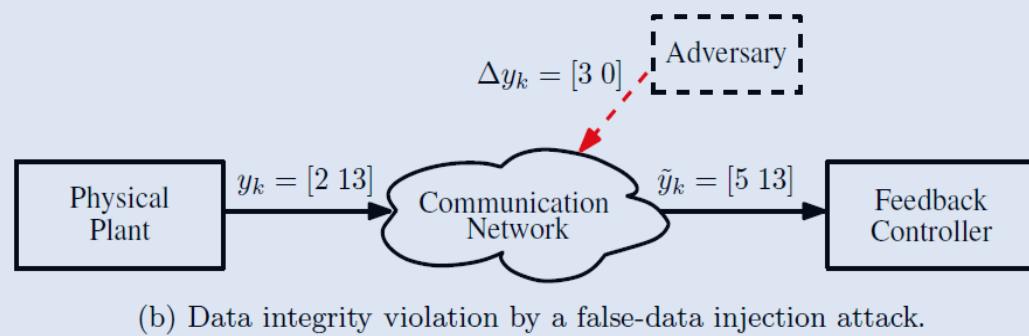
"Privacy"
(See recent work by Le Ny, Pappas, Dullerud, Cortes, Tanaka, Sandberg,…)

$y_k = [2\ 13]$

$y_k = [2\ 13]$ — Physical Plant → Communication Network → $y_k = [2\ 13]$ → Feedback Controller; Adversary

(a) Data confidentiality violation by a disclosure attack.
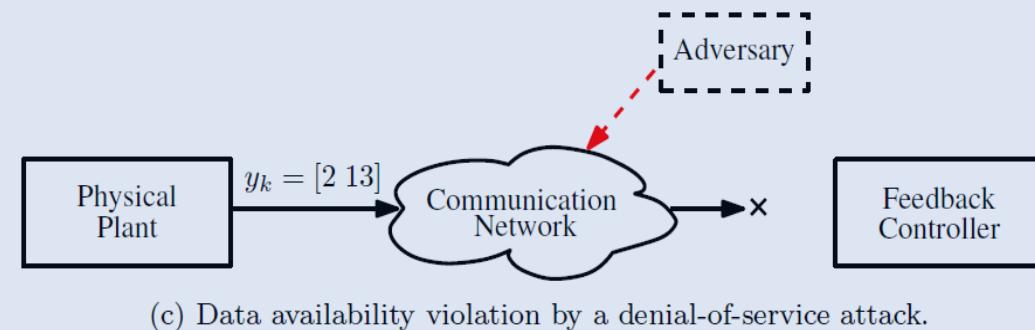
I – Integrity

"Security"
(Focus here. Good intro in CSM 2015 special issue)
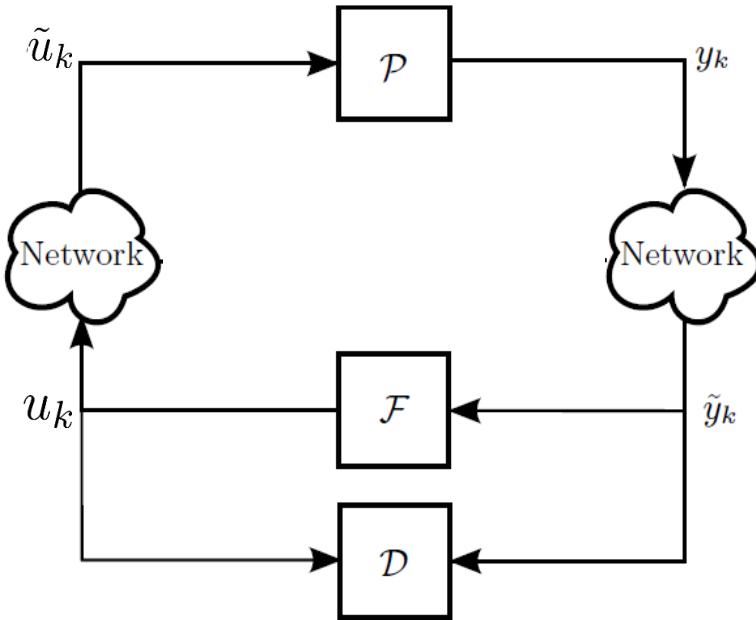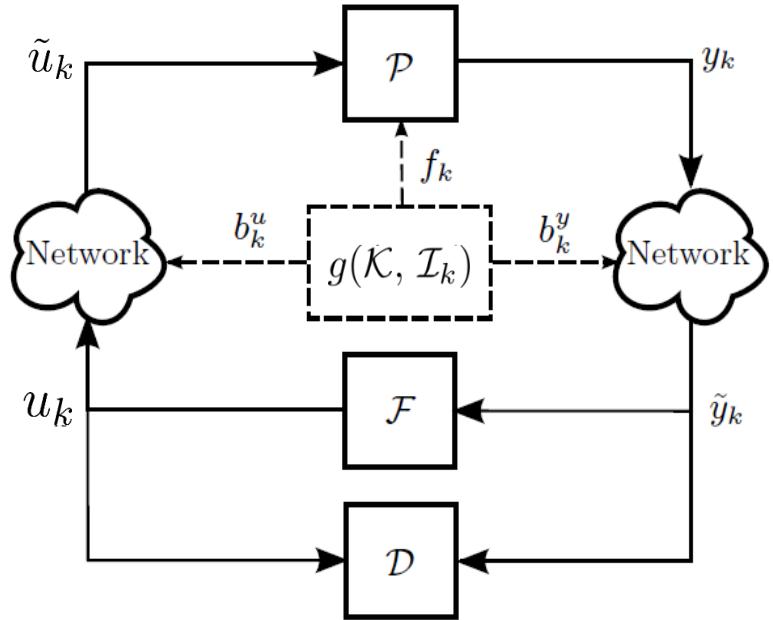
$\Delta y_k = [3\ 0]$ — Adversary

$y_k = [2\ 13]$ — Physical Plant → Communication Network → $\tilde{y}_k = [5\ 13]$ → Feedback Controller

(b) Data integrity violation by a false-data injection attack.

A – Availability

Adversary

$y_k = [2\ 13]$ — Physical Plant → Communication Network → × Feedback Controller

(c) Data availability violation by a denial-of-service attack.

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- Risk management

- Attack detectability and security metrics

- Attack identification and secure state estimation

Networked Control System under Attack
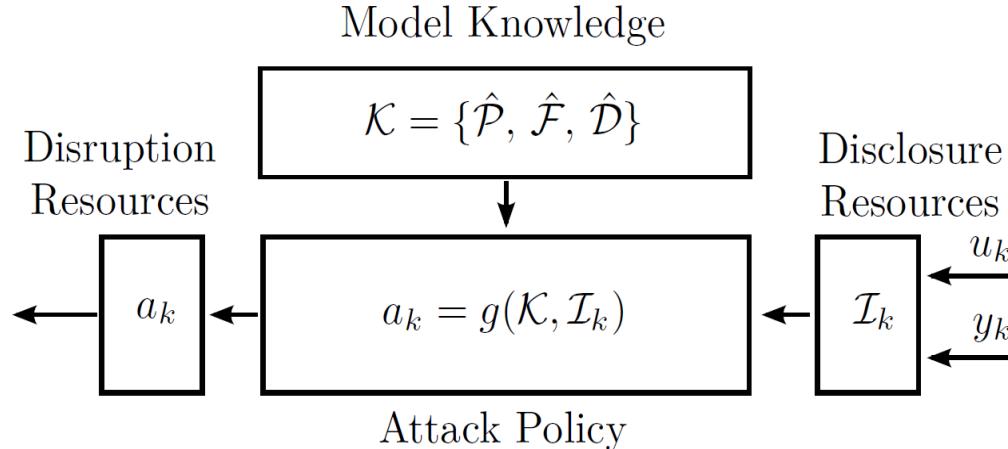
- Physical plant ($\mathcal{P}$)
- Feedback controller ($\mathcal{F}$)
- Anomaly detector ($\mathcal{D}$)

