

# Memory System

## Cache

Lin Gu  
CSE, HKUST

1

## Memory Hierarchy: Motivation The Principle Of Locality

- Programs usually access a relatively small portion of their address space (instructions/data) at any instant of time (loops, data arrays).
- Two Types of locality:
  - Temporal Locality:** If an item is referenced, it will tend to be referenced again soon.
  - Spatial locality:** If an item is referenced, items whose addresses are close by will tend to be referenced soon.
- The presence of locality in program behavior (e.g., loops, data arrays), makes it possible to satisfy a large percentage of program access needs (both instructions and operands) using memory levels with much less capacity than the program address space.

2

## Locality Example

Locality Example:

```
sum = 0;
for (i = 0; i < n; i++)
    sum += a[i];
return sum;
```

### Data

- Reference array elements in succession (stride-1 reference pattern):
- Reference `sum` each iteration:

Spatial locality

Temporal locality

### Instructions

- Reference instructions in sequence:
- Cycle through loop repeatedly:

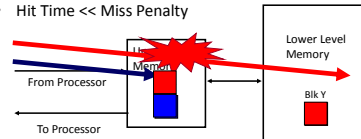
Spatial locality

Temporal locality

3

## Memory Hierarchy: Terminology

- A Block:** The smallest unit of information transferred between two levels.
- Hit:** Item is found in some block in the upper level (example: Block X)
  - Hit Rate:** The fraction of memory accesses found in the upper level.
  - Hit Time:** Time to access the upper level which consists of memory access time + time to determine hit/miss
- Miss:** Item needs to be retrieved from a block in the lower level (Block Y)
  - Miss Rate** =  $1 - (\text{Hit Rate})$
  - Miss Penalty:** Time to replace a block in the upper level + Time to deliver the block to the processor
- Hit Time  $\ll$  Miss Penalty



4

## Caching in a Memory Hierarchy

Level k: 

4	9	10	3
---	---	----	---

 Smaller, faster, more expensive device at level k caches a subset of the blocks from level k+1

10  
Data is copied between levels in block-sized transfer units

Level k+1: 

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

 Larger, slower, cheaper storage device at level k+1 is partitioned into blocks.

5

## General Caching Concepts

- Program needs object d, which is stored in some block b.
- Cache hit**
  - Program finds b in the cache at level k. E.g., block 14.
- Cache miss**
  - b is not at level k, so level k cache must fetch it from level k+1. E.g., block 12.
  - If level k cache is full, then some current block must be replaced (evicted). Which one is the "victim"?
    - Placement policy:** where can the new block go? E.g.,  $b \bmod 4$
    - Replacement policy:** which block should be evicted? E.g., LRU

6

### Cache Design & Operation Issues

- Q1: Where can a block be placed in cache?  
(*Block placement strategy & Cache organization*)
  - Fully Associative, Set Associative, Direct Mapped.
- Q2: How is a block found if it is in cache?  
(*Block identification*)
  - Tag/Block.
- Q3: Which block should be replaced on a miss?  
(*Block replacement*)
  - Random, LRU.
- Q4: What happens on a write?  
(*Cache write policy*)
  - Write through, write back.

7

### Types of Caches: Organization

Type of cache	Mapping of data from memory to cache	Complexity of searching the cache
Direct mapped (DM)	• DM and FA can be thought as special cases of SA • DM $\rightarrow$ 1-way SA • FA $\rightarrow$ All-way SA	Easy search mechanism
Set-associative (SA)	A memory value can be placed in <b>any of a set of locations</b> in the cache	Slightly more involved search mechanism
Fully-associative (FA)	A memory value can be placed in <b>any location</b> in the cache	Extensive hardware resources required to search (CAM)

8

### Cache Organization & Placement Strategies

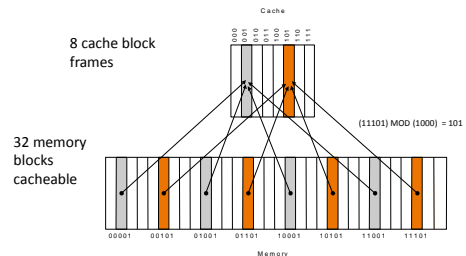
Placement strategies or mapping of a main memory data block onto cache block frame addresses divide cache into three organizations:

- **Direct mapped cache:** A block can be placed in one location only, given by:  
 $(\text{Block address}) \bmod (\text{Number of blocks in cache})$ 
  - Advantage: It is easy to locate blocks in the cache (only one possibility)
  - Disadvantage: Certain blocks cannot be simultaneously present in the cache (they can only have the same location)

9

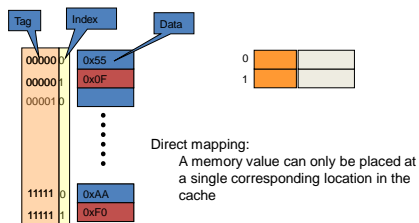
### Cache Organization: Direct Mapped Cache

A block can be placed in one location only, given by:  
 $(\text{Block address}) \bmod (\text{Number of blocks in cache})$   
 In this case:  $(\text{Block address}) \bmod (8)$



10

### Direct Mapping



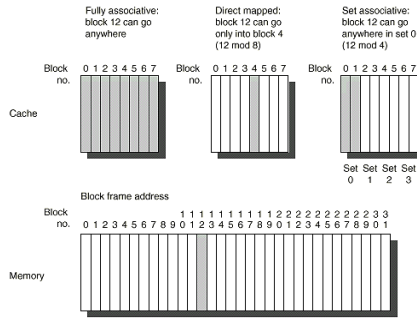
11

### Cache Organization & Placement Strategies

- **Fully associative cache:** A block can be placed anywhere in cache.
  - Advantage: No restriction on the placement of blocks. Any combination of blocks can be simultaneously present in the cache.
  - Disadvantage: Costly (hardware and time) to search for a block in the cache
- **Set associative cache:** A block can be placed in a restricted set of places, or cache block frames. A set is a group of block frames in the cache. A block is first mapped onto the set and then it can be placed anywhere within the set. The set in this case is chosen by:  
 $(\text{Block address}) \bmod (\text{Number of sets in cache})$ 
  - If there are  $n$  blocks in a set the cache placement is called  $n$ -way set-associative, or  $n$ -associative.
  - A good compromise between direct mapped and fully associative caches (most processors use this method).

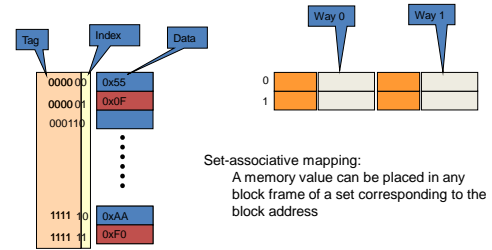
12

### Cache Organization Example



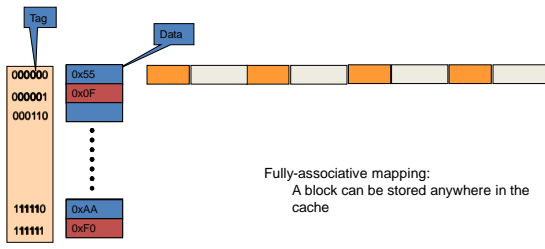
13

### Set Associative Mapping (2-Way)



14

### Fully Associative Mapping



15

### Cache Organization Tradeoff

- For a given cache size, there is a tradeoff between hit rate and complexity
- If  $L$  = number of lines (blocks) in the cache,  
 $L = \text{Cache Size} / \text{Block Size}$

How many places for a block to go	Name of cache type	Number of Sets
1	Direct Mapped	$L$
$n$	$n$ -way associative	$L/n$
$L$	Fully Associative	1

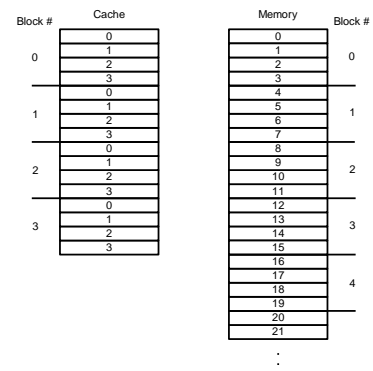
↑  
Number of comparators  
needed to compare tags

