

# Empirical Properties of Diversion Ratios <sup>\*</sup>

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## Abstract

A diversion ratio, which measures the fraction of consumers that switch from one product to an alternative after a price increase, is a central calculation of interest to antitrust authorities for analyzing horizontal mergers. Two ways to measure diversion are: the ratio of estimated cross-price to own-price demand derivatives, and second-choice data. Policy-makers may be interested in either, depending on whether they are more concerned about widespread small price increases, or product discontinuations. We estimate diversion in two applications – using observational price variation and experimental second-choice data respectively – to illustrate the trade-offs between different empirical approaches. Using our estimates of diversion, we identify candidate products for divestiture in several hypothetical mergers.

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# 1 Introduction

A diversion ratio, which measures the fraction of consumers that switch from one product to an alternative after a price increase, is one of the best ways economists have for understanding the nature of competition between sellers. If diversion to available alternatives is low, a seller does not lose many sales to his competitors after a price increase, which allows him to exercise market power. In contrast, if diversion to available alternatives is high, consumers have many close substitutes, which limit the seller’s market power. Diversion ratios can be understood through the lens of a Nash-in-prices equilibrium when sellers offer differentiated products. Products with a high degree of differentiation face lower diversion and softer price competition, whereas products with a high degree of similarity to competing goods face higher diversion and tougher price competition.

Not surprisingly, diversion ratios are a central calculation of interest to antitrust authorities for analyzing horizontal mergers. The current U.S. merger guidelines, released in 2010, place greater weight on diversion ratios relative to concentration measures more commonly used to understand competition in settings with homogeneous goods (e.g., the Herfindahl-Hirschman Index (HHI)).<sup>1</sup> In the context of merger reviews, antitrust authorities identify the concept of ‘unilateral effects’ as being important for understanding the impact of a proposed merger. Unilateral effects of a merger arise when competition between the products of the merged firm is reduced because the merged firm internalizes substitution between its jointly-owned products.<sup>2</sup> This can lead to an increase in the price of the products of the merged firm, potentially harming consumers. Diversion ratios are the key statistic of interest for measuring unilateral effects. The current U.S. merger guidelines, released in 2010, note that:

*Diversion ratios between products sold by one merging firm and products sold by the other merging firm can be very informative for assessing unilateral price effects, with higher diversion ratios indicating a greater likelihood of such effects.*

Thus, holding competitive responses fixed, antitrust agencies will be more concerned about

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<sup>1</sup>Researchers have pointed out a number of concerns with using concentration measures or other functions of market share to capture the strength of competition. One concern is that such measures require one to define a market; another is that they do not capture the closeness of competition when products are differentiated, as most products are thought to be.

<sup>2</sup>In contrast, the concept of harm via ‘coordinated effects’ arises if a proposed merger increases the probability that firms in the industry will be able to successfully coordinate their behavior in an anti-competitive way.

mergers that involve products with higher diversion ratios, because the scope for price increases due to unilateral effects is thought to be greater.

Although the use of diversion ratios in antitrust policy is well understood theoretically, in practice, one needs to estimate diversion ratios. The U.S. Guidelines discuss diversion ratios as being calculated from an estimated demand system, or observed from consumer survey data or in a firm’s course of business. In this paper, we analyze different ways of estimating diversion ratios and characterize their empirical properties.

The researcher or antitrust authority may prefer different measurements of diversion in different settings. For example, if the antitrust authority is concerned with the potential for small but widespread price increases, they may want to evaluate diversion by analyzing estimated own- and cross-price derivatives at pre-merger prices. In contrast, if the antitrust authority is concerned with the potential for product discontinuations, second-choice data may be more informative. To clarify this point, we interpret a diversion ratio as a treatment effect of an experiment in which the treatment is “not purchasing product  $j$ .” The diversion ratio measures the outcome of this treatment, (i.e., the fraction of consumers who switch from  $j$  to a substitute product  $k$ ). The treated group consists of consumers who would have purchased  $j$  at pre-existing prices, but no longer purchase  $j$  at a higher price.

When policy-makers are interested in measuring the effect of treating only those consumers who substitute away from  $j$  after a very small price increase, they are implicitly evaluating a marginal treatment effect (MTE) at pre-merger prices.<sup>3</sup> A challenge of directly implementing such an experiment is that treating a small number of the most price-sensitive individuals lacks statistical power. An alternative is to treat all individuals who would have purchased  $j$  at pre-existing prices, and thus estimate an average treatment effect (ATE). This can be accomplished by surveying consumers about their second-choice products, or by exogenously removing product  $j$  from the choice set. When the diversion ratio is constant, the ATE coincides with the evaluation of the MTE at pre-merger prices. However, we show that constant diversion is a feature of only the linear demand model and a ‘plain vanilla’ logit model. Other commonly-used models of demand, such as random-coefficients logit or log-linear models, do not feature constant diversion, and the ATE and MTE may diverge.

A related question for the antitrust authority is whether one can reliably estimate diversion ratios using data from only the merging entities.<sup>4</sup> To consider this question, it’s useful

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<sup>3</sup>As we discuss later, one can view treatment effects estimators for price increases of different sizes as local average treatment effects (LATE).

<sup>4</sup>Indeed, the guidelines state: *Diversion ratios between products sold by merging firms and those sold by non-merging firms have at most secondary predictive value.*

to consider two concepts: an *aggregate diversion ratio*, which Katz and Shapiro (2003) define as the “percentage of the total sales lost by a product when its price rises that are captured by all of the other products in the candidate market,”<sup>5</sup> and a ‘diversion matrix,’ as a matrix whose off-diagonal elements report diversion between each pair of products that could potentially be considered for inclusion in a market, and whose diagonal elements report diversion to the outside good. In this case, the aggregate diversion represents the sum of the off-diagonal elements along the row. Discrete choice models of demand imply a “summing up” constraint so that the sum of each row of the diversion matrix (the aggregate diversion ratio plus the diversion to the outside good) is equal to unity. Most parametric models of demand also imply restrictions across the various rows of the diversion matrix.

We consider the empirical properties of diversion ratios in two applications. In the first application, we estimate two discrete-choice models of demand. We use data from Nevo (2000) to explore the importance of different measures of diversion. We provide estimates of three different measures: a MTE, evaluated at pre-merger prices using a random-coefficients model; an ATE, estimated by simulating a product removal in the same random-coefficients model; and a ‘plain vanilla’ logit model, which assumes constant diversion proportional to marketshares. We show that the ATE and MTE measures differ by 6% on average for each product’s closest substitute, and by about 8.3% across all substitutes. Substitution can be both over- and understated. A ‘plain vanilla’ logit model that assumes constant diversion substantially understates substitution to the best substitute, and overstates substitution to the outside good compared to the MTE or ATE.

In the second application, we construct an empirical estimator for the ATE measure of the diversion ratio by exogenously removing individual products from a local market in a large-scale experiment. Specifically, we remove products from a set of vending machines and track subsequent substitution patterns. The experimental setting precludes us from estimating diversion that would be relevant to a small price change (i.e., a MTE) because we are not able to exogenously change prices, but it does not require any restrictions on aggregate diversion. In order to control for unobserved demand shocks, we provide two conditions on economic primitives and examine how they help to estimate experimental measures of the diversion ratio. The conditions are: (1) product removals cannot increase total sales, nor decrease total sales by more than the sales of the product removed, (2) diversion to any single product is between 0 and 100 percent. We incorporate the second condition through

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<sup>5</sup>When defining aggregate diversion, Katz and Shapiro (2003) also impose the condition that “The aggregate diversion ratio must lie between zero and 100 percent.”

a non-parametric Bayesian shrinkage estimator. We find that these two conditions improve our estimates of diversion, although our estimates are sensitive to the strength of the prior. Next, we impose the assumption that aggregate diversion plus diversion to the outside good sums to one. Our Bayesian shrinkage estimator incorporates this assumption by nesting the parametric structural estimates of diversion and the (quasi)-experimental measures in a single framework. With the “summing up” constraint, even a very weak prior yields very precise estimates of diversion ratios.

Our results highlight what we believe to be two important points: (1) Observing data from all products within the market, rather than only products involved in a merger is important when estimating diversion ratios; and (2) in discrete choice demand systems the somewhat reasonable “summing up” constraint may be doing much of the heavy lifting as opposed to the parametric distribution of error terms. Our applications also illustrate the fact that different measures of diversion may be relevant to policy-makers in different settings. Several recent merger cases have been concerned with the potential for small but widespread price increases, such as in airline prices, and consumer goods and services in larger markets.<sup>6</sup> Other cases have centered around the potential for product discontinuations, such as in hospital and airline networks, and in several business-to-business markets.<sup>7</sup>

Finally, our empirical exercise demonstrates how two different measures of diversion can be obtained in practice (i.e., through demand estimation or product removals), how these measures of diversion might vary, and how to design and conduct experiments to measure diversion. Using two of our estimates of diversion from our second application, we consider several hypothetical mergers within the single-serving snack foods industry. We consider diversion between the products of several potential merger partners (e.g., Kellogg’s acquire Kraft, or Mars acquiring Nestle). We evaluate diversion from a leading product of the acquiring firm to all products of the target firm (e.g., diversion from Snickers to all Nestle products), and re-evaluate diversion after imposing divestiture of a key substitute (e.g., Nestle’s Butterfinger). The exercise illustrates the ability of diversion estimates to identify strong candidate products for divestiture requirements.

## 1.1 Related Literature

A larger goal of the paper is to bring together two literatures – the applied theoretical literature that motivates the use of diversion for understanding merger impacts, and an

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<sup>6</sup>Examples include airlines (add cite), Anhauser-Busch/InBev (add cite).

<sup>7</sup>Examples include airline routes (add cite), a merger of two European machinery firms, data storage products in the Dell-EMC merger, and the proposed merger between AT&T and T-Mobile.

applied econometric literature that articulates estimation challenges in settings for which the treatment effect of a policy can vary across individuals and may be measured with error.

By exploring the assumptions required for a credible (quasi)-experimental method of measuring diversion, we connect directly to the nascent theoretical literature discussing the use and measurement of the diversion ratio.<sup>8</sup> Farrell and Shapiro (2010) suggest that firms themselves track diversion in their ‘normal course of business,’ or that the diversion ratio is essentially another piece of data likely to be uncovered in a Hart-Scott-Rodino filing. Hausman (2010) argues that the only acceptable way to measure a diversion ratio is as the output from a structural demand system. Reynolds and Walters (2008) examine the use of stated-preference consumer surveys in the UK for measuring diversion. A different strand of the applied theoretical literature in IO focuses on whether or not the diversion ratio is likely to be informative about the price effect of a merger in the first place. We don’t take a stand on this question.<sup>9</sup>

In spirit, our approach is similar to Angrist, Graddy, and Imbens (2000), which shows how a cost shock can identify a particular local average treatment effect (LATE) for the price elasticity in a single product setting. That approach does not extend to the differentiated products setting because the requisite monotonicity condition may no longer be satisfied. Our second empirical application illustrates a differentiated products setting in which the average diversion ratio is identified from second-choice data alone, even though the separate own- and cross-price elasticities may not be. This highlights the economic content of (even partial) second-choice data, which have been found to be valuable in the structural literature on demand estimation (Berry, Levinsohn, and Pakes 2004).<sup>10</sup>

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<sup>8</sup>The focus on measuring substitution away from product  $j$  (using second-choice data or stock-outs), rather than on the direct effect of a proposed merger, is more in line with the public finance literature on sufficient statistics (Chetty 2009).

<sup>9</sup>This literature goes back to at least Shapiro (1995) and Werden (1996), and is well summarized in reviews by Farrell and Shapiro (2010) and Werden and Froeb (2006). A debate about the relationship between measures of upward pricing pressure (UPP) and merger simulations has developed since the release of the 2010 Horizontal Merger Guidelines including: Carlton (2010), Schmalensee (2009), Willig (2011), and Hausman (2010). In related work, Jaffe and Weyl (2013) incorporate an estimated pass-through rate to map anticipated opportunity cost effects into price effects. There have also been recent attempts to validate the predictions using only diversion ratios in simulation (Miller, Remer, Ryan, and Sheu 2012) and empirically (Cheung 2011). Those papers find that the price effects of a merger, and errors in predicting these effects, depend on the nature of competition among non-merging firms, and whether prices are strategic substitutes or strategic complements.

<sup>10</sup>There has been a recent debate on the use of experimental or quasi-experimental techniques vis-a-vis structural methods within industrial organization (IO) broadly, and within merger evaluation specifically. Angrist and Pischke (2010) complain about the general lack of experimental or quasi-experimental variation in many IO papers, and advocate viewing a merger itself as the treatment effect of interest. Nevo and Whinston (2010) respond by pointing out that, while retrospective merger analysis is valuable, the salient

The paper proceeds as follows. Section 2 illustrates a diversion matrix and discusses alternative ways to measure diversion using a treatment effects framework. Our first empirical application is provided in section 3, which estimates a discrete-choice model of demand that imposes an assumption that aggregate diversion plus diversion to the outside good sums to one. Section 4 illustrates diversion outside of the context of discrete-choice demand models using an experimental setting in the snack foods industry. We discuss our experimental design, present results using three different measures of diversion, and discuss the role that aggregate diversion plays in our estimates. We also consider the impacts of divestiture under several hypothetical mergers through the lens of our estimated diversion measures. Section 5 concludes.

## 2 Theoretical Framework

The rationale for focusing on diversion ratios to understand the potential impact of a merger comes from an underlying supply-side model in which firms produce differentiated goods and compete according to a Nash-in-prices equilibrium. Farrell and Shapiro (2010) present such a model to motivate the key constructs of the 2010 U.S. merger guidelines, and we review their results here.<sup>11</sup>

For simplicity, consider a single market composed of  $J$  single-product firms, where firm  $j$  sets the price of product  $j$  to maximize profits:

$$\pi_j = (p_j - c_j(q_j)) q_j(p_j, p_{-j})$$

Under an assumption of constant marginal costs, the FOC for product  $j$  becomes

$$q_j(p_j, p_{-j}) + (p_j - c_j) \frac{\partial q_j(p_j, p_{-j})}{\partial p_j} = 0$$

We consider the potential for a merger to induce efficiency gains by lowering the cost of producing product  $j$ . This efficiency gain, denoted  $e_j$ , is defined as a percentage reduction in marginal cost:  $e_j = \frac{c_j^{(1)} - c_j^{(0)}}{c_j^{(0)}}$  where the superscripts (0) and (1) denote pre- and post-merger

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policy question is generally one of prospective merger analysis, and that merely comparing proposed mergers to similar previously consummated mergers is unlikely to be informative, especially when both the proposal and approval of mergers is endogenous. This relates to a much older debate going back to Leamer (1983), and discussed more recently by Heckman (2010), Leamer (2010), Keane (2010), Sims (2010), Stock (2010), and Einav and Levin (2010).

<sup>11</sup>We use slightly different notation to aid in our empirical applications later.

quantities respectively. Henceforth, we denote pre-merger costs as  $c_j$  and post-merger costs as  $(1 - e_j) \cdot c_j$ . A merger modifies the FOC of a single-product firm that owns  $j$  and acquires product  $k$ , when prices of all other goods  $p_{-j}$  are held fixed at the pre-merger values, to:

$$q_j(p_j^{(0)}, p_{-j}) + (p_j^{(0)} - c_j) \frac{\partial q_j(p_j^{(0)}, p_{-j})}{\partial p_j} = 0 \quad (\text{Pre-merger}) \quad (1)$$

$$q_j(p_j^{(1)}, p_{-j}) + (p_j^{(1)} - (1 - e_j) \cdot c_j) \frac{\partial q_j(p_j^{(1)}, p_{-j})}{\partial p_j} + (p_k - c_k) \cdot \frac{\partial q_k(p_j^{(1)}, p_{-j})}{\partial p_j} = 0 \quad (\text{Post-merger}) \quad (2)$$

The difference between the FOCs is given by:

$$(p_k - c_k) \cdot \underbrace{\frac{\partial q_k(p_j, p_{-j})}{\partial p_j} / \frac{\partial q_j(p_j, p_{-j})}{\partial p_j}}_{D_{jk}(p_j, p_{-j})} - e_j c_j \quad (3)$$

This difference measures the degree to which a merger changes the opportunity cost of selling good  $j$ . After the merger, the firm internalizes the fact that some lost sales of product  $j$  are recaptured by product  $k$ . We denote the fraction of consumers who switch from  $j$  to  $k$  when faced with an increase in the price of  $j$  from the pre-merger prices  $(p_j^{(0)}, p_{-j})$ , holding all other prices fixed, as the diversion ratio  $D_{jk}(p_j, p_{-j})$ .<sup>12</sup>

## 2.1 A Matrix of Diversion Ratios

We can define a  $J \times J$  matrix of diversion ratios where the  $(j, k)$ -th element is  $D_{jk}(\mathbf{p})$ . Rather than report  $D_{jj} = -1$ , we report  $D_{j0}$  (the diversion to the outside good) along the diagonal.

$$D(\mathbf{p}) = \begin{bmatrix} D_{10} & D_{12} & D_{13} \\ D_{21} & D_{20} & D_{23} \\ D_{31} & D_{32} & D_{30} \end{bmatrix}$$

We find this matrix is useful to make a number of conceptual points: (a) if all products are substitutes (rather than complements) and consumers make discrete choices, then the sum of each row of the matrix to equal unity:  $D(\mathbf{p}) \times \mathbf{1}_J = \mathbf{1}_J$ ; (b) the sum of the off-diagonal

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<sup>12</sup>The expression in (3) is sometimes referred to as *Upward Pricing Pressure* which measures how the merger changes the incentives to increase  $p_j$  that comes about because of the merger through changes in *opportunity costs*. These incentives are measured in the units of marginal cost rather than price. Farrell and Shapiro (2010) discuss how to use Diversion/UPP directly to estimate the likely effects of a merger: when prices are strategic complements this can be viewed as a lower bound on the overall effect. To translate directly from the change in opportunity cost to prices would also need an estimate of the pass-through rate, see Jaffe and Weyl (2013) for more details.



elements along a row  $j$  is known as the *aggregate diversion* for product  $j$ . Katz and Shapiro (2003) show this quantity is helpful in defining the relevant market; (c) most parametric models of demand use information from other rows  $j'$  when estimating diversion in row  $j$ .

Consider a hypothetical example in which diversion among three vehicles (Honda Civic, Toyota Prius, and Tesla) is given by a matrix of diversion ratios.

