



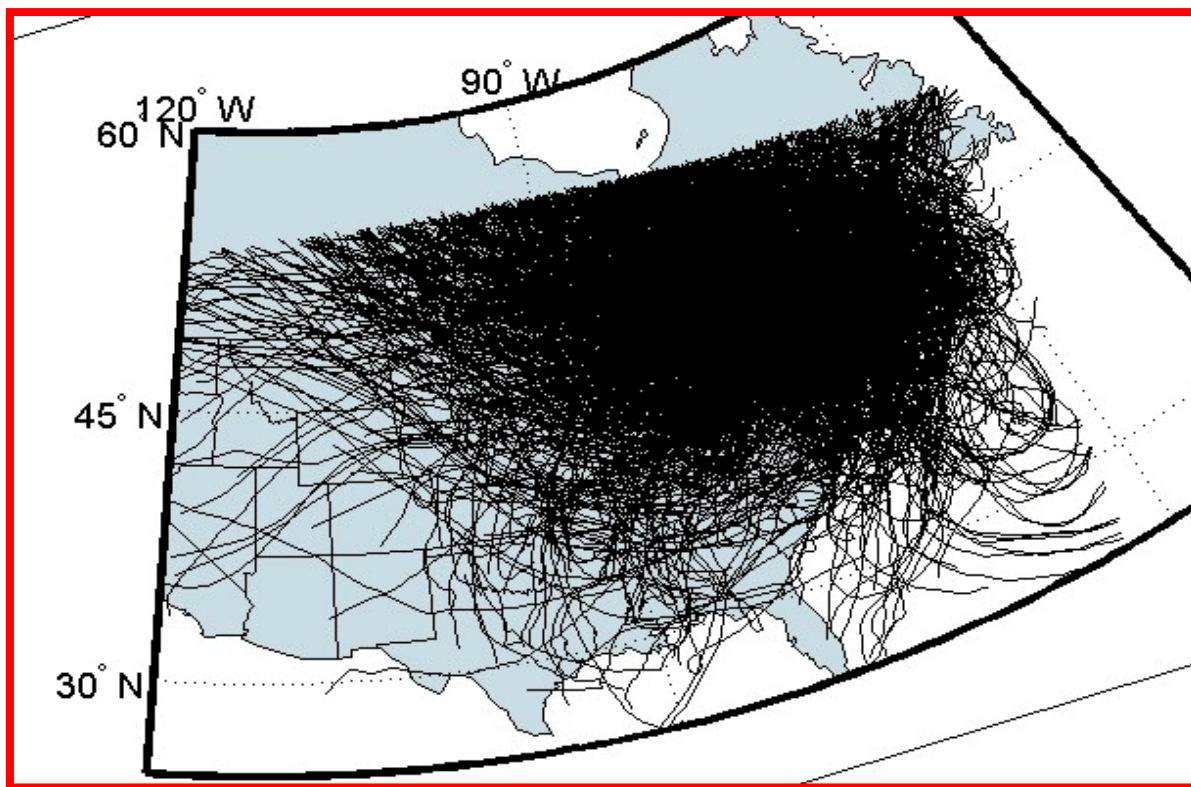
Trajectory Clustering Techniques

*Gary Kleiman, John Graham, Iyad Kheirbek,
Nicolas Hamel, Jaime Lehner, and Ingrid Ulbrich*
NESCAUM

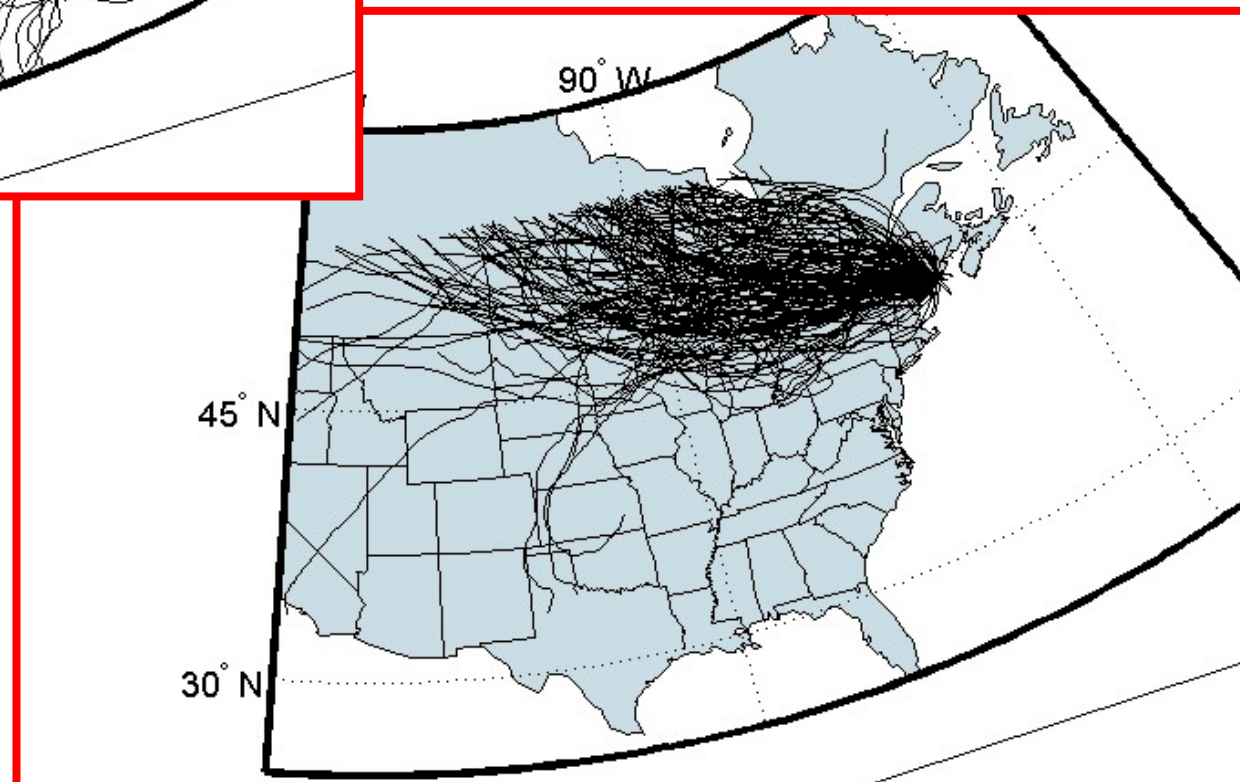
**Air and Waste Management Association
Visibility Specialty Conference
October 27, 2004**

ALL TRAJECTORIES

Acadia 1997



CLUSTER 3 TRAJECTORIES



PATH Analysis

- Patterns in Atmospheric Transport History
- Based on prior work by Jenny Moody (UVA) at Harvard Forest in Central MA
- Groups similar trajectories in 3-dimensions

PATH Algorithm

- Similarity quantified as distance between trajectories:

$$D_{ij} = \sqrt{\sum_{k=1}^n (Z_{ik}^{lat} - Z_{jk}^{lat})^2 + (Z_{ik}^{lon} - Z_{jk}^{lon})^2 + (Z_{ik}^{press} - Z_{jk}^{press})^2}$$

(Z represent **normalized** coordinates with 0 mean and standard deviation of 1)

Cluster Definition

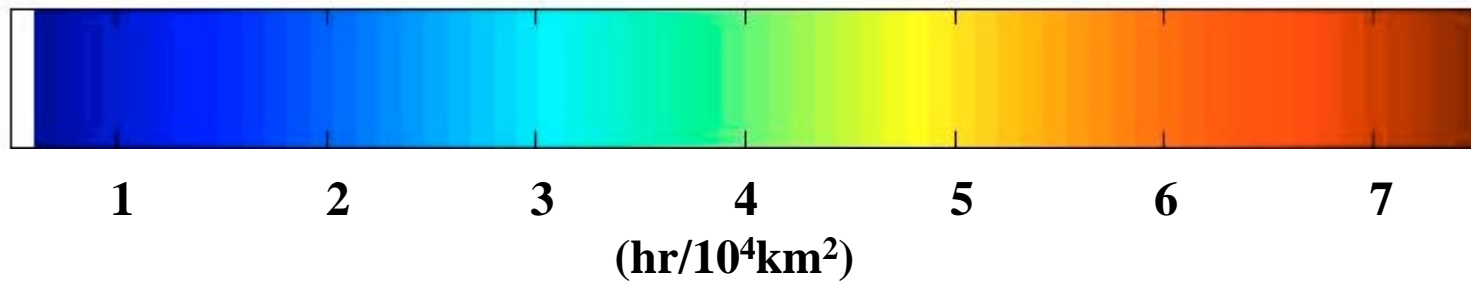
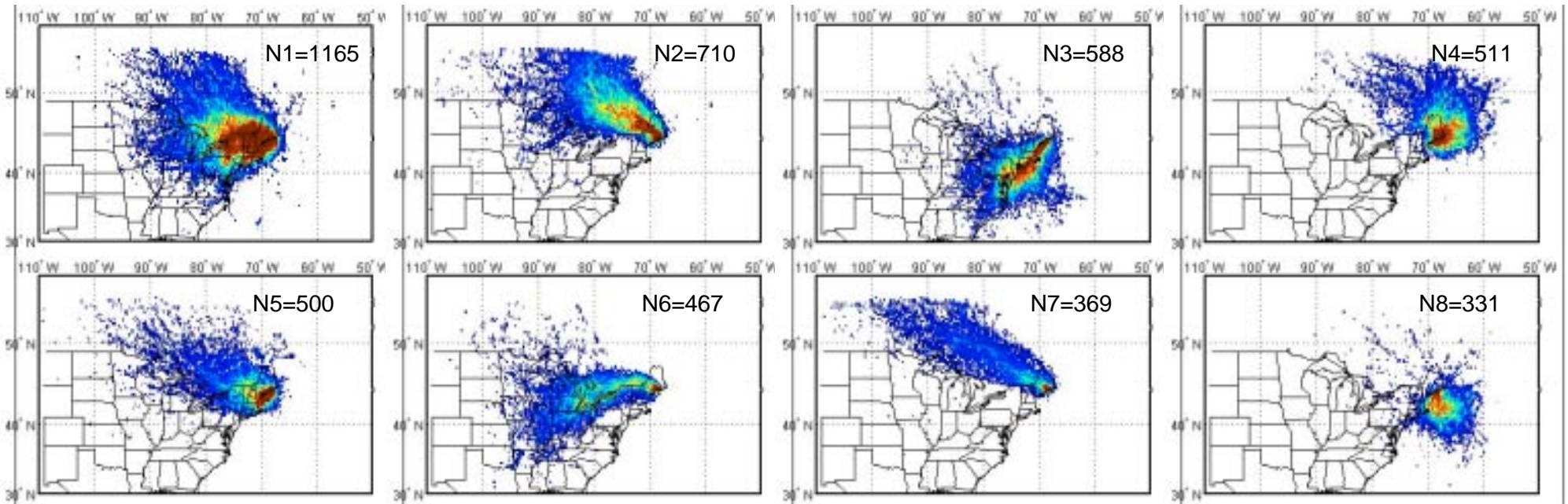
- Clusters are defined by establishing a radius of proximity R :

$$C(T_i) = \{ T_j \} \ni D_{ij} \leq R$$

The maximal cluster (largest number of elements) is removed from the analysis and the process is repeated