16

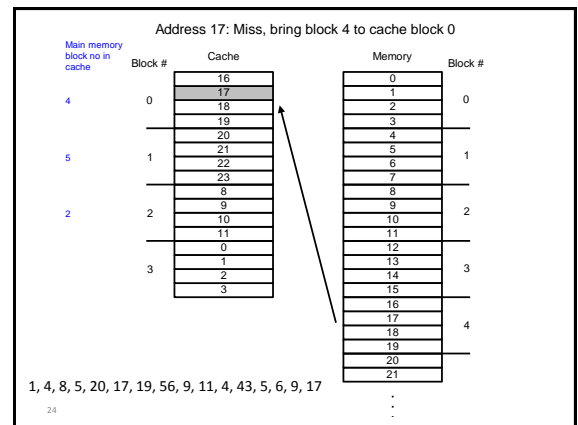
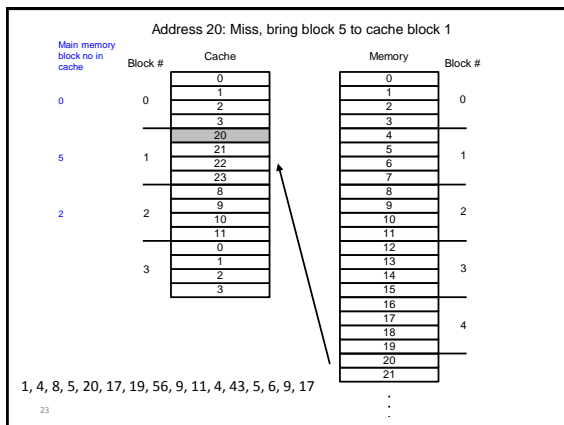
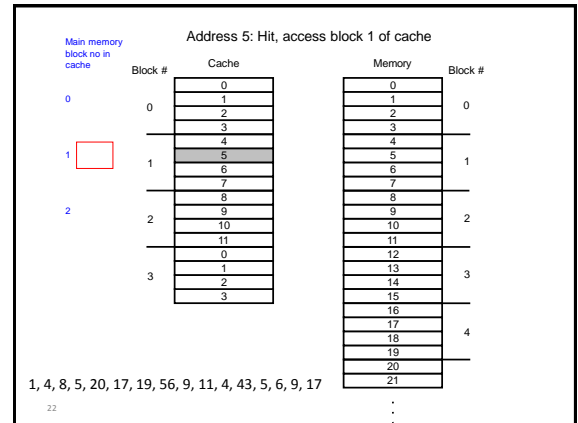
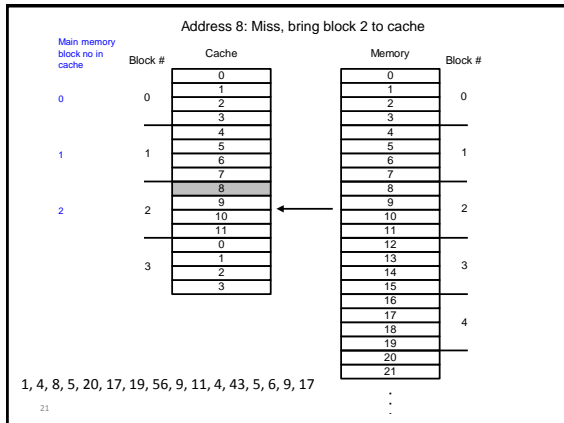
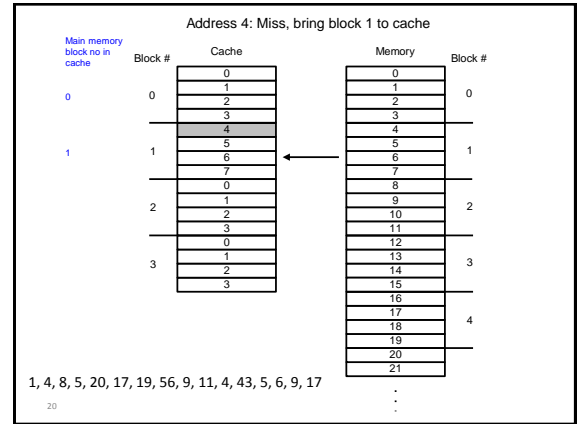
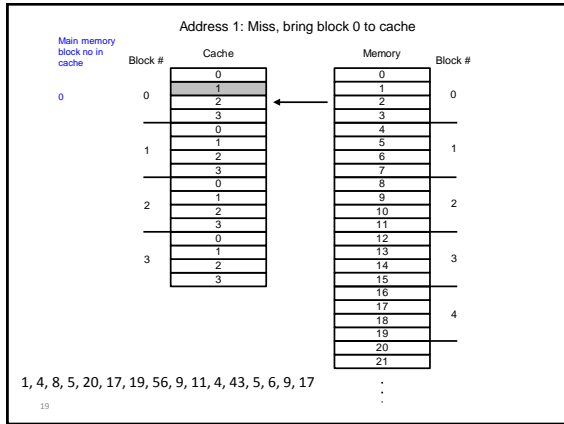
### An Example

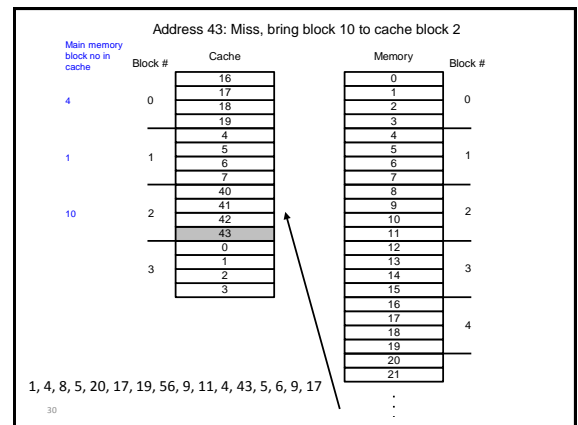
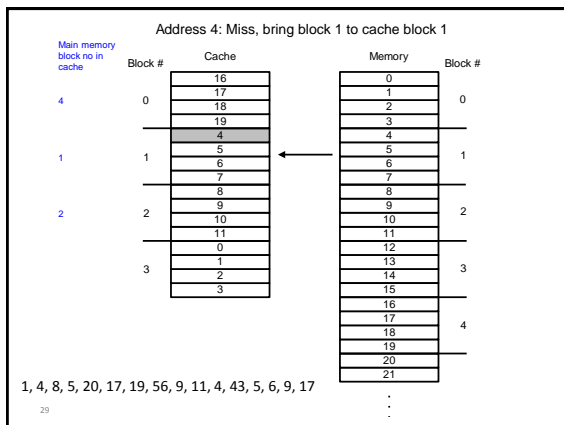
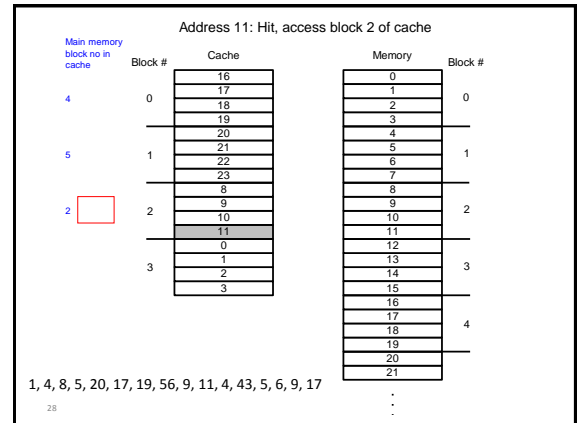
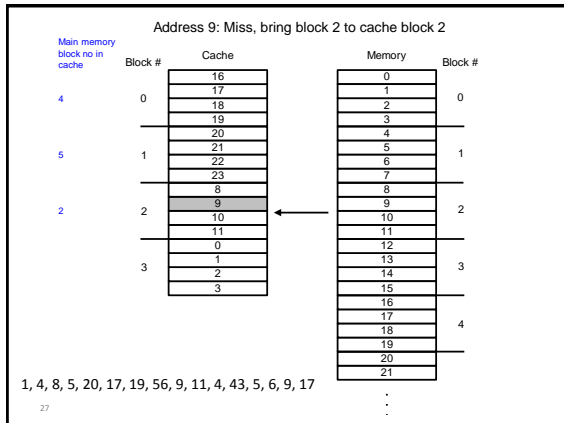
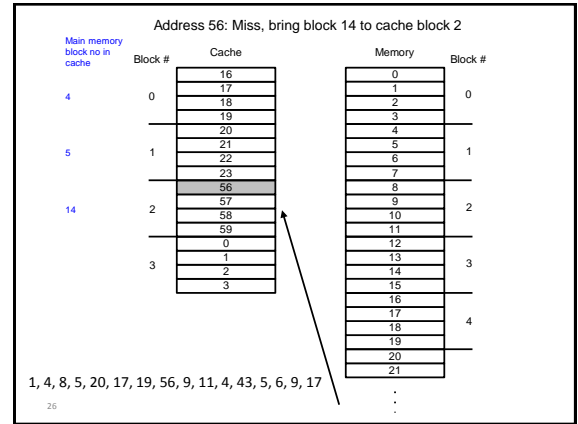
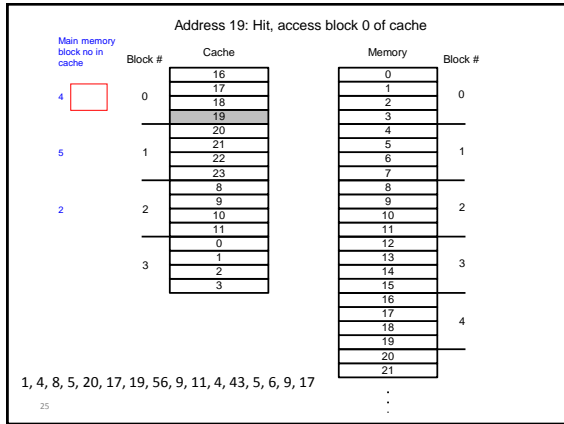
- Assume a **direct mapped** cache with **4-word blocks** and a total size of **16 words**.
- Consider the following string of address references given as word addresses:  
– 1, 4, 8, 5, 20, 17, 19, 56, 9, 11, 4, 43, 5, 6, 9, 17
- Show the hits and misses and final cache contents.