<i>from/to :</i>	<i>Civic</i>	<i>Prius</i>	<i>Tesla</i>
<i>Civic :</i>	50	40	10
<i>Prius :</i>	50	30	20
<i>Tesla :</i>	0	80	20

If we were interested in a merger between Honda and Toyota, is it acceptable to restrict our attention to diversion from Prius to Civic? Or, do we need to estimate diversion from the Prius to all possible alternatives (the entire row)? Do we also need to consider diversion from Civic to Prius? Is it important to understand other elements or functions of the matrix (e.g., aggregate diversion for the Prius)?

From a theoretical context, the information we require depends on the calculation we plan on performing. In order to calculate Upward Pricing Pressure (UPP) using equation (3), we only need the diversion from Civic to Prius (or vice versa). For a *partial merger simulation*, as in Hausman, Leonard, and Zona (1994), we calculate the effects of the merger on  $p_j$  holding fixed  $p_{-j}$  by solving equation (2), and we would need to observe the entire row  $j$ . In order to perform *full merger simulation* as in Nevo (2001) where we solve for the system of post-merger equilibrium prices  $\mathbf{p}$  now we need the entire matrix  $D(\mathbf{p})$  in order to calculate the competitive responses for other products in the market.

From an empirical perspective, we may be able to improve our estimates of  $\hat{D}_{jk}$  by using information from the rest of the row  $D_{jk'}$  or the sum of the row (the discrete choice assumption)  $\sum_{k=0, k \neq j}^J D_{jk} = 1$ , even while from a theoretical perspective the additional information might not be required.

## 2.2 Diversion as a Treatment Effect

Once we determine the elements or functions of the diversion matrix we are interested in, we face the related task of choosing a measurement of each of the relevant elements,  $D_{jk}(p_j, p_{-j}^0)$ . We consider a hypothetical experiment which raises the price of product  $j$  by  $\Delta p_j$ , so that  $p_j = p_j^0 + \Delta p_j$ . We can interpret diversion as a Wald estimator of a treatment effect with a binary treatment (i.e., not purchasing product  $j$ ) and a binary outcome (i.e., purchasing product  $k$  or not). We denote this as:

$$D_{jk}(p_j, p_{-j}^0) = \left| \frac{\Delta q_k}{\Delta q_j} \right| = \left| \frac{q_k(p_j^0 + \Delta p_j, p_{-j}^0) - q_k(p_j^0, p_{-j}^0)}{q_j(p_j^0 + \Delta p_j, p_{-j}^0) - q_j(p_j^0, p_{-j}^0)} \right| = \frac{\int_{p_j^0}^{p_j^0 + \Delta p_j} \frac{\partial q_k(p_j, p_{-j}^0)}{\partial p_j} dp_j}{\int_{p_j^0}^{p_j^0 + \Delta p_j} \frac{\partial q_j(p_j, p_{-j}^0)}{\partial p_j} dp_j} \quad (4)$$

The treated group corresponds to individuals who would have purchased product  $j$  at price  $p_j$  but do not purchase  $j$  at price  $p_j + \Delta p_j$ . The lower an individual's reservation price for  $j$ , the more likely an individual is to receive the treatment. Thus,  $\Delta p_j$  functions as an 'instrument' because it monotonically increases the probability of treatment.

By focusing on the numerator in equation (4), we can re-write the diversion ratio using the marginal treatment effects (MTE) framework of Heckman and Vytlacil (2005), in which  $D_{jk}(p_j, p_{-j}^0)$  is a marginal treatment effect that depends on  $p_j$ .<sup>13</sup>

$$\widehat{D_{jk}^{LATE}}(\Delta p_j) = \frac{1}{\Delta q_j} \int_{p_j^0}^{p_j^0 + \Delta p_j} \underbrace{\frac{\partial q_k(p_j, p_{-j}^0)}{\partial q_j}}_{\equiv D_{jk}(p_j, p_{-j}^0)} \frac{\partial q_j(p_j, p_{-j}^0)}{\partial p_j} \partial p_j \quad (5)$$

$$\widehat{D_{jk}^{ATE}} = \frac{1}{\Delta q_j} \int_{p_j^0}^{\bar{p}_j} D_{jk}(p_j, p_{-j}^0) \frac{\partial q_j(p_j, p_{-j}^0)}{\partial p_j} \partial p_j = \left| \frac{q_k(\bar{p}_j, p_{-j}^0) - q_k(p_j^0, p_{-j}^0)}{q_j(\bar{p}_j, p_{-j}^0) - q_j(p_j^0, p_{-j}^0)} \right| \quad (6)$$

As we vary  $p_j$ , we measure the weighted average of diversion ratios where the weights  $w(p_j) = \frac{1}{\Delta q_j} \frac{\partial q_j(p_j, p_{-j}^0)}{\partial p_j}$  correspond to the lost sales of  $j$  at a particular  $p_j$  as a fraction of all lost sales. This directly corresponds to Heckman and Vytlacil (2005)'s expression for the local average treatment effect (LATE); we average the diversion ratio over the set of consumers of product  $j$  who are most price sensitive. The LATE estimator varies with the size of the price increase because the set of treated individuals varies. In equation (6) the average treatment effect (ATE) is the expression for the LATE in which all individuals are treated. This corresponds to an increase in  $p_j$  all the way to the choke price  $\bar{p}_j$ . Evaluating  $D_{jk}(p_j^0, p_{-j}^0)$  at pre-merger prices is consistent with a MTE for which  $\Delta p_j$  is infinitesimally small.<sup>14</sup> As we choose larger values for  $\Delta p_j$  our LATE estimate may differ from the MTE evaluated at  $\mathbf{p}^0$ .

We can relate the divergence in the treatment effect measures of  $D_{jk}$  to the underlying economic primitives of demand. Consider what happens when we examine a "larger than

<sup>13</sup>The MTE is a non-parametric object which can be integrated over different weights to obtain all of the familiar treatment effects estimators: treatment on the treated, average treatment effects, local average treatment effects, average treatment on the control, etc.

<sup>14</sup>antitrust authorities also sometimes focus on the notion of a 'small but significant non-transitory increase in price (SSNIP).' The practice of antitrust often employs an SSNIP test of 5-10%.

infinitesimal” increase in price  $\Delta p_j \gg 0$ . We derive an expression for the second-order expansion of demand at  $(p_j, p_{-j})$ :

$$\begin{aligned} q_k(p_j + \Delta p_j, p_{-j}) &\approx q_k(p_j, p_{-j}) + \frac{\partial q_k(p_j, p_{-j})}{\partial p_j} \Delta p_j + \frac{\partial^2 q_k(p_j, p_{-j})}{\partial p_j^2} (\Delta p_j)^2 + O((\Delta p_j)^3) \\ \frac{q_k(p_j + \Delta p_j, p_{-j}) - q_k(p_j, p_{-j})}{\Delta p_j} &\approx \frac{\partial q_k(p_j, p_{-j})}{\partial p_j} + \frac{\partial^2 q_k(p_j, p_{-j})}{\partial p_j^2} \Delta p_j + O(\Delta p_j)^2 \end{aligned} \quad (7)$$

This allows us to compute an expression for the bias of a LATE estimate  $\widehat{D_{jk}^{LATE}}(\Delta p_j)$  compared to the marginal diversion ratio  $D_{jk}(p_j, p_{-j})$ , as well as the variance of the LATE estimator (under the assumption of (locally) constant diversion, for which  $\Delta q_k \approx D_{jk} \Delta q_j$ ):

$$Bias(\widehat{D_{jk}^{LATE}}) \approx - \frac{D_{jk} \frac{\partial^2 q_j}{\partial p_j^2} + \frac{\partial^2 q_k}{\partial p_j^2}}{\frac{\partial q_j}{\partial p_j} + \frac{\partial^2 q_j}{\partial p_j^2} \Delta p_j} \Delta p_j \quad (8)$$

$$Var(\widehat{D_{jk}^{LATE}}) \approx Var\left(\frac{\Delta q_k}{|\Delta q_j|}\right) \approx \frac{1}{\Delta q_j^2} \left( D_{jk}^2 \sigma_{\Delta q_j}^2 + \sigma_{\Delta q_k}^2 - 2 D_{jk} \rho \sigma_{\Delta q_j} \sigma_{\Delta q_k} \right) \quad (9)$$

The expression in (8) shows that the bias depends on two things: one is the magnitude of the price increase  $\Delta p_j$ , the second is the curvature of demand (the terms  $\frac{\partial^2 q_j}{\partial p_j^2}$  and  $\frac{\partial^2 q_k}{\partial p_j^2}$ ). This suggests that bias is minimized by considering small price changes. The disadvantage of considering a small price change  $\Delta p_j$  is that it implies that the size of the treated group  $\Delta q_j$  is also small, and thus the variance of our diversion measure is large, as shown in equation 9. This is the usual bias-variance tradeoff: a small change in  $p_j$  induces a small change in  $q_j$  and reduces the bias, but increases the potential variance; a larger  $\Delta p_j$  (and by construction  $\Delta q_j$ ) may yield a less noisy LATE, but may deviate from the quantity of interest.

A relevant question is: What are the economic implications of assuming a constant treatment effect, such that  $D_{jk}(p_j, p_{-j}) = D_{jk}$ ? We can see the answer by examining the case where the bias calculation in equation (8) is equal to zero. Economic theory provides guidance because the underlying objects are demand curves. Two functional forms for demand exhibit constant diversion and are always unbiased: the first is linear demand, for which  $\frac{\partial^2 q_k}{\partial p_j^2} = 0$ ,  $\forall j, k$ . The second is the IIA logit model, for which  $D_{jk} = -\frac{\partial^2 q_k}{\partial p_j^2} / \frac{\partial^2 q_j}{\partial p_j^2}$ . *Implicitly when we assume that the diversion ratio does not vary with price, we assume that the true demand system is well approximated by either a linear demand curve or the IIA logit model.* We derive these relationships, as well as expressions for diversion under other demand models in Appendix A.1, and show that random coefficients logit demand, and constant elasticity

demands (including log-linear demand) do not generally exhibit constant diversion.

If the primary concern in a given market is that the curvature of demand is steep, so that assuming a constant diversion ratio is unreasonable, one may need to consider a small price increase to avoid bias. However, if the primary concern is that sales are highly variable, one may need to consider a larger price increase to reduce variance.<sup>15</sup> Information about the elasticity (and super-elasticity) of demand for  $j$  can be informative. As noted in (5), the LATE estimate will concentrate more weight near  $\mathbf{p}^0$  when demand is more elastic, or if demand becomes increasingly inelastic as  $\Delta p_j$  becomes larger.

In figure 1, we consider what diversion might look like for three different hypothetical demand curves for a Toyota Prius. In the first example, we consider diversion to three alternatives (a Honda Civic, Tesla, and an outside good) when demand for a Prius is linear. As we vary price upwards from \$25,000 to \$50,000, diversion to the three alternatives is constant (as is required by linear demand): 63% of potential Prius buyers switch to a Honda Civic, 12% switch to a Tesla, and 25% switch to the outside option. The histogram along the bottom axis shows the rate at which Prius buyers leave the Prius (which is the rate at which consumers are ‘treated’ by a price increase).

The second example in figure 1 considers diversion to the same alternatives when demand for a Prius has a constant elasticity of  $\epsilon = -1$ . We refer to this as an inelastic constant elasticity demand curve. The rate at which Prius buyers leave is now higher near the market price than at higher prices (so the histogram along the horizontal axis assigns more weight near the market price). Furthermore, the diversion pattern differs as we consider higher price points. There is more substitution to the Honda Civic after a small price increase, and more substitution to the Tesla after a large price increase. Using the histogram to weight the diversion across the entire price spectrum (from \$25,000 to \$50,000) provides an estimate of aggregate diversion (ATE) that is 59% to the Honda Civic, 18% to the Tesla, and 22% to the outside good. However, for a small price increase, diversion to the Honda Civic is over 90%.

The third, and final example in figure 1 considers diversion when demand for a Prius is constant elasticity, but with an elasticity of  $\epsilon = -4$ . This greater elasticity changes the relative weighting across different hypothetical price increases, so that more consumers leave at smaller price changes. Although diversion to the three alternatives at any given price point is the same as the case of inelastic demand, the aggregate diversion (ATE) is now

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<sup>15</sup>Furthermore, if the policy maker believes that a proposed merger could induce firms to withdraw a product from the market or impose a large price increase, then the ATE calculation becomes the primary object of interest.

more heavily weighted towards consumers that leave at small price changes. Thus, aggregate diversion to the Honda Civic is 72%, with 10% diverting to a Tesla and 18% diverting to the outside good.

To summarize, the LATE/ATE provides a good approximation for the MTE at  $\mathbf{p}^0$  when the bias in (8) is small, which happens: (a) when the curvature of demand is low ( $\frac{\partial^2 q_k}{\partial p_j^2} \approx 0$ ), (b) when the true diversion ratio is constant (or nearly constant) so that  $D_{jk}(p_j, p_{-j}) = D_{jk}$ , or (c) when demand for  $j$  is steepest near the market price  $\left| \frac{\partial q_j(p_j, p_{-j})}{\partial p_j} \right| \gg \left| \frac{\partial q_j(p_j + \Delta p_j, p_{-j})}{\partial p_j} \right|$ .

## 2.3 Second-Choice Data

Often researchers have access to second-choice data. For example, Berry, Levinsohn, and Pakes (2004) observe not only marketshares of cars but also survey answers to the question: “If you did not purchase this vehicle, which vehicle would you purchase?” Consumer surveys provide a stated-preference method of recovering second-choice data. One may also construct second-choice data through a revealed-preference mechanism by experimentally removing product  $j$  from a consumer’s choice set for a period of time.<sup>16</sup> One can view such an exogenous product removal as being equivalent to an increase in price to the choke price  $\bar{p}_j$ , where  $q_j(\bar{p}_j, p_{-j}) = 0$ . Thus, an exogenous product removal measures the ATE, treating all of the pre-merger consumers of good  $j$  and minimizing the variance expression in (9).

Notice the relationship between the ATE measure of diversion  $\widehat{D_{jk}^{ATE}}$ , and second choice data, where  $A$  is the set of available products and  $A \setminus j$  denotes the set of available products after the removal of product  $j$ :

$$\widehat{D_{jk}^{ATE}} = \left| \frac{q_k(\bar{p}_j, p_{-j}^0) - q_k(p_j^0, p_{-j}^0)}{q_j(\bar{p}_j, p_{-j}^0) - q_j(p_j^0, p_{-j}^0)} \right| = \frac{q_k(\mathbf{p}^0, A \setminus j) - q_k(\mathbf{p}^0, A)}{q_j(\mathbf{p}^0, A)} \quad (10)$$

Under the ATE, all individuals in the population are treated. This has the effect of making the choice of instrument irrelevant in the measure of the treatment effect.

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<sup>16</sup>Another way to recover second-choice data is to use observational data on consumer choice sets. However, a problem with using observational choice-set variation is that the variation is typically non-random. If one simply compares retail locations that stock product  $j$  to locations that do not stock product  $j$ , one might expect the stocking decision to be correlated with demand for both  $j$  and other products. In previous work, Conlon and Mortimer (2013a) establish conditions under which a temporary stock-out event provides random variation in the choice set. The main intuition is that after one conditions on inventory and consumer demand, the timing of a stock-out follows a known random distribution; paired with the assumption that consumer arrival patterns do not respond to anticipated stock-out events, this provides (quasi)-random choice set variation.

### 3 Application to Nevo (2000)

In our first application, we use the well-known example from Nevo (2000). This application will allow us to measure diversion in two ways: first as the ratio of the estimated derivatives of demand evaluated at pre-merger prices (a MTE evaluated at  $\mathbf{p}_0$ ), and second as the response to a simulated removal of a product (an ATE). The discrete-choice nature of the demand system imposes a ‘summing-up constraint’ (i.e., that aggregate diversion plus diversion to the outside good sums to one).

The data consist of  $T = 94$  markets with  $J = 24$  brands per market and a  $I = 20$  point distribution of heterogeneity for each market. The specification allows for product fixed effects  $d_j$ , unobserved heterogeneity in the form of a multivariate normally distributed  $\nu_i$  with variance  $\Sigma$ , and observable demographic heterogeneity in the form of  $\Pi$  interacted with a vector of demographics  $d_{it}$ .

$$u_{ijt} = d_j + x_{jt} \underbrace{(\bar{\beta} + \Sigma \cdot \nu_i + \Pi \cdot d_{it})}_{\beta_{it}} + \Delta \xi_{jt} + \varepsilon_{ijt}$$

We estimate parameters following the MPEC approach of Dubé, Fox, and Su (2012).<sup>17</sup> The estimated coefficient on price is distributed as follows:<sup>18</sup>

$$\beta_{it}^{price} \sim N(-62.73 + 588.21 \cdot \text{income}_{it} - 30.19 \cdot \text{income}_{it}^2 + 11.06 \cdot \text{I[child]}_{it}, \sigma = 3.31)$$

We denote a measure of diversion evaluated for an infinitesimally small price change as an *MTE*. We refer to a ‘second choice’ estimate of diversion as an ATE. For comparison, we also evaluated a Logit model, under which diversion is assumed to be constant. These three treatment effects are defined as:

$$MTE = \frac{\frac{\partial s_k}{\partial p_j}}{\left| \frac{\partial s_j}{\partial p_j} \right|}, \quad ATE = \frac{s_k(A \setminus j) - s_k(A)}{|s_j(A \setminus j) - s_j(A)|}, \quad Logit = \frac{s_k(A)}{1 - s_j(A)}$$

We suppose that the policy-relevant calculation of interest is the *MTE*, and we quantify

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<sup>17</sup>Technically we employ the continuously updating GMM estimator of Hansen, Heaton, and Yaron (1996) and adapted to the BLP problem by Conlon (2016). For this dataset, CUE and 2-step GMM produce nearly identical point estimates.

<sup>18</sup>One motivation for choosing this particular example is that it demonstrates a large degree of heterogeneity in willingness to pay.

how well the other treatment effect estimators approximate the  $MTE$ .

	$MTE$	$ATE$	$Logit$
Best Substitute			
Med( $D_{jk}$ )	13.26	13.54	9.05
Mean( $D_{jk}$ )	15.11	15.62	10.04
% Agree with $MTE$	100.00	89.98	58.38
Outside Good			
Med( $D_{j0}$ )	35.30	32.40	54.43
Mean( $D_{j0}$ )	36.90	33.78	53.46

Table 1: Substitution to Best Substitute and Outside Good

Notes: An observation is a product-market pair. There are 94 markets and 24 products. The first panel reports diversion to each product-market pair’s best substitute. The second panel reports diversion to the outside good.