Top 8 Clusters for Acadia

Acadia, 1997-2002, 48hr, 500m, **R=6**

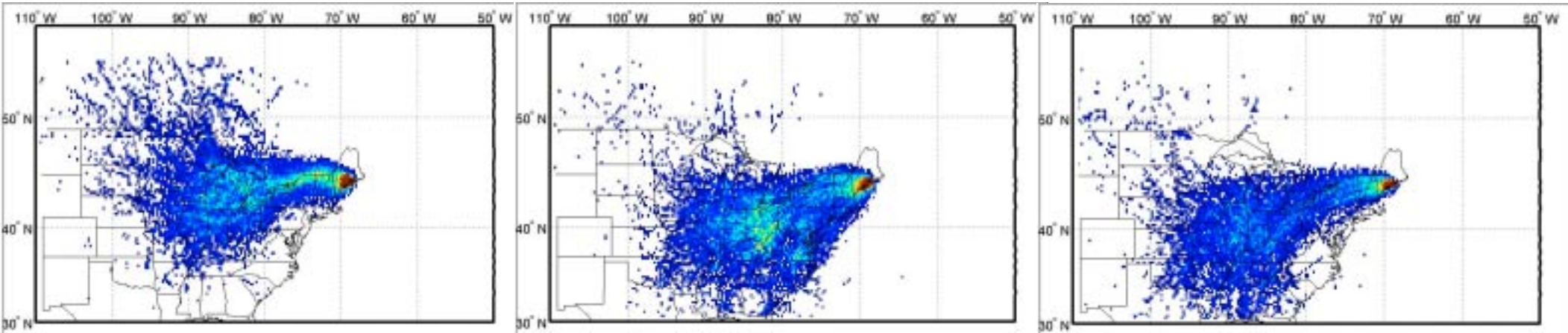


Free Parameters

- Radius of proximity
- Height of starting point
- Length of cluster calculation (e.g. 24 hr, 48 hr, 120hr)
- Temporal range (e.g. 97 vs. 97-02)
- Receptor site
- Resolution/completeness of met data