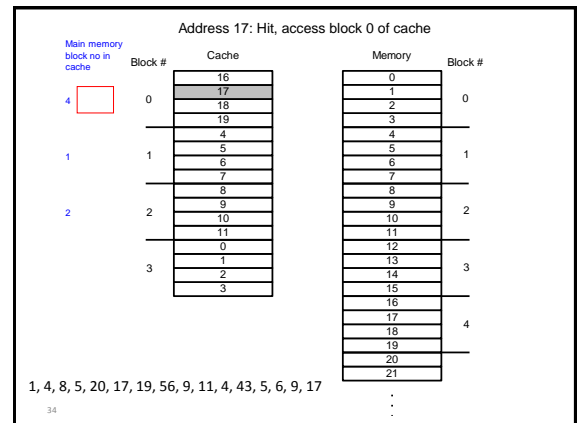
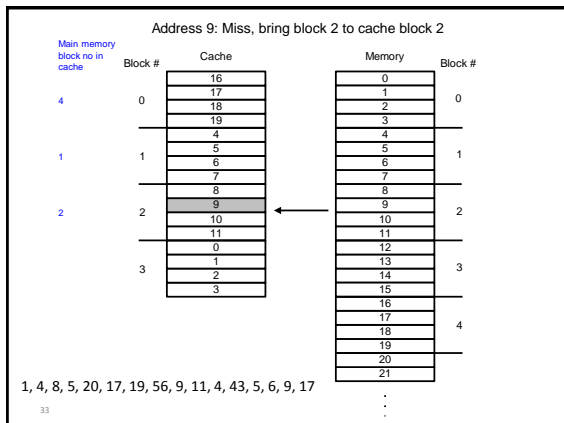
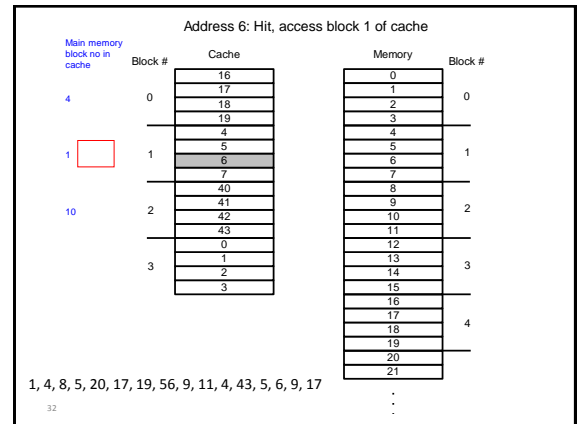
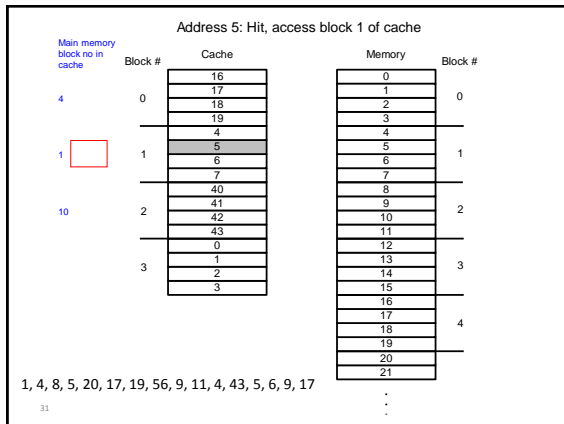
17



18







## Summary

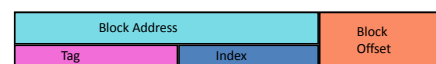
- Number of Hits = 6
- Number of Misses = 10
- Hit Ratio:  $6/16 = 37.5\%$  Unacceptable
- Typical Hit ratio: > 90%

Address	Miss/Hit
1	Miss
4	Miss
8	Miss
5	Hit
20	Miss
17	Miss
19	Hit
56	Miss
9	Miss
11	Hit
4	Miss
43	Miss
5	Hit
6	Hit
9	Miss
17	Hit

35

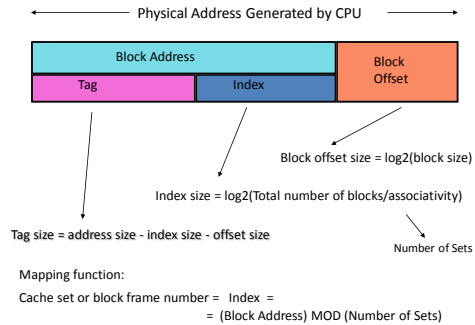
## Locating A Data Block in Cache

- Each block in the cache has an address tag.
- The tags of every cache block that might contain the required data are checked in parallel.
- A valid bit is added to the tag to indicate whether this cache entry is valid or not.
- The address from the CPU to the cache is divided into:
  - A block address, further divided into:
    - An index field to choose a block set in the cache. (no index field when fully associative).
    - A tag field to search and match addresses in the selected set.
  - A block offset to select the data from the block.



36

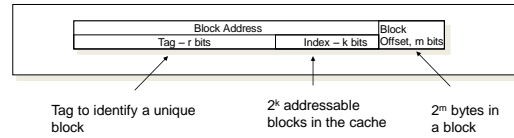
### Address Field Sizes



37

### Locating A Data Block in Cache

- Increasing associativity shrinks index, expands tag
  - Block index not needed for fully associative cache



38

### Direct-Mapped Cache Example

- Suppose we have a 16KB of data in a direct-mapped cache with 4 word blocks
- Determine the size of the tag, index and offset fields if we're using a 32-bit architecture
- Offset
  - need to specify correct byte within a block
  - block contains 4 words = 16 bytes =  $2^4$  bytes
  - need 4 bits to specify correct byte

39

### Direct-Mapped Cache Example

- Index: (~index into an "array of blocks")
    - need to specify correct row in cache
    - cache contains 16 KB =  $2^{14}$  bytes
    - block contains  $2^4$  bytes (4 words)
- # rows/cache = # blocks/cache (since there's one block/row)
- $$= \frac{\text{bytes/cache}}{\text{bytes/row}} = \frac{2^{14} \text{ bytes/cache}}{2^4 \text{ bytes/row}} = 2^{10} \text{ rows/cache}$$
- need 10 bits to specify this many rows

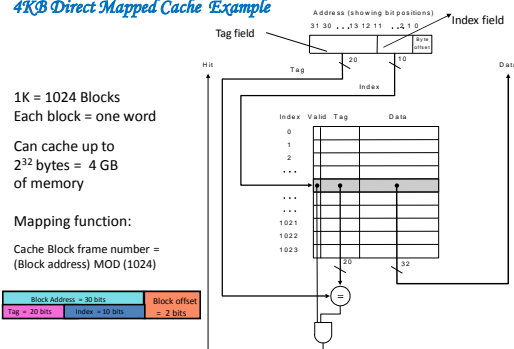
40

### Direct-Mapped Cache Example

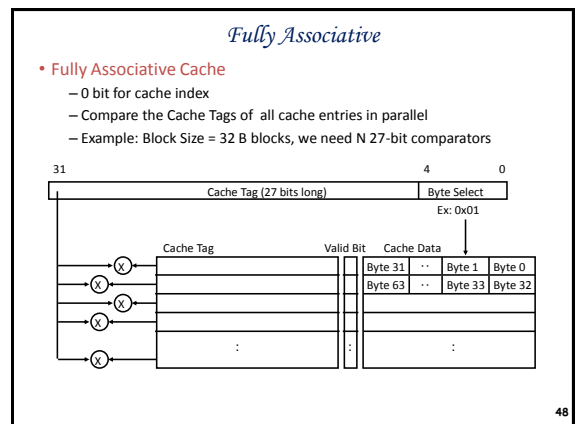
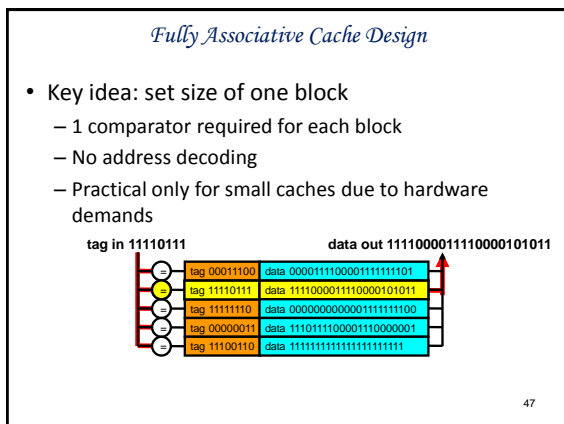
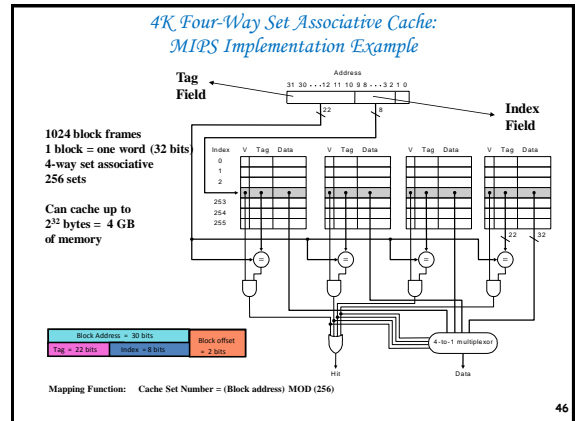
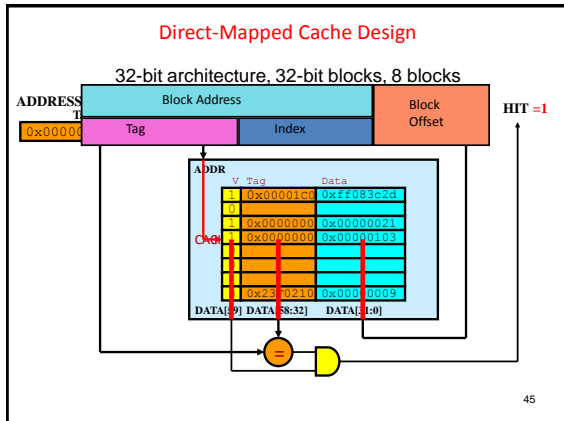
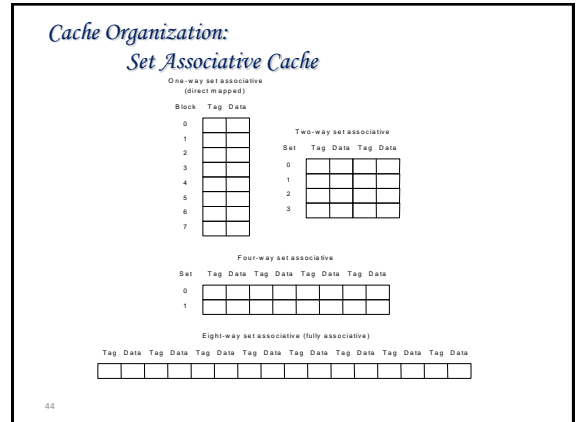
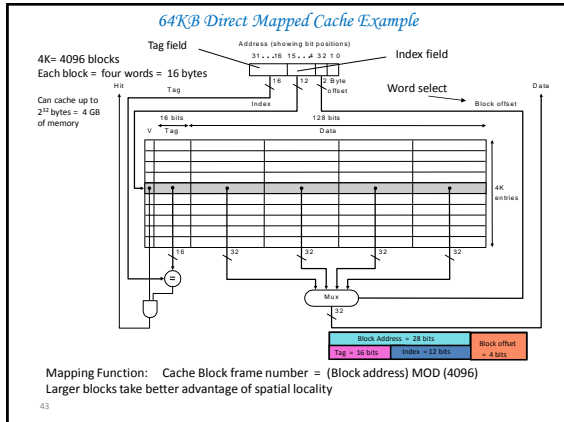
- Tag: use remaining bits as tag
  - tag length = mem addr length - offset - index
  - =  $32 - 4 - 10$  bits
  - = 18 bits
- so tag is leftmost 18 bits of memory address

41

### 4KB Direct Mapped Cache Example



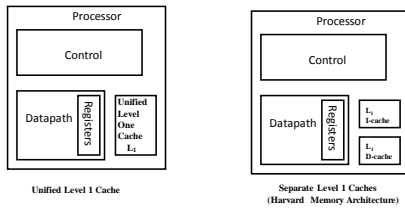
42





### Unified vs. Separate Level 1 Cache

- Unified Level 1 Cache  
A single level 1 cache is used for both instructions and data.
- Separate instruction/data Level 1 caches (Harvard Memory Architecture):  
The level 1 (L<sub>1</sub>) cache is split into two caches, one for instructions (instruction cache, L<sub>1</sub> I-cache) and the other for data (data cache, L<sub>1</sub> D-cache).