- Disclosure Attacks

- Physical Attacks f_k
- Deception Attacks

$$\tilde{u}_k = u_k + \Gamma^u b_k^u$$
$$\tilde{y}_k = y_k + \Gamma^y b_k^y$$

Adversary Model

Model Knowledge

$$\mathcal{K} = \{\hat{\mathcal{P}}, \hat{\mathcal{F}}, \hat{\mathcal{D}}\}$$

Disruption Resources

Disclosure Resources

a_k

$a_k = g(\mathcal{K}, \mathcal{I}_k)$

$\mathcal{I}_k$

u_k

y_k
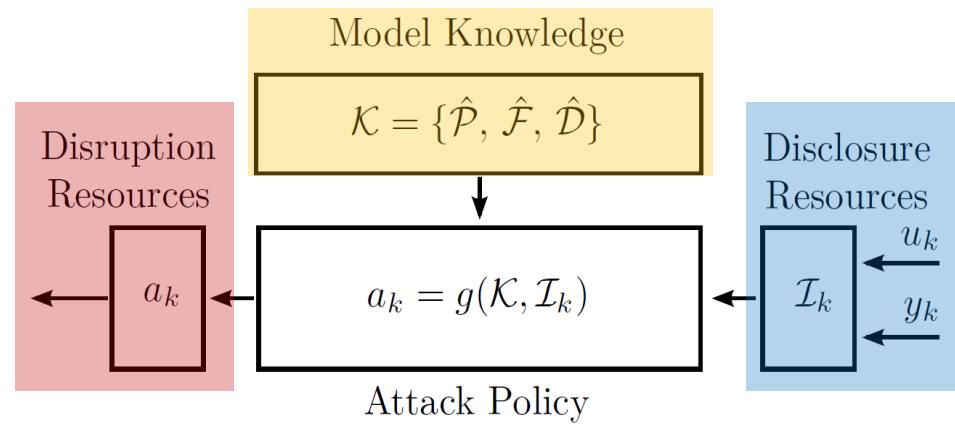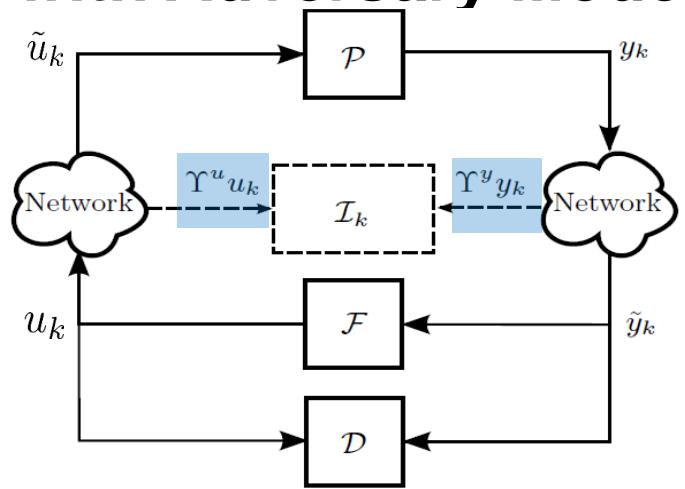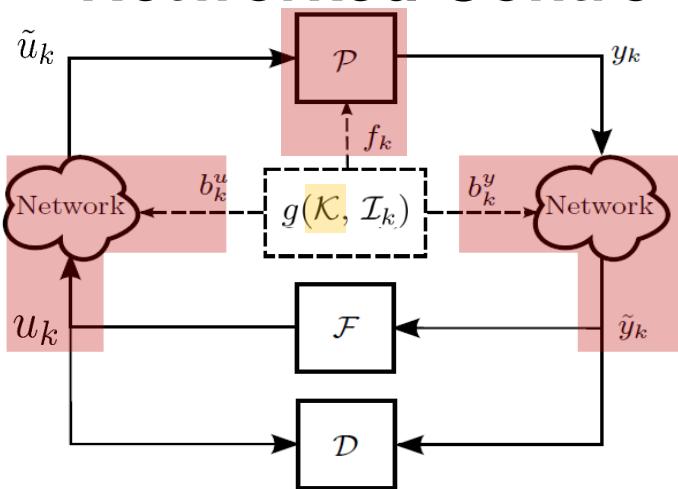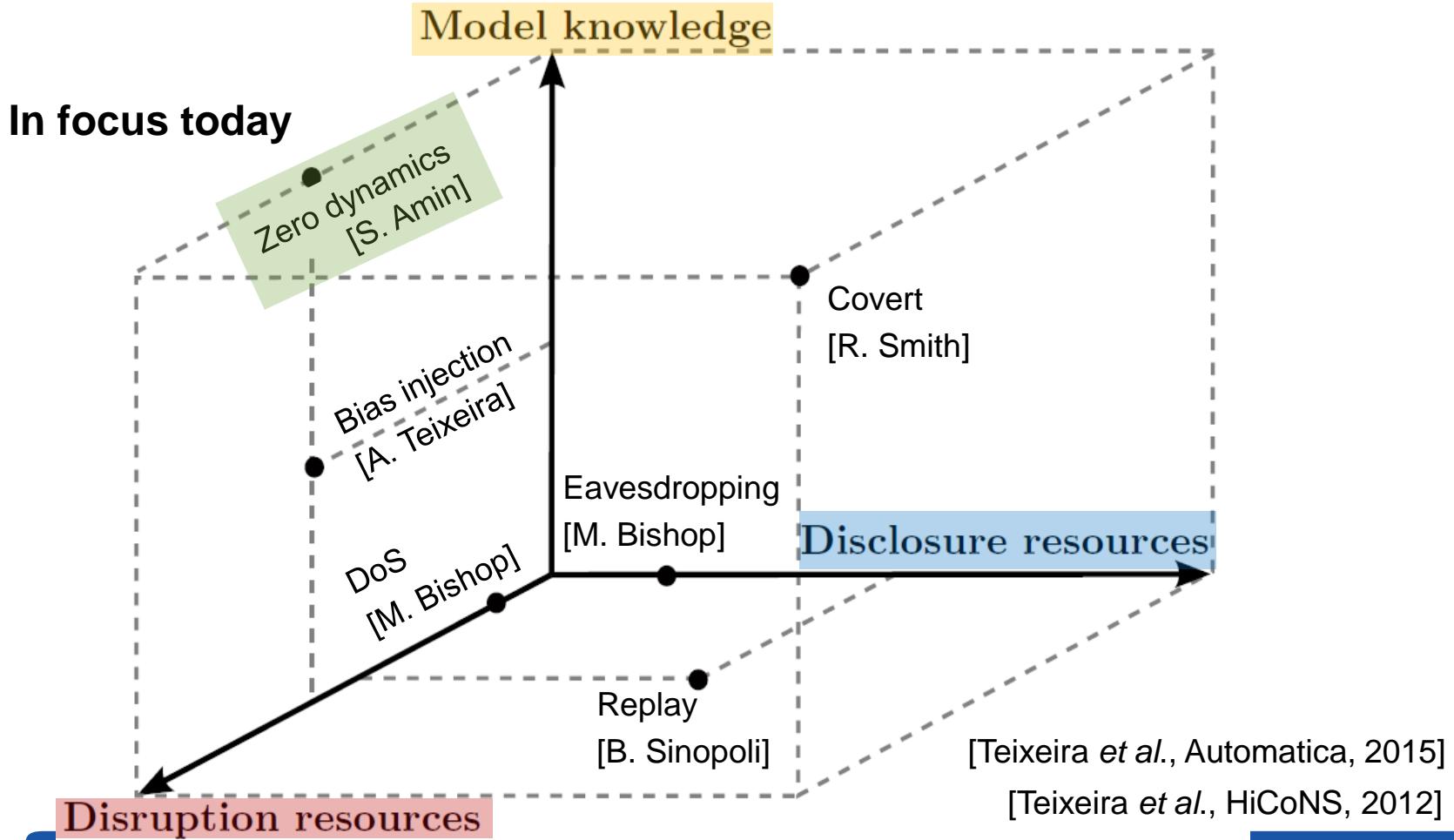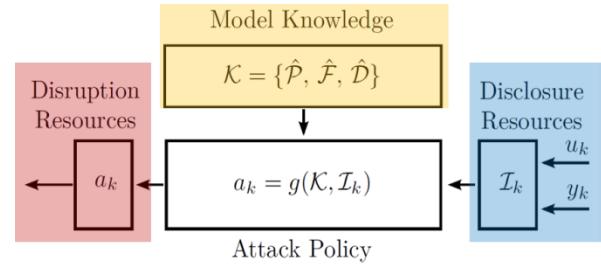
Attack Policy

- **Attack policy:** Goal of the attack? Destroy equipment, increase costs,…

- **Model knowledge:** Adversary knows models of plant and controller? Possibility for stealthy attacks…

- **Disruption/disclosure resources:** Which channels can the adversary access?