Starting height

Acadia, 1997-2002, 48hr, **200/500/1000m**, R=10



Cluster 5

Receptor Level= 200m

Mean Height= 892 m

Cluster 4

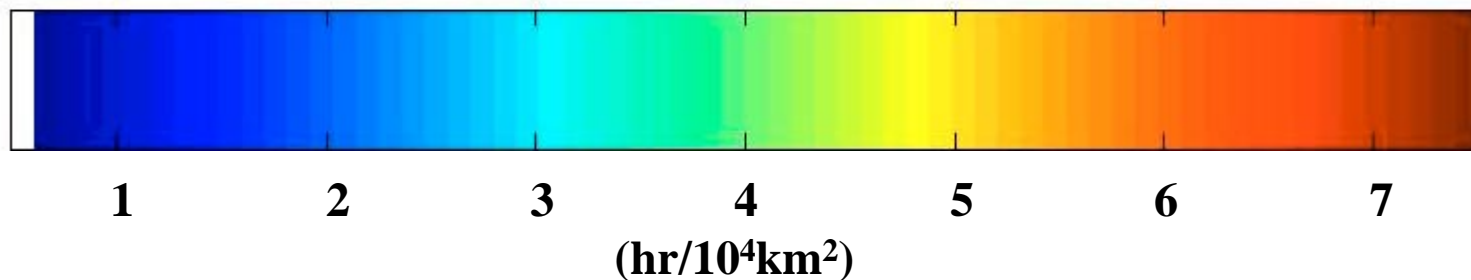
Receptor Level= 500m

Mean Height= 867 m

Cluster 5

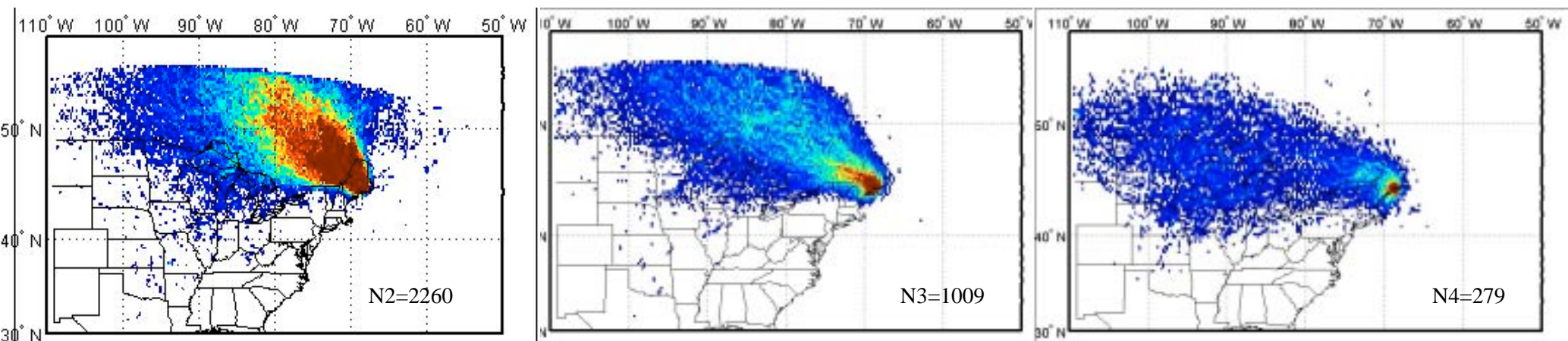
Receptor Level= 1000m

Mean Height= 1247 m



Length of cluster

Acadia, 1997-2002, **24/48/120hr**, 500m, R=6,10,16



Total Trajectories in 24 hr
Analysis = **14235 (99-02)**

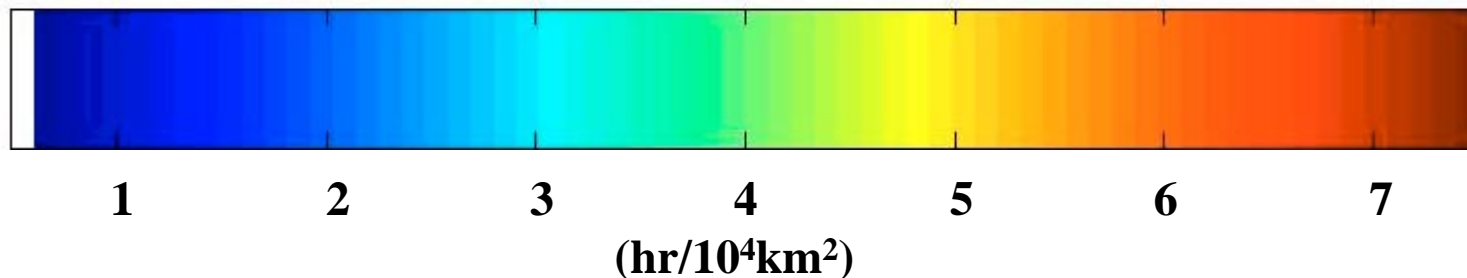
Mean Height= 1286 m

Total Trajectories in 48 hr
Analysis = **10592**

Mean Height= 1916 m

Total Trajectories in 120 hr
Analysis = **4429**

Mean Height= 1692 m

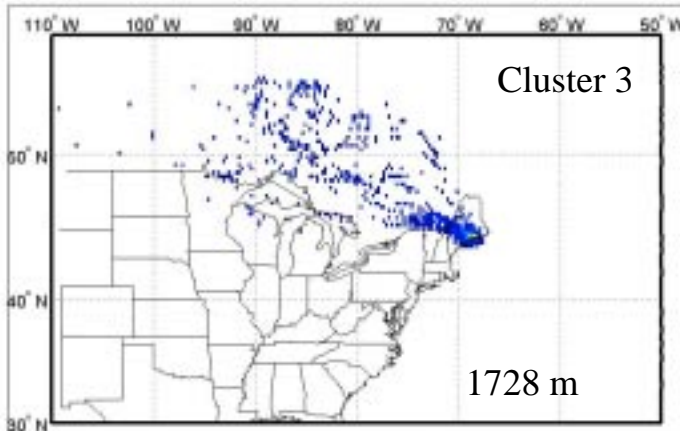


Temporal range

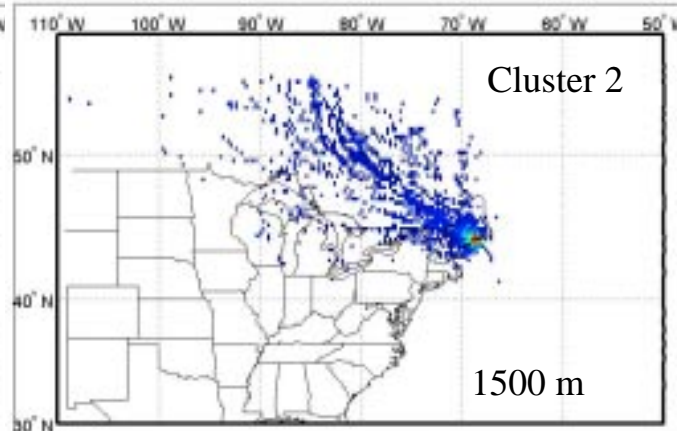


Acadia, **97/98/99/00/01/02/97-02**, 48hr, 500m, R=10

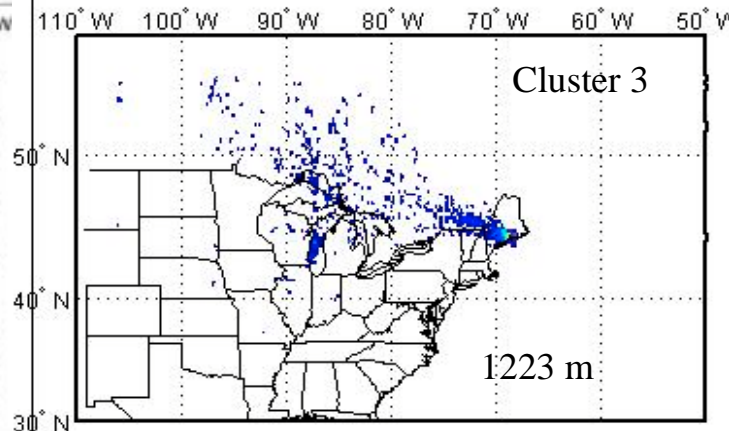
1997



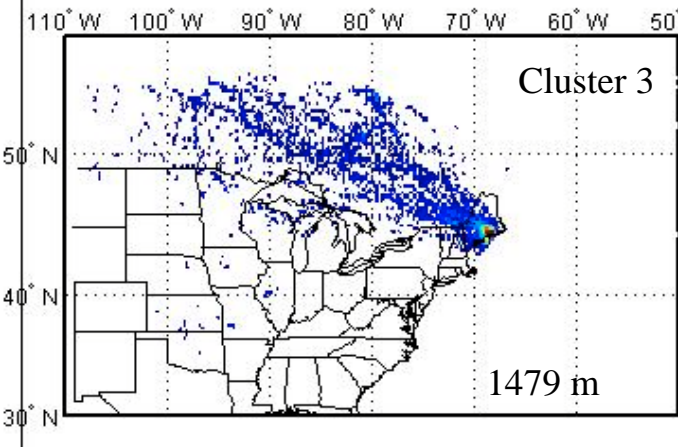
1998



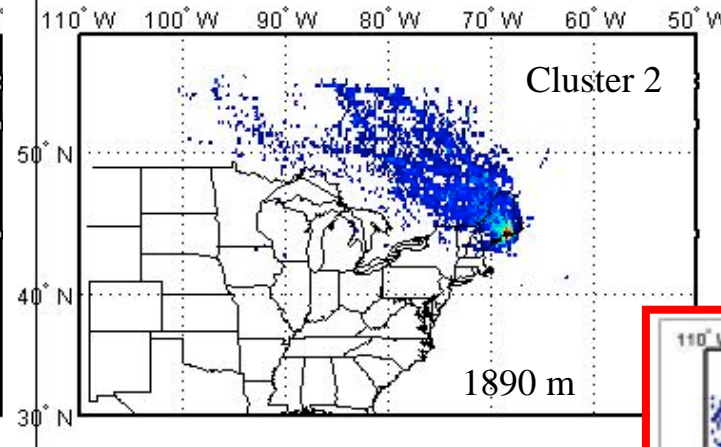
1999



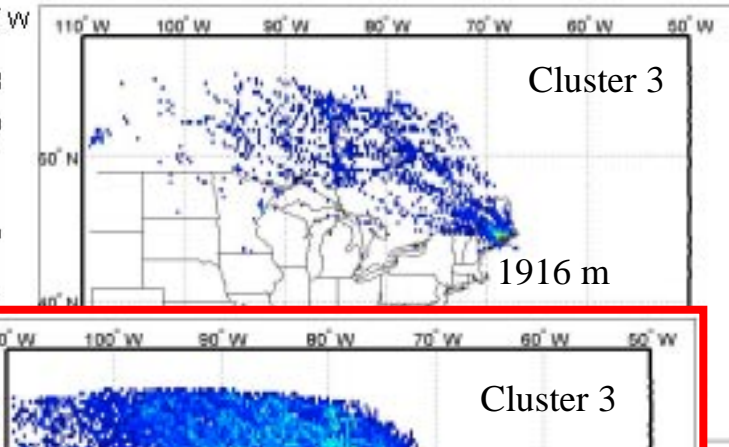
2000



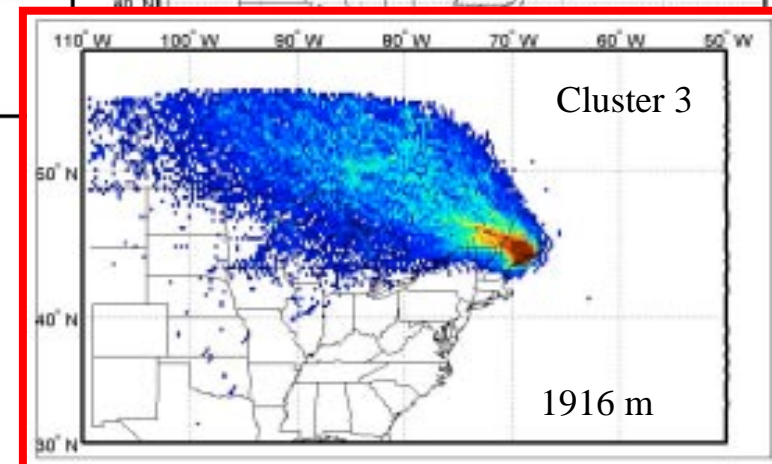
2001



2002



1997-2002

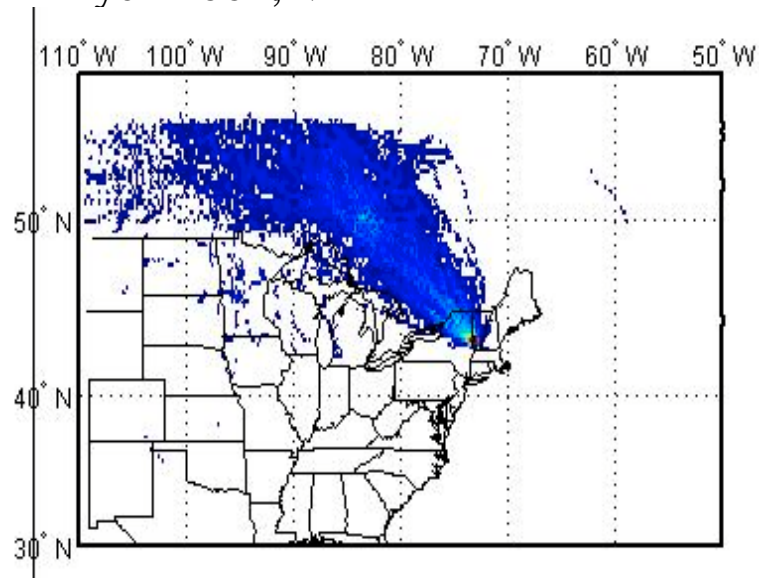


Atmospheric Modes vs. Clusters

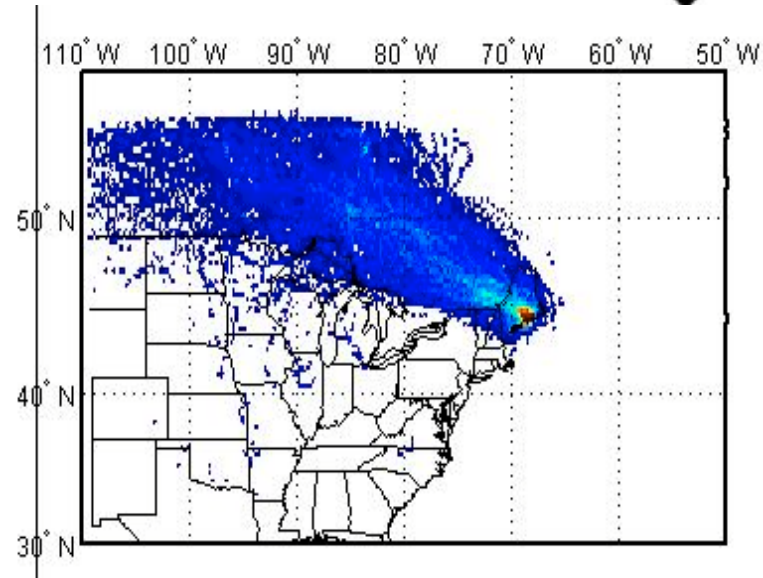
- *Clusters* are defined as groupings of similar trajectories during a specific time period
- *Atmospheric modes* describes the underlying meteorological phenomena that explain the observed clusters

Northwest Fast (NWF)

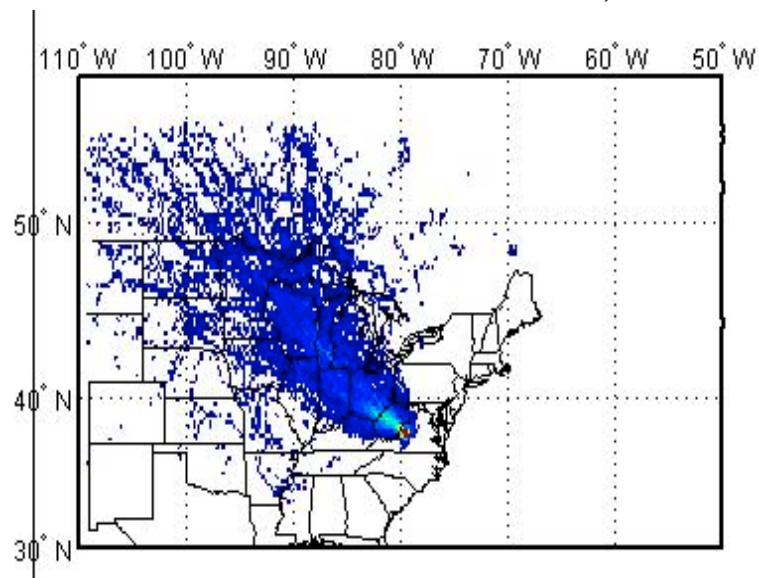
Lye Brook, VT



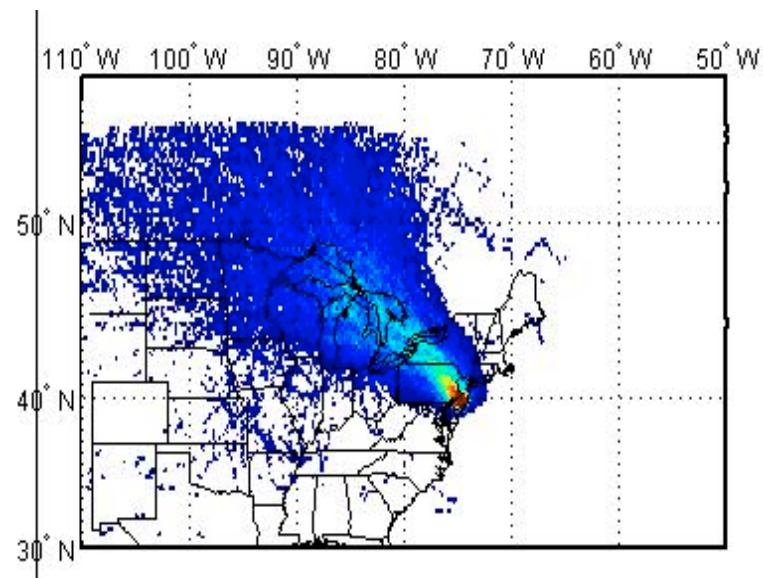
Acadia, ME



Jefferson/James River Face, VA

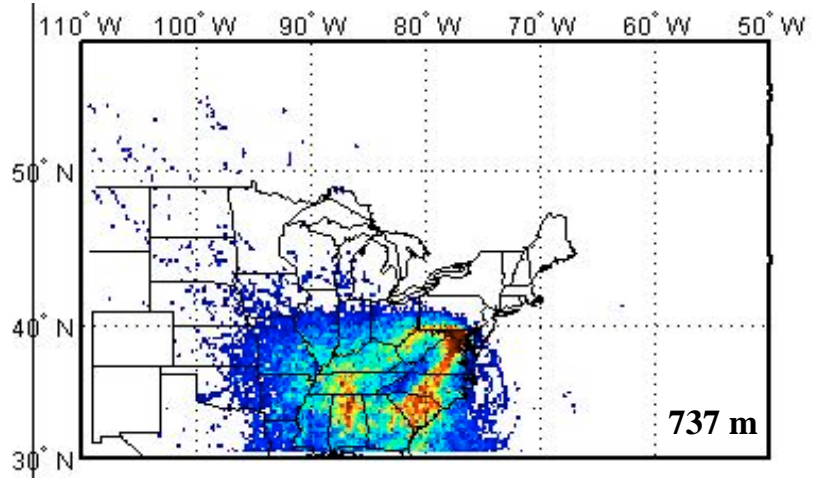


Brigantine, NJ



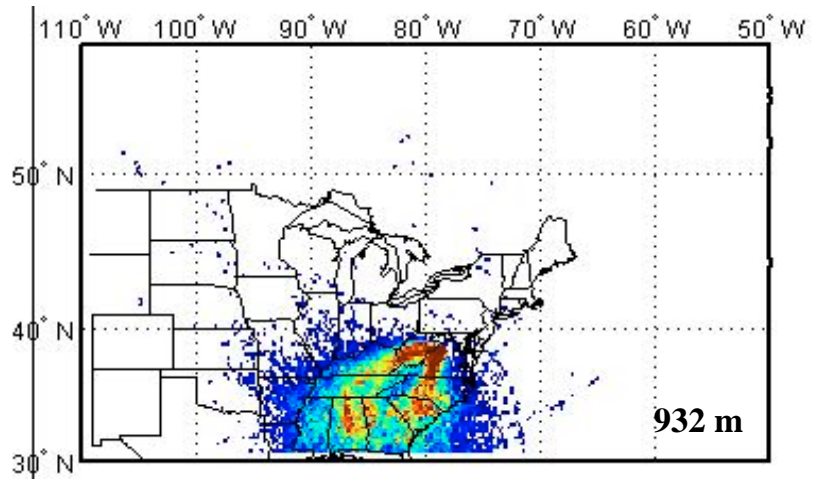
Southwest Bi-modal (SWB)