49

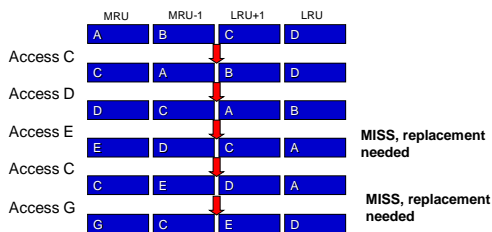
### Cache Replacement Policy

When a cache miss occurs the cache controller may have to select a block of cache data to be removed from a cache block frame and replaced with the requested data, such a block is selected by one of two methods (for direct mapped cache, there is only one choice):

- **Random:**
  - Any block is randomly selected for replacement providing uniform allocation.
  - Simple to build in hardware.
  - The most widely used cache replacement strategy.
- **Least-recently used (LRU):**
  - Accesses to blocks are recorded and the block replaced is the one that was not used for the longest period of time.
  - LRU is *expensive* to implement, as the number of blocks to be tracked increases, and is usually approximated.

50

### LRU Policy



51

### Miss Rates for Caches with Different Size, Associativity & Replacement Algorithm

#### Sample Data

Associativity:	2-way		4-way		8-way	
	LRU	Random	LRU	Random	LRU	Random
Size						
16 KB	5.18%	5.69%	4.67%	5.29%	4.39%	4.96%
64 KB	1.88%	2.01%	1.54%	1.66%	1.39%	1.53%
256 KB	1.15%	1.17%	1.13%	1.13%	1.12%	1.12%

52

### Cache and Memory Performance

Average Memory Access Time (AMAT), Memory Stall cycles

- The Average Memory Access Time (AMAT):** The average number of cycles required to complete a memory access request by the CPU.
- Memory stall cycles per memory access: The number of stall cycles added to CPU execution cycles for one memory access.
- For an ideal memory:  $AMAT = 1$  cycle, this results in zero memory stall cycles.
- Memory stall cycles per memory access =  $AMAT - 1$
- Memory stall cycles per instruction =  
Memory stall cycles per memory access  
x Number of memory accesses per instruction  
 $= (AMAT - 1) \times (1 + \text{fraction of loads/stores})$

Instruction Fetch

53

### Cache Performance

Unified Memory Architecture

- For a CPU with a single level (L1) of cache for both instructions and data and no stalls for cache hits:

With ideal memory

$$\text{Total CPU time} = (\text{CPU execution clock cycles} + \text{Memory stall clock cycles}) \times \text{clock cycle time}$$

Memory stall clock cycles =

$$(\text{Reads} \times \text{Read miss rate} \times \text{Read miss penalty}) + (\text{Writes} \times \text{Write miss rate} \times \text{Write miss penalty})$$

If write and read miss penalties are the same:

$$\text{Memory stall clock cycles} = \text{Memory accesses} \times \text{Miss rate} \times \text{Miss penalty}$$

54

### Cache Performance

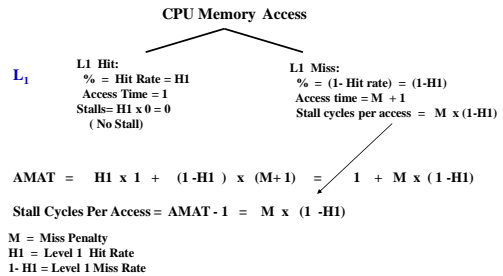
Unified Memory Architecture

- $CPU_{time} = \text{Instruction count} \times CPI \times \text{Clock cycle time}$
- $CPI_{\text{execution}} = CPI \text{ with ideal memory}$
- $CPI = CPI_{\text{execution}} + \text{MEM Stall cycles per instruction}$
- $CPU_{time} = \text{Instruction Count} \times (CPI_{\text{execution}} + \text{MEM Stall cycles per instruction}) \times \text{Clock cycle time}$
- $\text{MEM Stall cycles per instruction} = \text{MEM accesses per instruction} \times \text{Miss rate} \times \text{Miss penalty}$
- $CPU_{time} = IC \times (CPI_{\text{execution}} + \text{MEM accesses per instruction} \times \text{Miss rate} \times \text{Miss penalty}) \times \text{Clock cycle time}$
- $\text{Misses per instruction} = \text{Memory accesses per instruction} \times \text{Miss rate}$
- $CPU_{time} = IC \times (CPI_{\text{execution}} + \text{Misses per instruction} \times \text{Miss penalty}) \times \text{Clock cycle time}$

55

### Memory Access Tree

For Unified Level 1 Cache



56

### Cache Impact On Performance: An Example

Assuming the following execution and cache parameters:

- Cache miss penalty = 50 cycles
- Normal instruction execution CPI ignoring memory stalls = 2.0 cycles
- Miss rate = 2%
- Average memory references/instruction = 1.33

$$CPU_{time} = IC \times [CPI_{\text{execution}} + \text{Memory accesses/instruction} \times \text{Miss rate} \times \text{Miss penalty}] \times \text{Clock cycle time}$$

$$CPU_{time}^{\text{with cache}} = IC \times (2.0 + (1.33 \times 2\% \times 50)) \times \text{clock cycle time}$$

$$= IC \times 3.33 \times \text{Clock cycle time}$$

→ Lower  $CPI_{\text{execution}}$  increases the impact of cache miss clock cycles

57

### Cache Performance Example

- Suppose a CPU executes at Clock Rate = 200 MHz (5 ns per cycle) with a single level of cache.
- $CPI_{\text{execution}} = 1.1$
- Instruction mix: 50% arith/logic, 30% load/store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.

$$CPI = CPI_{\text{execution}} + \text{mem stalls per instruction}$$

$$\text{Mem Stalls per instruction} = \text{Mem accesses per instruction} \times \text{Miss rate} \times \text{Miss penalty}$$

$$\text{Mem accesses per instruction} = 1 + .3 = 1.3$$

$$\text{Mem Stalls per instruction} = 1.3 \times 0.015 \times 50 = 0.975$$

$$CPI = 1.1 + .975 = 2.075$$

The ideal memory CPU with no misses is  $2.075/1.1 = 1.88$  times faster

58

### Cache Performance Example

- Suppose for the previous example we double the clock rate to 400 MHz, how much faster is this machine, assuming similar miss rate, instruction mix?
- Since memory speed is not changed, the miss penalty takes more CPU cycles:

$$\text{Miss penalty} = 50 \times 2 = 100 \text{ cycles.}$$

$$CPI = 1.1 + 1.3 \times .015 \times 100 = 1.1 + 1.95 = 3.05$$

$$\text{Speedup} = (CPI_{\text{old}} \times C_{\text{old}}) / (CPI_{\text{new}} \times C_{\text{new}})$$

$$= 2.075 \times 2 / 3.05 = 1.36$$

The new machine is only 1.36 times faster rather than 2 times faster due to the increased effect of cache misses.

→ CPUs with higher clock rate, have more cycles per cache miss and more memory impact on CPI.

59

### Cache Performance

#### Harvard Memory Architecture

For a CPU with separate or split level one (L1) caches for instructions and data (Harvard memory architecture) and no stalls for cache hits:

$$CPU_{time} = \text{Instruction count} \times CPI \times \text{Clock cycle time}$$

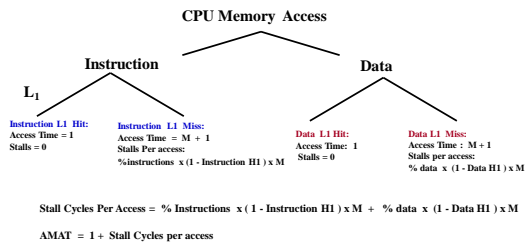
$$CPI = CPI_{\text{execution}} + \text{Mem Stall cycles per instruction}$$

$$CPU_{time} = \text{Instruction Count} \times (CPI_{\text{execution}} + \text{Mem Stall cycles per instruction}) \times \text{Clock cycle time}$$

$$\text{Mem Stall cycles per instruction} = \text{Instruction Fetch Miss rate} \times \text{Miss Penalty} + \text{Data Memory Accesses Per Instruction} \times \text{Data Miss Rate} \times \text{Miss Penalty}$$

60

### Memory Access Tree For Separate Level 1 Caches



61

### Typical Cache Performance Data Using SPEC92

Size	Instruction cache	Data cache	Unified cache
1 KB	3.06%	24.61%	13.34%
2 KB	2.26%	20.57%	9.78%
4 KB	1.78%	15.94%	7.24%
8 KB	1.10%	10.19%	4.57%
16 KB	0.64%	6.47%	2.87%
32 KB	0.39%	4.82%	1.99%
64 KB	0.15%	3.77%	1.35%
128 KB	0.02%	2.88%	0.95%