[Teixeira *et al*., HiCoNS, 2012]

Networked Control System with Adversary Model

Attack Space
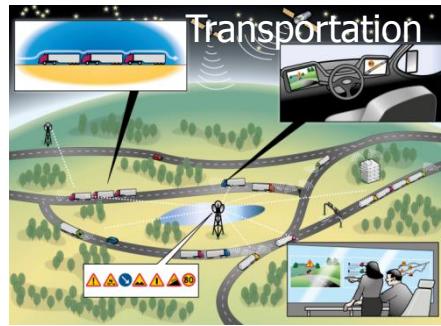
Outline
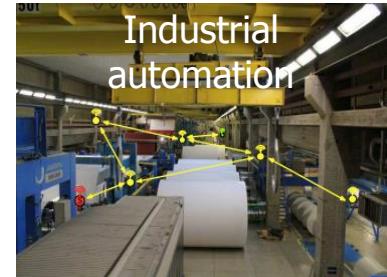
- Background and motivation

- CPS attack models

- **Risk management**

- Attack detectability and security metrics

- Attack identification and secure state estimation

Why Risk Management?

Transportation

Power transmission

Complex control systems with numerous attack scenarios

Industrial automation

Examples: Critical infrastructures (power, transport, water, gas, oil) often with weak security guarantees
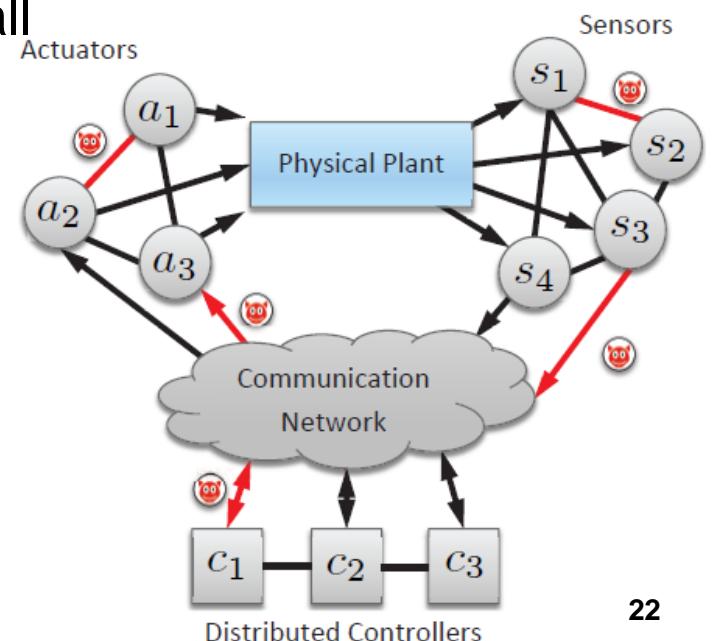
Too costly to secure the entire system against all attack scenarios

What scenarios to prioritize?

What components to protect?

When possible to identify attacks?
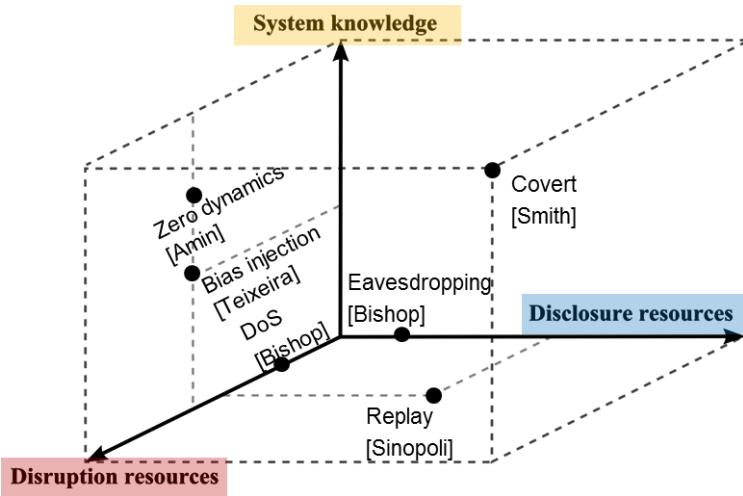
Defining Risk

Risk = (Scenario, Likelihood, Impact)

Scenario

• How to describe the system under attack?
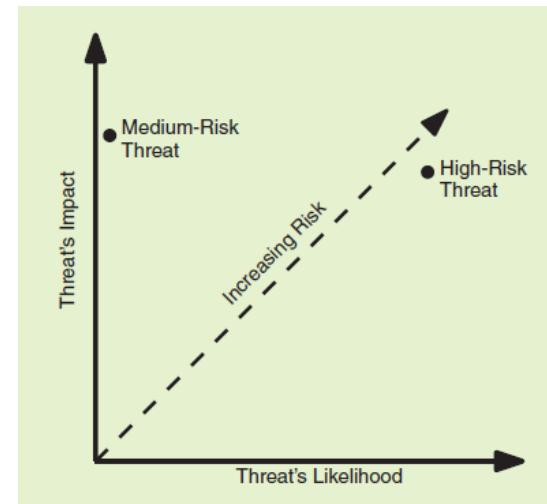
Likelihood

• How much effort does a given attack require?

Impact

• What are the consequences of an attack?
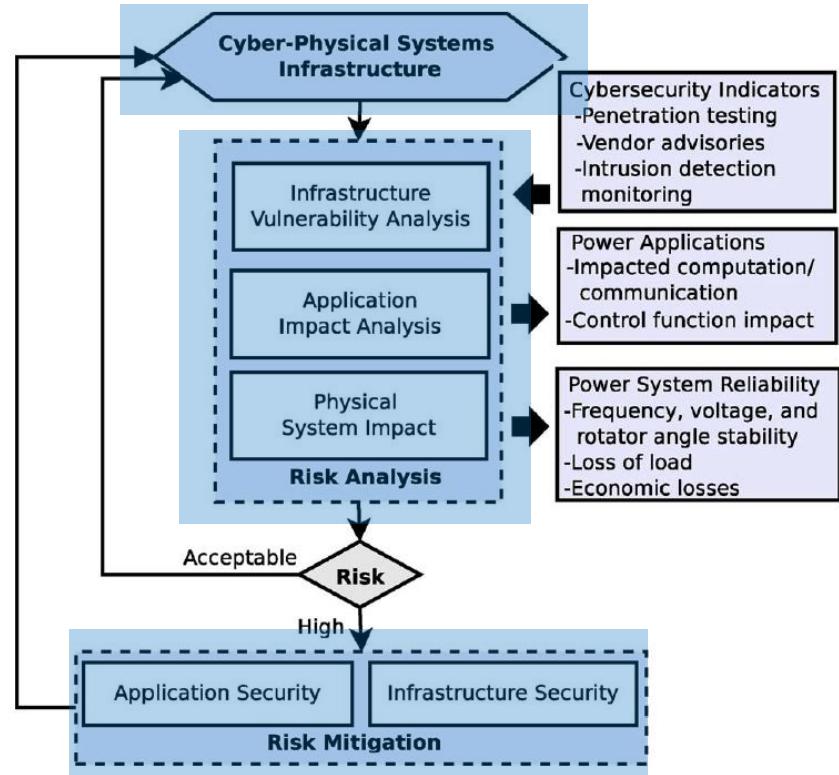
[Kaplan & Garrick, 1981], [Bishop, 2002]
([Teixeira *et al.*, IEEE CSM, 2015])