For each of the 94 markets and 24 products, we compute the best substitute for each product-market pair, and to calculate the diversion ratio to that product. In Table 1, we report these patterns. We find that for  $MTE$  and  $ATE$ , we get roughly the same amount of substitution on average to the best substitute (around 13-15%). As one might expect, the plain  $Logit$  fails to capture the closeness of competition and instead finds 9 – 10% substitution on average to the best substitute. We find that the  $ATE$  identifies the same best substitute as the  $MTE$  around 90% of the time, while the  $Logit$  (which identifies the same best substitute for all products) is only in agreement 58% of the time. We can repeat the exercise and calculate substitution to the outside good. Here we find that the  $MTE$  has slightly more outside good substitution (35 – 37%) than the  $ATE$  diversion measure (32 – 34%), but far less than the  $Logit$ , which predicts that around 54% of consumers switch to the outside good.

One can also compare the different measures of diversion. We treat the  $MTE$  as the baseline value and compare the difference in the calculated diversion. For example, we compare the difference between  $\log D_{jk}^{ATE} - \log D_{jk}^{MTE}$ .<sup>19</sup> The first and third panels of table 2 report this calculation for each product’s best substitute and the outside good, similar to table 1. The second panel reports differences for all  $J$  substitutes for each product. As indicated in table 2, this implies that the  $ATE$  measure of diversion is on average 2–3% higher than the  $MTE$  measure of diversion for each product’s best substitute. Across all substitute

<sup>19</sup>As in table 1, an observation is a product-market pair. Table 2 reports means and medians across these  $J \cdot T$  observations.

products, shown in the second panel, the *ATE* measure is around 6 – 8% higher than the *MTE* measure. When compared to the outside good, the *ATE* measure is around 8 – 9% lower than the *MTE* measure. We also report the mean and median absolute deviation. This indicates that we are both over- and understating substitution on a product-by-product basis, because these are larger in magnitude than the median and mean deviations. As one might expect, the *Logit* model substantially understates (by 40% or more) substitution to the best substitute, as well as substitution to other products (by 25% or more), and overstates substitution to the outside good by as much as 39%.

	med( $y - x$ )	mean( $y - x$ )	med( $ y - x $ )	mean( $ y - x $ )	std( $ y - x $ )
	Best Substitutes				
<i>ATE</i>	2.56	3.24	6.00	7.61	7.04
<i>Logit</i>	-44.19	-42.88	44.92	47.77	28.63
	All Products				
<i>ATE</i>	5.78	8.30	8.29	12.13	12.02
<i>Logit</i>	-35.90	-25.92	49.48	53.27	34.56
	Outside Good				
<i>ATE</i>	-7.93	-8.89	7.94	9.08	6.77
<i>Logit</i>	39.22	39.20	39.22	40.60	22.05

Table 2: Relative % Difference in Diversion Measures: Comparison  $x = \log(\widehat{D}^{MTE})$

Notes: An observation is a product-market pair. There are 94 markets and 24 products. The first panel compares three alternative measures of diversion to the *MTE* measure for each product-market pair’s best substitute. The second panel averages across all possible substitutes. The third panel provides comparisons of the three measures of diversion to the *MTE* diversion to the outside good.

There is no obvious theoretical reason as to why the *ATE* measure would overstate (understate) substitution to other products on average when compared to the *MTE* measure, other than the fact that the marginal consumer tends to become more (less) inelastic as the price increases due to the curvature of demand induced by the logit error term.<sup>20</sup> However, it’s clear that when we reduce an estimator’s ability to accommodate heterogeneity in consumer preferences, the *MTE* and *ATE* measures get closer together. In Appendix A.2, we repeat this exercise with a restricted version of the demand model at the original published

<sup>20</sup>The (random coefficients) logit model has an inflection point at  $s = 0.5$ . At the market level we know that  $s_j < 0.5$  for all  $j$  except for the outside good. We have  $s_0 > 0.5$  in some markets and  $s_0 < 0.5$  in others. At the individual level, it is not uncommon for  $s_{ij} > 0.5$ . For these reasons, we cannot necessarily sign the second derivative of demand  $\frac{\partial^2 q_k}{\partial p_j^2}$ .



estimates from Nevo (2000).<sup>21</sup> In Appendix A.3 we conduct Monte Carlo simulations with commonly-used parametric demand models, and report the maximum discrepancy between the MTE and ATE estimates.

## 4 Empirical Application to Vending

In our next empirical application, we estimate the ATE form of the diversion ratio using observed second-choice data. We run a series of experiments in which we exogenously remove a product from 66 vending machines located in office buildings in Chicago, and measure substitution to the remaining products. We begin with a discussion of the snack foods/vending industry, including potential antitrust issues in 4.1. We discuss our experimental design in 4.2, and describe our experimentally generated data in 4.3.

### 4.1 Description of Data and Industry

Globally, the snack foods industry is a \$300 billion a year business, composed of a number of large, well-known firms and some of the most heavily-advertised global brands. Mars Incorporated reported over \$50 billion in revenue in 2010, and represents the third-largest privately-held firm in the US. Other substantial players include Hershey, Nestle, Kraft, Kellogg, and the Frito-Lay division of PepsiCo. While the snack-food industry as a whole might not appear highly concentrated, sales within product categories can be very concentrated. For example, Frito-Lay comprises around 40% of all savory snack sales in the United States, and reported over \$13 billion in US revenues last year, but its sales outside the salty-snack category are minimal, coming mostly through parent PepsiCo's Quaker Oats brand and the sales of *Quaker Chewy Granola Bars*.<sup>22</sup> We report HHI's at both the category level and for all vending products in Table 3 from the region of the U.S. that includes Chicago. If the relevant market is defined at the category level, all categories are considered highly concentrated, with HHIs in the range of roughly 4500-6300. If the relevant market is defined as all products sold in a snack-food vending machine, the HHI is below the critical threshold of 2500. Any evaluation of a merger in this industry would hinge on the closeness of competition, and thus require measuring diversion.

Over the last 25 years, the industry has been characterized by a large amount of merger and acquisition activity, both on the level of individual brands and entire firms. For example,

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<sup>21</sup>The restriction imposed is that  $\pi_{inc^2, price} = 0$ .

<sup>22</sup>Most analysts believe Pepsi's acquisition of Quaker Oats in 2001 was unrelated to its namesake business but rather for Quaker Oats' ownership of Gatorade, a close competitor in the soft drink business.

the *Famous Amos* cookie brand was owned by at least seven firms between 1985 and 2001, including the Keebler Cookie Company (acquired by Kellogg in 2001), and the Presidential Baking Company (acquired by Keebler in 1998). *Zoo Animal Crackers* have a similarly complicated history, having been owned by Austin Quality Foods before they too were acquired by the Keebler Cookie Co. (which in turn was acquired by Kellogg).<sup>23</sup>

Our study measures diversion through the lens of a single medium-sized retail vending operator in the Chicago metropolitan area, Mark Vend Company. Each of Mark Vend’s machines internally records price and quantity information. The data track total vends and revenues since the last service visit on an item-level basis, but do not include time-stamps for each sale. Any given machine can carry roughly 35 products at one time, depending on configuration.

We observe retail and wholesale prices for each product at each service visit during a 38-month panel that runs from January 2006 to February 2009. There is relatively little price variation within a site, and almost no price variation within a category (e.g., chocolate candy) at a site. This is helpful from an experimental design perspective, but can pose a challenge to structural demand estimation. Very few “natural” stock-outs occur at our set of machines.<sup>24</sup> Most changes to the set of products available to consumers are a result of product rotations, new product introductions, and product retirements. Over all sites and months, we observe 185 unique products. Some products have very low levels of sales and we consolidate them with similar products within a category produced by the same manufacturer, until we are left with 73 ‘products’ that form the basis of the rest of our exercise.<sup>25</sup>

In addition to the data from Mark Vend, we also collect data on the characteristics of each product online and through industry trade sources.<sup>26</sup> For each product, we note its manufacturer, as well as the following set of product characteristics: package size, number

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<sup>23</sup>Snack foods have an important historic role in market definition. A landmark case was brought by *Tastykake* in 1987 in an attempt to block the acquisition of *Drake* (the maker of Ring-Dings) by *Ralston-Purina’s Hostess* brand (the maker of Twinkies). That case established the importance of geographically significant markets, as Drake’s had only a 2% marketshare nationwide, but a much larger share in the Northeast (including 50% of the New York market). Tastykake successfully argued that the relevant market was single-serving snack cakes rather than a broad category of snack foods involving cookies and candy bars. [Tasty Baking Co. v. Ralston Purina, Inc., 653 F. Supp. 1250 - Dist. Court, ED Pennsylvania 1987.]

<sup>24</sup>Mark Vend commits to a low level of stock-out events in its service contracts.

<sup>25</sup>For example, we combine Milky Way Midnight with Milky Way, and Ruffles Original with Ruffles Sour Cream and Cheddar.

<sup>26</sup>For consolidated products, we collect data on product characteristics at the disaggregated level. The characteristics of the consolidated product are computed as the weighted average of the characteristics of the component products, using vends to weight. In many cases, the observable characteristics are identical.

of servings, and nutritional information.<sup>27</sup>

## 4.2 Experimental Design

We ran four exogenous product removals with the help of Mark Vend Company. These represent a subset of a larger group of eight exogenous product removals that we have analyzed in two other projects, Conlon and Mortimer (2013b) and Conlon and Mortimer (2017). Our experiment uses 66 snack machines located in professional office buildings and serviced by Mark Vend. Most of the customers at these sites are ‘white-collar’ employees of law firms and insurance companies. Our goal in selecting the machines was to choose machines that could be analyzed together, in order to be able to run each product removal over a shorter period of time across more machines.<sup>28</sup> These machines were also located on routes that were staffed by experienced drivers, which maximized the chance that the product removal would be successfully implemented. The 66 machines used for each treatment are distributed across five of Mark Vend’s clients, which had between 3 and 21 machines each. The largest client had two sets of floors serviced on different days, and we divided this client into two sites. Generally, each site is spread across multiple floors in a single high-rise office building, with machines located on each floor.

For each treatment, we remove a product from all machines at a client site for a period of 2.5 to 3 weeks. The four products that we remove are the two best-selling products from either (a) chocolate maker Mars Incorporated (Snickers and Peanut M&Ms) or (b) cookie maker Kellogg’s (Famous Amos Chocolate Chip Cookies and Zoo Animal Crackers). We refer to exogenously-removed products as the *focal products* throughout our analysis.<sup>29</sup> Whenever a product was exogenously removed, poster-card announcements were placed at the front of the empty product column. The announcements read: *This product is temporarily unavailable. We apologize for any inconvenience.* The purpose of the card was two-fold: first,

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<sup>27</sup>Nutritional information includes weight, calories, fat calories, sodium, fiber, sugars, protein, carbohydrates, and cholesterol.

<sup>28</sup>Many high-volume machines are located in public areas (e.g., museums or hospitals), and feature demand patterns (and populations) that vary enormously from one day to the next, so we did not use machines of this nature. In contrast, the work-force populations at our experimental sites have relatively stable demand patterns.

<sup>29</sup>Not reported here are two experiments on best-selling products from Pepsi’s Frito Lay Division, which we omit for space considerations, and because Pepsi’s products already dominate the salty snack category (which makes merger analysis less relevant). We also ran two additional experiments in which we removed two products at once; again we omit those for space considerations and because they don’t speak to our diversion ratio example. These are analyzed in Conlon and Mortimer (2013b) and Conlon and Mortimer (2017).

we wanted to avoid dynamic effects on sales as much as possible, and second, Mark Vend wanted to minimize the number of phone calls received in response to the stock-out events.

The dates of the interventions range from June 2007 to September 2008, with all removals run during the months of May - October. We collected data for all machines for just over three years, from January of 2006 until February of 2009. During each 2-3 week experimental period, most machines receive service visits about three times. However, the length of service visits varies across machines, with some machines visited more frequently than others. Though data are recorded at the level of a service visit, it is more convenient to organize observations by week, because different visits occur on different days of the week. In order to do this, we assume that sales are distributed uniformly among the business days in a service interval, and assign sales to weeks. We allow our definition of when weeks start and end to depend on the client site and experiment, because different experimental treatments start on different days of the week.<sup>30</sup>

The cost of the experiment consisted primarily of driver costs. Drivers had to spend extra time removing and reintroducing products to machines, and the driver dispatcher had to spend time instructing the drivers, tracking the dates of each experiment, and reviewing the data as they were collected. Drivers are generally paid a small commission on the sales on their routes, so if sales levels fell dramatically as a result of the experiments, their commissions could be affected. Tracking commissions and extra minutes on each route for each driver would have been prohibitively expensive to do, and so drivers were provided with \$25 gift cards for gasoline during each week in which a product was removed on their route to compensate them for the extra time and the potential for lower commissions.

Our experiment differs somewhat from an ideal experiment. Ideally, we would be able to randomize the choice set on an individual level. Technologically, of course, that is difficult in both vending and traditional brick and mortar contexts. In contrast, online retailers are capable of showing consumers different sets of products and prices simultaneously. This leaves our design susceptible to contamination if for example, Kraft runs a large advertising campaign for Planters Peanuts that corresponds to the timing of one of our experiments. Additionally, because we remove all of the products at an entire client site for a period of 2.5 to 3 weeks, we lack a contemporaneous “same-side” group of untreated machines. We chose this design, rather than randomly staggering the product removals, because we (and the participating clients) were afraid consumers might travel from floor to floor searching for stocked-out products. This design consideration prevents us from using contemporane-

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<sup>30</sup>At some site-experiment pairs, weeks run Tuesday to Monday, while others run Thursday to Wednesday.

ous control machines in the same building, and makes it more difficult to capture weekly variation in sales due to unrelated factors, such as a client location hitting a busy period that temporarily induces long work hours and higher vending sales. Conversely, the design has the benefit that we can aggregate over all machines at a client site, and treat the entire site as if it were a single machine. Despite the imperfections of field experiments in general, these are often the kinds of tests run by firms in their regular course of business, and may most closely approximate the type of experimental information that a firm may already have available at the time when a proposed merger is initially screened.

### 4.3 Description of Experimental Data

We summarize the data generated by our experiments in Table 4. Across our four treatments and 66 machines, we observe between 161-223 treated machine-weeks. In the untreated group, we observe 8,525 machine-weeks and more than 700,000 units sold. Each treatment week exposes around 2,700-3,500 individuals, of which around 134-274 would have purchased the focal product in an average week. Each treatment lasts 2.5-3 weeks, and between approximately 14,000-19,000 sales are recorded during the treated periods. The treated group consists of the 400-1,200 individuals who would have purchased the focal product had it been available for each treatment. In general, we see that the overall sales per-machine week are higher during the treatment period (between 83.3-89.4) than during the control period (82.2) <sup>31</sup>

This highlights one of the main challenges of measuring diversion experimentally: for the purposes of measuring the treatment effect, only individuals who would have purchased the focal product, had it been available, are considered “treated,” yet we must expose many more individuals to the product removal, knowing that many of them were not interested in the focal product in the first place.

A second challenge is that there is a large amount of variation in overall sales at the weekly level, independent of our product removals. This weekly variation in overall sales is common in many retail environments. We often observe week-over-week sales that vary by over 20%. This can be seen in Figure 2, which plots the overall sales of all machines from one of the sites in our sample on a weekly basis. In our particular setting, many of the product removals were implemented during the summer of 2007, which was a high-point in demand

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<sup>31</sup>The per-week sales can be a bit misleading because not all machines are measured in every week during the treatment period. This is because experiments have slightly different start dates at different client site locations. This leads to a somewhat liberal definition of “treatment week” as only one or two machines might be treated in the final week.

at several sites, most likely due to macroeconomic conditions.

We explore this relationship further in Table 5, where we report the average sales by week during both the treatment and control periods for key substitutes. The third column reports the quantile that the sales during the mean treatment week corresponds to in the distribution of control weeks. For example, during our Snicker’s removal experiment we recorded an average of 472.5 M&M Peanut sales per week. The average weekly sales of M&M Peanuts was 309.8 units during the control weeks and the treatment average was greater than recorded sales of M&M Peanut during any of our control weeks (100th percentile). Likewise, the overall average weekly sales (across all products) were 5,358 during the treated weeks compared to a control average of 4,892 which corresponded to the 74.4th percentile of the control distribution for total sales.

#### 4.4 A Simple Matching Estimator for Diversion

There are a number of challenges to constructing an estimate of the diversion ratio: (1) the overall size of the market/rate of consumer arrivals varies substantially over time including among treatment and control periods; (2) the set of substitute products may vary across locations/machines; and (3) holding fixed the market size, variation in product-level sales could imply that  $\Delta q_k < 0$  or  $\Delta q_k > |\Delta q_j|$ .

Consider the Wald-type estimator, where  $Z = 1$  denotes the removal of product  $j$ :<sup>32</sup>

$$\widehat{D}_{jk} = \frac{\widehat{\Delta q_k}}{|\widehat{\Delta q_j}|} = \frac{E[q_k|Z = 1] - E[q_k|Z = 0]}{|E[q_j|Z = 1] - E[q_j|Z = 0]|}$$

We want to adjust our calculation of the expectation to address problem (1) as documented in Table 5. In other words, we want to adjust our control group to account for the fact that (on average) the treated weeks represent the 74th percentile (rather than the mean) of the overall sales distribution. To be explicit about the problem, we introduce a covariate  $x$  (demand shock):

$$E[q_k|Z = z] = \int q_k(x, z) f(x|Z = z) dx$$

The problem is that  $f(x|Z = 1) \neq f(x|Z = 0)$ , the treated and control periods have

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<sup>32</sup>One advantage of using product removal experiments is that  $E[q_j|Z = 1] = 0$  by construction (consumers cannot purchase products that are unavailable). This also helps rule out one set of potential defiers. The second set of defiers, those that purchase  $k$  only when  $j$  is available are ruled out if  $j, k$  are substitutes rather than complements.

different distributions of covariates (demand shocks). The typical solution involves *matching* or *balancing*, where one re-weights observations in the control period using measure  $g(\cdot)$  so that  $f(x|Z=1) = g(x|Z=0)$  and then calculates the expectation  $E_g[q_k|Z=0]$  with respect to measure  $g$ .<sup>33</sup> For each treated week  $t$ , we can construct a set of matched control weeks within a neighborhood  $S(x_t)$ :

$$\Delta q_{k,t}(x_t) = q_{k,t}(x_t) - \frac{1}{|\{s \in S(x_t)\}|} \sum_{s \in S(x_t)} q_{k,s} \quad \text{with} \quad \Delta q_k = \sum_t \Delta q_{k,t}(x_t) \quad (11)$$

Our first assumption places some obvious restrictions on potential control weeks:<sup>34</sup>

**Assumption 1.** *For a machine-week observation to be included as a control for  $q_{k,t}$  it must: (a) have product  $k$  available; (b) be from the same vending machine; (c) not be included in any of our treatments.*

The remaining question is how to define  $S(x_t)$ , the neighborhood of “similar enough” matches. Abadie and Imbens (2006) consider  $k$ -nearest neighbors in the space of  $x_t$ .<sup>35</sup> Our design is complicated by the fact that we don’t directly observe the demand shock  $x_t$ . Instead, we derive weaker conditions that help to balance the treatment and control periods without observing  $x_t$  directly. Our next assumption is a weak implication of all products being substitutes for one another.

