

This document contains my notes on [Steve Brunton's Control Bootcamp video series](#). Each section corresponds to the video of the same title.

## Contents

<a href="#">1 Overview</a>	1
----------------------------	---

## 1 Overview

- **Passive controls** attempt to control a system passively, i.e. they are built into the system and don't vary based on observations of the system.
- **Active controls** attempt to control a system actively, i.e. they change their behaviour based on observations of the system.
- **Open-loop controllers** don't observe the output of the system — their inputs are predetermined. One downside of this approach is that you may unnecessarily input energy into the system when it already has the desired output.
- **Closed-loop controllers** observe the output of the system to determine their inputs. They have several benefits over open-loop controllers:
  - They handle uncertainty in the system, e.g. if you don't always know how the system will respond, or if your model isn't completely accurate.
  - They handle disturbances in the system, e.g. if someone pushes a self-balancing inverted pendulum. It may not be possible to account for these in the model.
  - They can be more energy efficient than open-loop controllers, i.e. they don't have the downside mentioned above.
- The mathematical model used in this course is a state-space based system of linear differential equations

$$\dot{\mathbf{X}} = \mathbf{A}\mathbf{X}$$

where  $\mathbf{X}$  is the **state vector** — a vector containing all the system's values of interest — and  $\dot{\mathbf{X}}$  are their rates of change at a time  $t$ .

- The solution to the above equation is

$$\mathbf{X}(t) = e^{\mathbf{A}t}\mathbf{X}(0)$$

and the eigenvalues of  $\mathbf{A}$  can be used to determine the stability of the system, e.g. if they all have negative real components the system is stable.

- Control is introduced to the system by modifying the equation to

$$\dot{\mathbf{X}} = \mathbf{A}\mathbf{X} + \mathbf{B}\mathbf{U}$$

where  $\mathbf{B}$  is a coefficient matrix and  $\mathbf{U}$  is the input to the system.

- If we make the input to the system

$$\mathbf{U} = -\mathbf{K}\mathbf{X}$$

then

$$\begin{aligned}\dot{\mathbf{X}} &= \mathbf{A}\mathbf{X} - \mathbf{B}\mathbf{K}\mathbf{X} \\ &= (\mathbf{A} - \mathbf{B}\mathbf{K})\mathbf{X}\end{aligned}$$

and now it is the eigenvalues of  $\mathbf{A} - \mathbf{B}\mathbf{K}$  that determine the stability of the system, i.e. we can make an unstable system stable by appropriate choice of inputs.