Risk Management Cycle
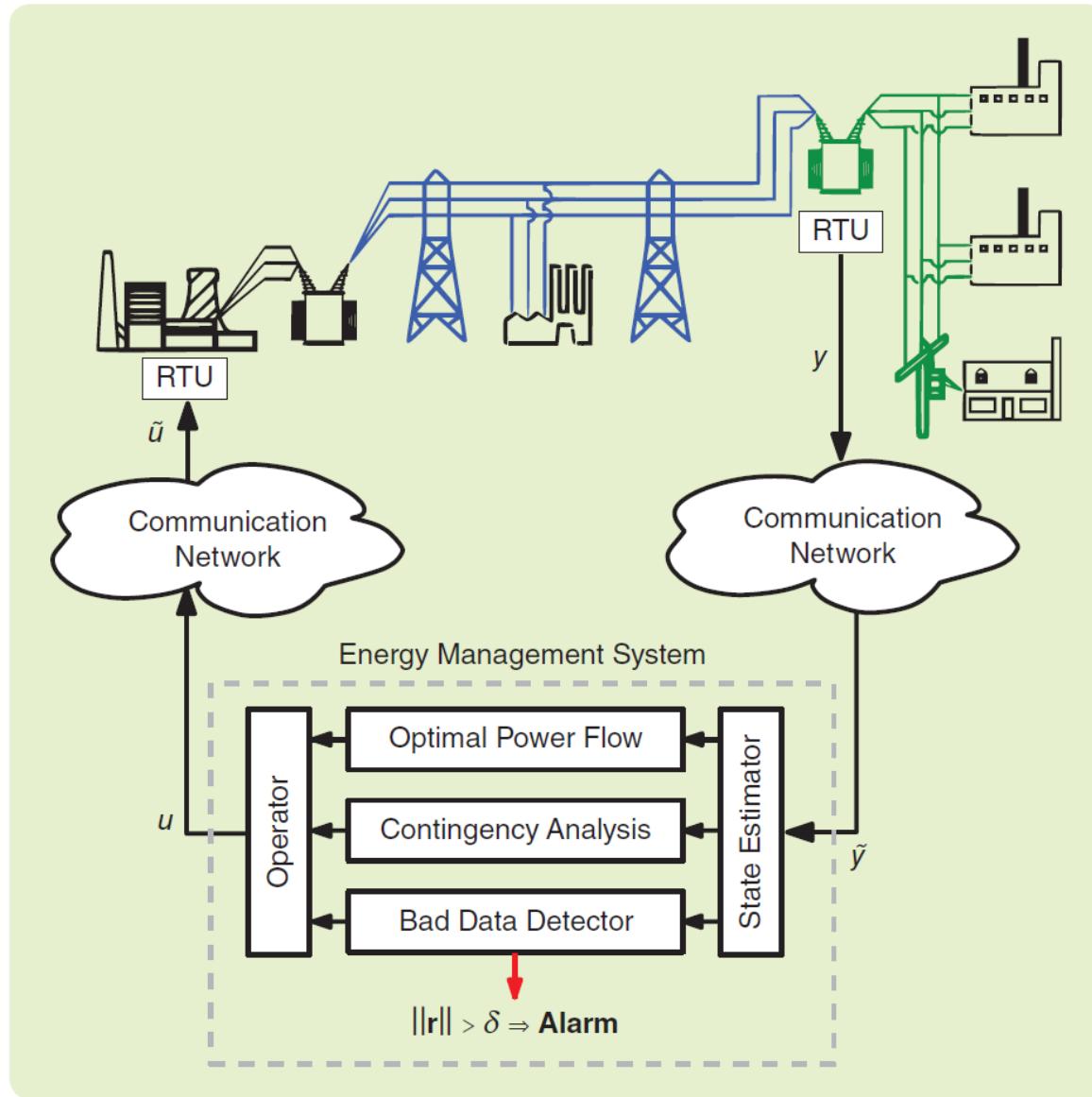
Main steps in risk management

- Scope definition
  - Models, Scenarios, Objectives

- Risk Analysis
  - **Threat Identification**
  - **Likelihood Assessment**
  - Impact Assessment

- Risk Treatment
  - **Prevention**, **Detection**, Mitigation
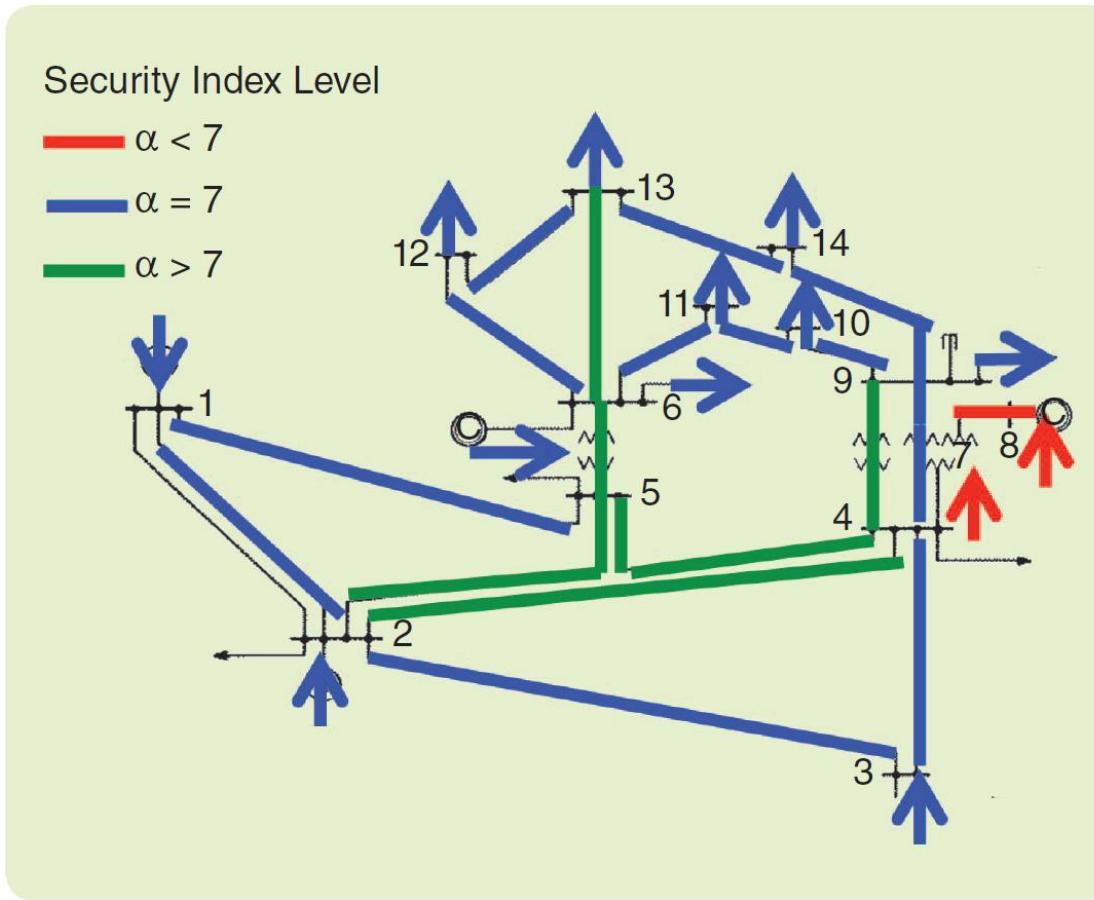
[Sridhar *et al.*, Proc. IEEE, 2012]

Example: Power System State Estimator

Example: Power System State Estimator

Security index α (to be defined) indicates sensors with inherent weak redundancy (~security). These should be secured first!

[Teixeira *et al.*, IEEE CSM, 2015], [Vukovic *et al.*, IEEE JSAC, 2012]

Outline

- Background and motivation

- CPS attack models

- Risk management

- **Attack detectability and security metrics**

- Attack identification and secure state estimation

Basic Notions:
Input Observability and Detectability

$$x(k+1) = Ax(k) + Bu(k), \quad x(k) \in \mathbb{R}^n, \ u(k) \in \mathbb{R}^m$$
$$y(k) = Cx(k) + Du(k), \quad y(k) \in \mathbb{R}^p$$

Definitions:

1. The input u is *observable with knowledge of $x(0)$* if $y(k) = 0$ for $k \geq 0$ implies $u(k) = 0$ for $k \geq 0$, provided $x(0) = 0$

2. The input u is *observable* if $y(k) = 0$ for $k \geq 0$ implies $u(k) = 0$ for $k \geq 0$ ($x(0)$ unknown)

3. The input u is *detectable* if $y(k) = 0$ for $k \geq 0$ implies $u(k) \to 0$ for $k \to \infty$ ($x(0)$ unknown)

[Hou and Patton, Automatica, 1998]

Basic Notions:
Input Observability and Detectability

The Rosenbrock system matrix:

$$P(z) = \begin{bmatrix} A - zI & B \\ C & D \end{bmatrix} \in \mathbb{C}^{(n+p) \times (n+m)}$$

First observations:

- Necessary condition for Definitions 1-3

$$\max_{z} \operatorname{rank} P(z) = m + n \Leftrightarrow \operatorname{normalrank} P(z) = m + n$$

- Fails if number of inputs larger than number of outputs ($m > p$)

- Necessary and sufficient conditions involve the *invariant zeros*:

$$\sigma(P(z)) := \{z : \operatorname{rank} P(z) < \operatorname{normalrank} P(z)\}$$

(Transmission zeros + uncontrollable/unobservable modes, Matlab command: `tzero`)

Basic Notions:
Input Observability and Detectability

$$P(z) = \begin{bmatrix} A - zI & B \\ C & D \end{bmatrix} \in \mathbb{C}^{(n+p) \times (n+m)}$$

Theorems. Suppose (A, B, C, D) is minimal realization.