**Assumption 2.** *“Substitutes”: Removing product  $j$  can never increase the overall level of sales during a period, and cannot decrease sales by more than the sales of  $j$ .*

We implement Assumption 2 as follows. We let  $Q_t$  denote the sales of all products during the treated machine-week, and  $Q_s$  denote the overall sales of a potential control machine-week. Given a treated machine-week  $t$ , we look for the corresponding set of control periods which satisfy Assumptions 1 and further restrict them to satisfy Assumption 2:

$$\{s : Z_s = 0, Q_s - Q_t \in [0, q_{js}]\} \quad (12)$$

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<sup>33</sup>We omit discussion of the conditional independence assumption because we have randomized assignment of  $Z$ .

<sup>34</sup>The first assumption is required because otherwise  $q_{k,s}$  is not defined. The second is designed to prevent our procedure from introducing additional unobserved heterogeneity. By restricting potential controls to different weeks at the same machine, we attempt to control for unobserved machine-level heterogeneity.

<sup>35</sup>There are stronger assumptions we could make in order to implement a more traditional matching or balancing estimator in the spirit of Abadie and Imbens (2006). Suppose a third product  $k'$  was similarly affected by the demand shock  $x$  but we knew ex-ante that  $D_{jk'} = 0$ , we could match on similar sales levels of  $q_{k'}$ . For our vending example this might be using sales at a nearby soft drink machine to control for overall demand at the snack machine, or it might be using sales of chips to control for sales of candy bars.

The problem with a direct implementation of (12) is that periods with (unexpectedly) higher sales of the focal product  $q_{js}$  are more likely to be included as a control, which would understate the diversion ratio. We propose a slight modification of (12) which is unbiased. We replace  $q_{js}$  with  $\widehat{q}_{js} = E[q_{js}|Q_s, Z = 0]$ . An easy way to obtain the expectation is to run an OLS regression of  $q_{js}$  on  $Q_s$  using data only from untreated machine-weeks satisfying Assumption 1:

$$S_t \equiv \{s : Z_s = 0, Q_s^0 - Q_t^1 \in [0, \widehat{b}_0 + \widehat{b}_1 Q_s^0]\} \quad (13)$$

Thus (13) defines the set of control periods  $S_t$  which correspond to treatment period  $t$  under our assumptions. The economic implication of Assumption 2 is that the sum of the diversion ratios from  $j$  to all other products is between zero and one (for each  $t$ ):  $\sum_{k \neq j} D_{jk,t} \in [0, 100\%]$ .

We explore the implications of Assumptions 1 and 2 and report our estimates of  $\widehat{\Delta q_j}, \widehat{\Delta q_k}$  and  $\widehat{D_{jk}} = \frac{\widehat{\Delta q_k}}{\widehat{\Delta q_j}}$  in Table 6 for the Snickers removal experiment.<sup>36</sup> The table is broken up into two panes. Each pane displays the number of treated weeks for each substitute, the average number of control-weeks matched to each treatment week, and our estimates for  $\Delta q_j, \Delta q_k$  and  $D_{jk} = \frac{\Delta q_j}{\Delta q_k}$ . In both panes, there is a large amount of variation in the number of treatment-weeks (and hence focal product sales:  $\Delta q_j$ ) across substitute products. The main source of this variation is that not every machine stocks every product, for some substitutes we have over 180 treated machine-weeks, while for others we have fewer than 10. With the addition of Assumption 2, we reduce the # of control weeks per treated machine-week from 90-120 to 7-10. In some cases, Assumption 2 eliminates treated machine-weeks because it cannot find any matches though this effect is generally small (less than 10% of treated machine-weeks).

The addition of Assumption 2 also improves our estimates of the diversion ratio  $\widehat{D_{jk}} = \frac{\widehat{\Delta q_k}}{\widehat{\Delta q_j}}$  somewhat. For example, with only Assumption 1 diversion to the outside good is measured as  $D_{j0} = \frac{-982}{|-929|} = -106\%$ , with the addition of Assumption 2 this constrains the set of potential control weeks and we estimate  $D_{k0} = \frac{461}{|-920|} = 47.5\%$ . However, the matching estimator alone does not produce “reasonable” looking estimates of the diversion ratio. Nearly half of products exhibit negative diversion ratios, and in both panes diversion to the top 5 substitutes exceeds 200%, so that two products are purchased for every lost Snickers sale. In both panes, the “best substitute” is the *Consolidated Non-Chocolate Nestle*

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<sup>36</sup>For our other removals: M&M Peanut, Famous Amos Cookies, and Animal Crackers consult the Online Appendix.



*Candy* (Willy Wonka, Runts, etc.) and the second best substitute is *M&M Peanut*. M&M Peanut is available in nearly every machine and we estimate diversion ratios of 52.7% and 39.4% respectively; the treatment mean exceeds any of the weekly sales during the control period (recall Table 5). The *Consolidated Non-Chocolate Nestle Candy* is only stocked in two machines, and its “best substitute” status is driven by the small size of its sample  $D_{jk} = \frac{9.4}{|-10.5|} = 89.5\%$ .

We were able to address problem (1), variation in the overall level of demand. We were able to partially address problem (2) by restricting our sample to cases where the substitute  $k$  was available, though this lead to differentially sized treatment groups  $\Delta q_j$  for different substitutes. The matching estimator did not do much to address problem (3), the noise in our estimates of the diversion ratio caused by variance at the product level; nor does it guarantee that our estimates of diversion look “sensible.”

#### 4.5 A Nonparametric Bayesian Estimator

Now we ask: given our matched estimates of  $\widehat{\Delta q_j}$  and  $\widehat{\Delta q_k}$  can we construct a better estimate of  $D_{jk}$  than  $\frac{\widehat{\Delta q_k}}{\widehat{\Delta q_j}}$ ? At first pass, this may seem like a ridiculous idea. If  $D_{jk} \equiv \frac{\Delta q_k}{\Delta q_j}$ , how can there be a better estimate than  $\frac{\widehat{\Delta q_k}}{\widehat{\Delta q_j}}$ ? However, we may be willing to place *ex-ante* restrictions on the domain of  $D_{jk}$ , for example we might be willing to rule out negative diversion ratios or diversion ratios in excess of 100%. Likewise, there may be additional information in pooling estimates of diversion ratios across substitute products  $k$ . We consider two additional assumptions below:

**Assumption 3.** “Unit Interval”:  $D_{jk} \in [0, 1]$ .

$\Delta q_k | \Delta q_j, D_{jk} \sim \text{Bin}(n = \Delta q_j, p = D_{jk})$  and  $D_{jk} | \mu_{jk}, m_{jk} \sim \text{Beta}(\mu_{jk}, m_{jk})$ .

**Assumption 4.** “Unit Simplex”:  $D_{jk} \in [0, 1]$  and  $\sum_{\forall k} D_{jk} = 1$

$\Delta q_k | \Delta q_j, D_{jk} \sim \text{Bin}(n = \Delta q_j, p = D_{jk})$  and  $D_{jk} \sim \text{Dirichlet}(\mu_{j0}, \mu_{j1}, \dots, \mu_{jK}, m_{jk})$ .

Assumption 3 restricts  $D_{jk}$  to the unit interval, while Assumption 4 goes further and restricts the *vector*  $\mathbf{D}_j$  to the unit simplex. In order to impose this structure we take a nonparametric Bayes approach. It is *nonparametric* in the sense that when we observe  $\Delta q_j$  trials of treated individuals and  $\Delta q_k$  successes and are looking to estimate the probability of success  $p = D_{jk}$ , the binomial distribution is not a substantive restriction. Under Assumption 4, the Dirichlet prior restricts the sum of the diversion ratios (for all goods including the outside good):  $\sum_{\forall k} D_{jk} = 1$ . It is *nonparametric* in the sense that when there are  $K$  substitutes, there are  $K + 1$  data points and  $K + 1$  free parameters.

There are two ways to parametrize the Beta (and Dirichlet) distributions. In the traditional  $Beta(\beta_1, \beta_2)$  formulation  $\beta_1$  denotes the number of prior successes and  $\beta_2$  denotes the number of prior failures (observed before any experimental observations). Under the alternative formulation  $Beta(\mu, m)$ :  $\mu = \frac{\beta_1}{\beta_1 + \beta_2}$  denotes the prior mean and  $m$  denotes the number of “pseudo-observations”  $m = \beta_1 + \beta_2$ . We work with the latter formulation for both the Beta and Dirichlet distributions.<sup>37</sup> This formula makes it easy to express the posterior mean (under Assumption 3) as a *shrinkage estimator* which combines our prior information with our experimental data:

$$\widehat{D}_{jk} = \lambda \cdot \mu_{jk} + (1 - \lambda) \frac{\Delta q_k}{\Delta q_j}, \quad \lambda = \frac{m_{jk}}{m_{jk} + \Delta q_j} \quad (14)$$

Here  $\lambda$  tells us how much weight to put on our prior mean versus our experimental observations, and directly depends on how many “pseudo-observations” we observed from our prior before observing experimental outcomes. One reason this estimator is referred to as a “shrinkage” estimator, is because as  $\Delta q_j$  becomes smaller (and our experimental outcomes are less informative),  $\widehat{D}_{jk}$  is shrunk towards  $\mu_{jk}$  (from either direction). Thus, when our experiments provide lots of information about diversion from  $j$  to  $k$  we rely on the experimental outcomes, but when our experiments are less informative we rely more on our prior information.<sup>38</sup>

Under either Assumption 3 or 4, the remaining challenge is how to select  $\mu_{jk}$ . An uniform or uninformative prior might be to let  $\mu_{jk} = \frac{1}{K+1}$  where  $K$  is the number of substitutes. An informative prior centered on the plain IIA logit estimates would let  $\mu_{jk} = \frac{s_k}{1-s_j}$  so that (prior) Diversion is proportional to marketshares. The IIA logit prior is useful not because it is the best estimate of the diversion ratio absent experimental data, but rather because assuming diversion proportional to marketshare is commonplace among practitioners in the absence of better data.<sup>39</sup> An advantage of the shrinkage estimator is that it allows us to nest the parametric estimate of diversion currently used in practice and the experimental

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<sup>37</sup>The Dirichlet is a generalization of the Beta to the unit simplex. The mean parameters  $[\mu_0, \mu_1, \dots, \mu_k]$  form a unit simplex while  $m$  denotes the number of pseudo-observations.

<sup>38</sup>We cannot provide a similar closed-form characterization under Assumption 4. Though there is a conjugacy relationship between the Dirichlet and the Multinomial, there is no conjugacy relationship between the Dirichlet and the Binomial except under the special case where the same number of treated individuals  $\Delta q_j$  are observed for each substitute  $k$ . For additional discussion regarding prior distributions consult Appendix A.4.

<sup>39</sup>If we had estimates from a random coefficients demand model, we could use those estimates of the diversion ratio instead. However, we find that under Assumption 4 the choice of  $\mu_{jk}$  becomes irrelevant. We explore robustness to different priors (including uninformative priors) in Appendix A.4.

outcomes, depending on our choice of  $m$ . Generally speaking, a smaller  $m$  implies a *weaker prior* and more weight on the observed data.

When  $\mu_{jt}$  is chosen as a function of the same observed dataset (including from estimated demand parameters) this is a form of an *Empirical Bayes* estimator. The development of Empirical Bayes shrinkage is attributed to Morris (1983) and has been widely used in applied microeconomics to shrink outliers from a distribution of fixed effects in teacher value added<sup>40</sup> or hospital quality.<sup>41</sup>

## 4.6 Estimates of Diversion

For each of our four experiments, we report our estimates of the diversion ratios in Table 7. Along with the number of treated machine-weeks for each substitute, we report the estimates of  $\widehat{\Delta q_j}, \widehat{\Delta q_k}$  from our matching estimator under Assumptions 1+2. The next four columns report: the “naive” or “raw” diversion ratio  $\widehat{\Delta q_j}/\widehat{\Delta q_k}$ , the beta-binomial adjusted diversion ratio under Assumption 3 (with a weak and strong prior), and the “multinomial” version of the diversion ratio under Assumption 4. When we incorporate a prior distribution, we center the mean at the IIA logit estimates  $\mu_{jk} = \frac{s_k}{1-s_j}$ .<sup>42</sup> For each experimental treatment, we report the 12 products with the highest “raw” diversion ratio as well as the outside good.

For Twix, in the second row of Table 7,  $\Delta q_k = 289.6$  and  $\Delta q_j = -702.4$  based on the 134 machine-weeks in which Twix was available. This implies a raw diversion ratio  $D_{jk} = 41.2\%$ . In the same table, we observe substitution from Snickers to Non-Chocolate Nestle products with only 3 machine-weeks in our sample.<sup>43</sup> This leads to  $\Delta q_j = -10.5$  and  $\Delta q_k = 9.4$  for an implied diversion ratio of  $D_{jk} = 89.5\%$ . Examining these raw diversion numbers may lead one to conclude that Non-Chocolate Nestle products are a closer substitute for Snickers than Twix. However, we observe more than 70 times as much information about substitution to Twix as we do to Non-Chocolate Nestle products. When we apply Assumption 3 with a weak prior ( $m_{jk} = 64$  pseudo-observations, one for each potential substitute), we shrink the estimates of both the Non-Chocolate Nestle products ( $89.5 \rightarrow 12.4$ ) much more than

<sup>40</sup>Chetty, Friedman, and Rockoff (2014) and Kane and Staiger (2008)

<sup>41</sup>Chandra, Finkelstein, Sacarny, and Syverson (2013)

<sup>42</sup>For the Dirichlet we add an additional small (uniform)  $\frac{1.3}{K+1}$  term to the logit probabilities in order to bound some of the very small prior probabilities away from zero. Sampling from zero and near-zero probability events is challenging. Note: this is not required for the Beta distribution because Beta-Binomial conjugacy provides a closed form. Because the market size is unobserved, we normalize  $\mu_0 = 0.25$  for the outside good. Setting  $\mu_0 = 0.75$  gives nearly identical results though requires adding more (uniform) pseudo observations to bound the small probabilities away from zero. See Appendix A.4.

<sup>43</sup>Non-Chocolate Nestle products include Willy Wonka candies such as Tart-N-Tinys, Chewy Tart-N-Tinys, Mix-ups, Mini Shockers, and Chewy Runtts.

Twix (41.2  $\rightarrow$  37.9). When we increase the strength of the prior to  $m_{jk} = 300$  pseudo-observations, we observe even more shrinkage towards the prior mean (89.5  $\rightarrow$  3.1) and (41.2  $\rightarrow$  29.5) respectively.

When we include Assumption 4, we utilize an extremely weak prior with  $m = 3.05$  pseudo-observations, but we see substantial shrinkage in our estimates from the *adding up* or *simplex* constraint  $\sum_k D_{jk} = 1$  and the constraint that  $D_{jk'} \geq 0$  for all  $k'$ . We no longer balance large positive diversion to some substitutes with large negative diversion to other substitutes, because negative diversion is ruled out *ex-ante*. This leads to smaller diversion estimates for both Non-Chocolate Nestle (89.5  $\rightarrow$  0.7) and Twix (41.2  $\rightarrow$  15.9). Under Assumption 4, Non-Chocolate Nestle went from our “best” substitute, to hardly a substitute at all, while Twix remained the second best substitute (now behind M&M Peanut which had a similar “raw” diversion measure, but a larger treated group  $\Delta q_j = -954.3$  compared to  $\Delta q_j = -702.4$ ). The simplex restriction shrinks outside good diversion from 47.5  $\rightarrow$  23.1.

In Table 9, we report the posterior distribution of our preferred diversion estimates under Assumption 4 and the very weak prior  $m = 3.05$ . We find that in most cases the posterior distribution defines a relatively tight 95% *credible* or *posterior* interval, even when we have relatively few experimentally-treated individuals. On one hand this indicates our estimates are relatively precise and insensitive to the prior distribution.<sup>44</sup> On the other, it demonstrates the power of cross substitute restrictions in Assumption 4; even with a diffuse prior, and very little experimental data for some substitutes, the simplex is sufficient to pin down diversion ratios.

While Assumption 4 appears relatively innocuous (most researchers are likely willing to assume a multinomial discrete choice framework) because it is so powerful in pinning down the diversion ratio estimates, we should be a little cautious. The important empirical decision is determining what the appropriate set of products  $\mathcal{K}$  is, such that  $\sum_{k \in \mathcal{K}} D_{jk} = 1$ . If, for example, we were interested in a merger where product  $j$  acquired both  $(k, k')$  but  $(k, k')$  were always rotated for one another and never available at the same time, we might want to vary the set of products over which we sum  $D_{jk'}$  for each alternative:  $\mathcal{K}_k$ .<sup>45</sup>

One of the perceived benefits of using diversion ratios or UPP alone rather than full merger simulation is that it requires data only from the merging parties, and not from firms

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<sup>44</sup>We compare results with different priors under Assumption 4 in Appendix A.4.

<sup>45</sup>Conlon and Mortimer (2013a) show that assuming all products are always available introduces bias in structural parametric estimates of demand.

outside the merger.<sup>46</sup> The power of Assumption 4 indicates that measuring diversion to all substitute goods (rather than just  $k$ ) can substantially improve our estimates of  $D_{jk}$ .<sup>47</sup> This suggests that although we need only (quasi)-experimental removals (or second-choice data) for the focal products involved in the merger, we should attempt to measure substitution to all available substitutes if possible.

