Introduction to Deep Larning Chris Arnold, Cardiff University, May 2022

Logistic Regression

y = P(y = 1 (x))

Parameters: WEIR", SEIR

Function  $y = \sigma(w_1 + 5)$ with  $\sigma(z) = \frac{1}{1+e^{-2}}$ 

LOSS facetion

goal: Liv for are we off?

L(9,4) = -[4 log 9 + (1-4) log (1-4)

if y = 1:

L(714) = - log q E but not 77

if 
$$y = 0$$
:
$$\mathcal{L}(y_1y) = -\log(1-\hat{y}) \text{ is small as possible}$$

$$\mathcal{L}(y_1y) = -\log(1-\hat{y}) \text{ but not } < 0$$

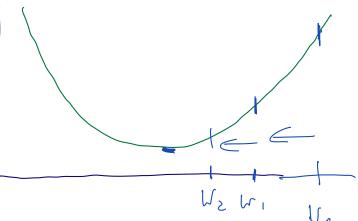
$$909l: \text{ minimise}$$

$$\mathcal{L}(y_1y_1) = -\frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(y_1y_1)$$

$$= -\frac{1}{m} \sum_{i=1}^{m} \left[ y_1^{(i)} \log y_1^{(i)} + (1-p_1) \log (1-\hat{y}_1^{(i)}) \right]$$

### Gradient Descent Intuition

Goal: min ( w.b)



$$w_z = w_1 - \alpha \frac{d J(w_1)}{dw}$$

Greneral Case:

 $\int (U,b)$ :

$$w := w - \alpha$$

$$y := W - Q \qquad \frac{\partial U \cup W \cup V}{\partial W}$$

$$b:=b-\alpha\frac{dJ(4,5)}{db}$$

Repeart:

$$\frac{\text{Refresh}}{\text{Z}} = \sqrt{1} + \frac{1}{4}$$

$$\hat{y} = a = \sqrt{2} = \frac{1}{1 + e^{-2}}$$

$$\mathcal{L}(a, y) = -\int_{-\infty}^{\infty} y \log(a) + (1 - y) \log(1 - a)$$

$$\begin{array}{c} x_{1} \\ w_{1} \\ \end{array}$$

$$\begin{array}{c} x_{2} \\ \end{array}$$

$$\begin{array}{c} 7 \\ \end{array}$$

$$da: \frac{d \mathcal{L}(a,y)}{da} = -\frac{y}{a} - \frac{1-y}{1-a}$$

$$\frac{d}{dz} = a(1-a)$$

$$\frac{d^2 d}{da} \cdot \frac{d^2 d}{dz} = \left(-\frac{4}{a} + \frac{1-4}{1-a}\right) \cdot a\left(1-a\right) = q-4 \quad 3$$

$$\int_{A_{v_i}} dv = x_i \cdot dz$$

$$\frac{dW_2}{dW_2} = x_2 \cdot dz$$

$$adb^{*}: \frac{dl}{db} = dz$$

$$w_1 = v_1 - \alpha A v_1$$

$$w_2 = w_2 - \alpha A v_2$$

$$b = b - \alpha A b$$

#### Neural Networks

No for hion

activation a

$$q \qquad \qquad \begin{bmatrix} q, \zeta, \zeta \\ q \zeta, \zeta, \zeta \\ q \zeta, \zeta, \zeta \\ q \zeta, \zeta, \zeta \end{bmatrix}$$

$$q^{[2]} = \gamma$$

veights w

bias 5

$$5^{[7]} = \begin{bmatrix} -7 \\ -7 \\ -7 \end{bmatrix}$$

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Shallow Neurol Network:

I Forward Propagation

$$\begin{array}{c}
LayN \\
Z_{i} = V_{i} = V_{i} \\
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\end{array}$$

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Verdon'sing goal: compose 2 as a rector

$$\begin{bmatrix}
\zeta_{1} \\
\zeta_{1}
\end{bmatrix} = \begin{cases}
\zeta_{1} \\
\zeta_{1}
\end{bmatrix} & \zeta_{0} \\
\zeta_{1}
\end{bmatrix} + \begin{cases}
\zeta_{1}
\end{bmatrix} \\
\zeta_{1}
\end{bmatrix} & (\zeta_{1})$$

$$\zeta_{1}
\end{bmatrix} = \begin{cases}
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\end{bmatrix} & (\zeta_{1})$$

$$(\zeta_{1}
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\end{bmatrix} & (\zeta_{1}
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$$(\zeta_{1}
)$$

### I How wrong is it?

Cost function:
$$J\left(w^{GJ}, 6^{GJ}, v^{EJ}, 6^{EJ}\right) = \frac{1}{m} \sum_{i=1}^{n} \mathcal{L}\left(\gamma_{i}\gamma\right)$$

# III Backprop the orror (skip in class)

g can be any activation

## Activation functions

tanh

$$a = \tanh(z) = \frac{e^{z} - e^{-z}}{e^{z} + e^{-z}}$$

relv:

$$a = max(0, z)$$

leaky wh:

### Why activation (vuctions?

$$a^{[i]} = \xi^{[i]} = V^{[i]} \times + \zeta^{[i]}$$

$$\int_{0}^{\infty} \left( w, b \right) = \int_{0}^{\infty} \sum_{i=1}^{\infty} \left( y^{(i)}, y^{(i)} \right) + \frac{2}{2m} \left\| w \right\|_{2}^{2}$$

$$\|w\|_{2}^{2} = \int_{0}^{\infty} \left( y^{(i)}, y^{(i)} \right) + \frac{2}{2m} \left\| w \right\|_{2}^{2}$$

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NN

$$\int (\sqrt{20}, \sqrt{20}) = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\sqrt{0}, \sqrt{0}) + \frac{7}{2m} \sum_{\ell=1}^{n} ||\sqrt{0}||_{2}^{2}$$

$$\| \omega^{[l]} \|_{z}^{z} = \sum_{i=1}^{[l-l]} \sum_{j=1}^{[\ell]} (\omega_{ij})^{z}$$

Tachprop

$$d \omega^{(l)} = from baldprop + \frac{2}{m} \omega^{(l)}$$

Up daking

$$[I] := W[I] - 2[from bp + \frac{2}{m} W[I]]$$

extra penalty depends on

. 2

· but also on w[l]