62

### Cache Performance Example

- To compare the performance of either using a 16-KB instruction cache and a 16-KB data cache as opposed to using a unified 32-KB cache, we assume a hit to take one clock cycle and a miss to take 50 clock cycles, and a load or store to take one extra clock cycle on a unified cache, and that 75% of memory accesses are instruction references. Using the miss rates for SPEC92 we get:

Overall miss rate for a split cache =  $(75\% \times 0.64\%) + (25\% \times 6.47\%) = 2.1\%$

- From SPEC92 data a unified cache would have a miss rate of 1.99%  
Average memory access time = 1 + stall cycles per access  
= 1 + % instructions x (Instruction miss rate x Miss penalty)  
+ % data x (Data miss rate x Miss penalty)

#### For split cache:

Average memory access time<sub>split</sub>  
= 1 + 75% x (0.64% x 50) + 25% x (6.47% x 50) = 2.05 cycles

#### For unified cache:

Average memory access time<sub>unified</sub>  
= 1 + 75% x (1.99% x 50) + 25% x (1 + 1.99% x 50) = 2.24 cycles

63

## Cache Write Strategies

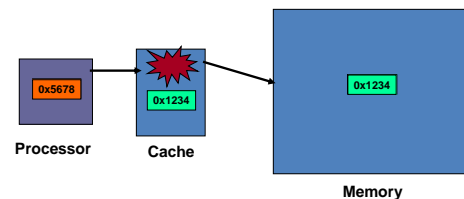
64

### Cache Read/Write Operations

- Statistical data suggest that reads (including instruction fetches) dominate processor cache accesses (writes account for 25% of data cache traffic).
- In cache reads, a block is read at the same time while the tag is being compared with the block address (searching). If the read is a hit the data is passed to the CPU, if a miss it ignores it.
- In cache writes, modifying the block cannot begin until the tag is checked to see if the address is a hit.
- Thus for cache writes, tag checking cannot take place in parallel, and only the specific data requested by the CPU can be modified.
- Cache is classified according to the write and memory update strategy in place: write through, or write back.

65

### Write-through Policy

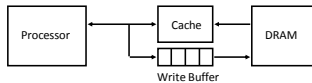


66

### Cache Write Strategies

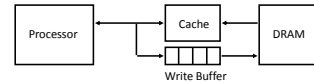
#### 1 Write Through: Data is written to both the cache block and the main memory.

- The lower level always has the most updated data; an important feature for I/O and multiprocessing.
- Easier to implement than write back.
- A write buffer is often used to reduce CPU write stall while data is written to memory.



67

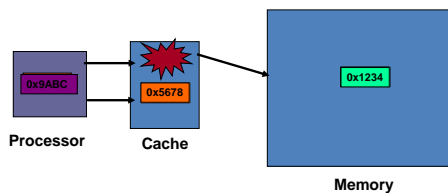
### Write Buffer for Write Through



- A Write Buffer is needed between the Cache and Memory
  - Processor: writes data into the cache and the write buffer
  - Memory controller: write contents of the buffer to memory
- Write buffer is just a FIFO queue:
  - Typical number of entries: 4
  - Works fine if: Store frequency (w.r.t. time)  $\ll 1 / \text{DRAM write cycle}$

68

### Write-back Policy



69

### Cache Write Strategies

#### 2 Write back: Data is written or updated only to the cache block.

- Writes occur at the speed of cache
- The modified or dirty cache block is written to main memory later (e.g., when it's being replaced from cache)
- A status bit called a dirty bit, is used to indicate whether the block was modified while in cache; if not the block is not written to main memory.
- Uses less memory bandwidth than write through.

70

### Write misses

- If we try to write to an address that is not already contained in the cache; this is called a **write miss**.
- Let's say we want to store **21763** into Mem[1101 0110] but we find that address is not currently in the cache.

Index	V	Tag	Data	Address	Data
...	...	...	...	...	...
110	1	00010	123456	1101 0110	6378
...	...	...	...	...	...

- When we update Mem[1101 0110], should we *also* load it into the cache?

71

### No write-allocate

- With a **no-write allocate** policy, the write operation goes directly to main memory *without affecting the cache*.

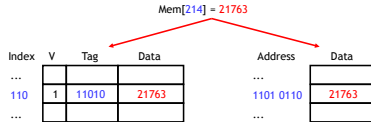
Index	V	Tag	Data	Address	Data
...	...	...	...	...	...
110	1	00010	123456	1101 0110	21763
...	...	...	...	...	...

- This is good when data is written but not immediately used again, in which case there's no point to load it into the cache yet.

72

### Write Allocate

- A **write allocate** strategy would instead load the newly written data into the cache.

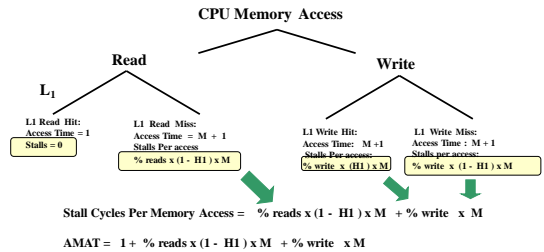


- If that data is needed again soon, it will be available in the cache.

73

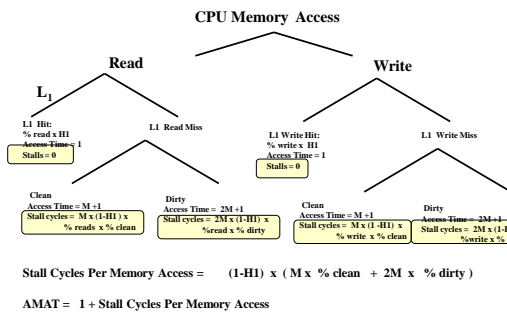
### Memory Access Tree, Unified L<sub>1</sub>

Write Through, No Write Allocate, No Write Buffer



74

### Memory Access Tree Unified L<sub>1</sub> Write Back, With Write Allocate



75

### Write Through Cache Performance Example

- A CPU with  $CPI_{\text{execution}} = 1.1$  uses a unified L1 Write Through, No Write Allocate and no write buffer.
- Instruction mix: 50% arith/logic, 15% load, 15% store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.

$$CPI = CPI_{\text{execution}} + \text{MEM stalls per instruction}$$

$$\text{MEM Stalls per instruction} = \text{MEM accesses per instruction} \times \text{Stalls per access}$$

$$\text{MEM accesses per instruction} = 1 + .3 = 1.3$$

$$\text{Stalls per access} = \% \text{ reads} \times \text{miss rate} \times \text{Miss penalty} + \% \text{ write} \times \text{Miss penalty}$$

$$\% \text{ reads} = 1.15/1.3 = 88.5\% \quad \% \text{ writes} = .15/1.3 = 11.5\%$$

$$\text{Stalls per access} = 50 \times (88.5\% \times 1.5\% + 11.5\%) = 6.4 \text{ cycles}$$

$$\text{Mem Stalls per instruction} = 1.3 \times 6.4 = 8.33 \text{ cycles}$$

$$AMAT = 1 + 6.4 = 7.4 \text{ cycles}$$

$$CPI = 1.1 + 8.33 = 9.43$$

The ideal memory CPU with no misses is  $9.43/1.1 = 8.57$  times faster

76

### Write Back Cache Performance Example

- A CPU with  $CPI_{\text{execution}} = 1.1$  uses a unified L1 with write back, write allocate, and the probability a cache block is dirty = 10%
- Instruction mix: 50% arith/logic, 15% load, 15% store, 20% control
- Assume a cache miss rate of 1.5% and a miss penalty of 50 cycles.

$$CPI = CPI_{\text{execution}} + \text{mem stalls per instruction}$$

$$\text{MEM Stalls per instruction} = \text{MEM accesses per instruction} \times \text{Stalls per access}$$

$$\text{MEM accesses per instruction} = 1 + .3 = 1.3$$

$$\text{Stalls per access} = (1 - H1) \times (M \times \% \text{ clean} + 2M \times \% \text{ dirty})$$

$$\text{Stalls per access} = 1.5\% \times (50 \times 90\% + 100 \times 10\%) = .825 \text{ cycles}$$

$$\text{Mem Stalls per instruction} = 1.3 \times .825 = 1.07 \text{ cycles}$$

$$AMAT = 1 + .825 = 1.825 \text{ cycles}$$

$$CPI = 1.1 + 1.07 = 2.17$$

The ideal CPU with no misses is  $2.17/1.1 = 1.97$  times faster

77

### Impact of Cache Organization: An Example

#### Given:

- A CPI with ideal memory = 2.0      Clock cycle = 2 ns
- 1.3 memory references/instruction      Cache size = 64 KB with
- Cache miss penalty = 70 ns, no stall on a cache hit

#### Compare two caches

- One cache is direct mapped with miss rate = 1.4%
- The other cache is two-way set-associative, where:
  - CPU clock cycle time increases 1.1 times to account for the cache selection multiplexor
  - Miss rate = 1.0%

78

### Impact of Cache Organization: An Example

Average memory access time = Hit time + Miss rate  $\times$  Miss penalty

Average memory access time<sub>1-way</sub> =  $2.0 + (.014 \times 70) = 2.98$  ns

Average memory access time<sub>2-way</sub> =  $2.0 \times 1.1 + (.010 \times 70) = 2.90$  ns

CPU time = IC  $\times$  [CPI<sub>execution</sub> + Memory accesses/instruction  $\times$  Miss rate  $\times$  Miss penalty]  $\times$  Clock cycle time

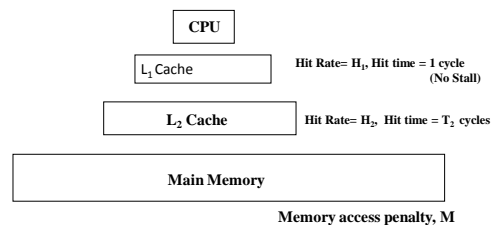
CPUtime<sub>1-way</sub> = IC  $\times$  ( $2.0 \times 2 + (1.3 \times .014 \times 70)$ ) =  $5.27 \times$  IC

CPUtime<sub>2-way</sub> = IC  $\times$  ( $2.0 \times 2 \times 1.10 + (1.3 \times 0.01 \times 70)$ ) =  $5.31 \times$  IC

- In this example, 1-way cache offers slightly better performance with less complex hardware.