## 4.7 Merger Evaluation

An important remedy available to the antitrust agencies is that mergers can be approved conditional on some divestiture.<sup>48</sup> We can measure whether divesting a product during a merger reduces  $\sum_{k \in \mathcal{F}_k} D_{jk}$  below some critical threshold. In Table 10, we report diversion from a key product of the acquiring firm to all products of the target firm. We then propose a divestiture of a key substitute product controlled by the target and recompute the diversion ratio to all of the target’s products absent the divested product. In some circumstances, divestiture of one or two key products might alleviate concerns around a particular merger. In addition to diversion ratios, we report 95% credible intervals below in parentheses.

We examine a potential acquisition in which Kellogg’s (Pop-Tarts, Zoo Animal Crackers, Famous Amos Cookies, Cheez-it, Rice Krispie Treats) acquires Kraft’s snack food division (Oreos, Lorna Doone, Planters Peanuts, Cheese Nips, and other Nabisco products). We examine the effects on both of Kellogg’s major products (Zoo Animal Crackers and Famous Amos) of the Kraft acquisition. We find that the diversion ratio from Zoo Animal Crackers to all Kraft products is 5.80%, and the diversion of Chocolate Chip Famous Amos is 11.85%. Given the diversion ratios, both of these would need to demonstrate substantial cost synergies to justify the merger. However, if Kraft were to divest its Planter’s Peanut line, the diversion ratios drop to 3.36% and 3.09% respectively.

Likewise one could consider an acquisition by Mars (Snickers, M&M’s, Milky Way, Three Musketeers, Skittles) of Nestle’s US confections business (Butterfinger, Raisinets, assorted Willy Wonka fruit flavored candies). If one is worried about the price effects that the

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<sup>46</sup>The 2010 Horizontal Merger Guidelines include the phrase: *Diversion ratios between products sold by merging firms and those sold by non-merging firms have at most secondary predictive value.* We disagree with this statement in terms of statistical properties, rather than economic theory.

<sup>47</sup>In broad strokes, this phenomenon is well understood by statisticians. This is related to Stein’s Paradox which shows that pooling information improves the parameter estimates for the mean of the multivariate normal, or the broader class of James-Stein shrinkage estimators. See Efron and Morris (1975) and James and Stein (1961).

<sup>48</sup>Two recent examples are the divestiture of gate slots at specific airports in the American/USAirways merger, and divestiture of the entire U.S. Modelo business during the acquisition of its global activities by Anheuser-Busch InBev.

acquisition might have on Snickers or M&M Peanut (the two largest brands in the chocolate category) we find that diversion from those products to Nestle products is 5.71% and 6.30% respectively, but that if Nestle were to divest Butterfinger, the diversion ratios would drop to 1.26% and 4.51% respectively. Again, this might be enough to convince the antitrust authorities not to block a proposed acquisition.<sup>49</sup>

Our hope is that these examples highlight both the advantages of our approach (that it is easy to detect which mergers require further investigation and which divestitures to consider), but also some of the limitations. For example, we can look at the effect on Snickers or M&M Peanut that the acquisition of Butterfinger might have, but we cannot say anything about the likely effect on the prices of Butterfinger of a Mars acquisition without conducting that experiment as well. This suggests that we either need observational/quasi-experimental data on many different stockout events, or we need some *ex ante* idea of which products are likely to have larger price impacts of the merger in order to tailor our experiments. The second limitation, which is not a limitation of our approach but of the unilateral effects approach more generally, is that it ignores diversion to existing brands. In the Snickers experiment, more than half of consumers already substitute to another Mars product, yet this has no bearing on the analysis of a proposed merger with Nestle (though it might if we considered the price effects on Butterfinger). This highlights what is likely to be a more general pattern in the unilateral effects approach: when large brands acquire smaller brands, the likely concern is the price of the smaller brand.

## 5 Conclusion

The 2010 revision to the Horizontal Merger Guidelines de-emphasized market definition and traditional concentration measures such as HHI in favor of a unilateral effects approach. The key input to this approach is the diversion ratio, which measures how closely two products substitute for one another.

We show that the diversion ratio can be interpreted as the treatment effect of an experiment in which the price of one product is increased by some amount. An important characteristic of many retail settings is that category-level sales can be more variable than product-level market shares. In practice, this makes most experiments that consider small price changes under-powered. We also show that second-choice data arising from random-

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<sup>49</sup>While this kind of divestiture may sound less realistic than Kraft divesting the Planters Peanuts line, these kinds of agreements are actually commonplace in the confections industry. For example in the United States, Kit-Kat is a Hershey product, but outside the United States Kit-Kat is a Nestle product.

ized experiments, quasi-experiments (such as stockouts), or second-choice survey data, can be used to estimate an average diversion ratio, where the average is taken over all possible prices from the pre-merger price to the choke price. We derive conditions based on economic primitives such as the curvature of demand, whereby the average diversion ratio from second-choice data (ATE) is a good approximation for the MTE.

We explore the empirical properties of diversion ratios in two applications. In the first, we estimate the discrete-choice demand model from Nevo (2000). In the second, we analyze a randomized field experiment, in which we exogenously remove products from consumers' choice sets and measure the ATE directly.

We develop a simple method to recover the diversion ratio from data, which enables us to combine both experimental and quasi-experimental measures with structural estimates as prior information. A non-parametric Bayes shrinkage approach enables us to use prior information (or potentially structural estimates) when experimental measures are not available, or when they are imprecisely measured, and to rely on experimental measures when they are readily available. This facilitates the combination of both first- and second-choice consumer data. We show that these approaches are complements rather than substitutes, and we find benefits from measuring diversion not only between products involved in a proposed merger, but also from merging products to non-merging products.

Our hope is that this makes a well-developed set of quasi-experimental and treatment effects tools available and better understood to both researchers in industrial organization and antitrust practitioners. While the diversion ratio can be estimated in different ways, researchers should think carefully about (1) which treatment effect their experiment (or quasi-experiment) is actually identifying; and (2) what the identifying assumptions required for estimating a diversion ratio implicitly assume about the structure of demand.

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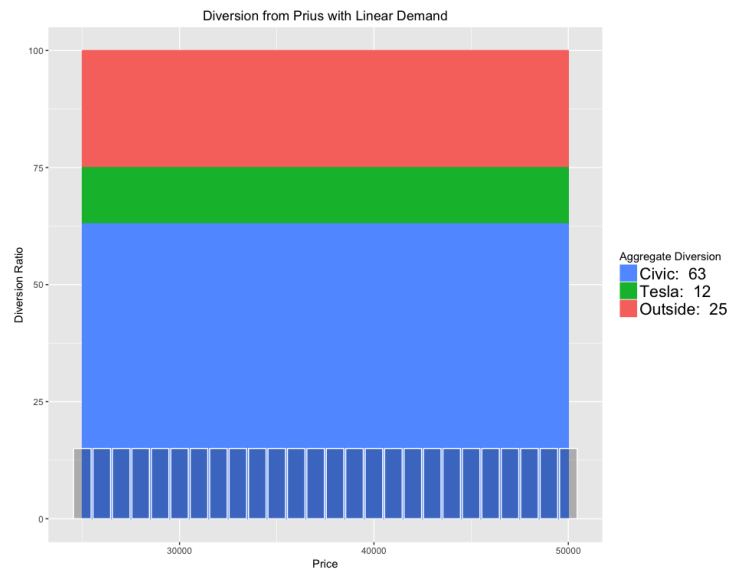
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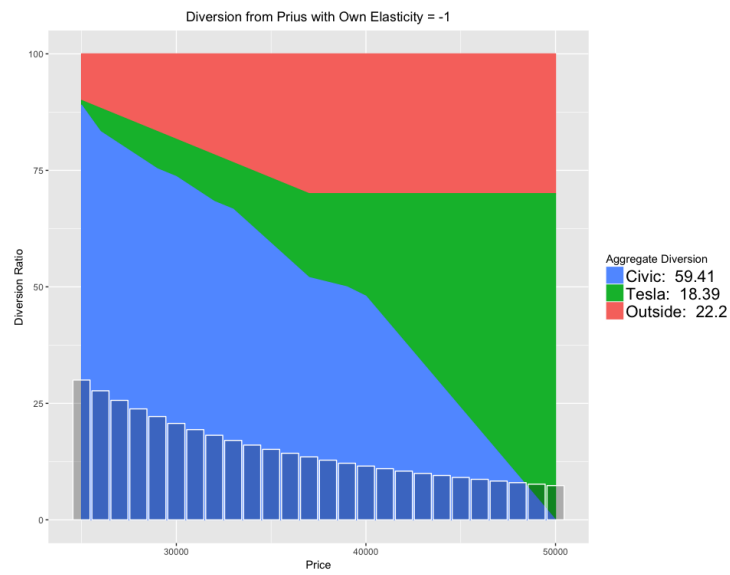
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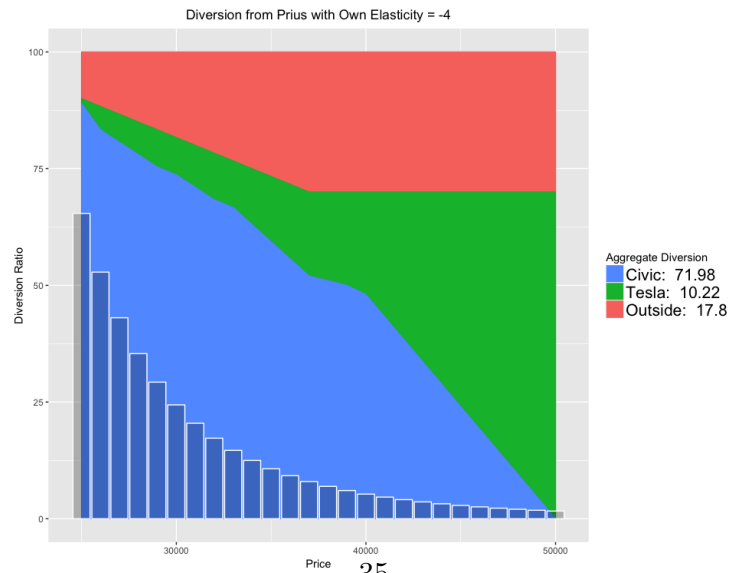
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(a) Linear Demand



(b) Inelastic CES Demand



(c) Elastic CES Demand

Figure 1: A Thought Experiment – Hypothetical Demand Curves for Toyota Prius

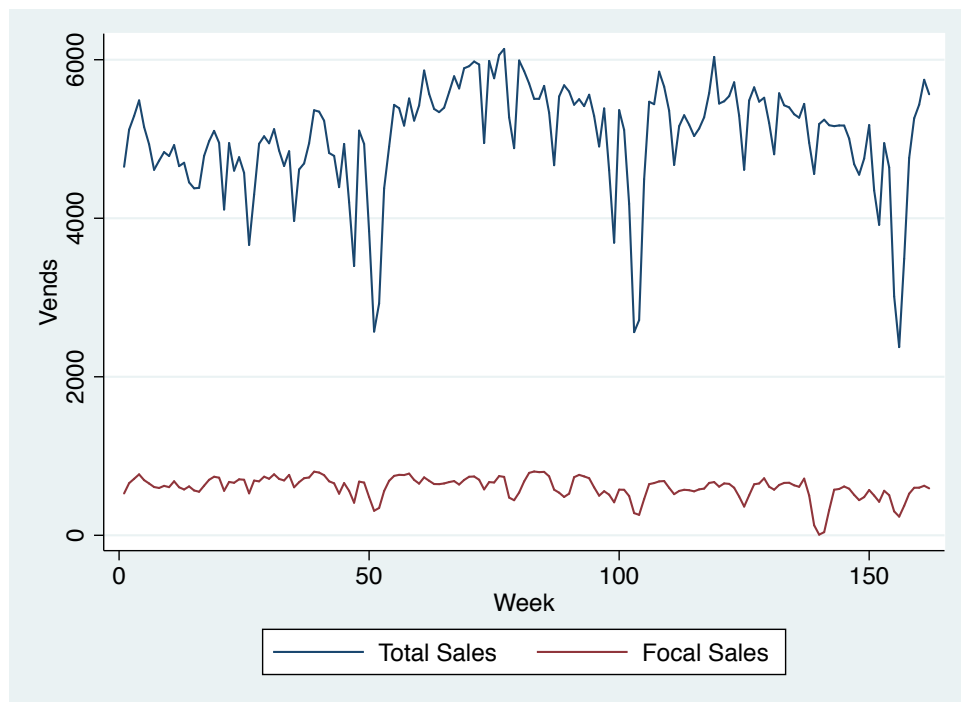


Figure 2: Total Overall Sales and Sales of Snickers and M&M Peanuts by Week

Manufacturer:	Category:			
	Salty Snack	Cookie	Confection	Total
PepsiCo	78.82	9.00	0.00	37.81
Mars	0.00	0.00	58.79	25.07
Hershey	0.00	0.00	30.40	12.96
Nestle	0.00	0.00	10.81	4.61
Kellogg's	7.75	76.94	0.00	11.78
Nabisco	0.00	14.06	0.00	1.49
General Mills	5.29	0.00	0.00	2.47
Snyder's	1.47	0.00	0.00	0.69
ConAgra	1.42	0.00	0.00	0.67
TGIFriday	5.25	0.00	0.00	2.46
Total	100.00	100.00	100.00	100.00
HHI	6332.02	6198.67	4497.54	2401.41

Table 3: Manufacturer Market Shares and HHI's by Category and Total

Source: IRM Brandshare FY 2006 and Frito-Lay Direct Sales For Vending Machines Data, Heartland Region, 50 best-selling products. ([http://www.vending.com/Vending\\_Affiliates/Pepsico/Heartland\\_Sales\\_Data](http://www.vending.com/Vending_Affiliates/Pepsico/Heartland_Sales_Data))

	Control Period <sup>†</sup>	Snickers	Zoo Animal Crackers	Famous Amos	M&M Peanut
# Machines	66	62	62	62	56
# Weeks	160	6	5	4	6
# Machine-Weeks	8,525	190	161	167	223
# Products	76	67	65	67	66
Total Sales	700,404.0	16,232.5	14,394.0	13,910.5	19,005.2
—Per Week	4,377.5	2,705.4	2,878.8	3,477.6	3,167.5
—Per Mach-Week	82.2	85.4	89.4	83.3	85.2
Total Focal Sales*		42,047.8	26,113.2	21,578.4	44,026.3
—Per Week		262.8	163.2	134.0	273.5
—Per Mach-Week		4.9	3.1	2.5	5.2

Table 4: Summary Statistics

<sup>†</sup> Numbers for Snickers removal. Summary statistics for other removals differ minimally because of different definition of the starting day of the week.

\* Focal sales during the control period. Focal sales during the treatment are close to zero. Any deviation from zero occurs because of the apportionment of service visit level sales to weekly sales.

Manufacturer	Product	Control Mean	Treatment Mean	Treatment Quantile
Snickers Removal				
Mars	M&M Peanut	309.8	472.5	100.0
Pepsi	Rold Gold (Con)	158.9	331.9	91.2
Mars	Twix Caramel	169.0	294.1	100.0
Pepsi	Cheeto LSS	248.6	260.7	61.6
Snyders	Snyders (Con)	210.2	241.6	52.8
Kellogg	Zoo Animal Cracker Austin	183.1	233.7	96.8
Kraft	Planters (Con)	161.1	218.8	96.0
	Total	4892.1	5357.9	74.4
Zoo Animal Crackers Removal				
Mars	M&M Peanut	309.7	420.3	99.2
Mars	Snickers	301.3	385.1	94.4
Pepsi	Rold Gold (Con)	158.9	342.4	92.0
Snyders	Snyders (Con)	210.3	263.0	67.2
Pepsi	Cheeto LSS	248.6	263.0	66.4
Mars	Twix Caramel	169.1	235.0	99.2
Pepsi	Baked Chips (Con)	169.6	219.7	89.6
	Total	4892.2	5608.6	89.6
Famous Amos Cookie Removal				
Mars	M&M Peanut	309.7	319.5	46.4
Mars	Snickers	301.2	316.6	52.0
Pepsi	Rold Gold (Con)	158.9	285.3	80.0
Pepsi	Cheeto LSS	248.7	260.7	64.8
Snyders	Snyders (Con)	210.1	236.4	52.8
Pepsi	Sun Chip LSS	150.2	225.5	100.0
Pepsi	Ruffles (Con)	206.9	218.3	62.4
	Total	4890.2	5262.4	64.0
M&M Peanut Removal				
Mars	Snickers	300.9	411.8	99.2
Snyders	Snyders (Con)	209.7	279.0	76.8
Pepsi	Rold Gold (Con)	158.9	276.9	80.8
Pepsi	Cheeto LSS	248.6	251.0	47.2
Mars	Twix Caramel	167.9	213.8	90.4
Kellogg	Zoo Animal Cracker Austin	182.6	198.0	65.6
Pepsi	Baked Chips (Con)	169.4	194.7	68.0
	Total	4886.1	5315.5	65.6

Table 5: Quantile of Average Treatment Period Sales in the Empirical Distribution of Control Period Sales.

Control Mean is the average number of sales of a given product (or all products) over all control weeks. Treatment Mean is the average number of sales of a given product (or all products) over all treatment weeks. A treatment week is any week in which at least one machine was treated. For client sites that were not treated during these weeks (because treatment occurs at slightly different dates at different sites), we use the average weekly sales for the client site when it was under treatment (otherwise we would be comparing treatment weeks with different number of treated machines in them). Treatment Quantile indicates in which quantile of the distribution of control-week sales the treatment mean places.