Baltimore



- Represents a mix of southwest coastal and southwest inland

Shenandoah



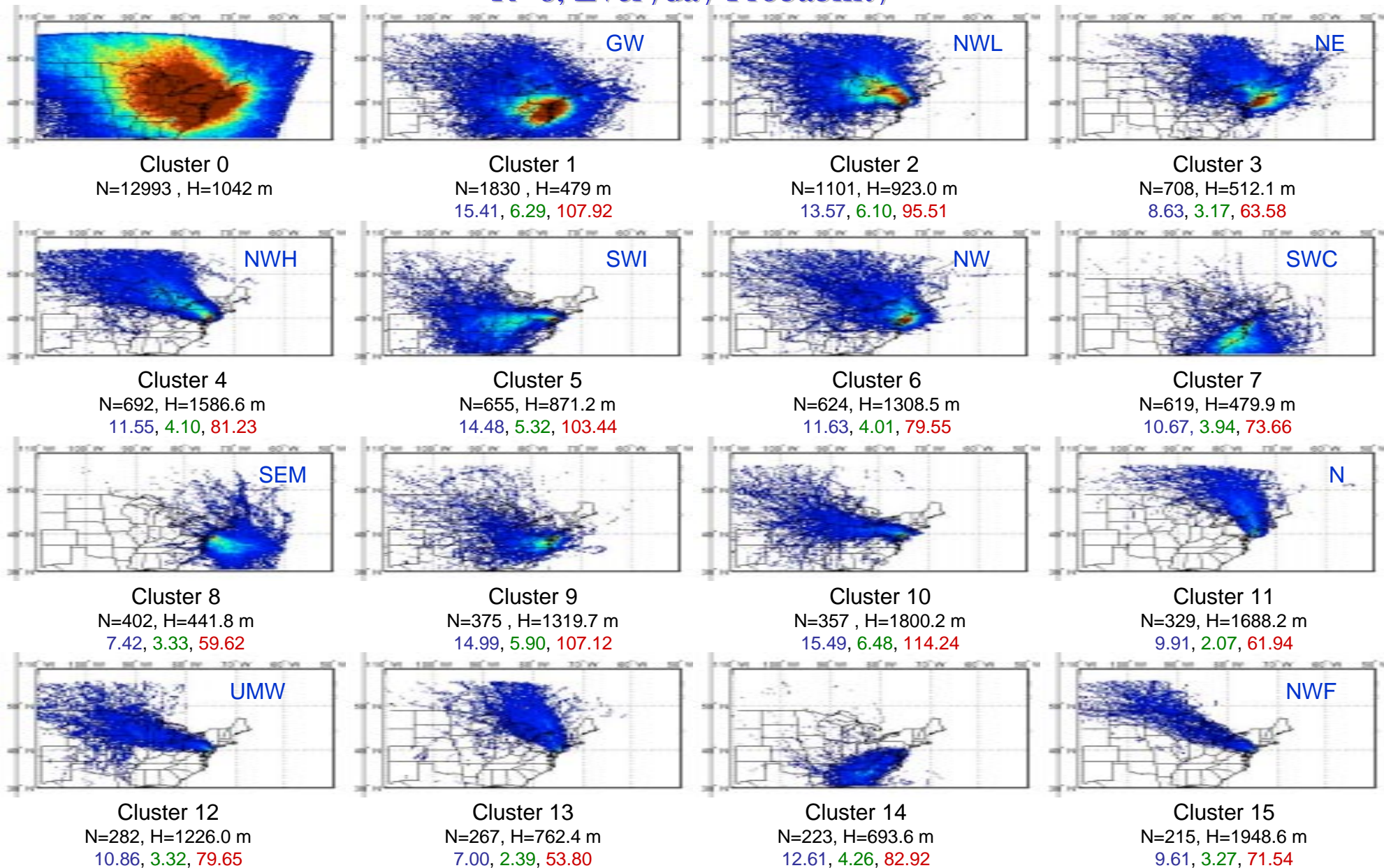
Predominant Meteorological Pathways and Influence on Air Quality



- Back-trajectory Clusters
- Pollution-Date Database
- Correlate dates to establish relationships between atmospheric modes and pollution tendencies

Brigantine 97-02 EDAS- 48 hrs

R=6, Everyday Probability



1997-2002 IMPROVE Averages:

Total $PM_{2.5}$ ($\mu g/m^3$)

$PM_{2.5}$ SO_4 ($\mu g/m^3$)

Reconstructed Extinction (Mm^{-1})

Trajectory Analysis: Multiple Metrics

Everyday Residence-time Probability

$$EP = \left(\frac{n_{ij}}{N} \right)$$

n_{ij} = total endpoints passing through grid cell i, j

N = total endpoints passing through all grid cells from all trajectories

High Day Residence-time Probability

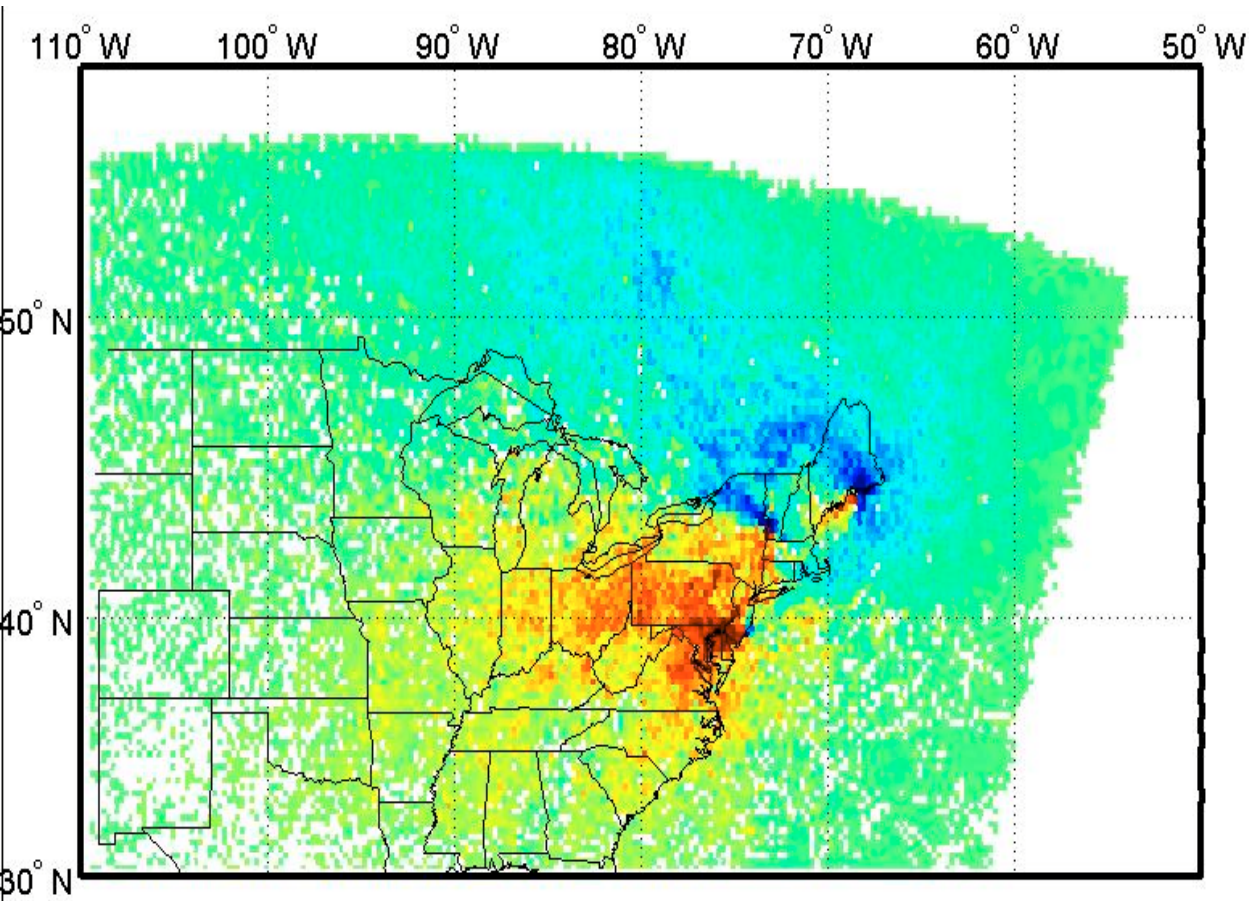
$$HP = \left(\frac{m_{ij}}{M} \right)$$

m_{ij} = total high day endpoints passing through grid cell i, j

M = total high day endpoints passing through all grid cells from high day trajectories