1. The input u is *observable with knowledge of* $x(0) \Leftrightarrow$

    $$\max_{z} \operatorname{rank} P(z) = m + n \Leftrightarrow \operatorname{normalrank} P(z) = m + n$$

2. The input u is *observable* $\Leftrightarrow$

    $$\forall z : \operatorname{rank} P(z) = m + n$$
    (no invariant zeros)

3. The input u is *detectable* $\Leftrightarrow$ (1) and

    $$\sigma(P(z)) \subseteq \{z : |z| < 1\}$$
    (invariant zeros are all stable = system is minimum phase)

[Hou and Patton, Automatica, 1998]

Basic Notions:
Input Observability and Detectability

$$P(z) = \begin{bmatrix} A - zI & B \\ C & D \end{bmatrix}, \quad O(z) = \begin{bmatrix} A - zI \\ C \end{bmatrix}$$

Theorems. (A, B, C, D) possibly non-minimal realization

1. The input u is *observable with knowledge of* $x(0) \Leftrightarrow$

$$\max_{z} \operatorname{rank} P(z) = m + n \Leftrightarrow \operatorname{normalrank} P(z) = m + n$$

2'. The input u is *observable* $\Leftrightarrow$ (1) and
$$\sigma(P(z)) = \sigma(O(z))$$
(invariant zeros are all unobservable modes)

3'. The input u is *detectable* $\Leftrightarrow$ (1) and
$$\sigma(P(z)) \setminus \sigma(O(z)) \subseteq \{z : |z| < 1\}$$
(invariant zeros that are not unobservable modes are all stable)

[Hou and Patton, Automatica, 1998]

Fault Detection vs. Secure Control

Typical condition used in fault detection/fault tolerant control:

1. The input u is *observable with knowledge of* $x(0)$ $\Leftrightarrow$ [Ding, Patton]

$$\max_z \text{rank } P(z) = m + n \Leftrightarrow \text{normalrank } P(z) = m + n$$

Typical conditions used in secure control/estimation:

2. The input u is *observable* $\Leftrightarrow$ [Sundaram, Tabuada]

$$\forall z : \text{rank } P(z) = m + n$$

(no invariant zeros)

3/3'. The input u is *detectable* $\Leftrightarrow$ (1) and   [Pasqualetti, Sandberg]

$$\sigma(P(z)) \subseteq \{z : |z| < 1\}$$

(invariant zeros are all stable = system is minimum phase)

Example

$$A = \begin{pmatrix} 0.9 & 0 & 0 \\ 0 & 0.8 & 0 \\ 0 & 0 & 0.9 \end{pmatrix}, \; B = \begin{pmatrix} 0.5 & 0 \\ 0 & 0.5 \\ 0 & 0.25 \end{pmatrix}, \; C = \begin{pmatrix} 0.4 & 0.6 & 0 \\ 0.2 & 0 & 0.4 \end{pmatrix}$$

$$G(z) = C(zI - A)^{-1}B + D = \begin{pmatrix} \frac{0.2}{z-0.9} & \frac{0.3}{z-0.8} \\ \frac{0.1}{z-0.9} & \frac{0.1}{z-0.9} \end{pmatrix}$$

Invariant zeros = $\sigma\big(P(z)\big) = \{1.1\}$

1. The input u is *observable with knowledge of $x(0)$*: Yes!

2. The input u is *observable:* No!

3. The input u is *detectable:* No!

With $x(0) = \begin{pmatrix} -0.705 \\ 0.470 \\ 0.352 \end{pmatrix}$ and $u(k) = 1.1^k \begin{pmatrix} -0.282 \\ 0.282 \end{pmatrix}$ then $y(k) = 0, k \geq 0$

OK for fault detection but perhaps not for security!

Attack and Disturbance Model

Consider the linear system $y = G_d d + G_a a$ (the controlled infrastructure):

$$x(k+1) = Ax(k) + B_d d(k) + B_a a(k)$$
$$y(k) = Cx(k) + D_d d(k) + D_a a(k)$$

- Unknown state $x(k) \in \mathbb{R}^n$ ($x(0)$ in particular)
- Unknown (natural) disturbance $d(k) \in \mathbb{R}^o$
- Unknown (malicious) attack $a(k) \in \mathbb{R}^m$
- Known measurement $y(k) \in \mathbb{R}^p$
- Known model A, B_d, B_a, C, D_d, D_a

- **Definition:** Attack signal a is *persistent* if $a(k) \nrightarrow 0$ as $k \to \infty$

- **Definition:** A (persistent) attack signal a is *undetectable* if there exists a simultaneous (masking) disturbance signal d and initial state $x(0)$ such that $y(k) = 0$, $k \geq 0$ (Cf. Theorem 3')

Undetectable Attacks and Masking

The Rosenbrock system matrix:

$$P(z) = \begin{bmatrix} A - zI & B_d & B_a \\ C & D_d & D_a \end{bmatrix}$$

- Attack signal $a(k) = z_0^k a_0$, $0 \neq a_0 \in \mathbb{C}^m$, $z_0 \in \mathbb{C}$, is *undetectable* iff there exists $x_0 \in \mathbb{C}^n$ and $d_0 \in \mathbb{C}^o$ such that

$$P(z_0) \begin{bmatrix} x_0 \\ d_0 \\ a_0 \end{bmatrix} = 0$$

- Attack signal is undetectable if indistinguishable from measurable (y) effects of natural noise (d) or uncertain initial states (x_0) [**masking**]

$$G(z) = C(zI - A)^{-1}B + D = \begin{pmatrix} G_d(z) & G_a(z) \end{pmatrix}$$

$$G_d(z) = \begin{pmatrix} \frac{0.2}{z-0.9} \\ \frac{0.1}{z-0.9} \end{pmatrix}, \quad G_a(z) = \begin{pmatrix} \frac{0.3}{z-0.8} \\ \frac{0.1}{z-0.9} \end{pmatrix}$$

Poles = $\{0.9, 0.9, 0.8\}$
Invariant zeros = $\sigma(P(z)) = \{1.1\}$

Undetectable attack: $a(k) = 1.1^k \cdot 0.282$

Masking initial state: $x_0 = \begin{pmatrix} -0.705 \\ 0.470 \\ 0.352 \end{pmatrix}$

Masking disturbance $d(k) = 1.1^k \cdot (-0.282)$

Undetectable Attacks and Masking (cont'd)

- Suppose operator observes the output $y(k)$, and does *not know* the true initial state $x(0)$ and true disturbance $d(k)$

- Let (x_0, d_0, a_0) be an undetectable attack, $0 = G_d d_0 + G_a a_0$ with initial state x_0

Consider the cases:

1. Un-attacked system $y = G_d d$, with initial state $x(0)$

2. Attacked system $y = G_d(d + d_0) + G_a a_0$, with initial state $x(0) + x_0$

If initial states $x(0)$ and $x(0) + x_0$ and disturbances d and $d + d_0$ are equally likely, then impossible for operator to decide which case is true $\Rightarrow$ **Attack is undetectable!**

Undetectable Attacks and Masking (cont'd)

- Suppose operator observes the output $y(k)$, and *knows* the true initial state $x(0) = 0$ and the disturbance $d(k) = 0, k \geq 0$
- Suppose system is asymptotically stable, $\rho(A) < 1$
- Let (x_0, a_0) be an undetectable attack, $0 = G_a a_0$ with initial state x_0

Consider the cases:

1. Un-attacked system $y_1(k) = 0, k \geq 0$, with initial state $x(0) = 0$
2. Attacked system $y_2(k) = (G_a a_0)(k) = -C A^k x_0 \rightarrow 0$ as $k \rightarrow \infty$, with initial state $x(0) = 0$

The attacked output y_2 is vanishing, and can be made arbitrarily close to y_1 by scaling $(x_0, a_0) \Rightarrow$ **Attack is asymptotically undetectable!**