79

### 2 Levels of Cache: $L_1, L_2$



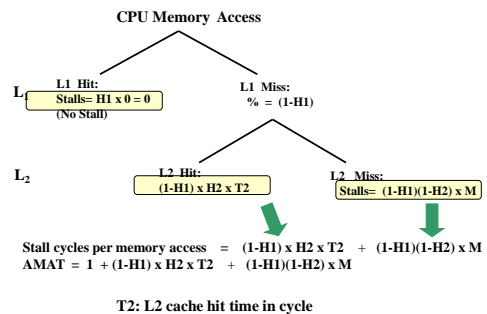
80

### Miss Rates For Multi-Level Caches

- Local Miss Rate: This rate is the number of misses in a cache level divided by the number of memory accesses to this level. Local Hit Rate =  $1 - \text{Local Miss Rate}$
- Global Miss Rate: The number of misses in a cache level divided by the total number of memory accesses generated by the CPU.
- Since level 1 receives all CPU memory accesses, for level 1:
  - Local Miss Rate = Global Miss Rate =  $1 - H_1$
- For level 2 since it only receives those accesses missed in level 1:
  - Local Miss Rate = Miss rate<sub>L2</sub> =  $1 - H_2$
  - Global Miss Rate = Miss rate<sub>L1</sub>  $\times$  Miss rate<sub>L2</sub> =  $(1 - H_1) \times (1 - H_2)$

81

### 2-Level Cache Performance Memory Access Tree



82

### 2-Level Cache Performance

CPUtime = IC  $\times$  (CPI<sub>execution</sub> + Mem Stall cycles per instruction)  $\times$  C

Mem Stall cycles per instruction = Mem accesses per instruction  $\times$  Stall cycles per access

- For a system with 2 levels of cache, assuming no penalty when found in  $L_1$  cache:
- Stall cycles per memory access =  

$$[\text{miss rate } L_1] \times [\text{Hit rate } L_2 \times \text{Hit time } L_2 + \text{Miss rate } L_2 \times \text{Memory access penalty}] = (1-H_1) \times H_2 \times T_2 + (1-H_1)(1-H_2) \times M$$

L1 Miss, L2 Hit

L1 Miss, L2 Miss:  
Must Access Main Memory

83

### Two-Level Cache Example

- CPU with CPI<sub>execution</sub> = 1.1 running at clock rate = 500 MHz
- 1.3 memory accesses per instruction.
- $L_1$  cache operates at 500 MHz with a miss rate of 5%
- $L_2$  cache operates at 250 MHz with local miss rate 40%, ( $T_2 = 2$  cycles)
- Memory access penalty,  $M = 100$  cycles. Find CPI.

CPI = CPI<sub>execution</sub> + MEM Stall cycles per instruction

With No Cache, CPI =  $1.1 + 1.3 \times 100 = 131.1$

With single  $L_1$ , CPI =  $1.1 + 1.3 \times .05 \times 100 = 7.6$

With  $L_1$  and  $L_2$  caches:

MEM Stall cycles per instruction =

MEM accesses per instruction  $\times$  Stall cycles per access

Stall cycles per memory access =  $(1-H_1) \times H_2 \times T_2 + (1-H_1)(1-H_2) \times M$

=  $.05 \times .6 \times 2 + .05 \times .4 \times 100$

=  $.06 + 2 = 2.06$

MEM Stall cycles per instruction =

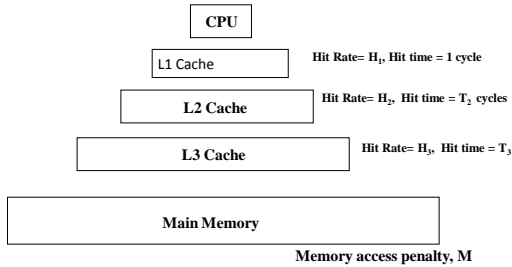
MEM accesses per instruction  $\times$  Stall cycles per access

=  $2.06 \times 1.3 = 2.678$

CPI =  $1.1 + 2.678 = 3.778$  Speedup =  $7.6/3.778 = 2$

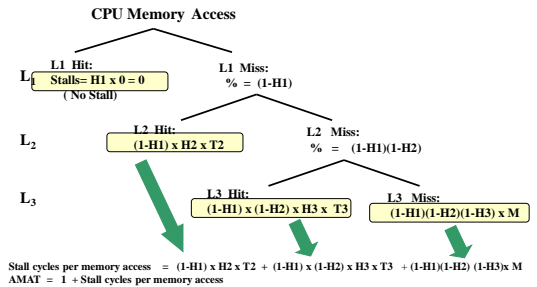
84

### 3 Levels of Cache



85

### 3-Level Cache Performance Memory Access Tree CPU Stall Cycles Per Memory Access



86

### 3-Level Cache Performance

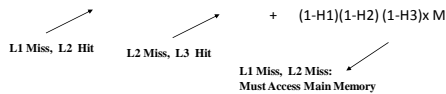
CPUtime = IC x (CPI<sub>execution</sub> + Mem Stall cycles per instruction) x C  
 Mem Stall cycles per instruction = Mem accesses per instruction x Stall cycles per access

- For a system with 3 levels of cache, assuming no penalty when found in L<sub>1</sub> cache:

Stall cycles per memory access =

$$[\text{miss rate } L_1] \times [\text{Hit rate } L_2 \times \text{Hit time } L_2 + \text{Miss rate } L_2 \times (\text{Hit rate } L_3 \times \text{Hit time } L_3 + \text{Miss rate } L_3 \times \text{Memory access penalty})] =$$

$$(1-H1) \times H2 \times T2 + (1-H1) \times (1-H2) \times H3 \times T3$$



87

### Three-Level Cache Example

- CPU with CPI<sub>execution</sub> = 1.1 running at clock rate = 500 MHZ
- 1.3 memory accesses per instruction.
- L<sub>1</sub> cache operates at 500 MHZ with a miss rate of 5%
- L<sub>2</sub> cache operates at 250 MHZ with a local miss rate 40%, (T<sub>2</sub> = 2 cycles)
- L<sub>3</sub> cache operates at 100 MHZ with a local miss rate 50%, (T<sub>3</sub> = 5 cycles)
- Memory access penalty, M= 100 cycles. Find CPI.

88

### Three-Level Cache Example

- Memory access penalty, M= 100 cycles. Find CPI.

With No Cache, CPI = 1.1 + 1.3 x 100 = 131.1

With single L<sub>1</sub>, CPI = 1.1 + 1.3 x .05 x 100 = 7.6

With L1, L2 CPI = 1.1 + 1.3 x (.05 x .6 x 2 + .05 x .4 x 100) = 3.778

CPI = CPI<sub>execution</sub> + Mem Stall cycles per instruction

Mem Stall cycles per instruction = Mem accesses per instruction x Stall cycles per access

$$\begin{aligned} \text{Stall cycles per memory access} &= (1-H1) \times H2 \times T2 + (1-H1) \times (1-H2) \times H3 \times T3 + (1-H1)(1-H2)(1-H3) \times M \\ &= .05 \times .6 \times 2 + .05 \times .4 \times .5 \times 5 + .05 \times .4 \times .5 \times 100 \\ &= .06 + .05 + 1 = 1.11 \end{aligned}$$

$$\text{CPI} = 1.1 + 1.3 \times 1.11 = 2.54$$

Speedup compared to L1 only = 7.6/2.54 = 3

Speedup compared to L1, L2 = 3.778/2.54 = 1.49

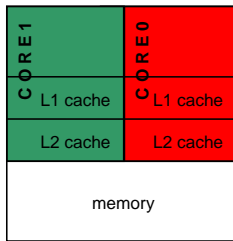
89

## Cache on Multicore

90

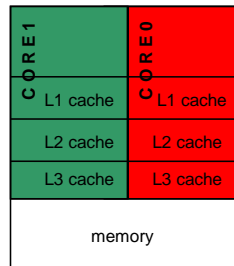
90

### Multi-Core and caches coherence



Both L1 and L2 are private

Examples: AMD Opteron,  
AMD Athlon, Intel Pentium D



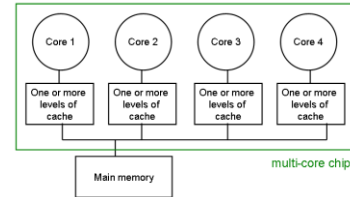
A design with L3 caches

Example: Intel Itanium 2

91

### The cache coherence problem

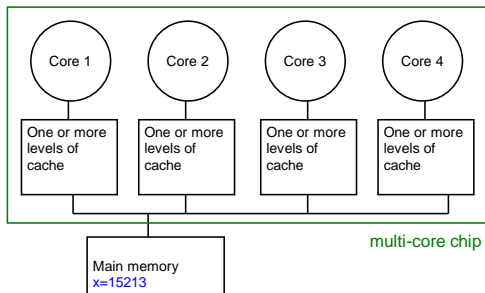
- Since we have private caches:  
How to keep the data consistent across caches?
- Each core should perceive the memory as a monolithic array, shared by all the cores



92

### The cache coherence problem

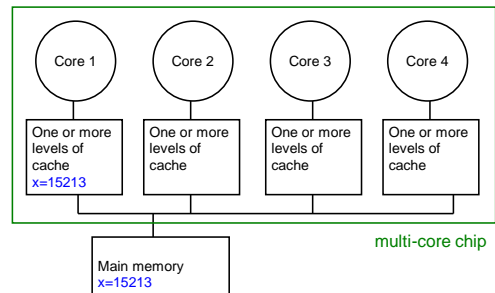
Suppose variable x initially contains 15213



