CPE 111 Discrete Mathematics for Computer Engineers International Program, 2022 Homework 1, due on LEB2 at noon on 17 Aug 2022

Chapter 1

Sec 1.1

1. Which of these are propositions? What are the truth values of those that are propositions?

(a) Do not eat in the classroom.

Not a proposition; it's a command.

b) What time is it?

Not a proposition; it's a question.
c) There is pollution in Bangkok.

This is a proposition that is true; there have sound and air polution.

d) 4 + x = 5.

Not a proposition; its truth value depends on x

e) The moon is made of green cheese

This is a proposition that is false.

f) $2n \ge 50$.

Not a proposition; its truth value depends on 17

2. Suppose that Smartphone A has 256MB RAM and 32GB ROM, and the resolution of its camera is 8 MP; Smartphone

B has 288 MB RAM and 64 GB ROM, and the resolution of its camera is 4 MP; and Smartphone C has 128 MB RAM and 32 GB ROM, and the resolution of its camera is 5 MP. Determine the truth value of each of these propositions.

b) Smartphone C has more ROM or a higher resolution camera than Smartphone B.

It's true because C has 5 MP resolution compared to B is only 4 MP.

d) If Smartphone B has more RAM and more ROM than Smartphone C, then it also has a higher resolution camera.

It's false due to the hypothesis is true but the conclusion is false.

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- 3. Determine whether these biconditionals are true or false.
 - a) 2 + 2 = 4 if and only if 1 + 2 = 3.

b) 1 + 1 = 2 if and only if 2 + 3 = 5.

c) 1 + 1 = 3 if and only if monkeys can fly.

d) 0 > 1 if and only if 2 > 1.

- **4.** Construct a truth table for each of these compound propositions.
 - c) $q \oplus (p \land q)$

p	q	p ∧ q	$q \oplus (p \wedge q)$		
Т	T	T	F√		
T	F	F	Τ _		
F	T	F	T 🗸		
F	F	F	F 🗸		

Wrong, Change to "F"

e) $(q \rightarrow \neg p) \rightarrow (p \leftrightarrow q)$

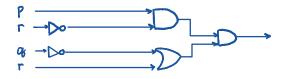
p	q	¬р	$q \rightarrow \neg p$	$p \leftrightarrow q$	$(q \to \neg p) \to (p \leftrightarrow q)$
T	T	F	F	τ	T V
T	F	F	T	F	F V
F	T	T	T	F	F V
F	F	T	T	Τ	T

- **5.** Evaluate each of these expressions.
- **√a)** (1 1011 ⊕ 1 1001) ⊕ 1 1010

b) (1,0011 v 0,1000) ∧ (1,0001 v 1,1010)

Sec 1.2

✓ 6. Construct a combinatorial circuit using inverters, OR gates, and AND gates that produces the output $(p \land \neg r) \land (\neg q \lor r)$ from input bits p, q, and r.



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Sec 1.3

- 7. Use De Morgan's laws to find the negation of each of the following statements.
- (a) Kwame will take a job in industry or go to graduate school.

Given
$$p \vee q$$
 Kwame will not take a job in industry and will not go to graduate school $\neg (p \vee q) = ?$ $\neg (p \vee q) = (\neg p) \wedge (\neg q) \#$

b) James is young and strong.

Given
$$p \wedge q$$
 James is not young, or he is not strong $\neg (p \wedge q) = ? \neg (p \wedge q) = (\neg p) \vee (\neg q) \#$

8. Determine whether $(\neg p \land (p \rightarrow q)) \rightarrow \neg q$ is a tautology. \therefore Proof that it is not a tautology #

р ¬р	q ~	$p \rightarrow q$	$(\neg p \land (p \to q)$	$(\neg p \land (p \to q)) \to \neg \ q$
TF	Т г	Т	F	T 🗸
T _F	F T	F	F	F 🗸
F T	T F	Т	Т	т 🗸
F τ	F T	Т	Ť	т ✓

9. Show that $\neg p \rightarrow (q \rightarrow r)$ and $q \rightarrow (p \lor r)$ are logically equivalent.

p	q	r	¬р	$q \rightarrow r$	pvr	$\neg p \rightarrow (q \rightarrow r)$	$q \rightarrow (p \ v \ r)$
T	Т	Т	F	Т	Т	Т	Τ 🗸
Т	Т	F	F	F	Т	Т	т 🗸
T	F	T	F	+	T	Т	T
T	F	F	F	Т	Т	Т	Τ 🗸
F	T	T	٢	Τ	T	T	T 🗸
F	T	F	٢	F	F	F	#
F	F	T	T	T	T	Τ	T 🗸
F	F	F	T	T	F	Т	T \

... They are logically equivalent #

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Sec 1.4

- 9. Let Q(x) be the statement "x + 10 > 2x." If the domain consists of all integers, what are these truth values?
 - a) Q(5) True
 - b) $\exists x \ Q(x)$ True
 - c) $\forall x Q(x)$ False
 - g) $\exists x \neg Q(x)$ True
- 10. Determine the truth value of each of these statements if the domain of each variable consists of all real numbers.
 - a) $\exists x(x^2=2)$ True
 - b) $\exists x(x^3 = -1)$ True
 - c) $\forall x(x^2+1 \ge 2)$ True FALSE when x = 0
 - d) $\exists x(x^2 \neq x)$ True
 - e) $\forall x(x^2 > x)$ False \checkmark

Sec 1.5

- 11. Determine the truth value of each of these statements if the domain of each variable consists of all real numbers.
 - a) $\forall x \exists y (x = y^2)$
 - b) $\exists x \forall y (xy = 0)$ True
 - c) $\exists x \exists y (x y = y x)$ True
 - d) $\exists x \forall y (y = 0 \rightarrow xy = 1)$
 - e) $\forall x \exists y (x+2y = 2 \land 2x + 4y = 5)$ Talse
 - f) $\forall x \forall y \exists z (z = (x + y) / 2)$