The Security Index α_i

$$\alpha_i := \min_{|z_0| \geq 1, x_0, d_0, a_0^i} \|a_0^i\|_0$$

$$\text{subject to} \qquad P(z_0) \begin{bmatrix} x_0 \\ d_0 \\ a_0^i \end{bmatrix} = 0$$

Notation: $\|a\|_0 := |\text{supp}(a)|$, a^i vector a with i-th element non-zero

Interpretation:

- Attacker persistently targets signal component a_i (condition $|z_0| \geq 1$)
- α_i is smallest number of attack signals that need to be simultaneously accessed to stage undetectable attack against signal a_i

Argument: Large $\alpha_i \Rightarrow$ malicious cyber attacks targeting a_i less likely

Problem NP-hard in general (combinatorial optimization, cf. matrix *spark*). Generalization of static index in [Sandberg *et al.*, SCS, 2010]

Simple Example of Security Index

$$P(z) = \begin{bmatrix} A - zI & B_d & B_a \\ 0 & 0 & D_a \end{bmatrix} \qquad D_a = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

- Measurements not affected by physical states and disturbances
- 3 measurements
- 4 attacks with security indices:
  - $\alpha_1 = 3$
  - $\alpha_2 = 3$
  - $\alpha_3 = 3$
  - $\alpha_4 = \infty$ (By definition. Even access to all attack signals not enough to hide attack)

Special Case 1: Critical Attack Signals

Signal with $\alpha_i = 1$ can be undetectably attacked without access to other elements $\Rightarrow$ **Critical Attack Signal**

$$P_i(z) = \begin{bmatrix} A - zI & B_d & B_{a,i} \\ C & D_d & D_{a,i} \end{bmatrix} \in \mathbb{C}^{(n+p)\times(n+o+1)}, \quad P_d(z) = \begin{bmatrix} A - zI & B_d \\ C & D_d \end{bmatrix} \in \mathbb{C}^{(n+p)\times(n+o)}$$

Simple test, $\forall i$: If there is $z_0 \in \mathbb{C}$, $|z_0| \geq 1$, such that $\text{rank}\,[P_d(z_0)] = \text{rank}\,[P_i(z_0)]$, then $\alpha_i = 1$

Even more critical case: If $\text{normalrank}\,[P_d(z_0)] = \text{normalrank}\,[P_i(z_0)]$ then there is undetectable critical attack for all frequencies z_o

Holds generically when more disturbances than measurements ($o \geq p$)!

Protect against these attack signals first in risk management!

Special Case 2: Transmission Zeros

$$P(z) = \begin{bmatrix} A - zI & B_d & B_a \\ C & D_d & D_a \end{bmatrix}$$

[Amin *et al.*, ACM HSCC, 2010]
[Pasqualetti *et al.*, IEEE TAC, 2013]

Suppose $P(z)$ has full column normal rank. Then undetected attacks only at finite set of transmission zeros $\{z_0\}$

Solve
$$\alpha_i := \min_{|z_0| \geq 1, x_0, d_0, a_0^i} \|a_0^i\|_0$$

$$\text{subject to} \qquad P(z_0) \begin{bmatrix} x_0 \\ d_0 \\ a_0^i \end{bmatrix} = 0$$

by inspection of corresponding zero directions $\Rightarrow$ **Easy in typical case of 1-dimensional zero directions**

Special Case 3: Sensor Attacks

$$P(z) = \begin{bmatrix} A - zI & 0 & 0 \\ C & D_d & D_a \end{bmatrix}$$

[Fawzi *et al.*, IEEE TAC, 2014]
[Chen *et al.,* IEEE ICASSP, 2015]
[Lee *et al.,* ECC, 2015]

$P(z)$ only loses rank in eigenvalues $z_0 \in \{\lambda_1(A), \dots, \lambda_n(A)\}$

Simple eigenvalues give one-dimensional spaces of eigenvectors $x_0 \Rightarrow$ **Simplifies computation of α_i**

Example: Suppose $D_a = I_p$ (sensor attacks), $D_d = 0$, and system observable from each y_i, $i = 1, \dots, p$:

- By the PBH-test: $\alpha_i = p$ or $\alpha_i = +\infty$ (if all eigenvalues stable, no persistent undetectable sensor attack exists)
- Redundant measurements increase α_i!

Special Case 4: Sensor Attacks for Static Systems

$$P(z) = \begin{bmatrix} I - zI & 0 & 0 \\ C & 0 & D_a \end{bmatrix}$$

[Liu *et al.*, ACM CCS, 2009]
[Sandberg *et al.*, SCS, 2010]

Since $A = I_n$ and $B_d = B_a = 0$, this is the steady-state case

Space of eigenvectors x_0 is n-dimensional $\Rightarrow$ **Typically makes computation of α_i harder than in the dynamical case!**

Practically relevant case in power systems where $p > n \gg 0$

- Problem NP-hard, but power system imposes special structures in C (unimodularity etc.)

- Several works on efficient and exact computation of α_i using min-cut/max-flow and ℓ_1-relaxation ([Hendrickx *et al.*, 2014], [Kosut, 2014], [Yamaguchi *et al.*, 2015])

Special Case 4: Solution by MILP
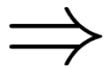
Big M reformulation:

$$\alpha_i := \min_{x_0, a_0} \|a_0\|_0$$

$$\text{subject to}$$

$$0 = Cx_0 + D_a a_0$$

$$a_{0,i} = 1$$

$\Longrightarrow$

$$\alpha_i := \min_{z_0, x_0, a_0,} \sum_k z_k$$

$$\text{subject to}$$

$$0 = Cx_0 + D_a a_0$$

$$a_{0,i} = 1$$

$$-Mz \le a_0 \le Mz$$
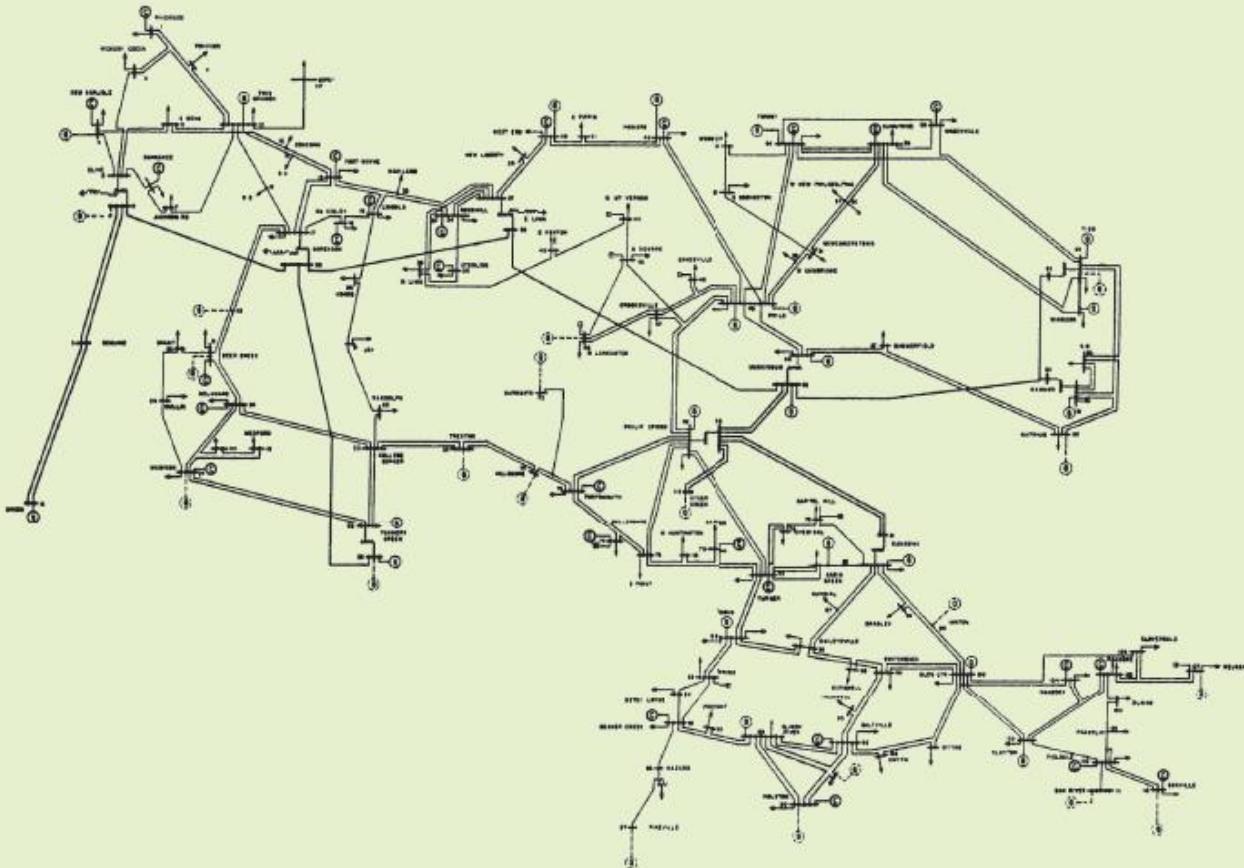
$$z_k \in \{0, 1\}$$