Trajectory Analysis: Multiple Metrics

Incremental Probability



$$IP = HP - EP$$

3-site average:
Acadia, Lye Brook, and Brigantine



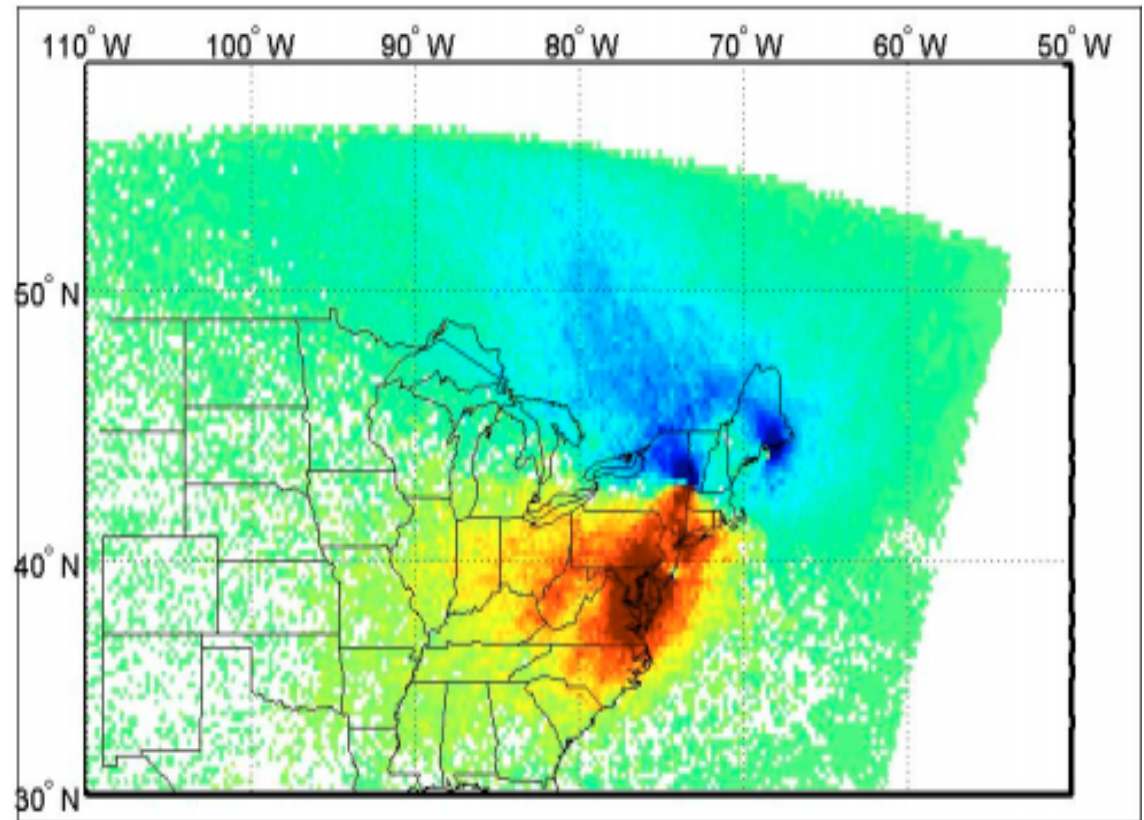
Trajectory Analysis: Multiple Metrics

Clustered Incremental Probability

$$CIP = \sum_{k \in K} RP_k - EP$$

K = Subset of clusters, 20% worst pollution days

RP_k = Residence - time probability for cluster k

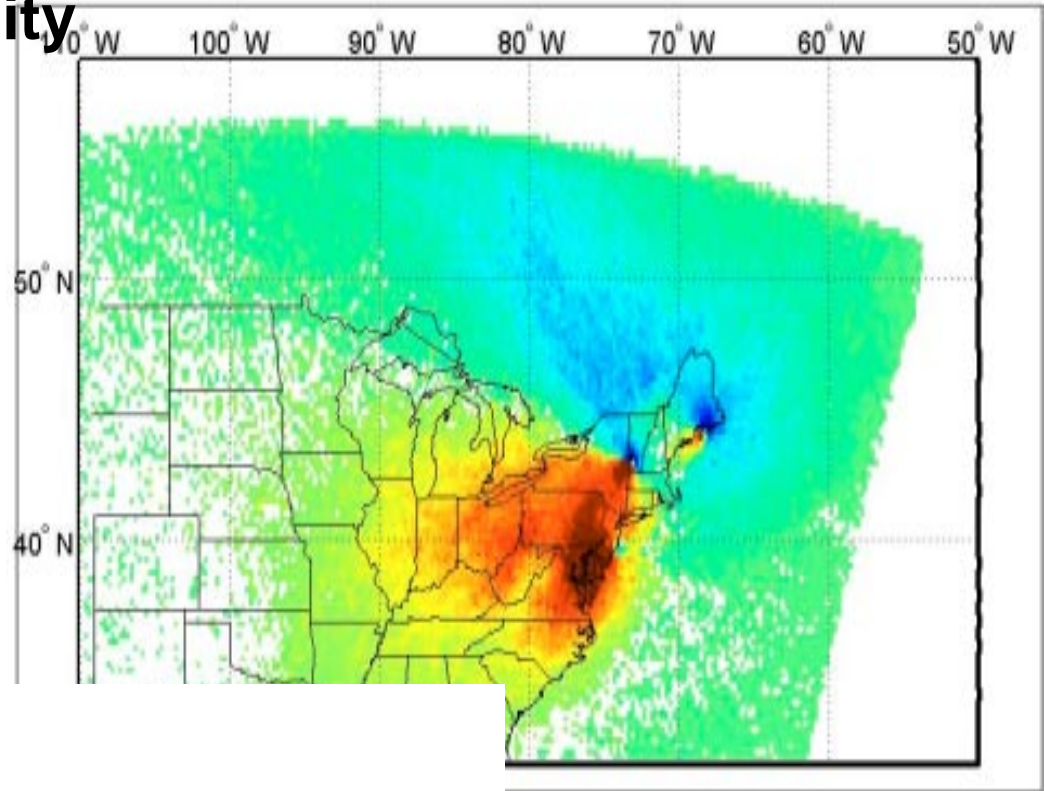


3-site average:
Acadia, Lye Brook, and Brigantine



Trajectory Analysis: Multiple Metrics

Cluster-Weighted Probability



$$CWP = \frac{1}{\bar{C}} \left(\sum_{i=1}^L (\bar{C})_i \cdot RP_i - \bar{C} \cdot EP \right)$$

L = total number of clusters calculated

$(\bar{C})_i$ = Average concentration (obs associated with cluster i)

\bar{C} = Average concentration (all days)

3-site average:

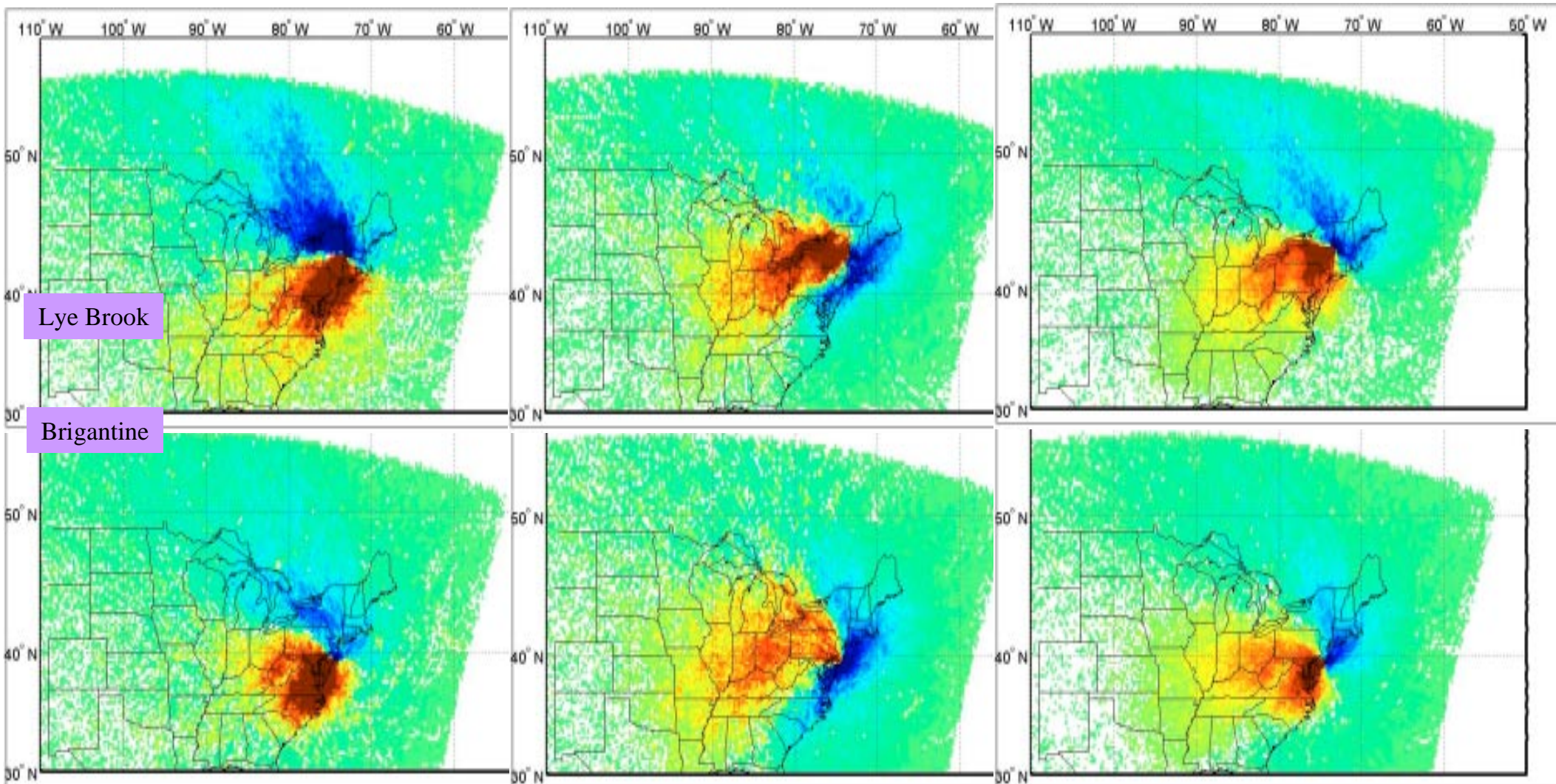
Acadia, Lye Brook, and Brigantine

Distribution of CIP for Sulfate Transport

Worst 20% days

Second worst 20% days

Worst 40% days

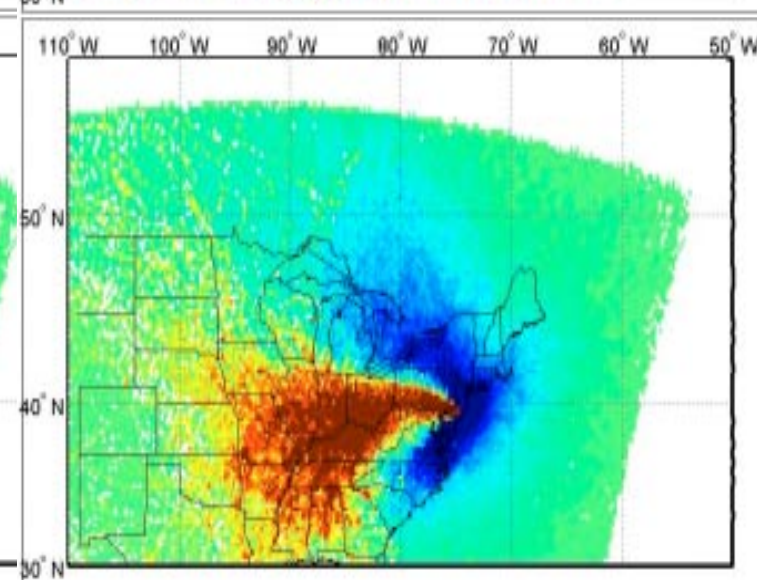
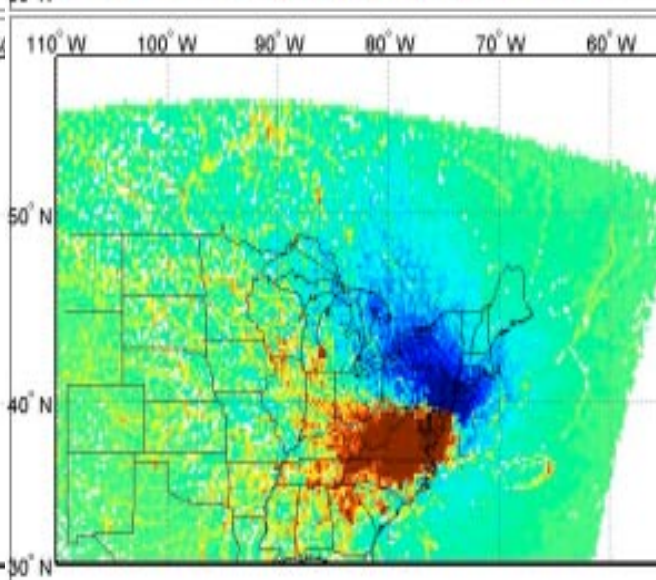
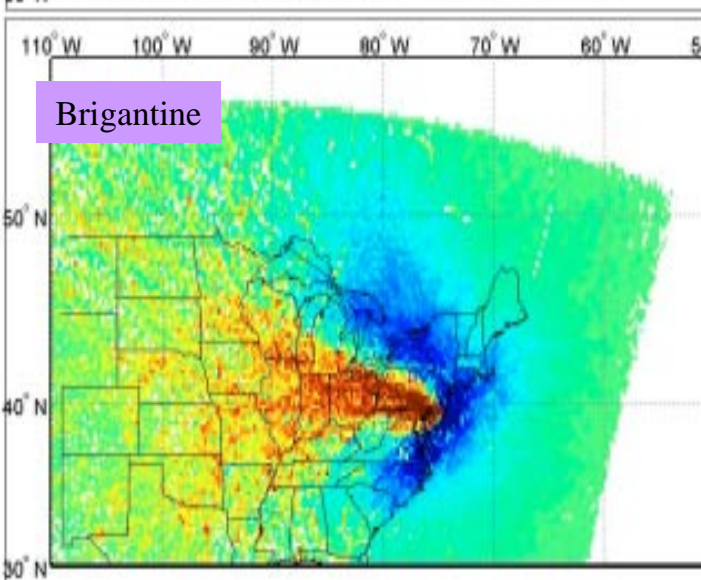
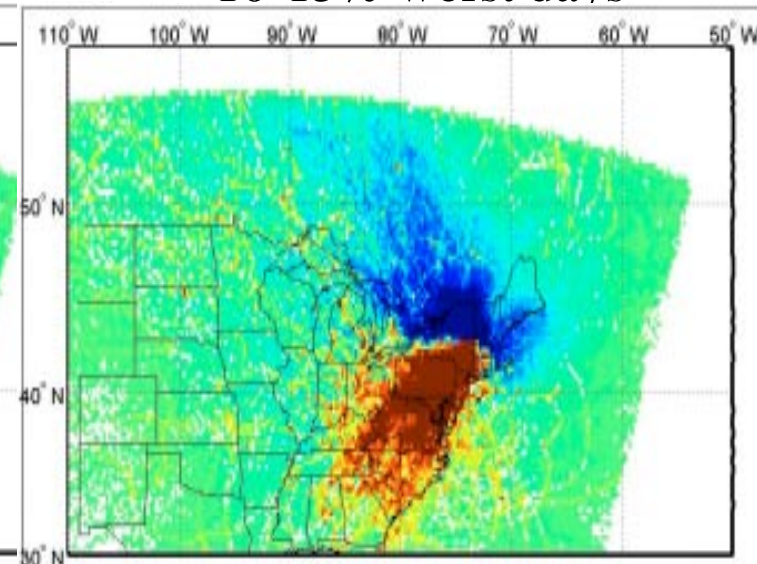
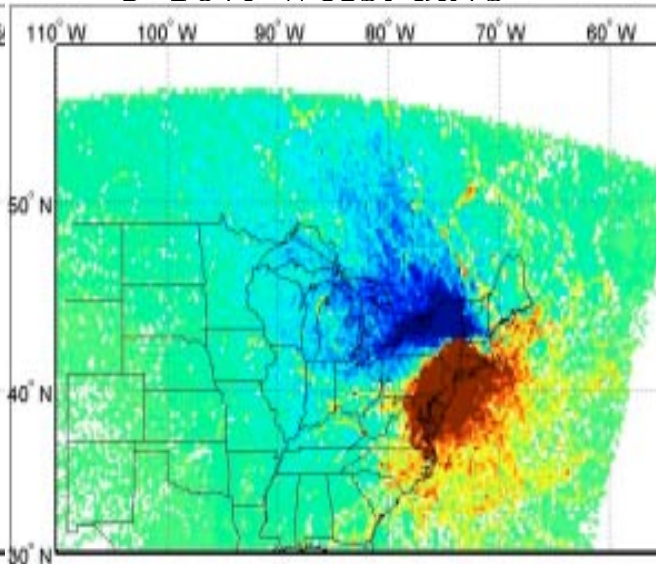
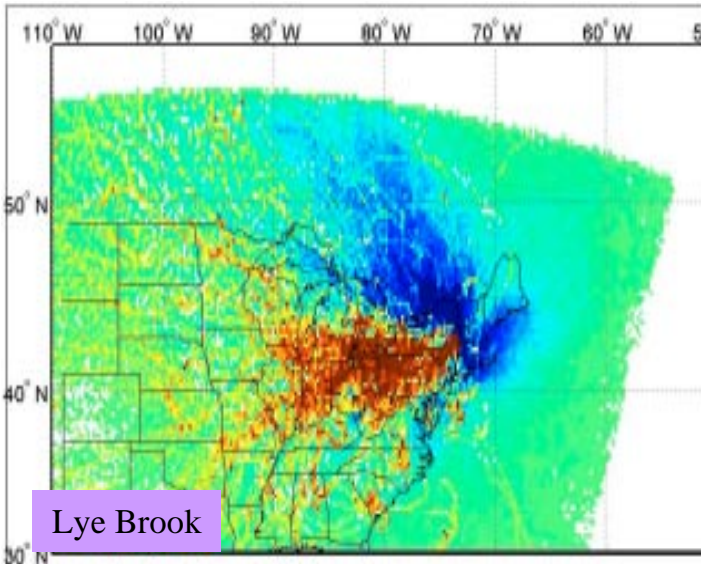


20 Percent is a lot of days...

0-5% worst days

5-10% worst days

10-15% worst days



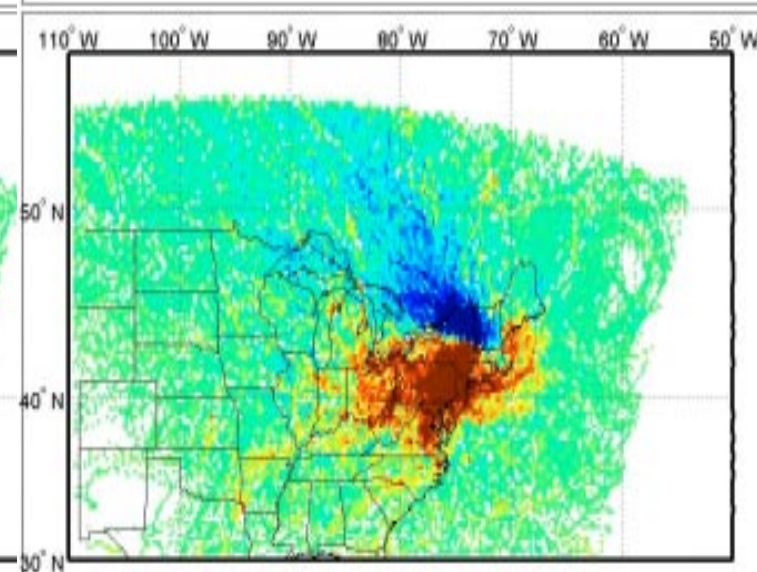
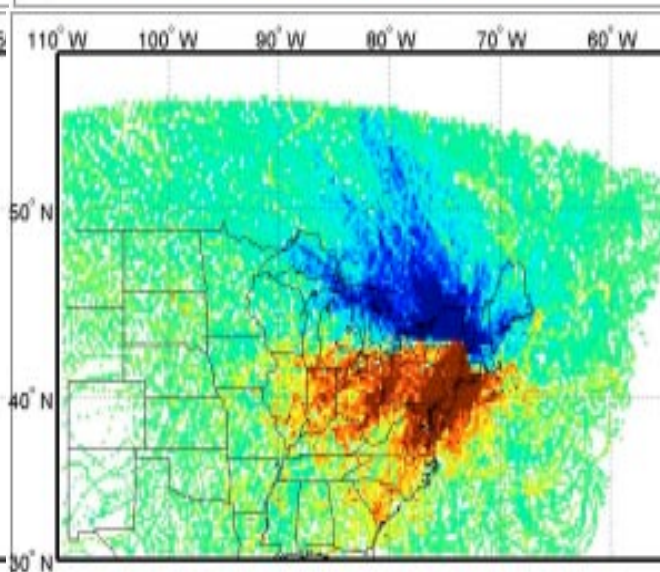
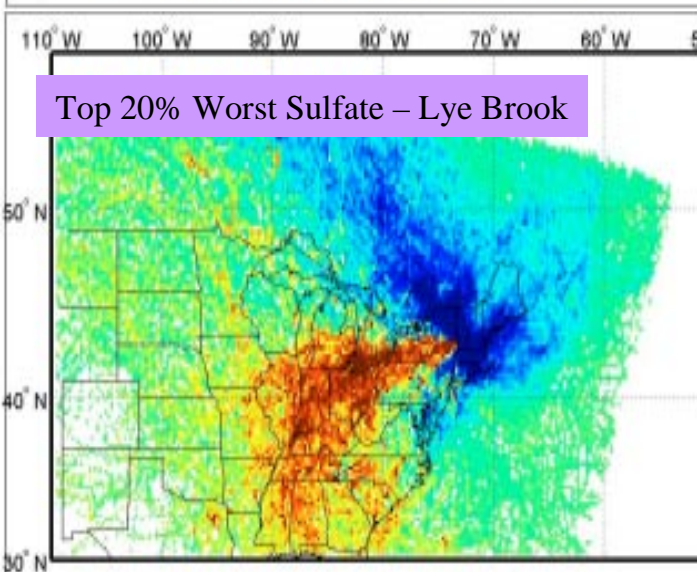
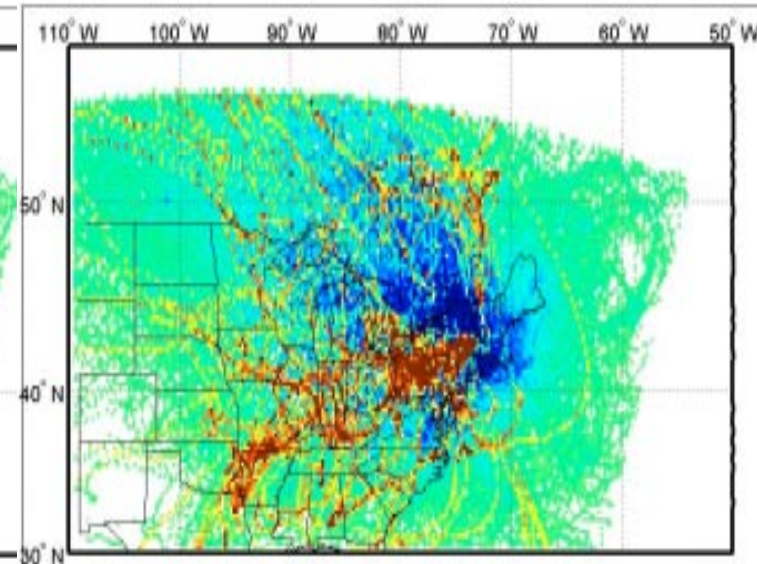
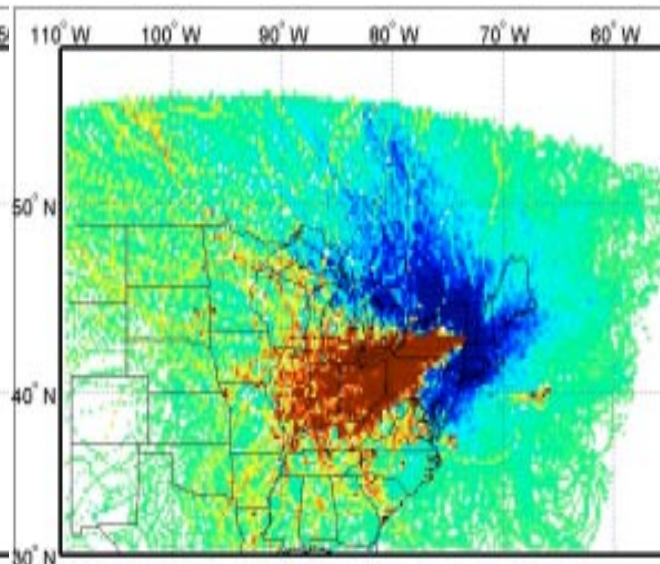
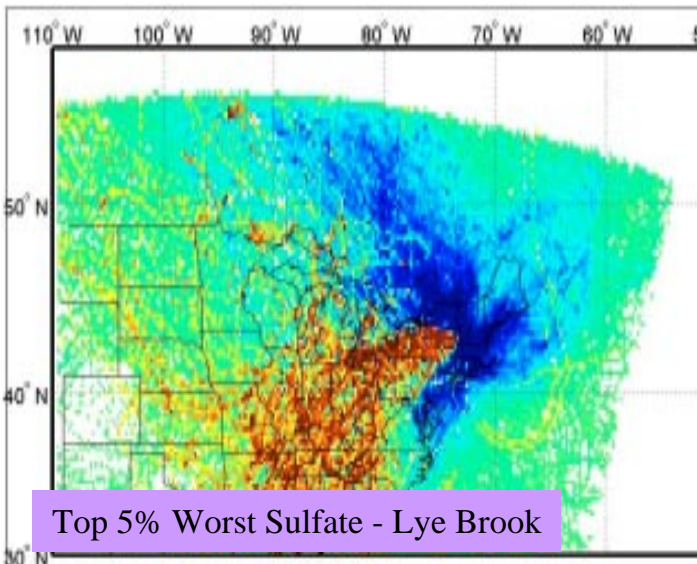
20 Percent covers a lot of seasons...