Manufacturer	Product	Assumption 1 Only					Assumption 1+2				
		Trt'd Mach- Weeks	Avg # Controls Per Trt	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k / \Delta q_j$ Raw Diversion	Trt'd Mach- Weeks	Avg # Controls Per Trt	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k / \Delta q_j$ Raw Diversion
Nestle	Nonchoc Nestle (Con)	6	80.3	14.1	-19.8	71.1	3	8.7	9.4	-10.5	89.5
Mars	M&M Peanut	186	120.3	482.4	-915.9	52.7	176	10.0	375.5	-954.3	39.4
Mars	Twix Caramel	143	120.3	339.6	-682.6	49.7	134	9.8	289.6	-702.4	41.2
Misc	Farleys (Con)	22	40.9	41.0	-121.2	33.8	18	4.6	14.9	-114.2	13.0
Hershey	Choc Herhsey (Con)	51	51.9	62.1	-210.0	29.6	41	8.8	29.8	-179.6	16.6
Mars	M&M Milk Chocolate	104	116.1	114.7	-454.6	25.2	97	10.6	71.8	-457.4	15.7
Pepsi	Rold Gold (Con)	186	82.8	215.5	-874.6	24.6	174	7.6	161.4	-900.1	17.9
Nestle	Butterfinger	63	95.5	78.8	-355.7	22.1	61	7.9	72.9	-362.8	20.1
Kraft	Planters (Con)	143	94.8	154.8	-708.0	21.9	136	7.9	78.0	-759.9	10.3
Kellogg	Rice Krispies Treats	20	93.8	15.9	-72.9	21.8	17	6.5	17.7	-66.5	26.7
Mars	Choc Mars (Con)	12	67.5	5.2	-34.7	14.9	11	16.2	6.4	-32.7	19.7
Hershey	Payday	2	84.0	1.4	-9.7	14.4	2	8.5	1.1	-9.8	10.9
Kellogg	Zoo Animal Cracker Austin	187	120.3	132.0	-923.6	14.3	177	9.5	65.7	-970.2	6.8
Kellogg	Choc SandFamous Amos	74	113.4	52.7	-369.9	14.2	69	10.0	33.9	-404.2	8.4
Hershey	Sour Patch Kids	34	124.9	17.0	-134.3	12.6	33	12.7	10.8	-152.9	7.1
Kellogg	Brown Sug Pop-Tarts	6	74.7	3.6	-30.4	11.8	6	8.2	2.3	-33.1	7.0
Pepsi	Sun Chip LSS	166	117.8	91.7	-814.5	11.3	159	9.1	45.3	-866.1	5.2
Sherwood	Ruger Wafer (Con)	162	82.7	80.9	-734.5	11.0	151	7.6	24.5	-778.0	3.1
Nestle	Choc Nestle (Con)	1	21.0	0.9	-9.3	9.2	0				
Kar's Nuts	Kar Sweet&Salty Mix 2oz	113	116.6	50.1	-565.7	8.8	104	8.9	27.6	-597.1	4.6
Kellogg	Choc Chip Famous Amos	190	119.0	81.8	-932.9	8.8	180	10.0	44.8	-971.8	4.6
Kraft	Fig Newton	6	77.0	2.1	-29.6	7.2	6	5.8	0.6	-31.3	2.0
Nestle	Raisinets	143	121.7	47.6	-678.8	7.0	133	10.0	11.6	-697.3	1.7
Pepsi	FritoLay (Con)	113	94.9	32.7	-507.0	6.4	104	9.7	16.8	-515.7	3.3
Pepsi	Baked Chips (Con)	176	113.5	49.5	-883.5	5.6	166	10.1	33.5	-911.7	3.7
Misc	Farleys Mixed Fruit Snacks	137	93.3	34.9	-666.8	5.2	129	7.2	13.0	-686.5	1.9
Pepsi	Dorito Blazin Buffalo Ranch LSS	95	57.6	20.0	-494.0	4.0	87	5.2	-27.6	-503.1	-5.5
Mars	Combos (Con)	132	78.2	27.5	-682.6	4.0	119	6.6	7.6	-663.6	1.2
Kellogg	Cheez-It Original SS	159	119.6	25.3	-794.1	3.2	150	10.4	2.1	-819.9	0.3
Mars	Starburst Original	31	108.5	4.2	-138.7	3.0	29	11.6	-1.7	-137.6	-1.2
Pepsi	Cheeto LSS	187	120.3	27.0	-918.7	2.9	177	10.0	-46.2	-957.4	-4.8
Mars	Marathon Chewy Peanut	7	83.0	0.9	-42.0	2.1	6	6.5	-5.0	-50.4	-9.9
Misc	BroKan (Con)	3	43.0	0.0	-0.2	1.5	3	42.0	0.0	0.0	
Kraft	Cherry Fruit Snacks	71	123.1	5.3	-398.1	1.3	68	9.3	-5.3	-419.3	-1.3
Misc	Popcorn (Con)	77	113.9	1.5	-387.1	0.4	76	9.8	-19.8	-425.2	-4.6
Snyders	Snyders (Con)	145	104.7	0.6	-630.6	0.1	137	9.2	-76.6	-668.6	-11.5
Misc	Rasbry Knotts	147	109.4	-1.8	-736.1	-0.2	136	9.3	-4.5	-727.7	-0.6
Pepsi	Ruffles (Con)	156	124.4	-2.9	-774.1	-0.4	148	10.4	-42.2	-794.9	-5.3
Kraft	Lorna Doone Shortbread Cookies	43	123.6	-0.8	-197.8	-0.4	41	11.3	-4.6	-202.3	-2.3
Misc	Other Pastry (Con)	4	91.0	-0.1	-17.0	-0.5	3	8.7	-0.1	-12.8	-0.6
Pepsi	Quaker Strwbry Oat Bar	44	78.2	-1.3	-186.6	-0.7	39	9.6	-7.3	-174.0	-4.2



Manufacturer	Product	Assumption 1 Only					Assumption 1+2				
		Trt'd Mach- Weeks	Avg # Controls Per Trt	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k / \Delta q_j$ Raw Diversion	Trt'd Mach- Weeks	Avg # Controls Per Trt	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k / \Delta q_j$ Raw Diversion
Kellogg	Strwbry Pop-Tarts	162	118.1	-6.0	-792.7	-0.8	154	9.9	-40.5	-819.4	-4.9
General Mills	Nature Valley Swt&Salty Alm	49	107.0	-2.3	-214.8	-1.1	43	9.6	-42.4	-195.3	-21.7
Pepsi	Chs PB Frito Cracker	48	95.0	-2.7	-220.5	-1.2	45	9.0	-6.4	-227.9	-2.8
Kraft	Ritz Bits Chs Vend	74	127.4	-5.3	-404.9	-1.3	71	9.4	0.2	-424.0	0.0
Mars	Nonchoc Mars (Con)	35	108.1	-2.1	-154.3	-1.3	31	13.1	1.0	-134.8	0.7
Kar's Nuts	KarNuts (Con)	40	99.3	-2.6	-183.8	-1.4	35	8.0	-27.7	-188.4	-14.7
Kraft	100 Cal Chse Nips Crisps	20	93.8	-1.1	-72.9	-1.5	17	6.5	-6.3	-66.5	-9.4
Pepsi	Smartfood LSS	67	125.5	-7.8	-365.3	-2.1	65	9.2	-25.0	-388.2	-6.4
Kellogg	Cherry Pop-Tarts	28	87.9	-3.0	-125.4	-2.4	28	7.5	2.4	-155.4	1.6
Mars	Milky Way	11	94.8	-1.4	-42.4	-3.3	9	4.6	-0.5	-37.9	-1.4
Pepsi	Dorito Nacho LSS	190	119.7	-37.2	-928.3	-4.0	180	10.0	-57.9	-969.1	-6.0
Misc	Hostess Pastry	16	114.4	-3.2	-76.6	-4.1	15	15.9	-11.7	-78.7	-14.8
Pepsi	Cheetos Flaming Hot LSS	69	124.8	-15.4	-371.5	-4.1	66	9.1	-22.3	-372.9	-6.0
Pepsi	Grandmas Choc Chip	119	114.6	-29.9	-589.7	-5.1	111	9.8	-36.3	-580.7	-6.3
Kraft	100 Cal Oreo Thin Crisps	23	94.0	-4.2	-75.3	-5.6	20	11.9	1.2	-66.5	1.7
Mars	Skittles Original	132	122.9	-37.8	-650.9	-5.8	125	9.7	-49.0	-672.5	-7.3
Misc	Cliff (Con)	4	32.0	-1.6	-22.9	-6.9	4	3.0	-1.6	-24.7	-6.6
Snyders	Jays (Con)	161	98.0	-58.3	-775.8	-7.5	150	8.6	-87.8	-809.4	-10.8
Pepsi	Frito LSS	154	106.0	-69.5	-749.8	-9.3	144	9.4	-84.4	-798.1	-10.6
General Mills	Oat n Honey Granola Bar	37	118.2	-24.9	-204.4	-12.2	36	9.0	-29.7	-197.1	-15.1
Misc	Salty Other (Con)	31	115.3	-18.8	-147.3	-12.8	30	12.5	-11.9	-163.8	-7.3
Pepsi	Lays Potato Chips 1oz SS	155	64.9	-96.2	-713.7	-13.5	143	5.5	-112.5	-744.1	-15.1
Misc	Salty United (Con)	11	76.5	-6.0	-30.1	-20.0	9	16.7	-9.6	-26.1	-36.8
Mars	3-Musketeers	3	52.0	-2.9	-8.3	-35.4	2	11.0	0.0	0.0	
Hershey	Twizzlers	55	53.9	-83.4	-216.4	-38.5	46	7.8	-75.6	-192.8	-39.2
	Outside Good	190	120.5	-982.6	-929.3	-105.7	180	10.0	460.9	-970.2	47.5

Table 6: Simple Matching Estimator (with and without Assumption 2)  
(Snickers Removal)

Assumption 1 restricts control machine-weeks to: the same machine, requires that  $k$  is available, and that control machine-weeks were not in any treatment.

Assumption 2 requires that removing a product cannot increase total sales during a period, and cannot decrease total sales by more than the expected sales of the removed product)

Trt'd Mach-Weeks shows the number of treated machine-weeks for which there was at least one control machine-week. Avg # Controls Per Trt is the average number of control machine-weeks per treatment machine-week over all treatment machine-weeks.

$\Delta q_k$  shows the change in substitute product sales from the control to the treatment period, while  $\Delta q_j$  Focal Sales shows the analogous change for focal product sales.

Manufacturer	Product	Treated Machine Weeks	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k/ \Delta q_j $ Diversio n	w/ Assn 3 Diversio n ( $m = K$ )	w/ Assn 3 Diversio n ( $m = 300$ )	w/ Assn 4 Diversio n ( $m = 3.3$ )
Snickers Removal								
Nestle	Nonchoc Nestle (Con)	3	9.4	-10.5	89.5	12.4	3.1	0.7
Mars	Twix Caramel	134	289.6	-702.4	41.2	37.9	29.5	15.9
Mars	M&M Peanut	176	375.5	-954.3	39.4	37.0	30.8	18.4
Kellogg	Rice Krispies Treats	17	17.7	-66.5	26.7	13.5	5.0	1.3
Nestle	Butterfinger	61	72.9	-362.8	20.1	17.1	11.2	4.5
Mars	Choc Mars (Con)	11	6.4	-32.7	19.7	6.5	2.0	0.4
Pepsi	Rold Gold (Con)	174	161.4	-900.1	17.9	16.8	13.9	7.5
Hershey	Choc Herhsey (Con)	41	29.8	-179.6	16.6	12.2	6.3	2.0
Mars	M&M Milk Chocolate	97	71.8	-457.4	15.7	13.8	9.8	4.1
Misc	Farleys (Con)	18	14.9	-114.2	13.0	8.3	3.7	1.0
Hershey	Payday	2	1.1	-9.8	10.9	1.4	0.4	0.1
Kraft	Planters (Con)	136	78.0	-759.9	10.3	9.6	7.8	3.8
	Outside Good	180	460.9	-970.2	47.5			23.1
Zoo Animal Crackers Removal								
Hershey	Payday	2	0.4	-0.4	84.7	0.6	0.1	
Kellogg	Rice Krispies Treats	13	23.5	-37.8	62.2	23.2	7.2	3.0
Misc	Salty United (Con)	6	10.4	-18.9	55.1	12.6	3.4	1.3
Kraft	100 Cal Oreo Thin Crisps	13	14.9	-37.8	39.4	14.7	4.5	1.8
Pepsi	Rold Gold (Con)	132	114.4	-440.8	25.9	22.9	16.2	9.9
Hershey	Choc Herhsey (Con)	30	33.6	-132.6	25.3	17.1	7.9	3.8
Misc	Hostess Pastry	11	14.7	-62.2	23.7	11.8	4.4	1.8
Kraft	100 Cal Chse Nips Crisps	13	8.7	-37.8	23.1	8.6	2.6	1.1
Mars	Milky Way	9	7.0	-30.8	22.6	7.5	2.2	0.9
Mars	Snickers	145	92.4	-483.6	19.1	17.3	13.0	7.6
Mars	M&M Peanut	142	77.7	-469.4	16.6	15.0	11.4	6.5
Mars	Twix Caramel	110	50.2	-339.0	14.8	12.7	8.7	4.6
	Outside Good	145	240.5	-482.9	49.8			22.0
Famous Amos Cookie Removal								
Nestle	Choc Nestle (Con)	1	0.8	-0.3	300.0	1.2	0.3	
Hershey	Choc Herhsey (Con)	38	48.6	-66.8	72.7	36.9	13.4	7.2
Kraft	100 Cal Oreo Thin Crisps	29	20.7	-43.3	47.9	19.2	6.1	3.1
Pepsi	Sun Chip LSS	139	143.6	-355.7	40.4	34.4	22.7	15.7
Hershey	Payday	2	2.6	6.8	38.9			
Misc	Salty United (Con)	18	9.9	-28.7	34.6	10.7	3.1	1.5
Pepsi	Chs PB Frito Cracker	34	26.9	-83.6	32.1	18.2	7.1	3.7
Kraft	Planters (Con)	121	82.1	-332.6	24.7	20.9	13.7	8.8
Kellogg	Choc SandFamous Amos	57	28.0	-122.0	22.9	15.1	6.8	3.7
Mars	Milky Way	26	13.9	-71.6	19.5	10.3	3.9	1.9
Pepsi	Dorito Blazin Buffalo Ranch LSS	72	38.1	-224.2	17.0	13.3	7.5	4.4
Pepsi	Frito LSS	119	49.9	-313.2	15.9	13.4	8.9	5.3
	Outside Good	156	192.9	-399.1	48.3			21.0

Manufacturer	Product	Treated Machine Weeks	$\Delta q_k$ Subst Sales	$\Delta q_j$ Focal Sales	$\Delta q_k/ \Delta q_j $ Diversio	w/ Assn 3 Diversio ( $m = K$ )	w/ Assn 3 Diversio ( $m = 300$ )	w/ Assn 4 Diversio ( $m = 3.3$ )
M&M Peanut Removal								
Misc	Hostess Pastry	11	12.5	-38.6	32.5	12.3	4.0	1.8
Mars	Snickers	218	296.6	-1239.3	23.9	22.9	19.9	16.5
Kellogg	Brown Sug Pop-Tarts	10	10.0	-43.5	22.9	9.2	2.9	1.4
Misc	Cliff (Con)	1	0.4	-1.8	22.2	0.6	0.1	0.0
Nestle	Nonchoc Nestle (Con)	1	0.9	-4.6	19.5	1.3	0.3	0.2
Mars	M&M Milk Chocolate	99	73.5	-529.6	13.9	12.5	9.2	6.3
Mars	Twix Caramel	176	110.9	-1014.3	10.9	10.4	8.9	6.8
Kellogg	Rice Krispies Treats	46	22.4	-220.2	10.2	7.9	4.4	2.5
Hershey	Twizzlers	62	33.0	-333.0	9.9	8.3	5.3	3.4
Hershey	Choc Herhsey (Con)	32	15.7	-160.0	9.8	7.0	3.5	1.9
Kellogg	Cherry Pop-Tarts	25	12.5	-160.3	7.8	5.6	2.8	1.6
Mars	Nonchoc Mars (Con)	45	14.6	-201.3	7.3	5.5	3.0	1.7
	Outside Good	218	606.2	-1238.5	48.9			36.3

Table 7: Raw and Bayesian Diversion Ratios.

Treated Machine Weeks shows the number of treated machine-weeks for which there was at least one control machine-week.  $\Delta q_k$  Subst Sales shows the change in substitute product sales from the control to the treatment period, while  $\Delta q_j$  Focal Sales shows the analogous change for focal product sales.  $\Delta q_j/|\Delta q_j|$  Diversio is the ratio of the change in substitute product sales to the absolute value of the change in focal product sales.

Beta-Binomial diversion ratios calculated under Assumptions 1, 2 (Substitutes), and 3 (Unit Interval). The weak prior uses the number of products in the choice set during the treatment period, which varies from  $m = 64 - 66$  as the number of pseudo-observations. The strong prior uses  $m = 300$  pseudo-observations.

The final column utilizes Assumptions 1, 2 and 4 with the Dirichlet prior and  $m = 3.3$  pseudo-observations.

The products included in this table are the 12 products with highest raw diversion ratio.

Manuf	Product	$\Delta$ Focal Sales	No Prior	Beta-Bin Diversion $m = J^\dagger$	Beta-Bin Diversion $m = 150$	Beta-Bin Diversion $m = 300$	Beta-Bin Diversion $m = 600$
Snickers Removal							
Nestle	Nonchoc Nestle (Con)	-10.5	89.5	12.4	5.9	3.1	1.6
Mars	Twix Caramel	-702.4	41.2	37.9	34.3	29.5	23.2
Mars	M&M Peanut	-954.3	39.4	37.0	34.5	30.8	25.5
Kellogg	Rice Krispies Treats	-66.5	26.7	13.5	8.4	5.0	2.9
Nestle	Butterfinger	-362.8	20.1	17.1	14.3	11.2	7.8
Mars	Choc Mars (Con)	-32.7	19.7	6.5	3.5	2.0	1.0
Pepsi	Rold Gold (Con)	-900.1	17.9	16.8	15.7	13.9	11.6
Hershey	Choc Herhsey (Con)	-179.6	16.6	12.2	9.1	6.3	3.9
Zoo Animal Crackers Removal							
Hershey	Payday	-0.4	84.7	0.6	0.3	0.1	0.1
Kellogg	Rice Krispies Treats	-37.8	62.2	23.2	12.7	7.2	3.9
Misc	Salty United (Con)	-18.9	55.1	12.6	6.3	3.4	1.8
Kraft	100 Cal Oreo Thin Crisps	-37.8	39.4	14.7	8.0	4.5	2.4
Pepsi	Rold Gold (Con)	-440.8	25.9	22.9	19.8	16.2	12.1
Hershey	Choc Herhsey (Con)	-132.6	25.3	17.1	12.0	7.9	4.7
Misc	Hostess Pastry	-62.2	23.7	11.8	7.2	4.4	2.5
Kraft	100 Cal Chse Nips Crisps	-37.8	23.1	8.6	4.7	2.6	1.4
Famous Amos Cookie Removal							
Nestle	Choc Nestle (Con)	-0.2	300.0	1.2	0.6	0.3	0.2
Hershey	Choc Herhsey (Con)	-66.8	72.7	36.9	22.5	13.4	7.4
Kraft	100 Cal Oreo Thin Crisps	-43.3	47.9	19.2	10.8	6.1	3.3
Pepsi	Sun Chip LSS	-355.7	40.4	34.4	28.9	22.7	16.1
Hershey	Payday	6.8	38.9				
Misc	Salty United (Con)	-28.7	34.6	10.7	5.6	3.1	1.7
Pepsi	Chs PB Frito Cracker	-83.6	32.1	18.2	11.6	7.1	4.1
Kraft	Planters (Con)	-332.6	24.7	20.9	17.5	13.7	9.8
M&M Peanut Removal							
Misc	Hostess Pastry	-38.6	32.5	12.3	6.9	4.0	2.3
Mars	Snickers	-1239.3	23.9	22.9	21.7	19.9	17.2
Kellogg	Brown Sug Pop-Tarts	-43.5	22.9	9.2	5.2	2.9	1.6
Misc	Cliff (Con)	-1.8	22.2	0.6	0.3	0.1	0.1
Nestle	Nonchoc Nestle (Con)	-4.6	19.5	1.3	0.6	0.3	0.2
Mars	M&M Milk Chocolate	-529.6	13.9	12.5	11.0	9.2	7.0
Mars	Twix Caramel	-1014.3	10.9	10.4	9.8	8.9	7.6
Kellogg	Rice Krispies Treats	-220.2	10.2	7.9	6.1	4.4	2.9

Table 8: Sensitivity of Beta-Binomial Diversion to Number of Pseudo Observations

<sup>†</sup> Number of pseudo observations is the number of products in the choice set during treatment period - 66, 64, 65, and 65, respectively.