Elementwise

"∞"
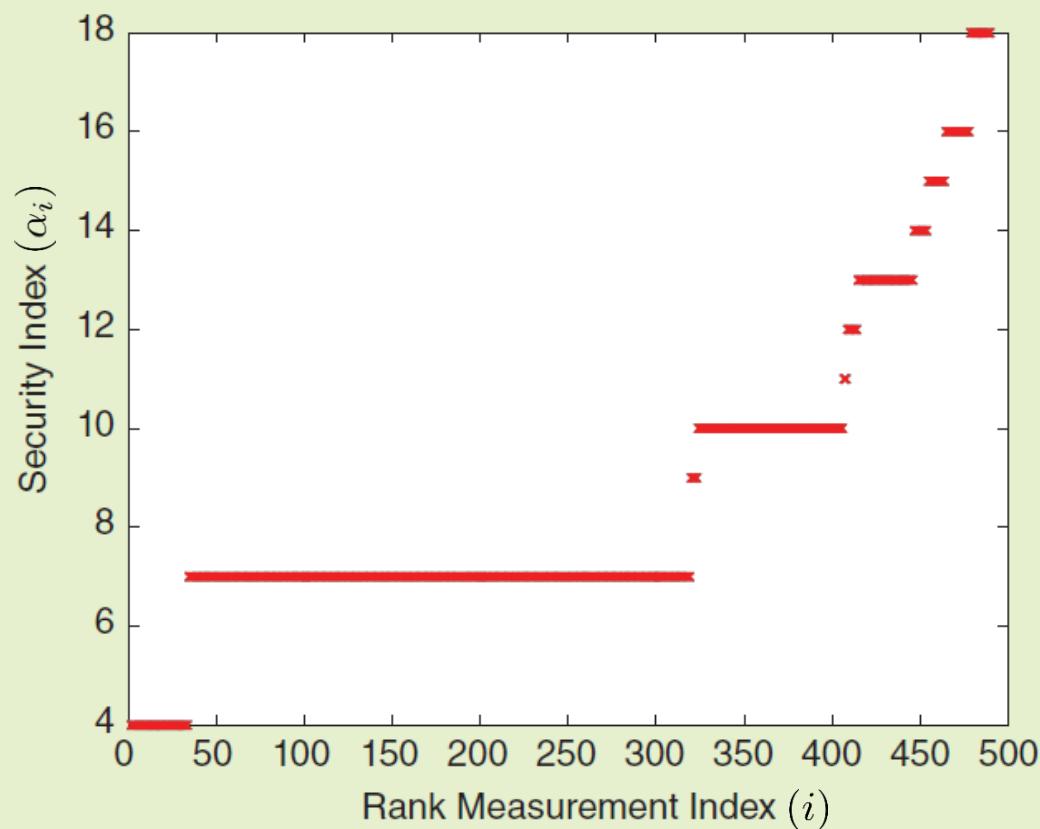
Example: Power System State Estimator for IEEE 118-bus System

- State dimension $n = 118$

- Number sensors $p \approx 490$

Example: Power System State Estimator for IEEE 118-bus System

- Computation time on laptop using min-cut method [Hendrickx *et al.*, IEEE TAC, 2014]: 0.17 sec
- Used for protection allocation in [Vukovic *et al.,* IEEE JSAC, 2012]

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Summary So Far

- Dynamical security index α_i defined

- Argued α_i useful in risk management for assessing likelihood of malicious attack against element a_i

- Computation is NP-hard in general, but often "simple" in special cases:
  - One-dimensional zero-dynamics
  - Static systems with special matrix structures (derived from potential flow problems)
  - Dynamics generally simplifies computation and redundant sensors increase α_i

- Fast computation enables greedy security allocation

Outline

- Background and motivation

- CPS attack models

- Risk management

- Attack detectability and Security metrics

- **Attack identification and secure state estimation**

Attack Identification

$$x(k + 1) = Ax(k) + B_d d(k) + B_a a(k)$$

$$y(k) = Cx(k) + D_d d(k) + D_a a(k)$$

- Unknown state $x(k) \in \mathbb{R}^n$

- Unknown (natural) disturbance $d(k) \in \mathbb{R}^o$

- Unknown (malicious) attack $a(k) \in \mathbb{R}^m$

- Known measurement $y(k) \in \mathbb{R}^p$

- Known model A, B_d, B_a, C, D_d, D_a

- When can we decide there is an attack signal $a_i \neq 0$?

- Which elements a_i can we track ("identify")?

- Not equivalent to designing an unknown input observer/secure state estimator (state not requested here). See end of presentation

Attack Identification

Definition: A (persistent) attack signal a is

- *identifiable* if for all attack signals $\tilde{a} \neq a$, and all corresponding disturbances d and $\tilde{d}$, and initial states $x(0)$ and $\tilde{x}(0)$, we have $\tilde{y} \neq y$;

- i-*identifiable* if for all attack signals a and $\tilde{a}$ with $\tilde{a}_i \neq a_i$, and all corresponding disturbances d and $\tilde{d}$, and initial states $x(0)$ and $\tilde{x}(0)$, we have $\tilde{y} \neq y$

Interpretations:

- Identifiability $\Leftrightarrow$ (different attack $a \Rightarrow$ different measurement y) $\Leftrightarrow$ attack signal is injectively mapped to $y \Rightarrow$ attack signal is detectable

- i-*identifiable* weaker than *identifiable*

- $\forall i: a$ *is* i-*identifiable* $\Leftrightarrow a$ is *identifiable*

- a is i-*identifiable:* Possible to track element a_i, but not necessarily a_j, $j \neq i$

Theorem

Suppose that the attacker can manipulate at most q attack elements simultaneously ($\|a\|_0 \leq q$).

i.   There exists persistent undetectable attacks $a^i \Leftrightarrow q \geq \alpha_i$;

ii. All persistent attacks are i-identifiable $\Leftrightarrow q < \alpha_i/2$;

iii. All persistent attacks are identifiable $\Leftrightarrow q < \min_i \alpha_i/2$.

Proof. Compressed sensing type argument. See [Sandberg and Teixeira, SoSCYPS, 2016] for details

Simple Example of Security Index (cont'd)

$$P(z) = \begin{bmatrix} A - zI & B_d & B_a \\ 0 & 0 & D_a \end{bmatrix} \qquad D_a = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Security indices: $\alpha_1 = 3,\ \ \alpha_2 = 3, \alpha_3 = 3, \alpha_4 = \infty$

Attacker with $q = 1$: Defender can identify (and thus detect) all attacks

$q = 2$: Defender can detect (not identify) all attacks against a_1, a_2, a_3 and identify all attacks against a_4

$q = 3 - 4$: Defender can identify all attacks against a_4. Exist undetectable attacks against a_1, a_2, a_3