93

### The cache coherence problem

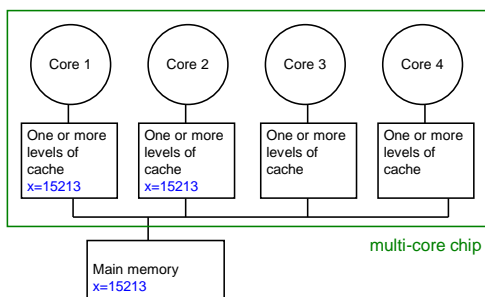
Core 1 reads x



94

### The cache coherence problem

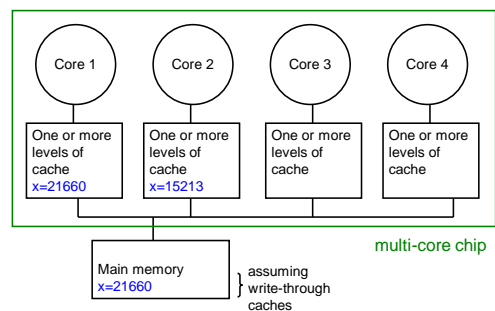
Core 2 reads x



95

### The cache coherence problem

Core 1 writes to x, setting it to 21660

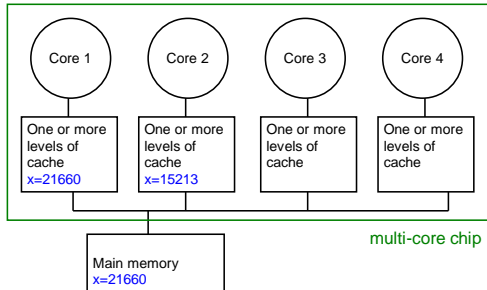


96



### The cache coherence problem

Core 2 attempts to read x... gets a stale copy



97

## Reduce Miss Rate

98

98

### Reducing Misses (3 Cs)

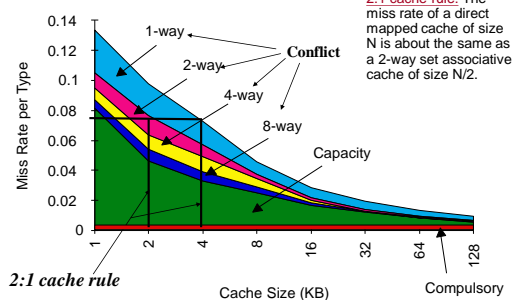
- Classifying Misses: 3 Cs

- Compulsory**—The first access to a block is not in the cache, so the block must be brought into the cache. These are also called *cold start misses* or *first reference misses*.  
(Misses even in infinite size cache)
- Capacity**—If the cache cannot contain all the blocks needed during the execution of a program, capacity misses will occur due to blocks being discarded and later retrieved.  
(Misses due to size of cache)
- Conflict**—If the block-placement strategy is not fully associative, conflict misses (in addition to compulsory and capacity misses) will occur because a block can be discarded and later retrieved if too many blocks map to its set. These are also called *collision misses* or *interference misses*.  
(Misses due to associativity and size of cache)

99

99

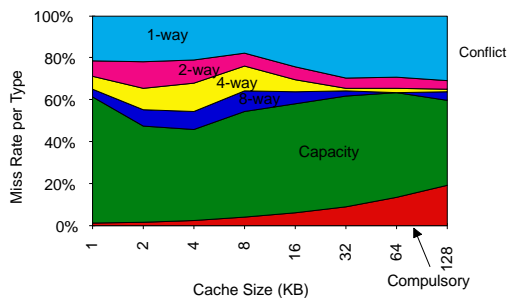
### 3Cs Absolute Miss Rates



100

100

### 3Cs Relative Miss Rate



101

101

### How to Reduce the 3 Cs Cache Misses?

- Increase Block Size
- Increase Associativity
- Use a Victim Cache
- Use a Pseudo Associative Cache
- Hardware Prefetching

102

102

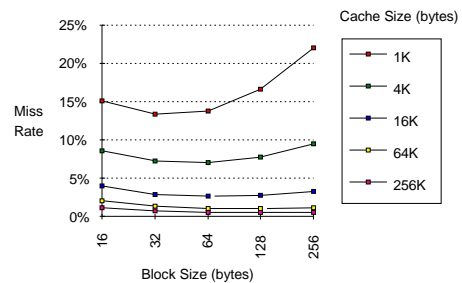
### 1. Increase Block Size

- One way to reduce the miss rate is to increase the block size
  - Take advantage of spatial locality
  - Reduce compulsory misses
- However, larger blocks have disadvantages
  - May increase the miss penalty (need to get more data)
  - May increase hit time
  - May increase conflict misses (smaller number of block frames)
- Increasing the block size can help, but don't overdo it.

103

103

### 1. Reduce Misses via Larger Block Size



104

104

### 2. Reduce Misses via Higher Associativity

- Increasing associativity helps reduce conflict misses (8-way should be good enough)
- 2:1 Cache Rule:
  - The miss rate of a direct mapped cache of size N is about equal to the miss rate of a 2-way set associative cache of size N/2
- Disadvantages of higher associativity
  - Need to do large number of comparisons
  - Need n-to-1 multiplexor for n-way set associative
  - Could increase hit time
    - Hit time for 2-way vs. 1-way external cache +10%, internal + 2%

105

105

### Example: Avg. Memory Access Time vs. Associativity

- Example: assume CCT = 1.10 for 2-way, 1.12 for 4-way, 1.14 for 8-way vs. CCT=1 of direct mapped.

(KB)	1-way	2-way	4-way	8-way
1	7.65	6.60	6.22	5.44
2	5.90	4.90	4.62	4.09
4	4.60	3.95	3.57	3.19
8	3.30	3.00	2.87	2.59
16	2.45	2.20	2.12	2.04
32	2.00	1.80	1.77	1.79
64	1.70	1.60	1.57	1.59
128	1.50	1.45	1.42	1.44

(Red means memory access time not improved by higher associativity)  
Does not take into account effect of slower clock on rest of program

106

106

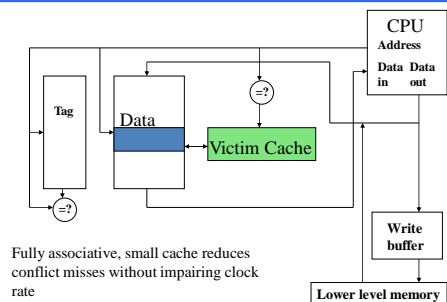
### 3. Reducing Misses via Victim Cache

- Add a small fully associative victim cache to hold data discarded from the regular cache
- When data not found in cache, check victim cache
- 4-entry victim cache removed 20% to 95% of conflicts for a 4 KB direct mapped data cache
- Get access time of direct mapped with reduced miss rate

107

107

### 3. Victim Cache



108

108

#### 4. Reducing Misses via Pseudo-Associativity

- How to combine fast hit time of direct mapped cache and the lower conflict misses of 2-way SA cache?
- Divide cache: on a miss, check other half of cache to see if there, if so have a **pseudo-hit** (slow hit).
- Usually check other half of cache by flipping the MSB of the index.

##### Drawbacks

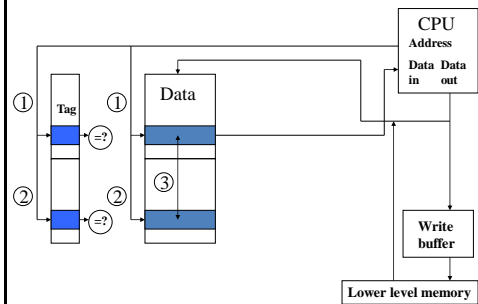
- CPU pipeline is hard if hit takes 1 or 2 cycles
- Slightly more complex design



109

109

#### Pseudo Associative Cache



110

110

#### 5. Hardware Prefetching

- Instruction Prefetching
  - Alpha 21064 fetches 2 blocks on a miss
  - Extra block placed in **stream buffer**
  - On miss check stream buffer
- Works with data blocks too:
  - 1 data stream buffer gets 25% misses from 4KB DM cache; 4 streams get 43%
  - For scientific programs: 8 streams got 50% to 70% of misses from 2 64KB, 4-way set associative caches
- Prefetching relies on having extra memory bandwidth that can be used without penalty

111

111

#### Summary

$$CPUtime = IC \times \left( CPI_{misses} + \frac{Memory\_accesses}{Instruction} \times Miss\_rate \times Miss\_penalty \right) \times Clock\_cycle\_time$$

- 3 Cs: Compulsory, Capacity, Conflict Misses
- Reducing Miss Rate
  - Larger Block Size
  - Higher Associativity
  - Victim Cache
  - Pseudo-Associativity
  - HW Prefetching Instr, Data

112

112

#### Pros and cons – Re-visit cache design choices

##### Larger cache block size

- Pros
  - Reduces miss rate
- Cons
  - Increases miss penalty

Important factors deciding cache performance: hit time, miss rate, miss penalty

113

113

#### Pros and cons – Re-visit cache design choices

##### Bigger cache

- Pros
  - Reduces miss rate
- Cons
  - May increase hit time
  - May increase cost and power consumption

114

114

### Pros and cons – Re-visit cache design choices

#### Higher associativity

- Pros
  - Reduces miss rate
- Cons
  - Increases hit time

115

115

### Pros and cons – Re-visit cache design choices

#### Multiple levels of caches

- Pros
  - Reduces miss penalty
- Cons
  - Increases cost and power consumption

116

116

### Multilevel Cache Design Considerations

- Design considerations for L1 and L2 caches are very different
  - Primary cache should focus on **minimizing hit time** in support of a shorter clock cycle
    - Smaller cache with smaller block sizes
  - Secondary cache (s) should focus on **reducing miss rate** to reduce the penalty of long main memory access times
    - Larger cache with larger block sizes and/or higher associativity

117

### Key Cache Design Parameters

	L1 typical	L2 typical
Total size (blocks)	250 to 2000	4000 to 250,000
Total size (KB)	16 to 64	500 to 8000
Block size (B)	32 to 64	32 to 128
Miss penalty (clocks)	10 to 25	100 to 1000
Miss rates (global for L2)	2% to 5%	0.1% to 2%