Spring

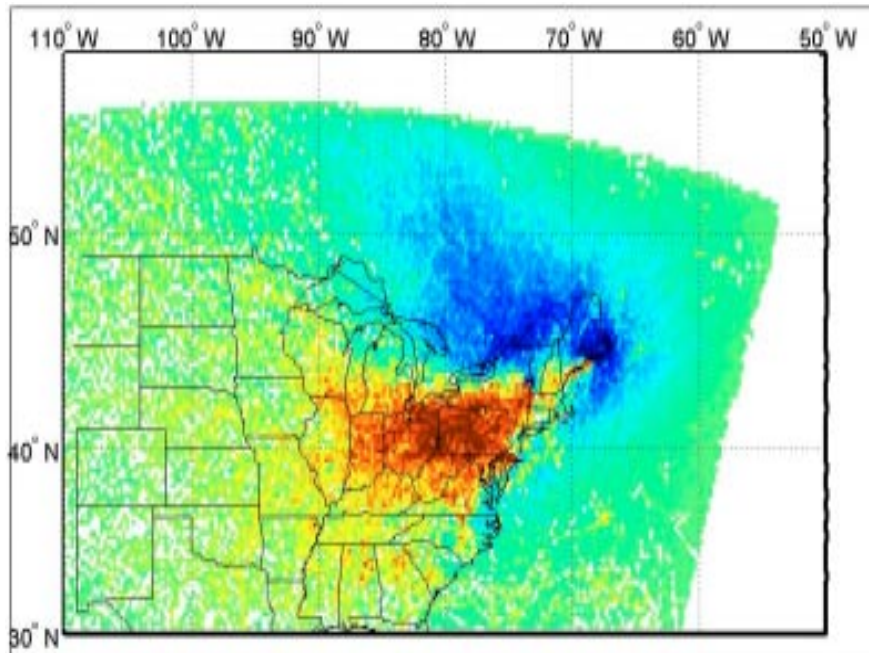
Summer

Fall

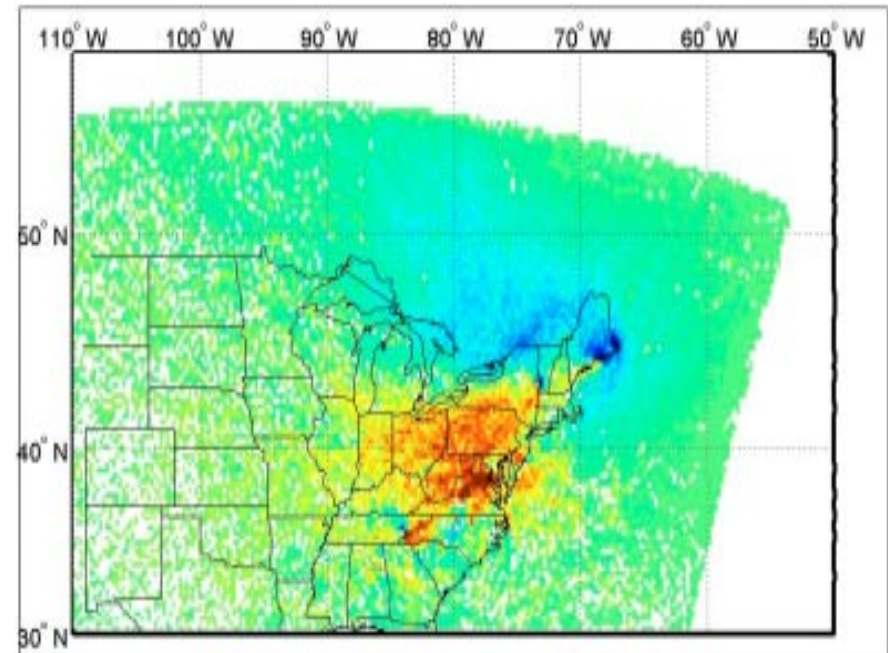




5% worst days from the perspective of multiple sites



Acad, Brig, Lybr, Moos



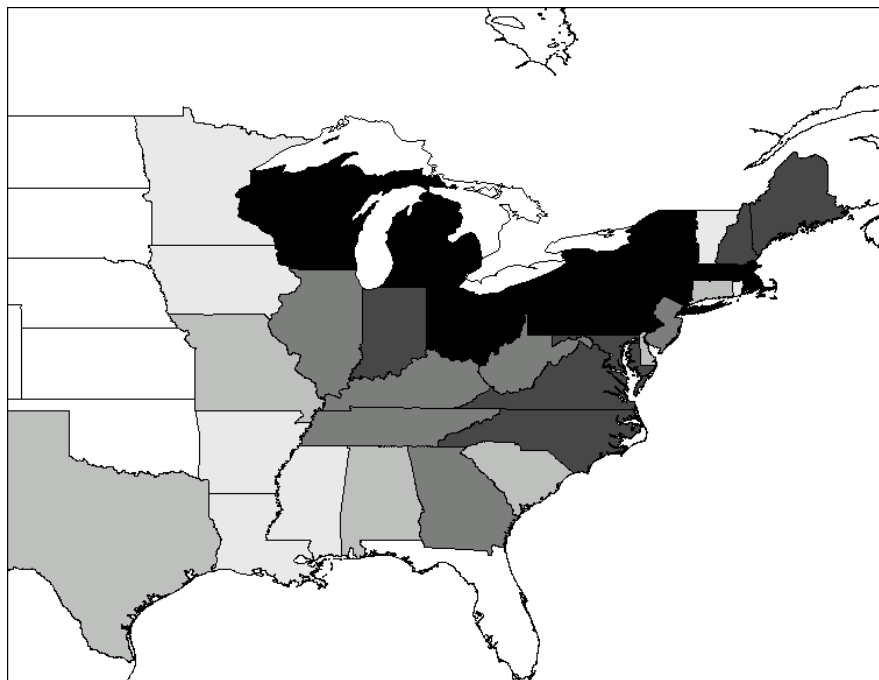
**Acad, Brig, Lybr, Grsm, Moos,
Shen, Wash, Jeff**