$\Delta$  Focal Sales shows the change in focal product sales from the control to the treatment period. No Prior is the raw diversion calculated as the ratio of the change in substitute product sales to the absolute value of the change in focal product sales.

Beta-Bin Diversion is the diversion ratio calculated under Assumptions 1,2, and 3 (Unit Interval), using different number of pseudo-observations.

The products included in this table are the 8 products with highest raw diversion ratio.

Manuf	Product	Mean	2.5 <sup>th</sup> Quantile	25 <sup>th</sup> Quantile	50 <sup>th</sup> Quantile	75 <sup>th</sup> Quantile	97.5 <sup>th</sup> Quantile
Snickers Removal							
Nestle	Nonchoc Nestle (Con)	0.67	0.31	0.51	0.65	0.81	1.17
Mars	Twix Caramel	15.88	14.28	15.32	15.88	16.45	17.53
Mars	M&M Peanut	18.40	16.79	17.83	18.39	18.95	20.02
Kellogg	Rice Krispies Treats	1.30	0.78	1.09	1.28	1.49	1.95
Nestle	Butterfinger	4.45	3.53	4.10	4.43	4.78	5.48
Mars	Choc Mars (Con)	0.44	0.16	0.31	0.42	0.55	0.85
Pepsi	Rold Gold (Con)	7.54	6.49	7.15	7.53	7.92	8.69
	Outside Good	23.12	21.34	22.50	23.11	23.73	24.91
Zoo Animal Crackers Removal							
Kellogg	Rice Krispies Treats	2.99	1.93	2.56	2.95	3.36	4.28
Misc	Salty United (Con)	1.25	0.61	0.97	1.21	1.49	2.12
Kraft	100 Cal Oreo Thin Crisps	1.85	1.04	1.51	1.81	2.14	2.88
Pepsi	Rold Gold (Con)	9.89	8.24	9.30	9.88	10.46	11.66
Hershey	Choc Herhsey (Con)	3.81	2.66	3.35	3.77	4.22	5.17
Misc	Hostess Pastry	1.80	1.02	1.47	1.76	2.08	2.79
Kraft	100 Cal Chse Nips Crisps	1.10	0.51	0.83	1.06	1.32	1.91
	Outside Good	21.98	19.64	21.15	21.96	22.78	24.43
Famous Amos Cookie Removal							
Hershey	Choc Herhsey (Con)	7.18	5.38	6.49	7.14	7.83	9.21
Kraft	100 Cal Oreo Thin Crisps	3.05	1.90	2.59	3.01	3.47	4.47
Pepsi	Sun Chip LSS	15.75	13.53	14.94	15.72	16.52	18.11
Misc	Salty United (Con)	1.47	0.70	1.13	1.42	1.75	2.49
Pepsi	Chs PB Frito Cracker	3.74	2.51	3.25	3.70	4.19	5.21
Kraft	Planters (Con)	8.75	7.04	8.13	8.72	9.35	10.64
Kellogg	Choc SandFamous Amos	3.69	2.47	3.21	3.65	4.12	5.15
	Outside Good	20.95	18.43	20.05	20.94	21.83	23.57
M&M Peanut Removal							
Misc	Hostess Pastry	1.85	1.00	1.49	1.80	2.17	2.95
Mars	Snickers	16.47	14.83	15.89	16.46	17.04	18.15
Kellogg	Brown Sug Pop-Tarts	1.41	0.69	1.10	1.37	1.68	2.39
Misc	Cliff (Con)	0.00	0.00	0.00	0.00	0.00	0.03
Nestle	Nonchoc Nestle (Con)	0.15	0.00	0.05	0.11	0.21	0.54
Mars	M&M Milk Chocolate	6.26	4.96	5.78	6.25	6.73	7.68
Mars	Twix Caramel	6.76	5.60	6.34	6.74	7.16	7.99
	Outside Good	36.35	34.21	35.61	36.34	37.09	38.47

Table 9: Posterior Distribution of Dirichlet  $\alpha_{jk} = \frac{s_j}{1-s_j} + \frac{1.3}{K+1}$ ,  $m_{jk} = 3.3$

The products included in this table are the 7 products with highest raw diversion ratio.

Proposed Merger	Diversion Direction	Diversion Ratio	Proposed Divestiture	Diversion Ratio Under Divestiture
Mars & Hershey	Snickers to Hershey	2.83 (2.05, 3.73)	Reese's Peanut Butter Cups	2.83* (2.05, 3.73)
	M&M Peanut to Hershey	7.14 (5.63, 8.80)	Reese's Peanut Butter Cups	5.30 (3.98, 6.79)
Mars & Kraft	Snickers to Kraft	3.97 (3.16, 4.84)	Planters Peanuts	0.15 (0.02, 0.41)
	M&M Peanut to Kraft	4.22 (3.26, 5.29)	Planters Peanuts	0.62 (0.21, 1.25)
Mars & Nestle	Snickers to Nestle	5.72 (4.67, 6.88)	Butterfinger	1.27 (0.78, 1.86)
	M&M Peanut to Nestle	6.32 (5.13, 7.59)	Butterfinger	4.52 (3.56, 5.58)
Mars & Kellogg's	Snickers to Kellogg's	8.56 (7.34, 9.86)	Famous Amos Cookies <sup>†</sup>	4.60 (3.69, 5.58)
	M&M Peanut to Kellogg's	5.67 (4.24, 7.30)	Famous Amos Cookies <sup>†</sup>	5.50 (4.08, 7.13)
	Zoo Animal Crackers to Mars	21.78 (19.43, 24.23)	Famous Amos Cookies <sup>†</sup>	21.78 (19.43, 24.23)
Kellogg's & Kraft	Zoo Animal Crackers to Kraft	5.81 (4.41, 7.37)	Planters Peanuts	3.38 (2.27, 4.68)
	Choc Chip Famous Amos to Kraft	11.82 (9.77, 14.05)	Planters Peanuts	3.07 (1.91, 4.48)

Table 10: Hypothetical Mergers with Forced Divestitures

Note: 95% equal-tail credible intervals shown in parentheses.

\* Reese's Peanut Butter Cups are unavailable in all treatment weeks for this experiment.

<sup>†</sup> Divestiture of both "Choc Chip Famous Amos" and "Choc SandFamous Amos".

For upward pricing pressure not to be positive under the assumptions that  $p = 0.45$  and  $c = 0.15$ , marginal cost reductions must be at least twice as large as the diversion estimates.

# A Appendix:

## A.1 Diversion Under Parametric Demands

This section derives explicit formulas for the diversion ratio under common parametric forms for demand. The focus is whether or not a demand model implies that the diversion ratio is constant with respect to the magnitude of the price increase. It turns out that the IIA Logit and the Linear demand model exhibit this property, while the log-linear model, and mixed logit model do not necessarily exhibit this property. We go through several derivations below:

### Linear Demand

The diversion ratio under linear demand has the property that it does not depend on the magnitude of the price increase. To see this consider that the linear demand is given by:

$$Q_k = \alpha_k + \sum_j \beta_{kj} p_j.$$

This implies a diversion ratio corresponding to a change in price  $p_j$  of  $\Delta p_j$ :

$$D_{jk} = \frac{\Delta Q_k}{\Delta Q_j} = \frac{\beta_{kj} \Delta p_j}{\beta_{jj} \Delta p_j} = \frac{\beta_{kj}}{\beta_{jj}} \quad (\text{A.15})$$

This means that for any change in  $p_j$  from an infinitesimal price increase, up to the choke price of  $j$ ; the diversion ratio,  $D_{jk}$  is constant. This also implies that under linear demand, divergence is a global property. Any magnitude of price increase evaluated at any initial set of prices and quantities, will result in the same measure of diversion.

### Log-Linear Demand

The log-linear demand model does not exhibit constant diversion with respect to the magnitude of the price increase. The log-linear model is specified as:

$$\ln(Q_k) = \alpha_k + \sum_j \varepsilon_{kj} \ln(p_j)$$

If we consider a small price increase  $\Delta p_j$  the diversion ratio becomes:

$$\begin{aligned} \frac{\Delta \log(Q_k)}{\Delta \log(Q_j)} &\approx \underbrace{\frac{\Delta Q_k}{\Delta Q_j}}_{D_{jk}} \cdot \frac{Q_j(\mathbf{p})}{Q_k(\mathbf{p})} = \frac{\varepsilon_{kj} \Delta \log(p_j)}{\varepsilon_{jj} \Delta \log(p_j)} = \frac{\varepsilon_{kj}}{\varepsilon_{jj}} \\ D_{jk} &\approx \frac{Q_k(\mathbf{p})}{Q_j(\mathbf{p})} \cdot \frac{\varepsilon_{kj}}{\varepsilon_{jj}} \end{aligned} \quad (\text{A.16})$$

This holds for small changes in  $p_j$ . However for larger changes in  $p_j$  we can no longer use the simplification that  $\Delta \log(Q_j) \approx \frac{\Delta Q_j}{Q_j}$ . So for a large price increase (such as to the choke

price  $p_j \rightarrow \infty$ ), log-linear demand can exhibit diversion that depends on the magnitude of the price increase.

## IIA Logit Demand

The plain logit model exhibits IIA and proportional substitution. This implies that the diversion ratio does not depend on the magnitude of the price increase. Here we consider two price increases, an infinitesimal one and an increase to the choke price  $p_j \rightarrow \infty$ .

Consider the derivation of the diversion ratio  $D_{jk}$  under simple IIA logit demands. We have utilities and choice probabilities given by the well known equations, where  $a_t$  denotes the set of products available in market  $t$ :

$$u_{ijt} = \underbrace{x_{jt}\beta - \alpha p_{jt}}_{\tilde{v}_{jt}} + \varepsilon_{ijt}$$

$$S_{jt} = \frac{\exp[\tilde{v}_{jt}]}{1 + \sum_{k \in a_t} \exp[\tilde{v}_{kt}]} \equiv \frac{V_{jt}}{IV(a_t)}$$

Under logit demand, an infinitesimal price change in  $p_j$  exhibits identical diversion to setting  $p_j \rightarrow \infty$  (the choke price). For an infinitesimally small price change,

$$\widehat{D_{jk}} = \frac{\frac{\partial S_k}{\partial p_j}}{\left| \frac{\partial S_j}{\partial p_j} \right|} = \frac{\alpha S_k S_j}{\alpha S_j (1 - S_j)} = \frac{S_k}{(1 - S_j)}$$

For a price change to the choke price,

$$\overline{D_{jk}} = \frac{\frac{e^{V_k}}{1 + \sum_{l \in a \setminus j} e^{V_l}} - \frac{e^{V_k}}{1 + \sum_{l' \in a} e^{V_{l'}}}}{0 - \frac{e^{V_j}}{1 + \sum_{l \in a} e^{V_l}}} = \frac{S_k}{(1 - S_j)}$$

As an aside  $\frac{S_k}{1 - S_j} = \frac{Q_k}{M - Q_j}$ , so we either need to observe market shares or quantities plus a measure of market size. In both cases, diversion is merely the ratio of the marketshare of the substitute good divided by the share not buying the focal good (under the initial set of prices and product availability). It does not depend on any of the estimated parameters  $(\alpha, \beta)$ .

We can also show that the bias expression for the diversion ratio is equal to zero with logit demand (i.e., that  $D_{jk} = \frac{\partial^2 q_k}{\partial p_j^2} / \frac{\partial^2 q_j}{\partial p_j^2}$ ):



$$\begin{aligned}
\frac{\partial^2 q_j}{\partial p_j^2} &= \alpha^2(1 - 2S_j)(S_j - S_j^2) \\
\frac{\partial^2 q_k}{\partial p_j^2} &= -\alpha^2(1 - 2S_j)S_j S_k \\
\frac{\frac{\partial^2 q_k}{\partial p_j^2}}{\frac{\partial^2 q_j}{\partial p_j^2}} &= \frac{S_k}{1 - S_j} = D_{jk}
\end{aligned}$$

### Random Coefficients Logit Demand

Random Coefficients Logit demand relaxes the IIA property of the plain Logit model, which can be undesirable empirically, but it also means that the diversion ratio varies with original prices and quantities, as well as with the magnitude of the price increase. Intuitively a small price increase might see diversion from the most price sensitive consumers, while a larger price increase might see substitution from a larger set of consumers. If price sensitivity is correlated with other tastes, then the diversion ratio could differ with the magnitude of the price increase.

We can repeat the same exercise for the logit model with random coefficients, by discretizing a mixture density over  $i = 1, \dots, I$  representative consumers, with population weight  $w_i$ :

$$u_{ijt} = \underbrace{x_{jt}\beta - \alpha p_{jt} + \xi_{jt}}_{\delta_{jt}} + \mu_{ijt} + \varepsilon_{ijt}$$

Using the chain rule (for an arbitrary  $z_{jt}$ ) we can write:

$$\frac{\partial V_{ijt}}{\partial z_{jt}} = \frac{\partial V_{ijt}}{\partial \delta_{jt}} \cdot \frac{\partial \delta_{jt}}{\partial z_{jt}} + \frac{\partial V_{ijt}}{\partial \mu_{ijt}} \cdot \frac{\partial \mu_{ijt}}{\partial z_{jt}}$$

Absent taste heterogeneity for  $z_{jt}$  we have that  $\frac{\partial \mu_{ijt}}{\partial z_{jt}} \equiv 0$  and  $\frac{\partial V_{ijt}}{\partial z_{jt}} = 1 \cdot \frac{\partial \delta_{jt}}{\partial z_{jt}} = \beta_z$ . When consumers have a common price parameter  $\frac{\partial V_{ik}}{\partial p_j} = \alpha$ ,

$$\widehat{D_{jk}} = \frac{\frac{\partial S_k}{\partial p_j}}{\left| \frac{\partial S_j}{\partial p_j} \right|} = \frac{\int s_{ij} s_{ik} \frac{\partial V_{ik}}{\partial p_j}}{\int s_{ij} (1 - s_{ij}) \frac{\partial V_{ij}}{\partial p_j}} \rightarrow \frac{\int s_{ij} s_{ik}}{\int s_{ij} (1 - s_{ij})} \quad (\text{A.17})$$

$$\overline{D_{jk}} = \frac{\int \frac{e^{V_{ik}}}{1 + \sum_{l \in a \setminus j} e^{V_{il}}} - \frac{e^{V_{ik}}}{1 + \sum_{l' \in a} e^{V_{il'}}}}{\int -\frac{e^{V_{ij}}}{1 + \sum_{l \in a} e^{V_{il}}}} = \frac{1}{s_j} \int \frac{s_{ij} s_{ik}}{(1 - s_{ij})} \quad (\text{A.18})$$

Now, each individual exhibits constant diversion, but weights on individuals vary with  $p$ , so that diversion is only constant if  $s_{ij} = s_j$ . Otherwise observations with larger  $s_{ij}$  are given more weight in correlation of  $s_{ij}s_{ik}$ . The more correlated ( $s_{ij}, s_{ik}$ ) are (and especially as they are correlated with  $\alpha_i$ ) the greater the discrepancy between marginal and average diversion. We generate a single market with  $J$  products, and compute the  $J \times J$  matrix of diversion ratios two ways. The MTE method is by computing  $\frac{\partial q_k}{\partial p_j} / |\frac{\partial q_j}{\partial p_j}|$ .

For any model within the logit family, it should be clear that the ATE form of the diversion ratio does not depend on the price “instrument” (A.18), as long as we drive the purchase probability to zero. Second choice data doesn’t depend on whether price is increased or quality (or some component thereof) is decreased. When the entire population (buyers of  $j$ ) is treated, the instrument that selects individuals into treatment does not matter.

Likewise, because the random coefficients model is a single index model, any  $z_{jt}$  which affects only the mean utility component  $\delta_{jt}$  and not the unobserved heterogeneity  $\mu_{ijt}$  yields the same marginal diversion  $\hat{D}_{jk}$ . This can be seen in (A.17) which does not depend on  $\partial V_{ijt} / \partial p_{jt}$ . This has the advantage that the (marginal/infinitesimal) diversion ratio can be identified in the random coefficients logit model even when a (common) price parameter  $\alpha$  is not identified. The easiest choice of a non-price  $z_{jt}$  is  $\xi_{jt}$ , the unobserved product quality term. The role of  $\beta_z$  is to determine how many individuals receive the treatment as we vary the instrument, but this matters neither in the infinitesimal case, nor in the ATE (second-choice) case.

It is important to note that for any two variables for which there is no preference heterogeneity, they yield the same infinitesimal diversion ratios under the logit family. Likewise any two variables (irrespective of preference heterogeneity) yield the same ATE (second choice diversion ratios). This is in contrast with the treatment effects literature, where different instruments trace out different MTEs. Thus, the single index of the logit family places an important restriction on the treatment effects (which may or may not be reasonable).