118

### Reducing Miss rate with programming

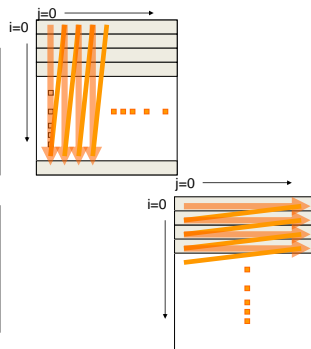
Examples:  
cold cache, 4-byte words, 4-word cache blocks

```
int sumarraycols(int a[M][N])
{
    int i, j, sum = 0;
    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];
    return sum;
}
```

Miss rate = **~100%**

```
int sumarrayrows(int a[M][N])
{
    int i, j, sum = 0;
    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];
    return sum;
}
```

119 Miss rate = **~1/N**



### Reducing Miss Penalty

120

120

### The cost of a cache miss

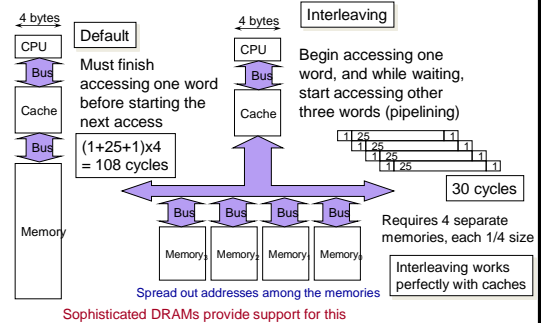
- For a memory access, assume:
  - 1 clock cycle to send address to memory
  - 25 clock cycles for each DRAM access (clock cycle 2ns, 50 ns access time)
  - 1 clock cycle to send each resulting data word
- Miss access time (4-word block)
  - $4 \times (\text{Address} + \text{access} + \text{sending data word})$
  - $4 \times (1 + 25 + 1) = 108$
  - = 108 cycles for each miss

This actually depends on the bus speed

121

121

### Memory Interleaving



122

122

### Memory Interleaving: An Example

Given the following system parameters with single cache level  $L_1$ :

Block size=1 word Memory bus width=1 word Miss rate =3% Miss penalty=27 cycles  
 (1 cycle to send address 25 cycles access time/word, 1 cycle to send a word)  
 Memory access/instruction = 1.2 Ideal CPI (ignoring cache misses) = 2  
 Miss rate (block size=2 words) = 2% Miss rate (block size=4 words) =1%

- The CPI of the base machine with 1-word blocks =  $2 + (1.2 \times 0.03 \times 27) = 2.97$
- Increasing the block size to two words gives the following CPI:
  - 32-bit bus and memory, no interleaving =  $2 + (1.2 \times .02 \times 2 \times 27) = 3.29$
  - 32-bit bus and memory, interleaved =  $2 + (1.2 \times .02 \times (28)) = 2.67$
- Increasing the block size to four words; resulting CPI:
  - 32-bit bus and memory, no interleaving =  $2 + (1.2 \times 0.01 \times 4 \times 27) = 3.29$
  - 32-bit bus and memory, interleaved =  $2 + (1.2 \times 0.01 \times (30)) = 2.36$

123

123

### Summary

$$CPUtime = IC \times \left( CPI_{\text{misses}} + \frac{\text{Memory accesses}}{\text{Instruction}} \times \text{Miss rate} \times \text{Miss penalty} \right) \times \text{Clock cycle time}$$

- Interleaving
- Multiple levels of caches
- Other advanced techniques...

124

124

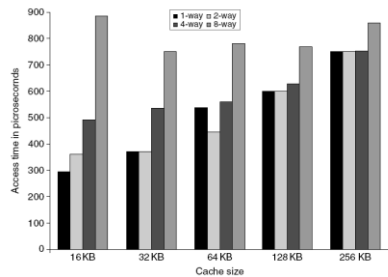
### Cache Optimization

- Six basic cache optimizations:
  - Larger block size
    - Reduces compulsory misses
    - Increases capacity and conflict misses, increases miss penalty
  - Larger total cache capacity to reduce miss rate
    - Increases hit time, increases power consumption
  - Higher associativity
    - Reduces conflict misses
    - Increases hit time, increases power consumption
  - Higher number of cache levels
    - Reduces overall memory access time
  - Giving priority to read misses over writes
    - Reduces miss penalty
  - Avoiding address translation in cache indexing
    - Reduces hit time

### Ten Advanced Optimizations

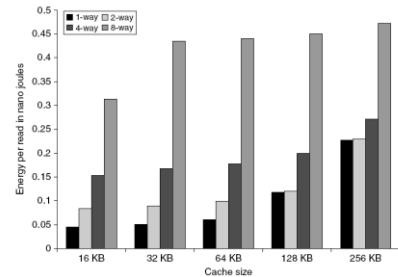
- Small and simple first level caches
  - Critical timing path:
    - addressing tag memory, then
    - comparing tags, then
    - selecting correct set
  - Direct-mapped caches can overlap tag compare and transmission of data
  - Lower associativity reduces power because fewer cache lines are accessed

### L1 Size and Associativity



Access time vs. size and associativity

### L1 Size and Associativity



Energy per read vs. size and associativity

### Way Prediction

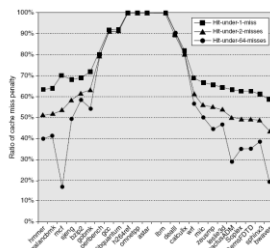
- To improve hit time, predict the way to pre-set mux
  - Mis-prediction gives longer hit time
  - Prediction accuracy
    - > 90% for two-way
    - > 80% for four-way
    - I-cache has better accuracy than D-cache
  - First used on MIPS R10000 in mid-90s
  - Used on ARM Cortex-A8
- Extend to predict block as well
  - "Way selection"
  - Increases mis-prediction penalty

### Pipelining Cache

- Pipeline cache access to improve bandwidth
  - Examples:
    - Pentium: 1 cycle
    - Pentium Pro – Pentium III: 2 cycles
    - Pentium 4 – Core i7: 4 cycles
- Increases branch mis-prediction penalty
- Makes it easier to increase associativity

### Nonblocking Caches

- Allow hits before previous misses complete
  - "Hit under miss"
  - "Hit under multiple miss"
- L2 must support this
- In general, processors can hide L1 miss penalty but not L2 miss penalty



### Multibanked Caches

- Organize cache as independent banks to support simultaneous access
  - ARM Cortex-A8 supports 1-4 banks for L2
  - Intel i7 supports 4 banks for L1 and 8 banks for L2
- Interleave banks according to block address

Block address	Bank 0	Block address	Bank 1	Block address	Bank 2	Block address	Bank 3
0		1		2		3	
4		5		6		7	
8		9		10		11	
12		13		14		15	

Figure 2.6 Four-way interleaved cache banks using block addressing. Assuming 64 bytes per blocks, each of these addresses would be multiplied by 64 to get byte addressing.

### Critical Word First, Early Restart

- Critical word first
  - Request missed word from memory first
  - Send it to the processor as soon as it arrives
- Early restart
  - Request words in normal order
  - Send missed work to the processor as soon as it arrives
- Effectiveness of these strategies depends on block size and likelihood of another access to the portion of the block that has not yet been fetched

### Merging Write Buffer

- When storing to a block that is already pending in the write buffer, update write buffer
- Reduces stalls due to full write buffer
- Do not apply to I/O addresses

Write address	V	V	V	V	
100	1	Mem[100]	0	0	0
108	1	Mem[108]	0	0	0
116	1	Mem[116]	0	0	0
124	1	Mem[124]	0	0	0

No write buffering

Write address	V	V	V	V				
100	1	Mem[100]	1	Mem[108]	1	Mem[116]	1	Mem[124]
	0	0		0	0		0	
	0	0		0	0		0	
	0	0		0	0		0	

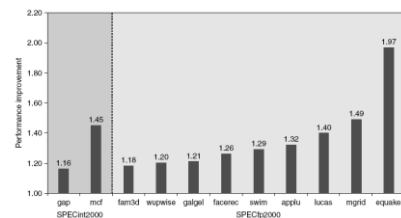
Write buffering

### Compiler Optimizations

- Loop Interchange
  - Swap nested loops to access memory in sequential order
- Blocking
  - Instead of accessing entire rows or columns, subdivide matrices into blocks
  - Requires more memory accesses but improves locality of accesses

### Hardware Prefetching

- Fetch two blocks on miss (include next sequential block)



Pentium 4 Pre-fetching

### Compiler Prefetching

- Insert prefetch instructions before data is needed
- Non-faulting: prefetch doesn't cause exceptions
- Register prefetch
  - Loads data into register
- Cache prefetch
  - Loads data into cache
- Combine with loop unrolling and software pipelining

### Summary

Technique	Hit time	Bandwidth	Miss rate	Power consumption	Hardware cost/complexity	Comment
Small and simple caches	+	–	–	+	0	Trivial, widely used
Way-predicting caches	+	–	–	+	1	Used in Pentium 4
Pipelined cache access	–	+	–	–	1	Widely used
Nonblocking caches	+	+	–	–	3	Widely used
Banked caches	+	–	–	+	1	Used in L2 of both i7 and Core i7
Critical word first and early restart	–	–	–	–	2	Widely used
Merging write buffer	–	–	–	–	1	Widely used with write-through
Compiler techniques to reduce cache misses	–	–	–	–	0	Software is a challenge, but many compilers handle common linear algebra calculations
Hardware prefetching of instructions and data	+	+	–	–	2 (instr., 3 data)	Most provide prefetch instructions; modern high-end processors also automatically prefetch in hardware
Compiler-controlled prefetching	–	–	–	–	3	Needs nonlocking cache; possible instruction overhead in many CPUs

Figure 2.11 Summary of 10 advanced cache optimizations showing impact on cache performance, power consumption, and complexity. Although generally a technique helps only one factor, prefetching can reduce misses if done sufficiently early. If not, it can reduce miss penalty. + means the technique improves the factor, – means it hurts that factor, and blank means it has no impact. The complexity measure is subjective, with 0 being the easiest and 3 being a challenge.