REMSAD v.7.10

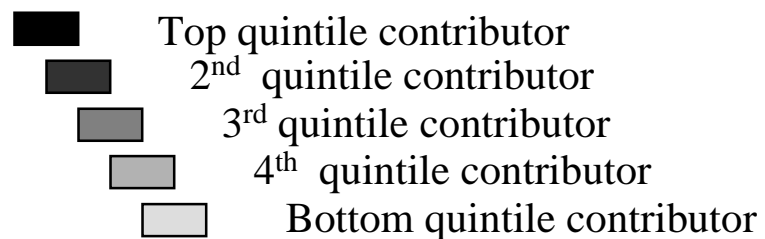
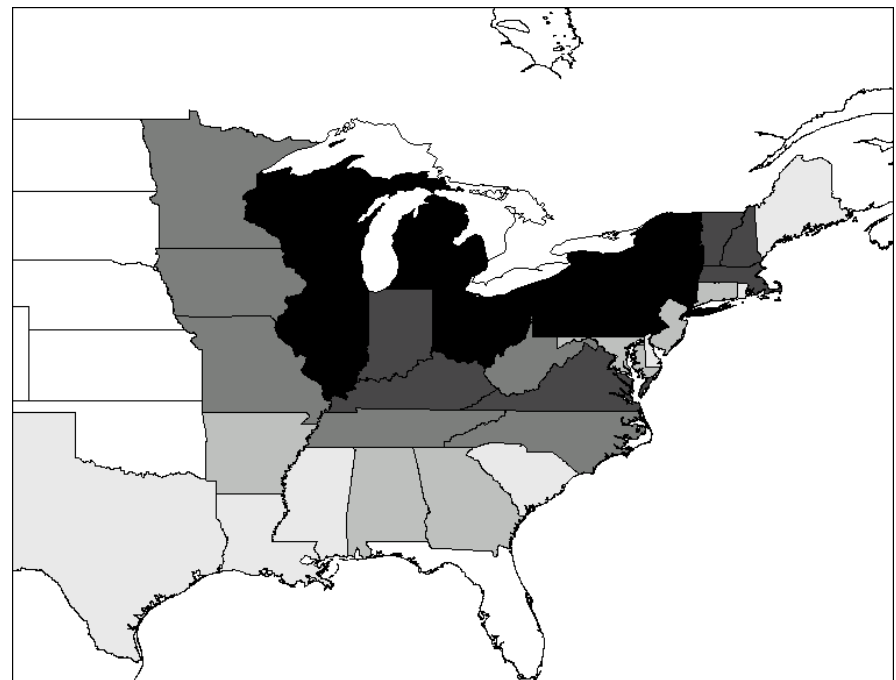
- Allows for source tagging (up to 11 tags per run)
- Meteorology and Emissions from EPA Clear Skies Act (2003) platform
- Tagged SO₂ emissions from elevated point sources in 33 Eastern U.S. states

Compare to REMSAD

REMSAD 7.10



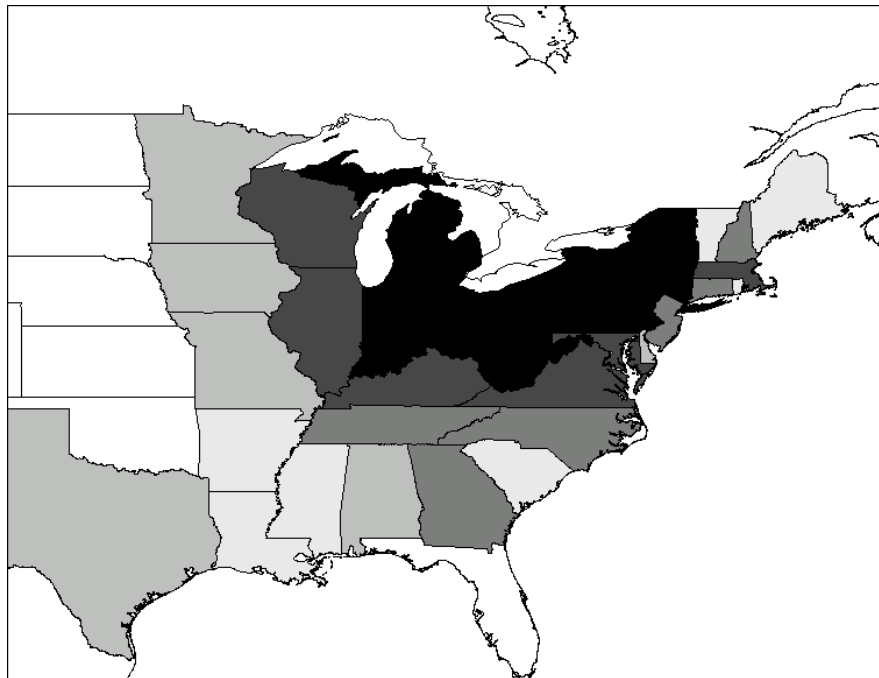
Cluster-Weighted Probability



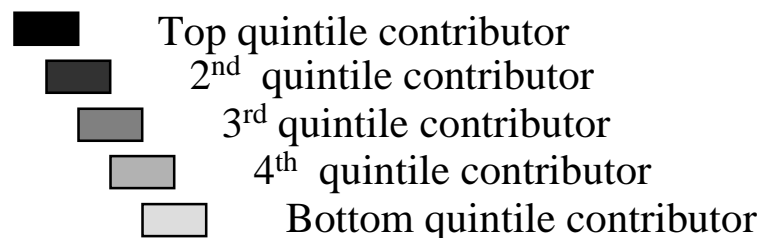
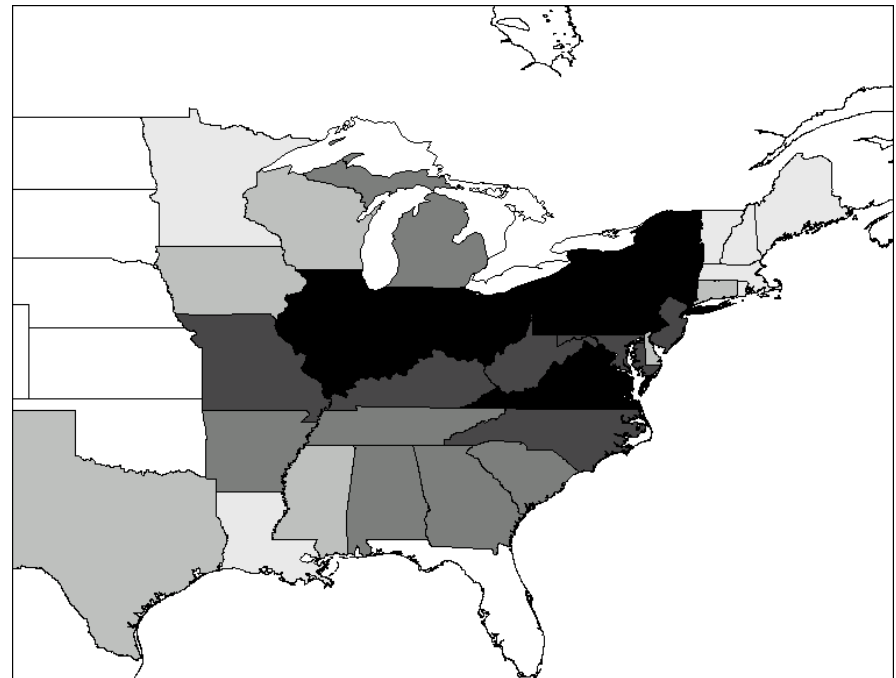
Acadia National Park, ME

Compare to REMSAD

REMSAD 7.10



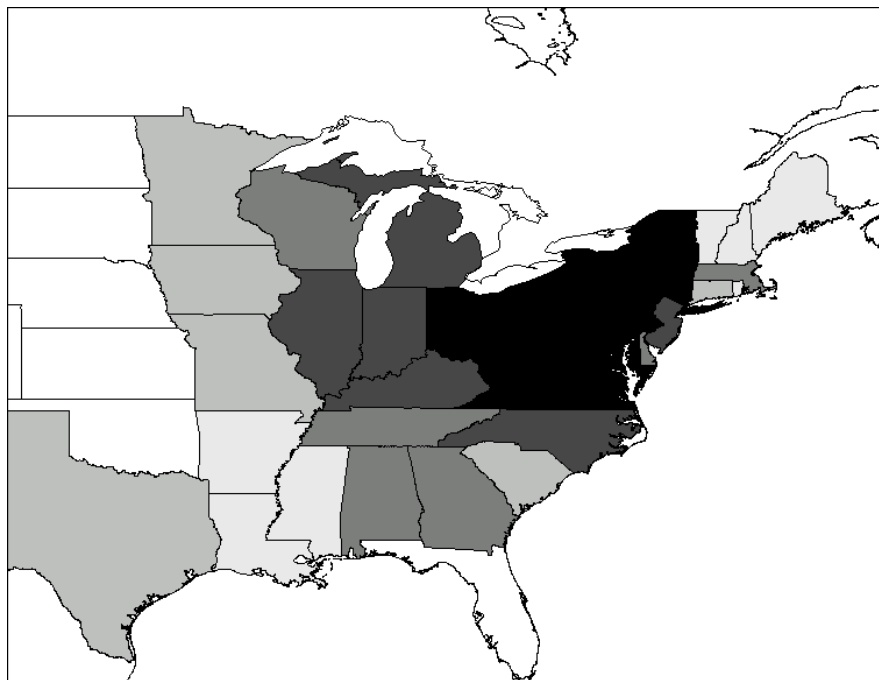
Cluster-Weighted Probability



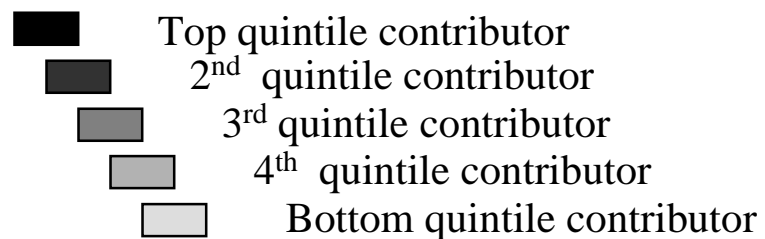
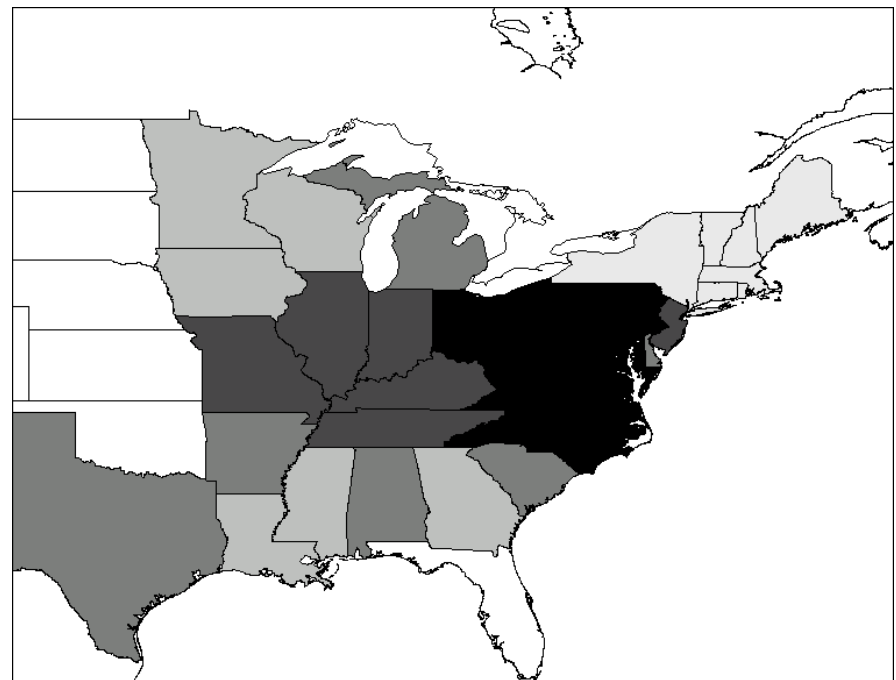
Lye Brook Wilderness, VT

Compare to REMSAD

REMSAD 7.10



Cluster-Weighted Probability



Brigantine Wilderness, NJ