## A.2 Alternative Specifications for Nevo (2000) Example

Here we repeat the same exercise as in section 3 from the text, but with different parameter estimates. In the first case we use the original published estimates from Nevo (2000) where  $\beta_{it}^{price}$  exhibited substantially less heterogeneity, while in the second we consider a restricted MPEC estimator which imposes the demographic interaction between  $income^2$  and  $price$  is equal to zero:  $\pi_{inc^2, price} = 0$ . We report those parameter estimates below as well as the estimates in the text from Dubé, Fox, and Su (2012):

$$\begin{aligned} \text{DFS (2012): } \beta_{it}^{price} &\sim N(-62.73 + 588.21 \cdot income_{it} - 30.19 \cdot income_{it}^2 + 11.06 \cdot I[child]_{it}, \sigma = 3.31) \\ \text{Nevo(2000): } \beta_{it}^{price} &\sim N(-32.43 + 16.60 \cdot income_{it} - 0.66 \cdot income_{it}^2 + 11.63 \cdot I[child]_{it}, \sigma = 1.85) \\ \text{Restricted: } \beta_{it}^{price} &\sim N(-34.09 + 8.53 \cdot income_{it} + 18.16 \cdot I[child]_{it}, \sigma = 1.04) \end{aligned}$$

In both cases we observe substantially less heterogeneity in  $\beta_{it}^{price}$  and we also observe that  $MTE_p, MTE_q, ATE$  are more similar to one another in Table 11.

	med( $y - x$ )	mean( $y - x$ )	med( $ y - x $ )	mean( $ y - x $ )	std( $ y - x $ )
	Nevo (2000) Estimates				
	All Products				
<i>MTE<sub>q</sub></i>	0.62	1.76	2.85	4.57	5.06
<i>ATE</i>	1.05	1.91	3.18	4.97	5.42
<i>Logit</i>	-29.15	-29.09	33.98	40.05	31.60
	Best Substitutes				
<i>MTE<sub>q</sub></i>	0.75	1.56	2.15	3.50	3.88
<i>ATE</i>	1.39	2.45	2.51	4.16	5.00
<i>Logit</i>	-31.83	-35.01	32.72	38.40	29.13
	Outside Good				
<i>MTE<sub>q</sub></i>	-2.32	-2.39	2.67	3.05	2.23
<i>ATE</i>	-2.90	-3.24	3.09	3.76	3.05
<i>Logit</i>	32.52	40.49	32.52	41.02	30.67
	Restricted Estimates $\pi_{inc^2, price} = 0$				
	All Products				
<i>MTE<sub>q</sub></i>	1.37	3.22	6.84	10.51	10.93
<i>ATE</i>	2.02	3.11	7.34	11.12	11.39
<i>Logit</i>	-33.48	-19.13	50.80	56.00	36.46
	Best Substitutes				
<i>MTE<sub>q</sub></i>	1.68	3.93	4.49	6.86	7.36
<i>ATE</i>	2.52	5.26	4.77	7.78	9.02
<i>Logit</i>	-41.56	-40.50	43.23	47.47	29.60
	Outside Good				
<i>MTE<sub>q</sub></i>	-4.51	-5.44	4.55	5.72	4.59
<i>ATE</i>	-5.11	-6.45	5.14	6.70	5.73
<i>Logit</i>	30.46	35.38	30.56	37.05	27.04

Table 11: Alternative Specifications for Nevo (2000).

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Mu	0.1	0.1	1	1	2	3	3
Sigma	0.5	1	0.5	1	1	1	2
Outside Good Share	0.97	0.85	0.91	0.77	0.94	0.99	0.90
Avg Own Elas	-5.37	-3.50	-4.64	-3.12	-3.70	-4.41	-1.93
Avg Max Discrepancy	1.51	3.68	1.72	2.37	2.13	2.04	3.00
Std. Max Discrepancy	0.36	1.18	0.50	0.66	0.60	0.59	1.32
Worst Case Avg ATE	7.14	14.18	9.29	12.38	10.80	9.08	15.01
Worst Case Avg MTE	5.62	10.50	7.58	10.01	8.67	7.04	12.01

Table 12: Simulation comparing ATE and MTE for Random Coefficients Logit

### A.3 Discrepancy Between Average and Marginal Treatment Effects

We can perform a Monte Carlo study to analyze the extent to which the average treatment effect deviates from the marginal treatment effect. We generate data by simulating from a random coefficients logit model with a single random coefficient on price. Our simulations follow the procedure in Armstrong (2013), Judd and Skrainka (2011) and Conlon (2016) where prices are endogenously solved for via a Bertrand-Nash game given the other utility parameters, rather than directly drawn from some distribution.

We generate the data in the following manner:  $u_{it} = \beta_0 + x_j\beta_1 - \alpha_i p_j + \xi_j + \varepsilon_{ij}$  and  $mc_j = \gamma_0 + \gamma_1 x_j + \gamma_2 z_j + \eta_j$  where  $x_j, z_j \sim N(0, 1)$ , with  $\xi_j = \rho\omega_{j1} + (1 - \rho)\omega_{j2} - 1$  and  $\eta_j = \rho\omega_{j1} + (1 - \rho)\omega_{j3} - 1$  and  $(\omega_1, \omega_2, \omega_3) \sim^{i.i.d.} U[0, 1]$ . Following Armstrong (2013) and Conlon (2016), we use the values  $\beta = [-3, 6]$  and  $\gamma = [2, 1, 1]$  and  $\rho = 0.9$ . To mimic our empirical example we let there be  $J = 30$  products and assign each product at random to one of 5 firms. We solve for prices in a Bertrand-Nash equilibrium.

For each of our sets of trials, we let  $\alpha_i \sim -\text{lognormal}(\mu, \sigma)$  and we vary the values of price heterogeneity in the population by changing  $(\mu, \sigma)$ . We simulate 100 trials from each  $(\mu, \sigma)$  pair and report characteristics of that market (average outside good share, average own price elasticity) as well as describe the discrepancy between the ATE and the MTE approach to computing diversion. We report those results for the pair of products in each trial with the largest discrepancy between the ATE and MTE calculations.

Though there are some simulations where the  $ATE < MTE$ , in the vast majority of simulations the random coefficients model with a lognormally distributed price coefficient implies that using the stock-out based ATE overstates the true MTE for the diversion ratio by 1-3 points in the worst-case scenario (the maximum over the entire  $J \times J$  matrix of diversion ratios). The degree of overstatement appears to be decreasing in the lognormal location parameter (as consumers become more price sensitive) and increasing in the dispersion parameter (as consumers become more heterogeneous).

$\alpha$	-0.500	-0.500	-0.500	-0.500	-1.000	-1.000	-1.000	-1.000
$\sigma_p$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$\sigma_x$	0.500	1.000	2.000	3.000	0.500	1.000	2.000	3.000
$s_0$	0.031	0.037	0.063	0.100	0.109	0.123	0.167	0.213
own elas	-0.318	-0.318	-0.319	-0.310	-1.523	-1.520	-1.514	-1.511
avg max dev	0.028	0.107	0.340	0.636	0.038	0.130	0.386	0.630
std max dev	0.023	0.084	0.270	0.501	0.028	0.089	0.260	0.461
max dev ATE	15.287	15.863	16.684	18.942	13.102	13.646	15.307	17.444
max dev MTE	15.260	15.757	16.344	18.306	13.064	13.516	14.921	16.814
pct dev	0.167	0.630	1.924	3.207	0.273	0.915	2.486	3.522

Table 13: Monte Carlo Simulations

$\alpha$	-1.000	-1.000	-1.000	-1.000	-1.000	-1.000	-1.000	-1.000
$\sigma_p$	0.250	0.250	0.250	0.250	0.500	0.500	0.500	0.500
$\sigma_x$	0.500	1.000	2.000	3.000	0.500	1.000	2.000	3.000
$s_0$	0.116	0.130	0.171	0.217	0.134	0.149	0.182	0.223
own elas	-1.510	-1.514	-1.487	-1.479	-1.476	-1.459	-1.431	-1.399
avg max dev	0.624	0.670	0.842	1.033	2.538	2.578	2.398	2.447
std max dev	0.227	0.253	0.376	0.565	0.878	0.971	0.836	0.987
max dev ATE	12.479	12.821	14.785	16.757	13.019	13.328	13.572	16.109
max dev MTE	11.858	12.154	13.943	15.727	10.490	10.782	11.255	13.920
pct dev	5.594	5.778	6.179	6.617	26.241	25.913	23.570	19.643

Table 14: Monte Carlo Simulations

$\alpha$	-2.000	-2.000	-2.000	-2.000	-2.000	-2.000	-2.000	-2.000
$\sigma_p$	0.250	0.250	0.250	0.250	0.500	0.500	0.500	0.500
$\sigma_x$	0.500	1.000	2.000	3.000	0.500	1.000	2.000	3.000
$s_0$	0.591	0.580	0.565	0.553	0.578	0.575	0.562	0.555
own elas	-3.846	-3.836	-3.832	-3.834	-3.479	-3.487	-3.498	-3.523
avg max dev	0.351	0.443	0.771	1.245	1.164	1.177	1.373	1.807
std max dev	0.096	0.147	0.367	0.836	0.324	0.354	0.474	0.784
max dev ATE	8.349	8.950	11.787	15.819	9.522	10.096	12.414	15.775
max dev MTE	7.998	8.507	11.016	14.574	8.358	8.919	11.041	13.968
pct dev	4.640	5.463	7.097	8.395	14.941	14.131	13.127	13.416

Table 15: Monte Carlo Simulations

$\alpha$	-4.000	-4.000	-4.000	-4.000	-4.000	-4.000	-4.000	-4.000
$\sigma_p$	0.500	0.500	0.500	0.500	1.000	1.000	1.000	1.000
$\sigma_x$	0.500	1.000	2.000	3.000	0.500	1.000	2.000	3.000
$s_0$	0.989	0.987	0.975	0.951	0.965	0.962	0.944	0.928
own elas	-7.735	-7.718	-7.811	-7.895	-5.183	-5.253	-5.440	-5.548
avg max dev	0.151	0.236	0.859	1.010	2.001	1.961	1.576	4.352
std max dev	0.059	0.087	0.340	0.851	0.587	0.634	0.717	2.611
max dev ATE	1.185	2.090	6.923	10.958	6.968	7.354	8.882	22.866
max dev MTE	1.034	1.854	6.064	9.973	4.967	5.393	7.344	20.779
pct dev	15.557	13.608	15.475	12.682	44.081	40.072	25.468	25.107

Table 16: Monte Carlo Simulations

#### A.4 Robustness to Alternative Priors Under Assumption 4

Our formulation of Assumption 4 uses Dirichlet prior centered on the IIA logit diversion estimates (proportional to marketshare).<sup>50</sup> Because some potential substitutes see  $\Delta q_k \leq 0$  and may have priors  $s_k$  near zero, we need to bound the prior probabilities away from zero in order to avoid drawing from degenerate distributions. Therefore we add 1.3 pseudo observations from a uniform prior  $\frac{1}{K+1}$  to each substitute. This gives a Dirichlet parameter of  $\alpha_k = \frac{s_k}{1-s_j} + \frac{1.3}{K+1}$ . We then choose  $\alpha_0$  so that outside good share  $\mu_0 = 0.25$  for the prior distribution. This results in  $m = 3.05$  pseudo observations for our (very weak) prior distribution.

For robustness we consider two other (weak) priors. For one, we keep everything else the same but choose  $\mu_0 = 0.75$ . For the other we consider the “uninformative” or uniform prior of  $\alpha_k = \frac{1}{K+1}$  with  $m = 1.1$  pseudo observations. An additional approach is to choose a prior distribution that more closely resembles a logit model. This approach is known as the *over-parametrized normal* which is a common technique in the statistics literature and is better behaved for rare events. See Gelman, Bois, and Jiang (1996) and Blei and Lafferty (2007).<sup>51</sup>

**Alternative Assumption.** “Unit Simplex”:  $D_{jk} \in [0, 1]$  and  $\sum_{\forall k} D_{jk} = 1$   
 $\Delta q_k | \Delta q_j, D_{jk} \sim \text{Bin}(n = \Delta q_j, p = D_{jk})$  and  $\eta_{jk} | \mu_{jk}, \sigma_{jk} \sim N(\mu_{jk}, \sigma_{jk})$ ,  $D_{jk} = \frac{\exp[\eta_{jk}]}{\sum_{k'} \exp[\eta_{jk}]}$

For each of these specifications we report the maximum absolute deviations for the posterior mean of the estimated diversion ratios  $L_\infty = \max_k |\hat{D}_{jk} - \tilde{D}_{jk}|$  where the base  $\tilde{D}_{jk}$  is given by our Dirichlet prior centered on the (adjusted) IIA logit estimates  $\alpha_k = \frac{s_k}{1-s_j} + \frac{1.3}{K+1}$  with  $m = 3.05$  pseudo-observations. The discrepancies between these priors are reported in Table 17. We obtain nearly identical results (differences less than 0.03 *percentage points*) when

<sup>50</sup>One can transform the Dirichlet as follows:  $\text{Dirichlet}(\alpha_0, \dots, \alpha_K)$  has  $\mu_k = \frac{\alpha_k}{m}$  and  $m = \sum_{k'=0}^K \alpha_{k'}$ .

<sup>51</sup>We can interpret this as a multinomial logit model with product intercepts  $\eta_{jk}$  which are estimates with some sampling error  $\sigma_{jk}$ . However, as  $\sigma$  increases, because the multinomial logit transformation is nonlinear this tends towards  $\mu_{jk} = \frac{1}{K+1}$ .

Experiment Prior Mean $\mu_j =$ Prior Strength	Dirichlet $\frac{s_k}{1-s_j}$ ( $s_j = 0.75$ ) $m = 9.60$	Dirichlet $\frac{1}{K+1}$ $m = 1.1$	Normal-Logit $\frac{1}{K+1}$ $\sigma^2 = 100$
Snickers	0.218	0.023	0.017
Zoo Animal Crackers	0.428	0.020	0.014
Famous Amos Cookie	0.537	0.033	0.028
M&M Peanut	0.216	0.014	0.025

Table 17: Maximum Absolute Deviation (percentage points) between Dirichlet parametrized by (adjusted) IIA logit shares ( $\alpha_k = \frac{s_k}{1-s_j} + \frac{1.3}{K+1}$ ,  $\mu_0 = 0.25$ ,  $m = 3.05$ ) and alternatives.

compared to the Dirichlet with a the uniform  $\frac{1}{K+1}$  prior and  $m = 1.1$  pseudo-observations and the multinomial logit transformed normal prior. There is a somewhat larger discrepancy (differences less than 0.5 *percentage points*) when compared to a somewhat stronger ( $m = 9.6$ ) Dirichlet prior with a larger outside good share  $\mu_0 = 0.75$ , which we attribute stronger prior rather than the share of the outside good.<sup>52</sup>

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<sup>52</sup>We need a somewhat stronger prior to bound small probabilities away from zero when the outside good share is larger.

## A.5 Alternative Merger And Divestitures Table

This reports the Merger and Divestiture effects from Table 10 under the alternative assumption of a Beta prior and  $m = J$  pseudo-observations (without assumption 4). The 95% credible posterior intervals are much larger, and for close substitutes tend to substantially overstate the degree of substitution (sometimes by an order of magnitude). In part this is because we also estimate large negative diversion to some products.

Proposed Merger	Diversion Direction	Diversion Ratio	Proposed Divestiture	Diversion Ratio Under Divestiture
Mars & Hershey	Snickers to Hershey	18.72 (13.61, 24.82)	Reese's Peanut Butter Cups	18.72* (13.61, 24.82)
	M&M Peanut to Hershey	20.15 (16.12, 24.50)	Reese's Peanut Butter Cups	15.33 (11.51, 19.43)
Mars & Kraft	Snickers to Kraft	11.59 (8.88, 15.34)	Planters Peanuts	2.02 (0.35, 5.29)
	M&M Peanut to Kraft	8.51 (6.20, 11.31)	Planters Peanuts	2.92 (1.07, 5.57)
Mars & Nestle	Snickers to Nestle	30.48 (23.40, 39.00)	Butterfinger	13.41 (7.34, 21.28)
	M&M Peanut to Nestle	12.13 (9.28, 16.60)	Butterfinger	8.47 (6.04, 12.63)
Mars & Kellogg's	Snickers to Kellogg's	35.44 (28.60, 43.19)	Famous Amos Cookies <sup>†</sup>	23.71 (17.44, 31.17)
	M&M Peanut to Kellogg's	22.94 (17.74, 30.15)	Famous Amos Cookies <sup>†</sup>	22.49 (17.29, 29.75)
	Zoo Animal Crackers to Mars	60.20 (52.41, 68.94)	Famous Amos Cookies <sup>†</sup>	60.20 (52.41, 68.94)
Kellogg's & Kraft	Zoo Animal Crackers to Kraft	32.24 (23.58, 42.34)	Planters Peanuts	25.71 (17.42, 35.57)
	Choc Chip Famous Amos to Kraft	40.55 (32.67, 49.23)	Planters Peanuts	19.76 (12.91, 27.68)

Table 18: Hypothetical Mergers with Forced Divestitures

Note: 95% equal-tail credible intervals shown in parentheses.

\* Reese's Peanut Butter Cups are unavailable in all treatment weeks for this experiment.

<sup>†</sup> Divestiture of both "Choc Chip Famous Amos" and "Choc SandFamous Amos".

For upward pricing pressure not to be positive under the assumptions that  $p = 0.45$  and  $c = 0.15$ , marginal cost reductions must be at least twice as large as the diversion estimates.



## A.6 Stan Code for MCMC Estimator

This is code for the R library *stan* (Team 2015) which recovers the MCMC estimator of the diversion ratio under assumptions (1)-(4).

```
% Main Specification: Dirichlet Prior
data {
  int<lower=1> J;           // number of products, including outside good
  int<lower=1> N[J];        // number of trials
  int<lower=0> y[J];        // number of successes for each product j
  vector[J] priors;        // mean of the distribution of alpha
}

parameters {
  simplex[J] theta;
}

model {
  theta ~ dirichlet(priors);
  for (j in 1:J) {
    y[j] ~ binomial(N[j], theta[j]);
  }
}

% Alternative Specification: Multinomial Logit/Normal
data {
  int J;                   // number of products, including outside good
  int N[J];                // number of trials
  int y[J];                // number of successes for each product j
  real mu_prior[J];        // mean of the distribution of alpha
  real sigma_prior[J];     // standard deviation of the distribution of alpha
}

parameters {
  row_vector[J] alpha;      // probability of success = exp(alpha[j])/(sum(exp(alpha[j])))
}

transformed parameters {
  row_vector[J] theta;
  for (j in 1:J)
    theta[j] <- exp(alpha[j])/(sum(exp(alpha))); // don't normalize the outside good
}

model {
  for (j in 1:J)
    alpha[j] ~ normal(mu_prior[j], sigma_prior[j]);

  for (j in 1:J) {
    y[j] ~ binomial(N[j], theta[j]);
  }
}
```