MODULE 2: Data Representation

Lecture 2.2 Signed Data Representation

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Lecture 2.2 Objectives

- Explain the difference between signed and unsigned representation
- Convert between signed decimal numbers and signed binary numbers using two's complement representation and using signed magnitude representation
- Explain the difference between the two's complement operation and two's complement representation
- Calculate the negative of a signed binary number



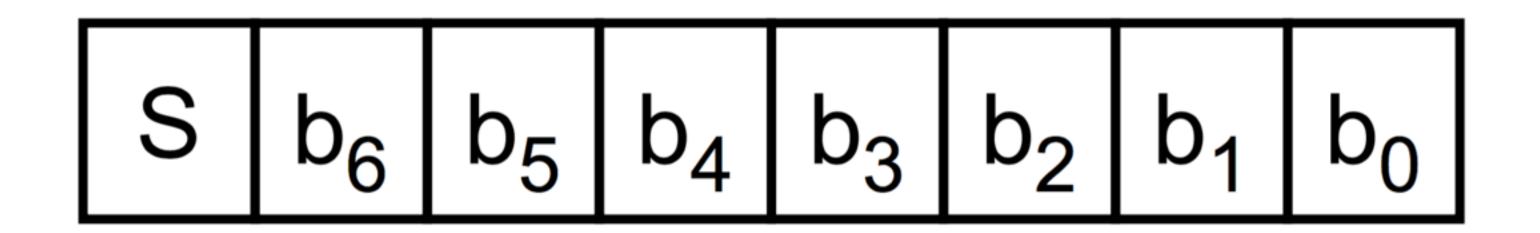
Signed Numbers

- Computers need to be able to represent signed (positive and negative) values as well as unsigned values
- Unsigned values are treated implicitly as positive, but there is no explicit information stored indicating that they are positive
- Signed numbers require that information is explicitly provided indicating if the value is positive or negative

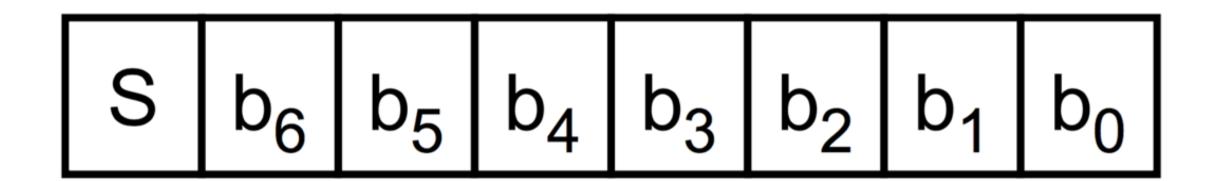


Signed Magnitude

- A simple way to indicate if a value is positive or negative is to add one bit, usually to the left of the most significant bit (MSB), indicating the sign
 - 0⇒positive
 - 1⇒negative
- For an 8-bit integer representation, there would be one sign bit (S) and seven magnitude bits (b₆ - b₀)



Signed Magnitude Example



- For this scheme, the range is +127 to -127
 - 0111111 (+127) to 1111111 (-127)
- Conversion done by converting magnitude to or from binary and adding the sign bit
- Examples
 - $-(+27)_{10} = (00011011)_2$
 - $-(-27)_{10} = (10011011)_2$
 - $(0)_{10}$ = $(00000000)_2$ or $(10000000)_2$





As a checkpoint of your understanding, please pause the video and make sure you can do the following:

Using 8 bits, compute the signed magnitude representation of (-25)₁₀



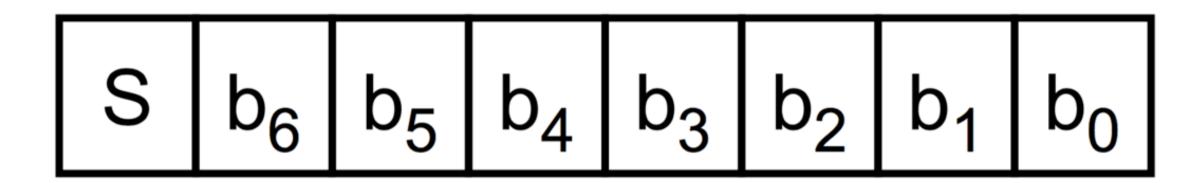
Answer:

• (-25)₁₀ in (8 bits) signed magnitude representation: 10011001

If you have any difficulties, please review the lecture video before continuing.