Back to Risk Management

$$P(z) = \begin{bmatrix} A - zI & B_d & B_a \\ 0 & 0 & D_a \end{bmatrix} \qquad D_a = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Security indices: $\alpha_1 = 3, \ \alpha_2 = 3, \alpha_3 = 3, \alpha_4 = \infty$
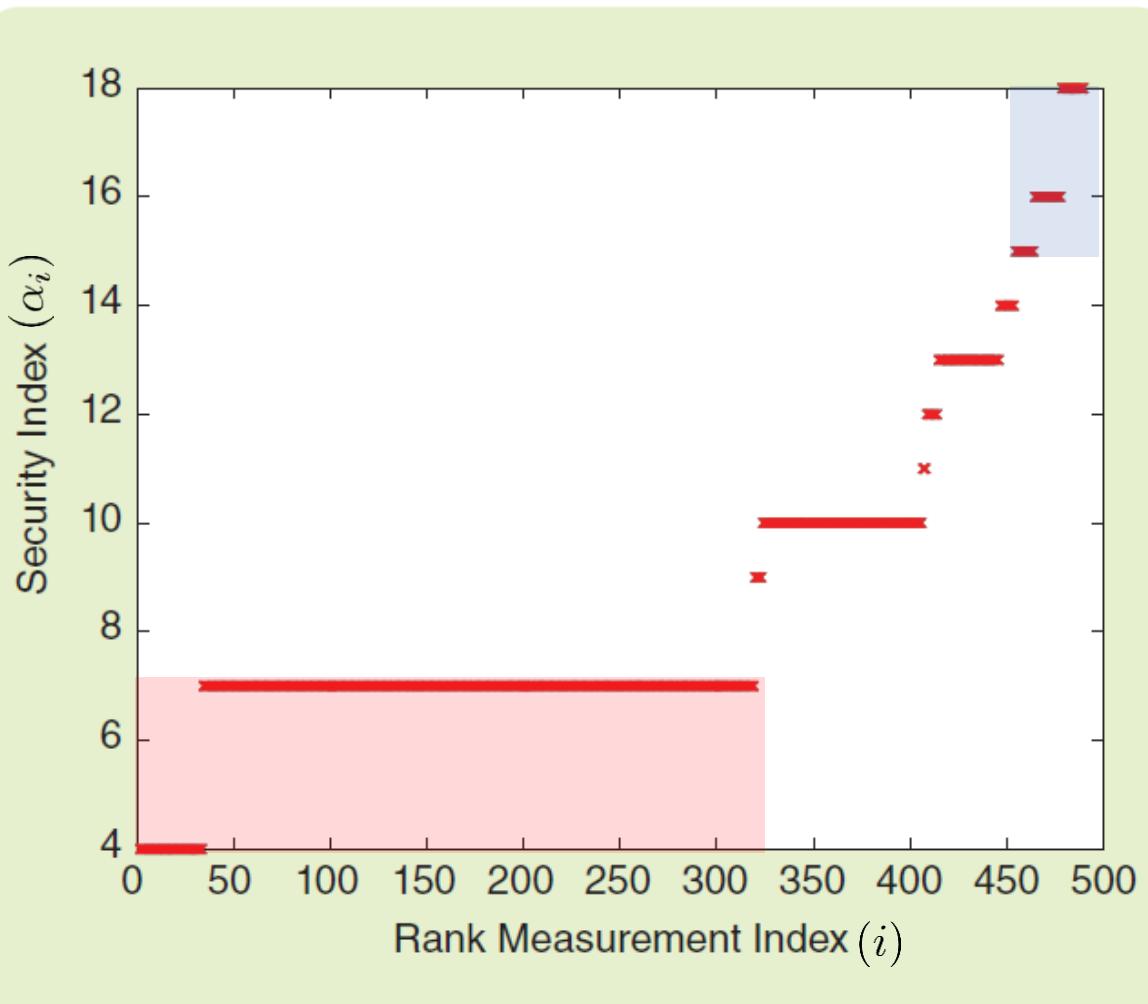
- Suppose the operator can choose to block *one* attack signal (through installing physical protection, authentication, etc.).

- Which signal a_1, a_2, a_3, or a_4 should she/he choose?

- Among the one(s) with lowest security index! Choose a_1.

- New attack model and security indices: $\alpha_2 = \alpha_3 = \alpha_4 = \infty$

$$D_a = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

- By explicitly blocking one attack signal, all other attacks are implicitly blocked (they are identifiable)

Example: Power System State Estimator for IEEE 118-bus System

- Suppose number of attacked elements is $q \leq 7$

- Signals susceptible to undetectable attacks

- Signals were all attacks are identifiable

- Other signals will, if attacked, always result in non-zero output y

Secure state estimate $\hat{x}$: Regardless of disturbance d and attack a, the estimate satisfies $\hat{x} \rightarrow x$ as $k \rightarrow \infty$

1. Rename and transform attacks and disturbances:

$$\begin{bmatrix} B_d \\ D_d \end{bmatrix} d + \begin{bmatrix} B_a \\ D_a \end{bmatrix} a = \begin{bmatrix} B_f \\ D_f \end{bmatrix} f, \quad \text{such that} \begin{bmatrix} B_f \\ D_f \end{bmatrix} \text{full column rank}$$

2. Compute security indices α_i with respect to f

Theorem: A secure state estimator exists iff

1. (C, A) is detectable; and

2. $q < \min\limits_{i} \dfrac{\alpha_i}{2}$, where q is max number of non-zero elements in f.

Proof. Existence of UIO by [Sundaram *et al.*, 2007] plus previous theorem

How to Identify an Attack Signal?

Use decoupling theory from fault diagnosis literature [Ding, 2008]

Suppose that $y = G_d d + G_a a$ and

$$\text{normalrank} [G_d(z)] = m',$$
$$\text{normalrank} [G_d(z) \ G_a(z)] = m' + m''$$

Then there exists linear decoupling filter R such that

$$\begin{bmatrix} r \\ y' \end{bmatrix} = R(G_d d + G_a a) = \begin{bmatrix} 0 & \Delta \\ G'_d & G'_a \end{bmatrix} \begin{bmatrix} d \\ a \end{bmatrix},$$

$$\text{normalrank} [G'_d(z)] = \text{normalrank} [G'_d(z) \ G'_a(z)] = m'$$
$$\text{normalrank} [\Delta(z)] = m''$$

How to Identify an Attack Signal?
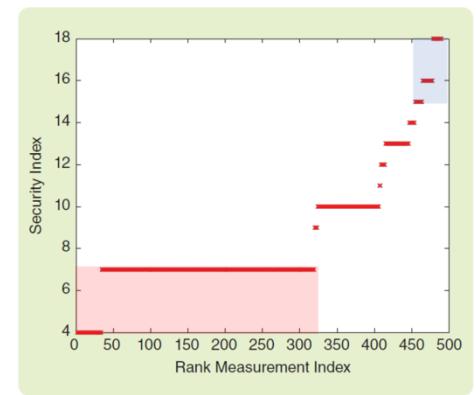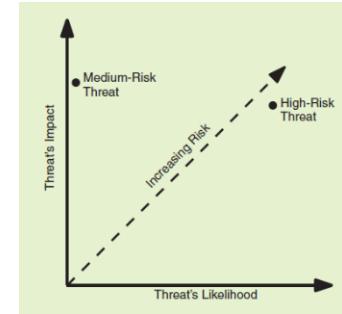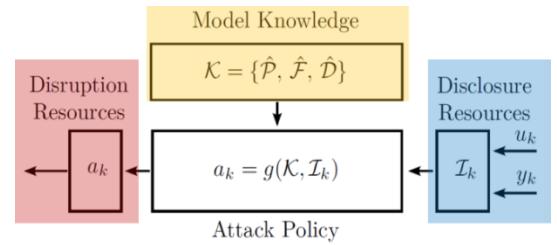
Suppose a is identifiable ($q < \min_{i} \alpha_i / 2$)

1. Decouple the disturbances to obtain system $r = \Delta a$

2. Filter out uncertain initial state component in r to obtain $r' = \Delta a$

3. Compute left inverses of $\Delta_I := [\Delta_i]_{i \in I}$ formed out of the columns Δ_i of Δ, for all subsets $|I| = q$, $I \subseteq \{1, \dots, m\}$ (**Bottleneck! Compare with compressed sensing**)

4. By identifiability, if estimate $\hat{a}_I$ satisfies $r' = \Delta \hat{a}_I$, then $\hat{a}_I \equiv a$

(Similar scheme applies if a is only i-identifiable)

Summary

- There is a need for CPS security
- Briefly introduced CPS attack models and concept of risk management

- Input observability and detectability
  $\Rightarrow$ Undetectable attacks and masking initial states and disturbances

- A security metric α_i for risk management
  - Suppose attacker has access to q resources:
    - Undetectable attacks against a_i iff $q \geq \alpha_i$
    - Attack against a_i identifiable iff $q < \alpha_i/2$

- Many useful results in the fault diagnosis literature, especially for identifiable attacks: Unknown input observers, decoupling filters, etc.
- Future research direction: More realistic attacker models, estimate attack likelihoods and impacts, corporation with IT security,…

Further Reading

Introduction to CPS/NCS security

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