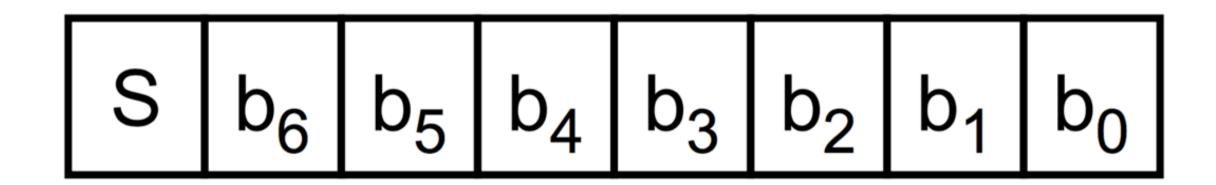
Two's Complement Representation

- Two's complement representation is the most widely used signed representation for fixed point values
 - Single representation of zero
 - Arithmetic operations are easily implemented
- For an 8-bit integer representation, there would be one sign bit (S) and seven magnitude bits (b₆ b₀), but the magnitude bits are not simply the magnitude





Two's Complement Example



- For this scheme, the range is +127 to -128
 - 0111111 (+127) to 10000000 (-128)
- Conversion done by:
 - Forming positive value of number (same as positive signed magnitude representation)
 - Performing two's complement *operation* on the positive number if the value is negative

Two's Complement Operation (1)

Process:

- Invert (complement) every bit by changing each 1 to a 0 and each 0 to a 1
- Add 1 to the value (using binary addition) and ignore overflow
- For binary addition
 - -0+0=0 (no carry)
 - -0+1=1 (no carry)
 - -1+0=1 (no carry)
 - -1+1=0 (carry 1 to the next digit)

Two's Complement Operation (2)

- Example: find the two's complement of the 8-bit value 01001100
 - First, invert every bit: 10110011
 - Then, add 1 to this value

$$\begin{bmatrix} 0000011 \end{bmatrix}$$
 carry bits 10110011 $+1$ $00110100 \longrightarrow \text{sum}$

- Two's complement of 01001100 is 10110100



Two's Complement Conversion

- Example (using 8 bits): (+27)₁₀
 - $-(+27)_{10} = (00011011)_2$
 - Since it is a positive number, this is the same as the signed magnitude representation
- Example (using 8 bits): (-27)₁₀
 - $-(+27)_{10} = (00011011)_2$
 - Since we want the negative value, perform the two's complement operation on the representation of +27
 - $-(-27)_{10} = (11100101)_2$
 - This is different than if we were using signed magnitude



Negation with Two's Complement

- To negate a number, just perform the two's complement operation
- Example: find the negative of (11100101)₂
 - Invert every bit: 00011010
 - Add 1: 00011011
 - We started with (-27)₁₀ and then negated to get the representation for (+27)₁₀





As a checkpoint of your understanding, please pause the video and make sure you can do the following:

Using 8 bits, compute the two's complement negative of (+27)₁₀



Answer:

The two's complement of $(+27)_{10}$ is 00011011. To negate this, we perform the two's complement operation on 00011011:

- 00011011 <— original
- 11100100 <—after bit inversion
- 11100101 <—after +1
- Therefore, the two's complement negation of +27₁₀ is 11100101.

If you have any difficulties, please review the lecture video before continuing.



Summary

- Computer systems may store values as unsigned or signed
- Note that the meaning of a sequence of bits is usually implicit, e.g., software or hardware must know whether to treat as signed or unsigned
- Signed magnitude is a simple representation, but requires relatively complex hardware or software for arithmetic
- Two's complement is a more complex representation (to us), but uses simpler logic for arithmetic



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